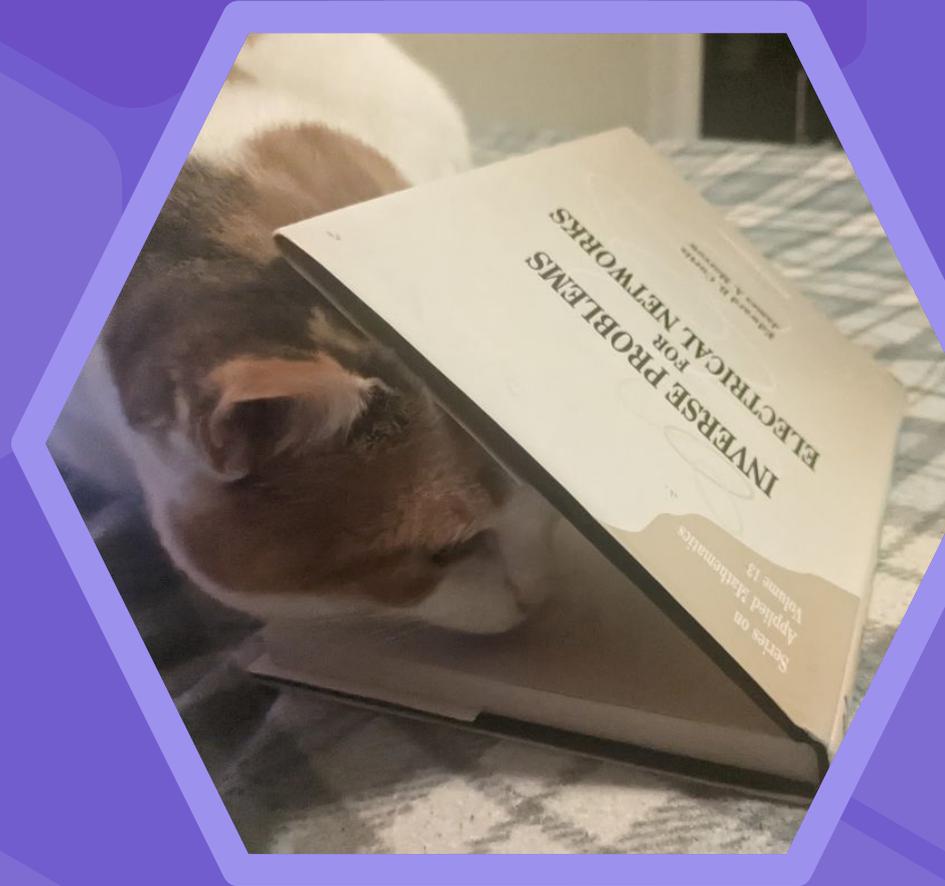


02: Introduction to Circuits

Reminders:

- Complete HWO1 (short survey) by Monday
(everyone should do this, not just people wanting to get on the waitlist)
- Complete Prelab 1 by Monday
Bring kits to lab if you have them (we'll ask people who don't have kits to form groups with people who do)





Group project/Capstone

No exams for this class → convince me you **met the learning goals** via the project

Demo & project report, revisions after feedback

More details after shopping period

Capstone: additional functionality you add on to final project + demo to me



Review

Embedded systems are everywhere, have specific purposes, and unique challenges

Microcontrollers (MCUs) have CPU, I/O, memory on one chip

In lab you will begin working with an MCU and embedded hardware



Why would we as software engineers care about circuits, analog components, how I/O works, etc?

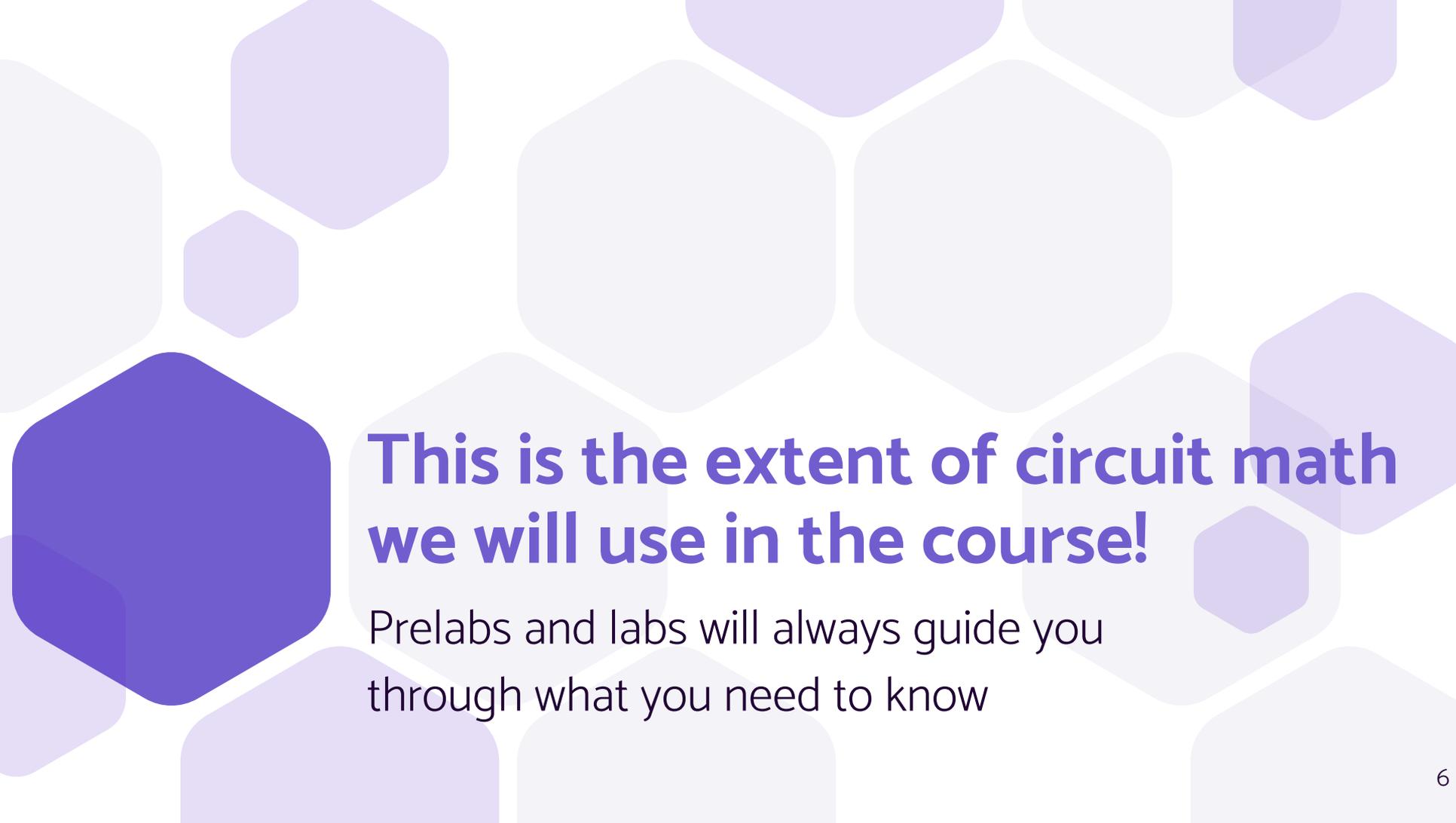
Hardware constrains what kind of software we write

Understanding what kind of computations are optimized for your hardware

Need to know the assumptions behind the input you are getting

Less constrained to what exists already

Limitations o

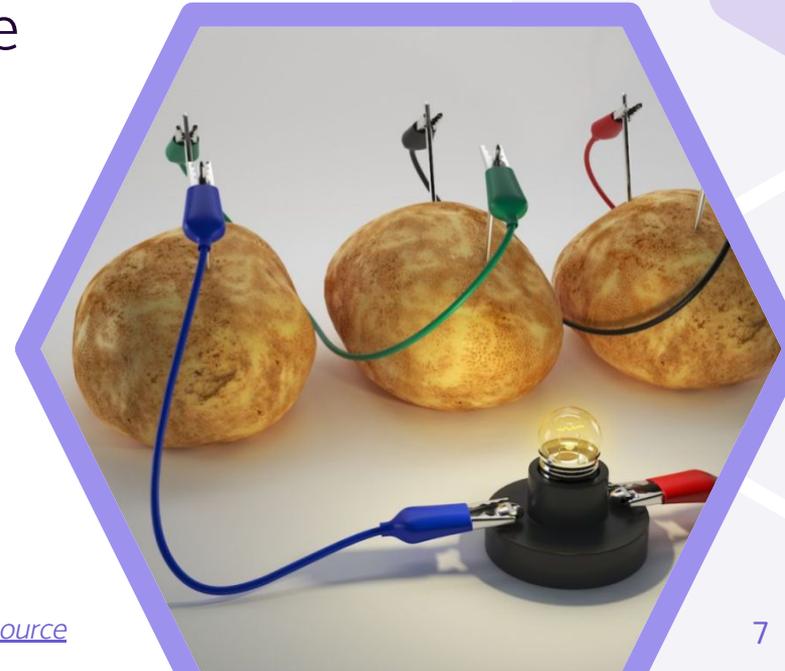


**This is the extent of circuit math
we will use in the course!**

Prelabs and labs will always guide you
through what you need to know

Electrical circuit

- ◆ **Loop** through which electricity flows
- ◆ Consists of at least a power source and conductors
- ◆ Some quantities that are useful to measure:
 - ◇ Voltage
 - ◇ Current
 - ◇ Power



[Image source](#)

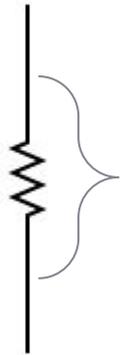


Voltage

Difference in electric potential

Measured between two points (or one point and implicit ground)

We say we measure voltage **across** a component



Voltage across resistor



Current

Rate of flow of charged particles through a circuit

Convention in circuits: imagine particles flowing from positive to negative terminal (or from a power source to ground)



We say we measure current **through** a component

Current through resistor



Ohm's law & power law

Ohm's law: $\mathbf{V = IR}$ (SI units: volts, amperes, ohms)

Power law: $\mathbf{P = IV}$ (SI units: watts, amperes, volts)

Useful for:

- Computing values needed to build circuit

- Figuring out the limits of what you can attach to your microcontroller

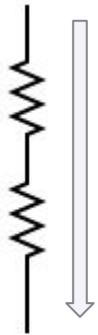
- Writing down accurate math for modeling your system

“

Given Ohm's law ($V = IR$) and the Power law ($P = IV$), what is the maximum power output of your Arduino pin (rated at 3.3 V, 7 mA)

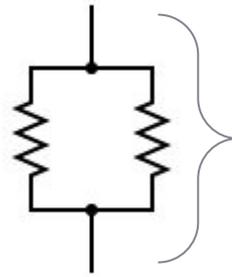
Parallel and series components

Series



Current is the same
through both components
Voltage: ???

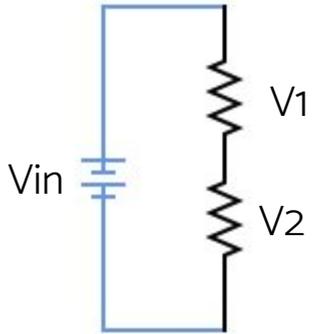
Parallel



Voltage is the same
across both
components
Current: ???

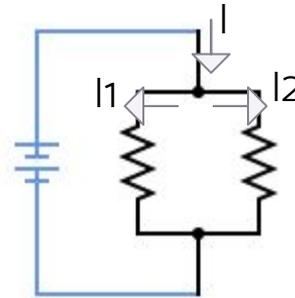
Kirchoff's laws

Sum of **voltages** around a closed loop is zero



$$\begin{aligned} -V_{in} + V1 + V2 &= 0 \\ V_{in} &= V1 + V2 \end{aligned}$$

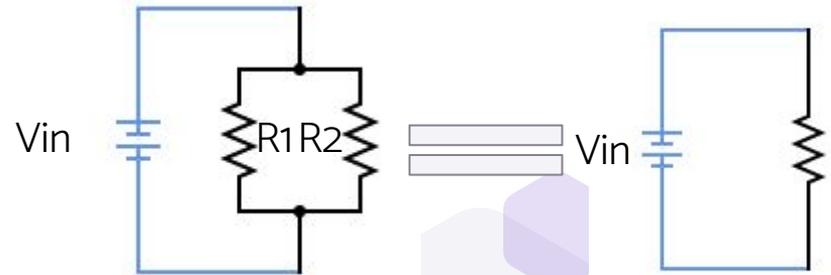
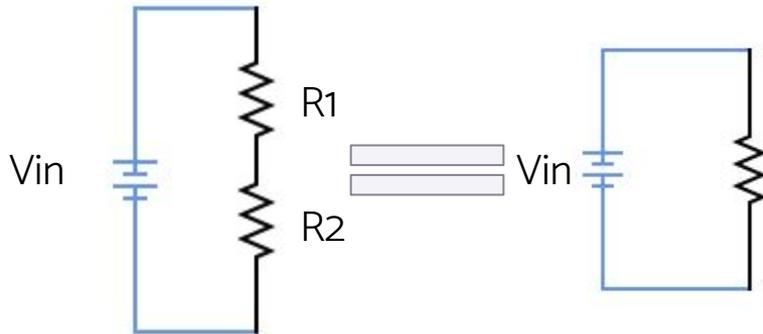
Sum of **currents** flowing *into* a node is the same as sum of currents flowing *out* of the node



$$I = I1 + I2$$

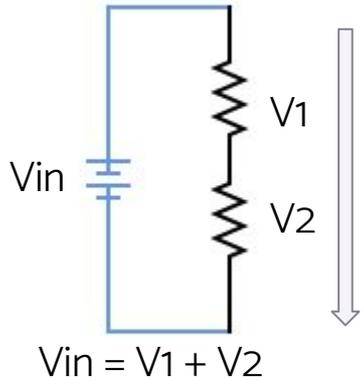
Thevenin equivalent circuit

Any linear electrical network containing current sources, voltage sources, and resistors can be replaced by an equivalent circuit with one voltage source and one resistor

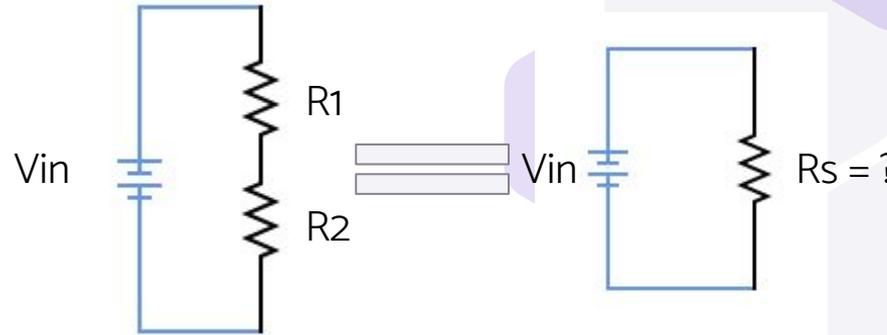


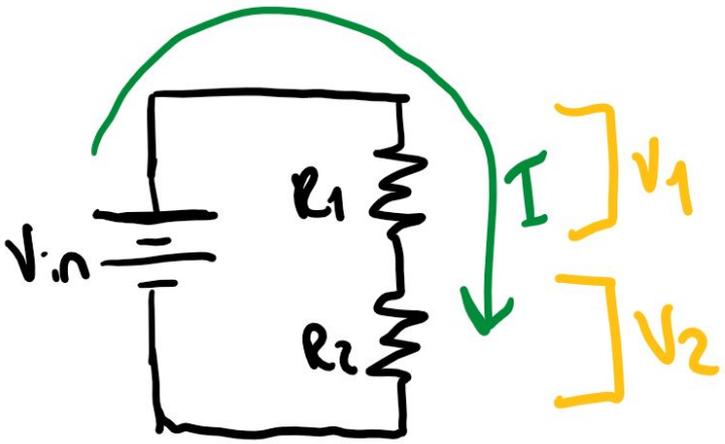
Thevenin for resistors in series

$$V = IR$$



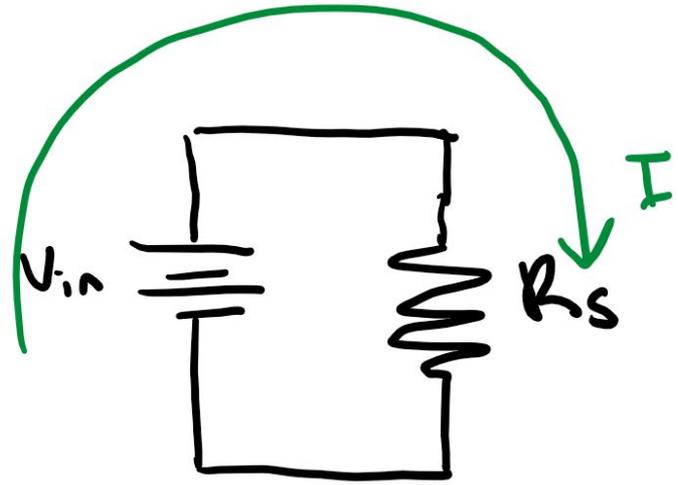
Current is the same through both components





$$V_1 = R_1 \cdot I$$

$$V_2 = R_2 \cdot I$$



$$V_{in} = R_s \cdot I$$

$$(V_1 + V_2) = R_s \cdot I$$

$$(R_1 \cdot I + R_2 \cdot I) = R_s \cdot I$$

$$R_s = R_1 + R_2$$



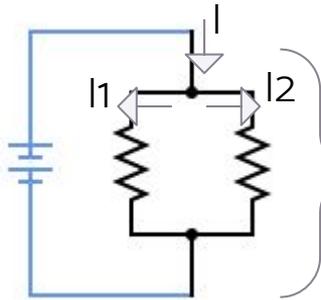
What's the point?

Understanding that resistance in series is additive helps you reason about the limitations of how much you can attach in series to one pin

You have more flexibility in terms of the resistors you use

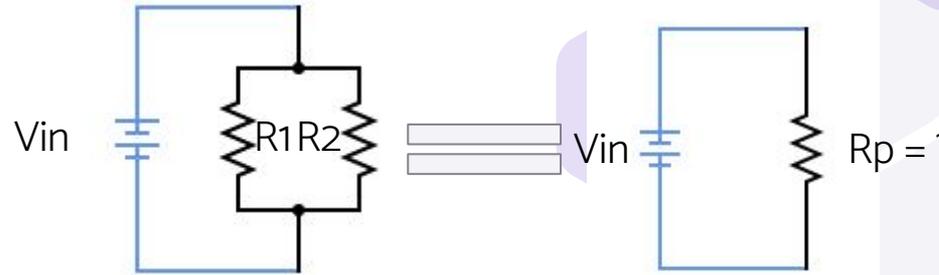
Thevenin for resistors in parallel

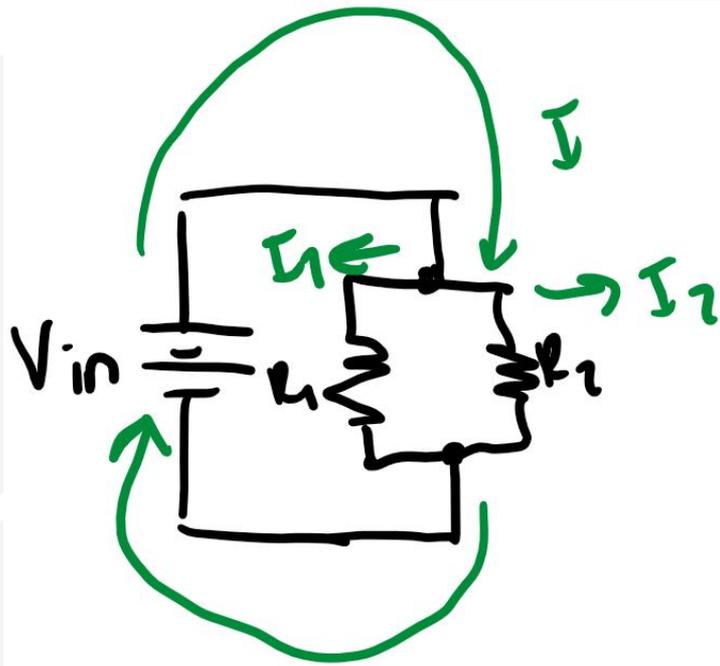
$$V = IR$$



Voltage is the same
across both
components

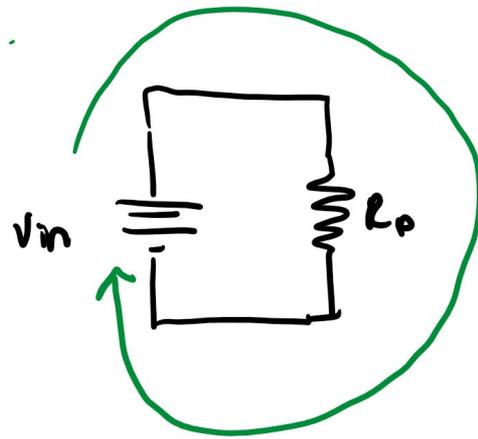
$$I = I_1 + I_2$$





$$I = I_1 + I_2$$

$$V_{in} = I_1 \cdot R_1$$



$$V_{in} = I \cdot R_p$$

$$V_{in} = (I_1 + I_2) R_p$$

$$V_{in} = \left(\frac{V_{in}}{R_1} + \frac{V_{in}}{R_2} \right) R_p$$

$$1 = \left(\frac{1}{R_1} + \frac{1}{R_2} \right) R_p$$

$$\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2}$$



What's the point?

Resistance of circuit connected in parallel will be smaller than resistance of each resistor

The smaller the resistance, the larger the current
→ connecting too many components in parallel might draw too much current