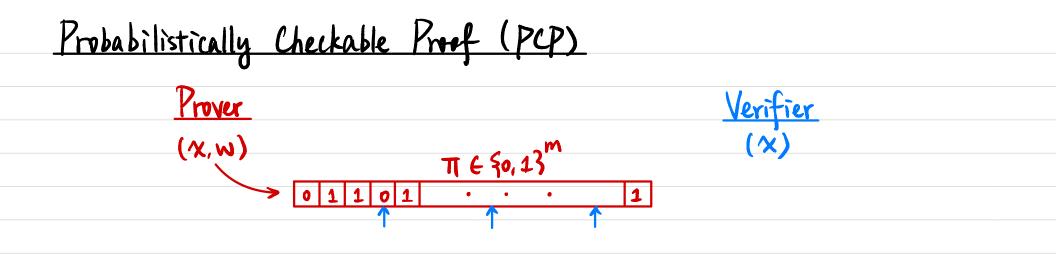
# CSCI 1515 Applied Cryptography

### This Lecture:

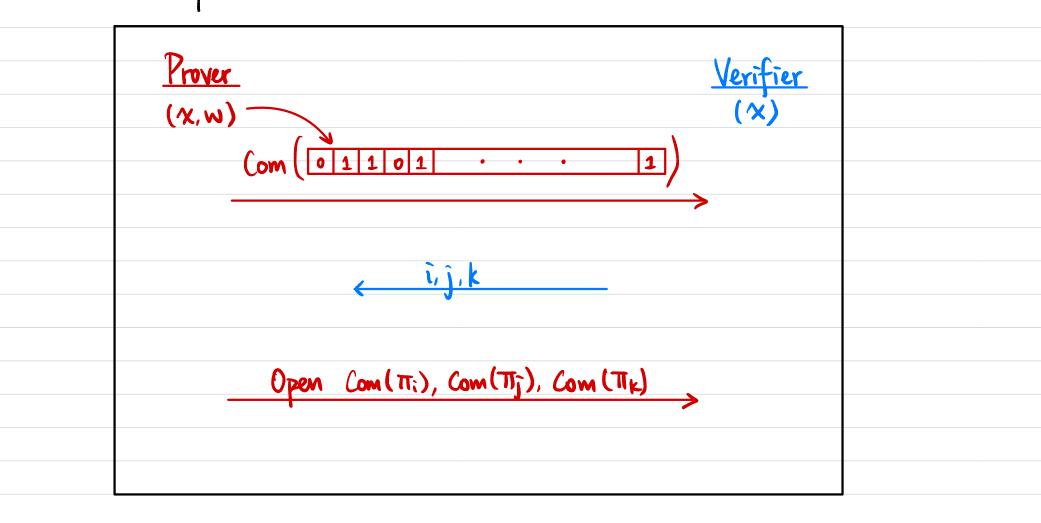
- · SNARGS from PCP (continued)
- · SNARGS from Linear PCP
- · Introduction to MPC

· SNARK: Succinct Non-Interactive Argument of Knowledge · ZK-SNARG/ZK-SNARK: SNARG/SNARK + Zero-Knowledge

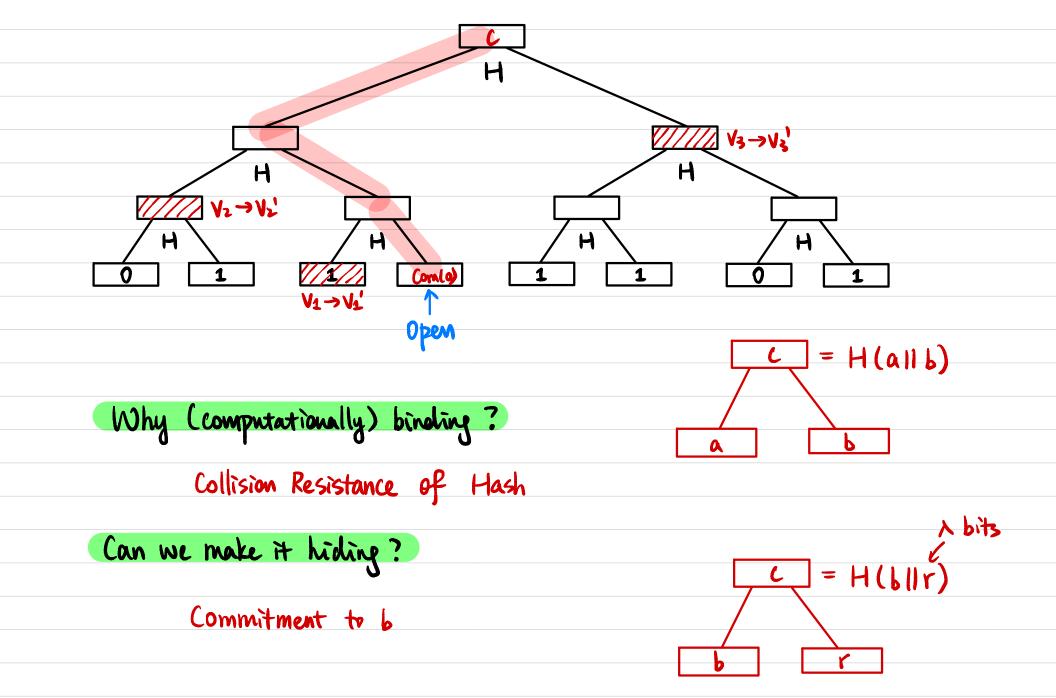




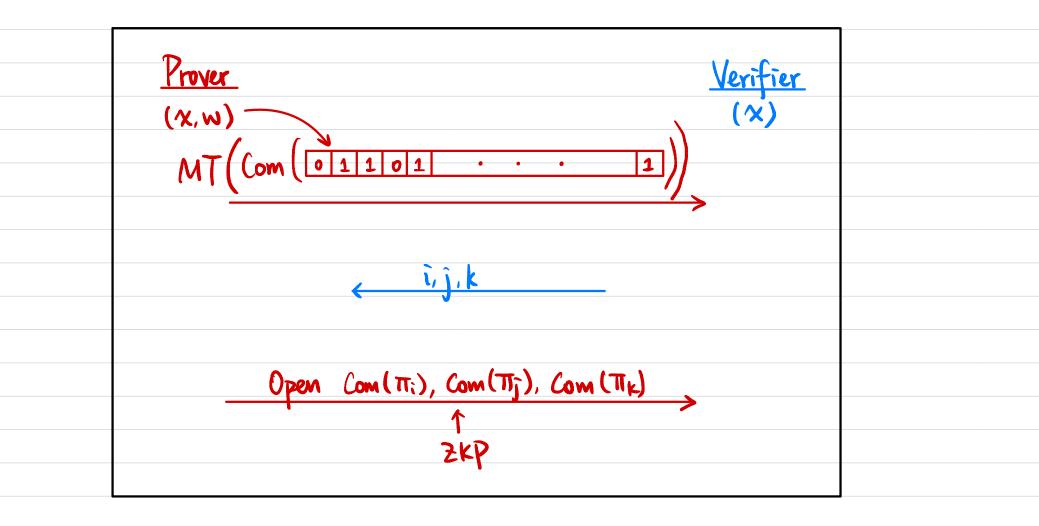
## First Attempt

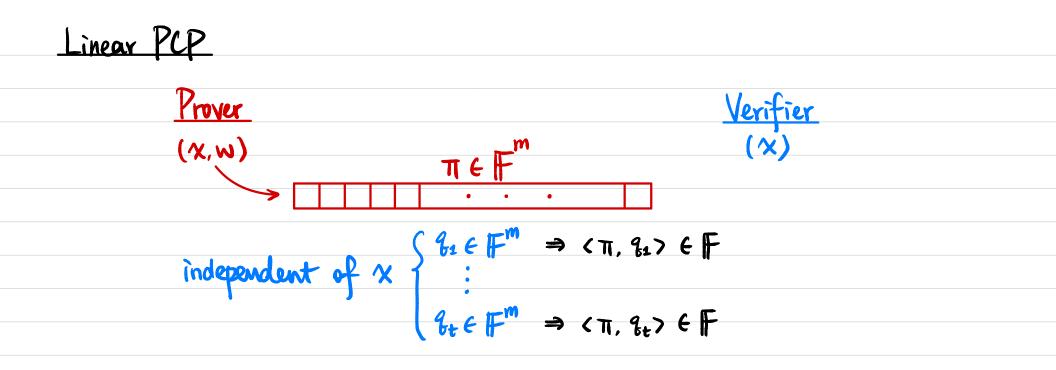


### Merkle Tree

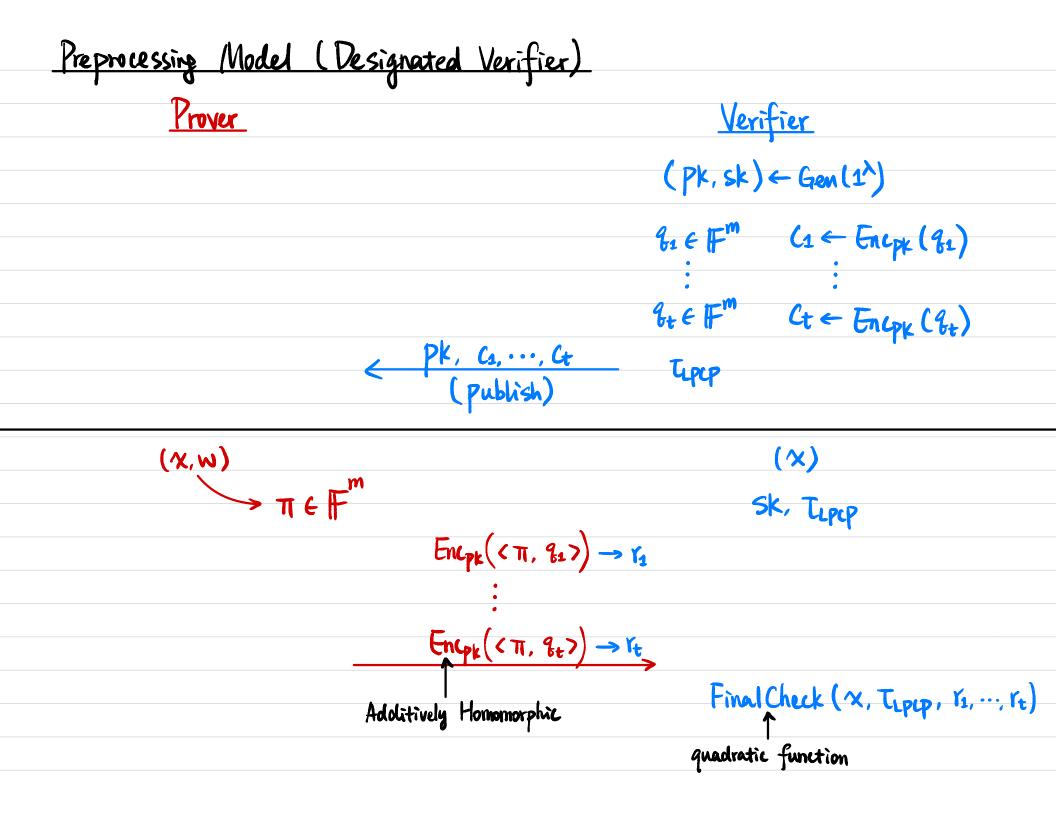


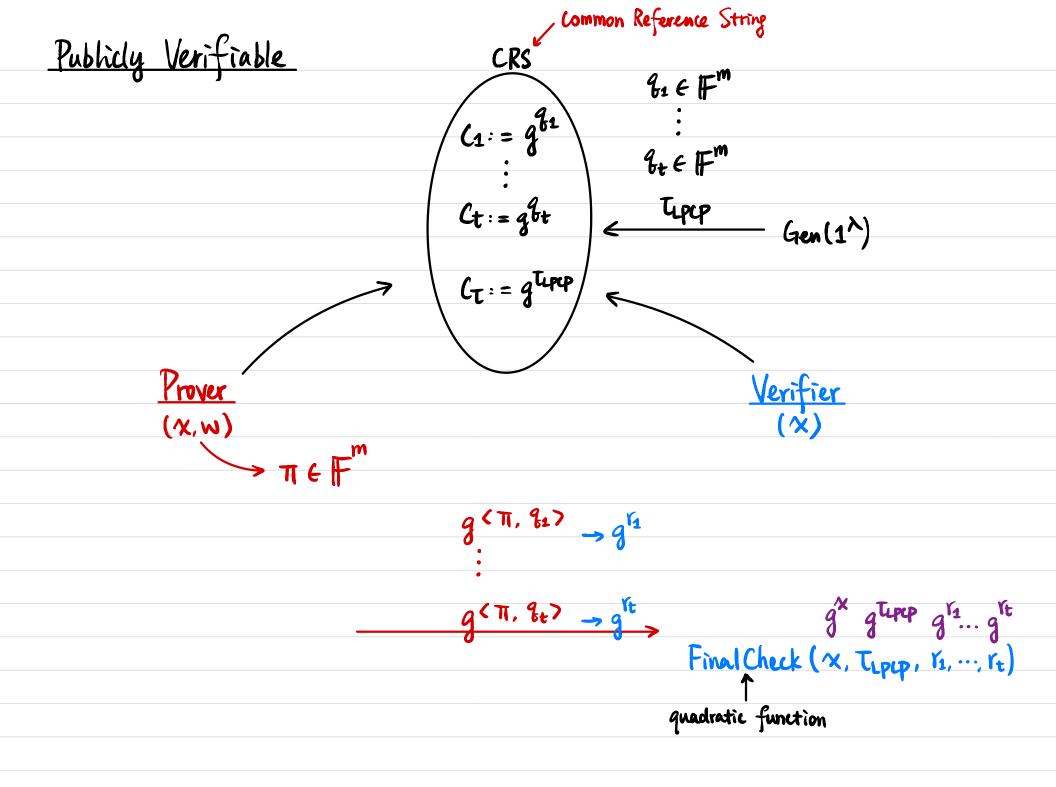
#### Is it ZK?





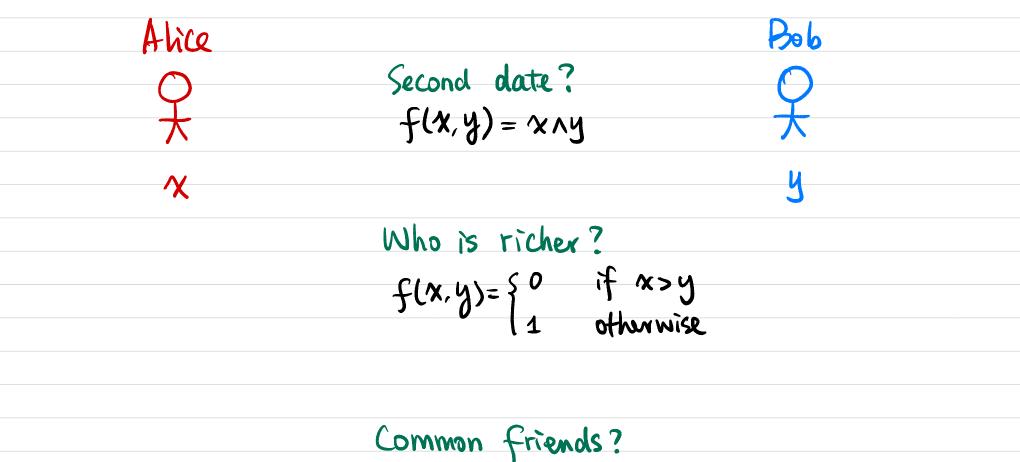
- From Walsh-Hadard code,  $m = O(|c|^2)$
- From quadratic span programs, m=O(ICI)



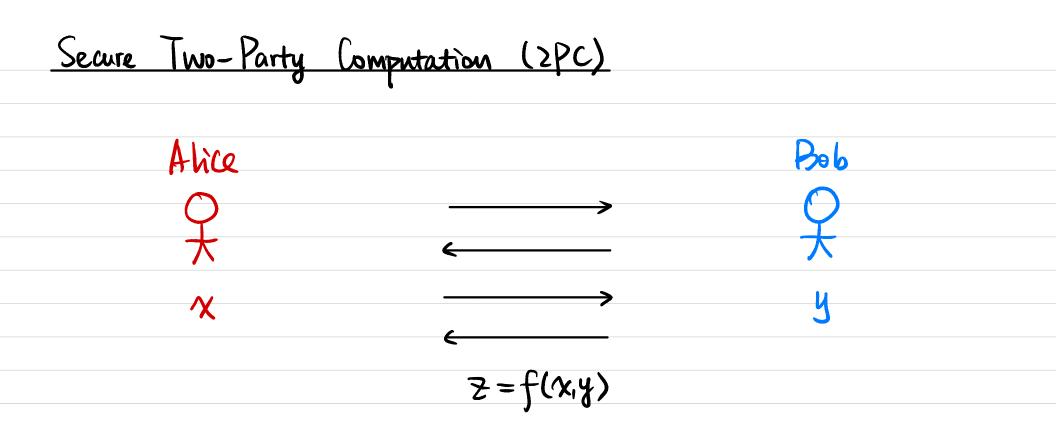


Bilinear Pairings  
Cyclic groups 62. 62. 67 with generators 
$$g_2, g_3, g_7$$
, respectively.  
 $e: G_2 \times G_2 \longrightarrow G_7$   
 $e(g_2^A, g_2^b) = g_7^{Ab}$   
Symmetric peiring:  
 $e: G \times G \longrightarrow G_7$   
 $e(g^A, g^b) = g_7^{Ab}$ 

Secure Multi-Party Computation



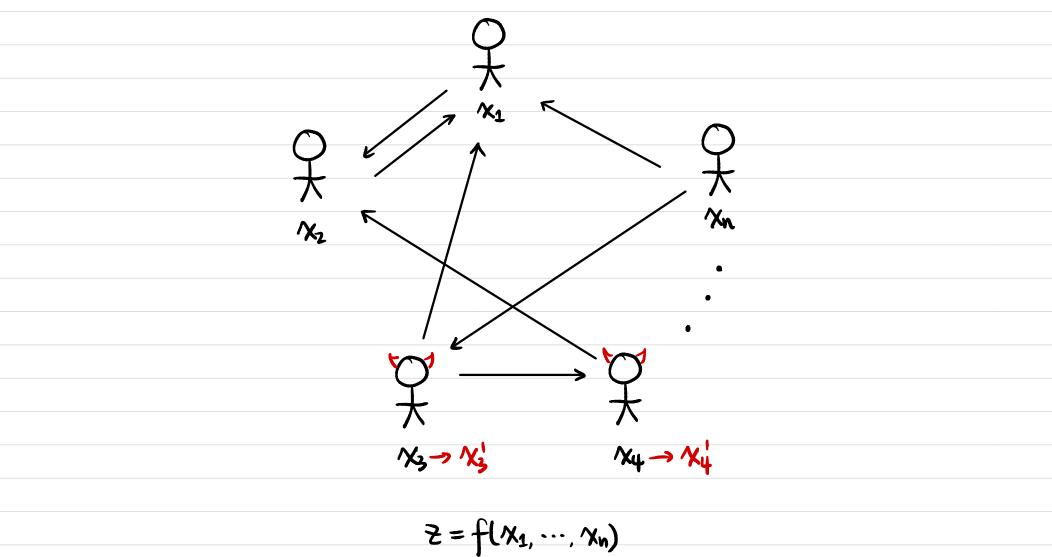
 $f(x, \gamma) = \chi \cap \gamma$ 



### Applications:

- Password Breach Alert (Chrome/Firefox/Azure/iOS Keychain)
- Privacy-Preserving Contact Tracing for COVID-19 (Apple & Google)
- Ads Conversion Measurements / Personalized Advertising (Google/Meta)

## Secure Multi-Party Computation (MPC)



## Secure Multi-Party Computation (MPC)

## Applications:

- Privacy-Preserving Inventory Matching (J.P. Morgan)
- Setup Ceremony to securely generate CRS (Zcash)
- Distributed Key Management (Unbound / Coinbase)
- Federated Learning (Google Keyboard Search Suggestion)
- Auctions (Danish Sugar beet auction)
- Boston gender wage gap (Boston Women's Workforce Council)
- Study / Analysis on Medical Data
- Fraud Detection (banks)

Setting

- n parties Pi, Pz, ..., Pn
   with private inputs X1, X2, ..., Xn
- · Jointly compute  $f(X_1, X_2, ..., X_n)$
- Communication:
   Authenticated secure point-to-point channels between each pair (Pi, Pj)
   (Sometimes also assume broadcast channel)

What properties do we want?

General Security Properties · Correctness: The function is computed correctly. · Privacy. Only the output is revealed. · Independence of Inputs: Parties cannot choose inputs depending on others' inputs · Security with Abort: Adversary may "abort" the protocol. (preventing honest parties from receiving the output) · Fairness: If one party receives output, then all receive output. · Guaranteed Output Delivery (GOD): Honest parties always receive output.

### Adversary's Power

### Allowed adversarial behavior.

· Semi-honest/passive/honest-but-curious:

Follow the protocol description honestly,

but try to extract more information by inspecting transcript.

· Malicious /active:

Can deviate arbitrarily from the protocol description.