# Autonomous Bidding in the

## Trading Agent Competition

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## Key TAC Features

#### Simultaneous Auctions

#### **Combinatorial Valuations**

#### Complements

$$-v(X\bar{Y}) + v(\bar{X}Y) \le v(XY)$$

- camera, flash, and tripod

#### Substitutes

$$-v(X\bar{Y}) + v(\bar{X}Y) \ge v(XY)$$

- Canon AE-1 and Canon A-1

## **Examples**

#### **FCC** auctions

## eBay auctions

- o proxy bidding agents
- $\circ$  bid up to the value of good x

## v(Camera + Flash)

- o autonomous bidding agents
- $\circ$  bid up to the marginal value of good x

#### Bid Determination

#### Allocation

o given the set of goods I hold, what is the maximum valuation I can attain?

#### Acquisition

 given the set of goods I hold, and given ask prices in any open auctions, on what set of additional goods should I bid to maximize valuation less costs?

#### Requisition

 given the set of goods I hold, and given bid prices in any open auctions, on what set of goods should I place asks to maximize valuation plus profits?

#### Completion

 given the set of goods I hold, and given ask and bid prices in any open auctions, on what set of goods should I place bids or asks to maximize my valuation less costs plus profits?

## Overview

- o TAC Market Game
- TAC Agent Architecture
- RoxyBot Agent Architecture

#### TAC Market Game

Score = Valuation - Costs + Profits

#### Supply

- Flights Inbound and Outbound
- Hotels Grand Hotel and Le FleaBag Inn
- Entertainment Red Sox, Symphony, Phantom

#### **Auctions**

- Flights infinite supply, prices follow random walk, clear continuously, no resale permitted
- Hotels ascending, multi-unit, 16th price auctions, transactions clear and random auction closes once per minute, no resale permitted
- Entertainment continuous double auctions, initial endowment, resale is permitted

## TAC Market Game

#### **Demand**

| Client | IAD | IDD | HV  | RV  | SV  | TV  |
|--------|-----|-----|-----|-----|-----|-----|
| 1      | 1   | 3   | 99  | 134 | 118 | 65  |
| 2      | 1   | 4   | 131 | 170 | 47  | 49  |
| 3      | 1   | 2   | 147 | 13  | 55  | 49  |
| 4      | 3   | 4   | 145 | 130 | 60  | 85  |
| 5      | 1   | 4   | 82  | 136 | 68  | 87  |
| 6      | 2   | 4   | 53  | 94  | 51  | 105 |
| 7      | 1   | 3   | 54  | 156 | 126 | 71  |
| 8      | 1   | 5   | 113 | 119 | 187 | 143 |

## Feasible Packages

- o arrival date prior to departure date
- o same hotel on all intermediate nights
- o at most one entertainment event per night
- o at most one of each type of entertainment

## TAC Market Game

#### Valuation

$$1000 - travelPenalty + hotelBonus + funBonus$$
 
$$travelPenalty = 100(|IAD - AD| + |IDD - DD|)$$
 
$$hotelBonus = \begin{cases} HV & \text{if } H = G\\ 0 & \text{otherwise} \end{cases}$$
 
$$funBonus = entertainment values$$

#### **Allocation**

| Client | AD | DD | Н | Ticket        | Valuation |
|--------|----|----|---|---------------|-----------|
| 1      | 1  | 3  | G | SV1, RV2      | 1351      |
| 2      | 1  | 3  | G | RV1           | 1201      |
| 3      | 1  | 2  | G |               | 1147      |
| 4      | 3  | 4  | G | RV3           | 1275      |
| 5      | 1  | 3  | F | RV1, TV2      | 1123      |
| 6      | 3  | 4  | G | TV3           | 1058      |
| 7      | 1  | 3  | F | SV1, RV2      | 1282      |
| 8      | 1  | 5  | G | TV1, SV3, RV4 | 1562      |

## TAC Agent Architecture

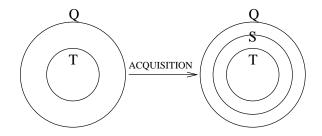
#### REPEAT

- 1. how many copies of each good do i want?
- 2. on the goods i want, should i bid now or later?
- 3. for the goods i want now, what am i willing to pay?

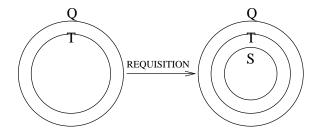
UNTIL game over

## **Bid Determination**

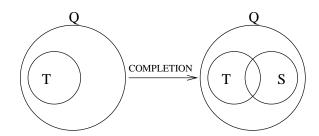
## $\operatorname{Bid} \text{ on } S \setminus T$



## 



## $\begin{array}{c} \text{Bid on } S \setminus T \\ \text{Ask for } T \setminus S \end{array}$



#### **Observations**

#### $WD \cong Allocation$

 WD: auctioneer seeks the set of combinatorial bids that maximizes profits, given feasibility constraints

## WDR $\cong$ Acquisition

 WDR (WD with reserve prices): auctioneer seeks the set of combinatorial bids that maximizes the difference between profits and reserve prices

BD problems in simultaneous auctions  $\cong$  WD problems in combinatorial auctions

#### **Pricelines**

#### **Buying Priceline**

$$ec{p}_g = \langle 0,0,0,0,20,30,\infty,\infty,\ldots 
angle$$
 $orall g, \quad n ext{Buy}(S,g) = \sum_{ec{q} \in S} q_g$ 
 $orall g, \quad ext{Cost}_g(S,P) = \sum_{n=1}^n p_{gn}$ 
 $\operatorname{Cost}(S,P) = \sum_{g \in G} \operatorname{Cost}_g(S,P)$ 

#### Selling Priceline

$$ec{\pi}_g = \langle 10, 5, 2, 1, 0, 0, 0, 0, -\infty, -\infty, \ldots \rangle$$

$$\forall g, \quad n \text{Sell}(S, g) = \sum_{ec{q} \notin S} q_g$$

$$\forall g, \quad \text{Profit}_g(S, \Pi) = \sum_{n=1}^{n} \pi_{gn}$$

$$\text{Profit}(S, \Pi) = \sum_{g \in G} \text{Profit}_g(S, \Pi)$$

#### **Formalization**

#### Acquisition

```
Inputs: set of packages Q set of buying pricelines P valuation function v:Q\to\mathbb{R}^+ Output: S^*\in \arg\max_{S\subseteq Q}(\mathsf{Valuation}(S,v)-\mathsf{Cost}(S,P))
```

#### Requisition

```
Inputs: set of packages Q set of selling pricelines \Pi valuation function v:Q\to\mathbb{R}^+ Output: S^*\in \arg\max_{S\subseteq Q}(\operatorname{Valuation}(S,v)+\operatorname{Profit}(S,\Pi))
```

#### Completion

```
Inputs: set of packages Q set of buying pricelines P set of selling pricelines \Pi valuation function v:Q\to\mathbb{R}^+ Output: S^*\in \arg\max_{S\subset Q}(\operatorname{Val}(S,v)-\operatorname{Cost}(S,P)+\operatorname{Profit}(S,\Pi))
```

#### **Formalization**

#### Acquisition

```
Inputs: set of packages Q set of buying pricelines P valuation function v:Q\to\mathbb{R}^+ Output: S^*\in \arg\max_{S\subseteq Q}(\mathsf{Valuation}(S,v)-\mathsf{Cost}(S,P))
```

#### Requisition

```
Inputs: set of packages Q set of selling pricelines \Pi valuation function v:Q\to\mathbb{R}^+ Output: T^*\in \arg\max_{T\subseteq Q}(\operatorname{Valuation}(T,v)+\operatorname{Profit}(T,\Pi))
```

#### Completion

```
Inputs: set of packages Q set of buying pricelines P set of selling pricelines \Pi valuation function v:Q\to\mathbb{R}^+ Output: S^*,T^*\in \arg\max_{S,T\subseteq Q}(\operatorname{Valuation}(S,v)-\operatorname{Cost}(S,P)+\operatorname{Profit}(T,\Pi)-\operatorname{Cost}(T,P))
```

## Completion → Acquisition

#### **Buying Priceline**

$$\vec{p}_g = \langle 0, 0, 0, 0, 20, 30, \infty, \infty, \ldots \rangle$$

#### Selling Priceline

$$\vec{\pi}_g = \langle 10, 5, 2, 1, 0, 0, 0, 0, -\infty, -\infty, \ldots \rangle$$

#### 1st Reduction

o add reverse of selling pricelines to buying pricelines:  $\vec{p}_g$  + reverse( $\vec{\pi}_g$ ) =  $\langle 1, 2, 5, 10, 20, 30, \infty, \infty, \ldots \rangle$ 

#### 2nd Reduction

 $\circ$  extend package input set with singleton packages, one for each copy of each good in selling pricelines; assign selling prices as dummy package valuations:  $\vec{\pi}_g \longmapsto$  4 new packages with valuations 10, 5, 2, 1

Bid Determination in double-sided auctions → Bid Determination in single-sided auctions

## Utility

#### Acquisition

Inputs: set of packages Q set of buying pricelines P valuation function  $v:Q\to\mathbb{R}^+$  Output:  $S^*\in \arg\max_{S\subseteq Q}(\operatorname{Valuation}(S,v)-\operatorname{Cost}(S,P))$   $u(S^*)=\max_{S\subseteq Q}(\operatorname{Valuation}(S,v)-\operatorname{Cost}(S,P))$ 

#### Example

valuations

$$v(XYZ) = v(XY) = v(YZ) = 500$$
  
 $v(X) = v(Y) = v(Z) = v(XZ) = 0$ 

pricelines

$$p(X) = p(Y) = p(Z) = 100$$

#### utilities

$$u(XY) = u(YZ) = 300$$

## Marginal Utility

for the goods i want now, what am i willing to pay?

#### Acquisition

Inputs: set of packages Q set of buying pricelines P valuation function  $v:Q\to\mathbb{R}^+$  Output:  $S^*\in \arg\max_{S\subseteq Q}(\operatorname{Valuation}(S,v)-\operatorname{Cost}(S,P))$   $u(S^*)=\max_{S\subseteq Q}(\operatorname{Valuation}(S,v)-\operatorname{Cost}(S,P))$ 

#### **Answer**

$$u(x) = u(A \cup \{x\}) - u(A)$$
, with  $p(x) = 0 \& p(x) = \infty$ 

#### Example

$$u(X) = u(XYZ) - u(YZ) = 400 - 300 = 100$$
  
 $u(Y) = u(XYZ) - u(XZ) = 400 - 0 = 400$   
 $u(Z) = u(XYZ) - u(XY) = 400 - 300 = 100$ 

#### **Bids**

$$b(Y) = 300, \ b(X) = b(Z) = 100$$
  
 $v(Y) - p(Y) = 200$ 

## RoxyBot

how many copies of each good do i want?

#### Acquisition

```
Inputs: set of packages Q set of buying pricelines P valuation function v:Q\to\mathbb{R}^+ Output: S^*\in \arg\max_{S\subseteq Q}(\operatorname{Valuation}(S,v)-\operatorname{Cost}(S,P)) u(S^*)=\max_{S\subset Q}(\operatorname{Valuation}(S,v)-\operatorname{Cost}(S,P))
```

#### **Answer**

$$n \mathrm{Buy}(S^*,g) = \sum_{ec{q} \in S^*} q_g$$

#### Example

$$n \text{Buy}(\{XY\}, X) = 1$$
  
 $n \text{Buy}(\{XY\}, Y) = 1$   
 $n \text{Buy}(\{XY\}, Z) = 0$   
 $X \text{OR}$   
 $n \text{Buy}(\{YZ\}, X) = 0$   
 $n \text{Buy}(\{YZ\}, Y) = 1$   
 $n \text{Buy}(\{YZ\}, Z) = 1$ 

## Marginal Utility, Revisited

for the goods i want now, what am i willing to pay?

#### Acquisition

Inputs: subset of packages Q set of buying pricelines P valuation function  $v:Q\to\mathbb{R}^+$  Output:  $S^*\in \arg\max_{S\subseteq Q}(\operatorname{Valuation}(S,v)-\operatorname{Cost}(S,P))$   $u(S^*)=\max_{S\subseteq Q}(\operatorname{Valuation}(S,v)-\operatorname{Cost}(S,P))$ 

#### **Answer**

$$u(x) = u(A \cup \{x\}) - u(A)$$
, with  $p(x) = 0 \& p(x) = \infty$ 

#### Example

$$u(X) = u(XY) - u(Y) = 400 - 0 = 400$$
  
 $u(Y) = u(XY) - u(X) = 400 - 0 = 400$ 

#### **Bids**

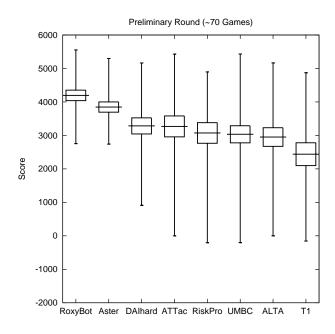
$$b(X) = b(Y) = 400, b(Z) = 0$$
  
 $v(XY) - p(X) - p(Y) = 300$ 

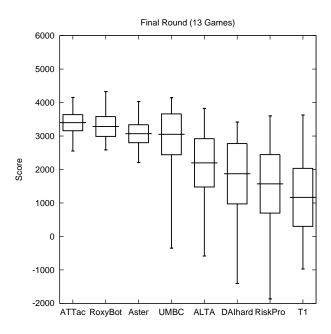
## RoxyBot 2000 Architecture

#### (A) REPEAT

- 1. Ping server to update current prices and holdings
- 2. Estimate clearing prices and build buy/sell pricelines
- 3. Run completer to find optimal buy/sell quantities
- Bid/ask marginal valuationsUNTIL game over
- (B) Run allocator

## TAC 2000 Statistics





## Price Uncertainty

for the goods i want now, what am i willing to pay?

#### Example

$$p(x)=0$$
, with probability  $\frac{1}{2}$ , and  $p(x)=200$ , with probability  $\frac{1}{2}$ , for all  $x\in\{X,Y,Z\}$ 

#### **Answer**

average marginal utility

#### **Bidding Policy**

| X    | Y   | Z   | u(X) | u(Y) | u(Z) |
|------|-----|-----|------|------|------|
| 0    | 0   | 0   | 0    | 500  | 0    |
| 200  | 0   | 0   | 0    | 500  | 200  |
| 0    | 200 | 0   | 0    | 500  | 0    |
| 0    | 0   | 200 | 200  | 500  | 0    |
| 200  | 200 | 0   | 0    | 500  | 200  |
| 200  | 0   | 200 | 200  | 300  | 200  |
| 0    | 200 | 200 | 200  | 500  | 0    |
| 200  | 200 | 200 | 200  | 300  | 200  |
| Bids |     |     | 100  | 450  | 100  |

## RoxyBot Under Uncertainty

how many copies of each good do i want?

#### **Answer**

sound and complete set of packages

## Example

$$n \operatorname{Buy}(\{XY\}, X) = 1$$
 
$$n \operatorname{Buy}(\{XY\}, Y) = 1$$
 
$$n \operatorname{Buy}(\{XY\}, Z) = 0$$

## **Bidding Policy**

| X    | Y   | u(X) | u(Y) |
|------|-----|------|------|
| 0    | 0   | 500  | 500  |
| 200  | 0   | 500  | 300  |
| 0    | 200 | 300  | 500  |
| 200  | 200 | 300  | 300  |
| Bids |     | 400  | 400  |

## **Bidding Under Uncertainty**

| X      | Y   | Z   | ATTac | RoxyBot |
|--------|-----|-----|-------|---------|
| 0      | 0   | 0   | 500   | 500     |
| 200    | 0   | 0   | 500   | 300     |
| 0      | 200 | 0   | 300   | 300     |
| 0      | 0   | 200 | 500   | 500     |
| 200    | 200 | 0   | 300   | 100     |
| 200    | 0   | 200 | 0     | 300     |
| 0      | 200 | 200 | 300   | 300     |
| 200    | 200 | 200 | -200  | 100     |
| Scores |     |     | 275   | 300     |

## RoxyBot 2001 Architecture

#### **INPUTS**

Truncation Parameter  $t_0 \in [0.5, 1.0]$ Schedule by which to Decay  $t_0$ 

#### (A) REPEAT

- 1. Updates prices and winnings
- 2. Estimate clearing price distributions
- 3. Initialize d = 0, s = 8, n = 0, and  $t = t_0$
- 4. REPEAT
  - (a) Sample clearing price distributions
  - (b) Compute optimal completion  $D_n$
  - (c) Store  $D_n$  in completion list
  - (d) Increment n
  - (e) Tally results
    - i. for all items i
      - o initialize #i = 0
      - $\circ$  for all completions  $D_n$ 
        - if  $i \in D_n$ , increment #i
      - $\circ$  if #i/n > t
        - increment d
        - add i to D
      - $\circ$  if #i/n < 1-t
        - decrement s
        - delete i from S
  - (f) Discard from list inconsistent completions
  - (g) Set n equal to length of completion list
  - (h) Decay t

UNTIL d = s or TIME OUT

(B) Run allocator

## Future Work

## **Empirical Testing**

- o Completion vs. No Completion
- o Sampling vs. No Sampling
- o ILP vs. LP Relaxation

## Theoretical Study

- timing—optimal stopping problem
- o estimate joint price distributions