

Topic 13

Evaluating Pose Likelihood

A photograph of a lighthouse at night. The lighthouse is illuminated from below, and several powerful searchlights are directed upwards from the top of the lighthouse, creating a fan of light beams against the dark night sky. The surrounding area is dark, with some distant lights visible on the horizon.

Range and Bearing Estimation

Particle filter recap

posterior

likelihood

dynamics

prior

$$p(\mathbf{x}_k | \mathbf{Z}_k) = \alpha p(\mathbf{Z}_k | \mathbf{x}_k) \int p(\mathbf{x}_k | \mathbf{x}_{k-1}) p(\mathbf{x}_{k-1} | \mathbf{Z}_{k-1})$$

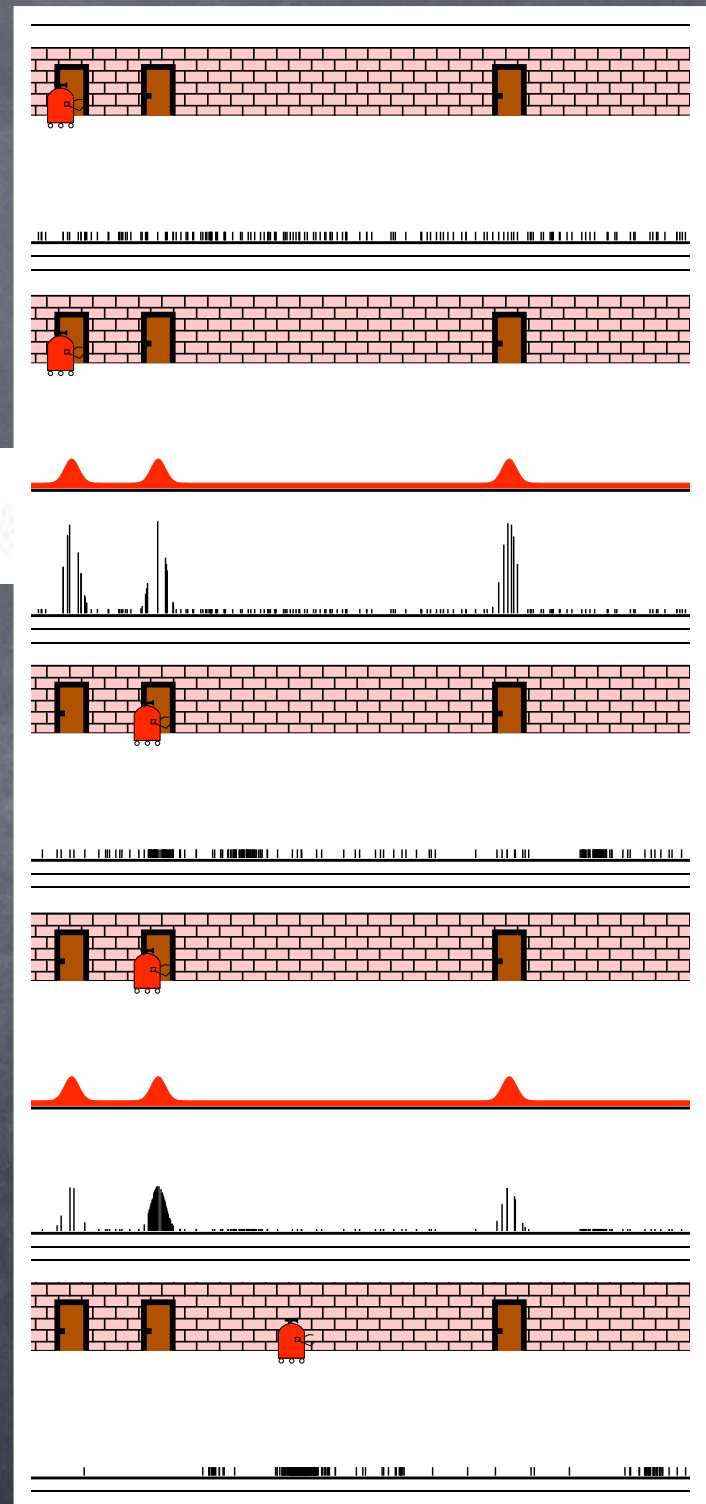
“belief
at t=k”

“update”

“predict”

“belief
at t=k-1”

- Bayes filter model to estimate true pose from all possible poses
- recursive Markovian inference over time with predict-update loop
- Particle filter algorithms predict-update with sample set of poses



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dynamics

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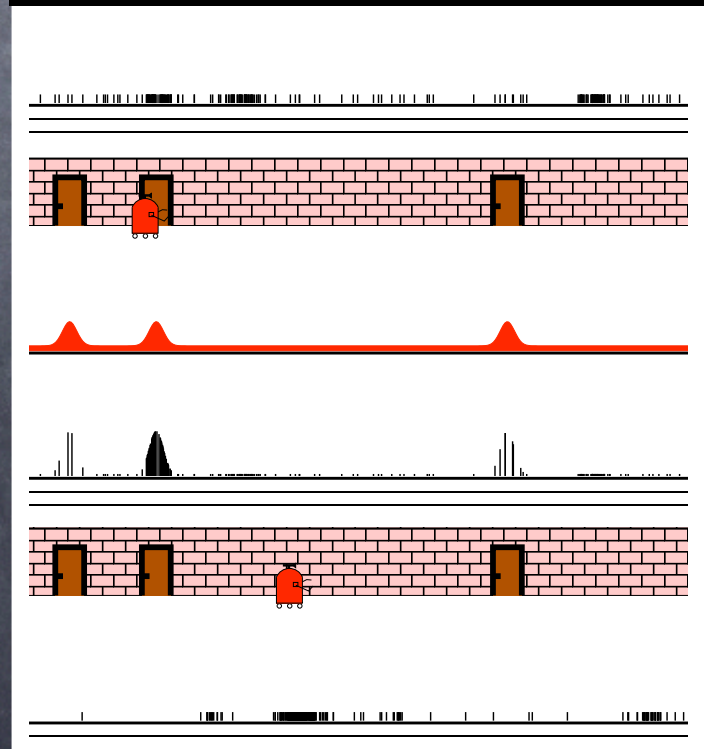
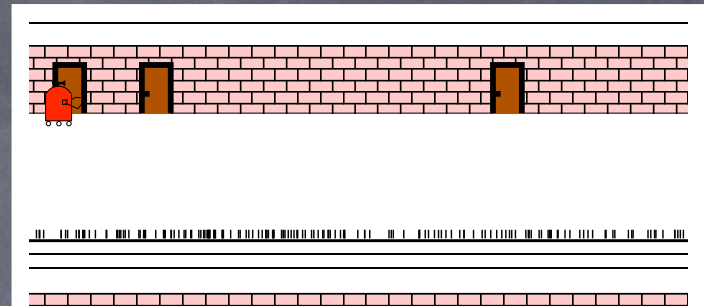
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What are we still missing to compute localization?



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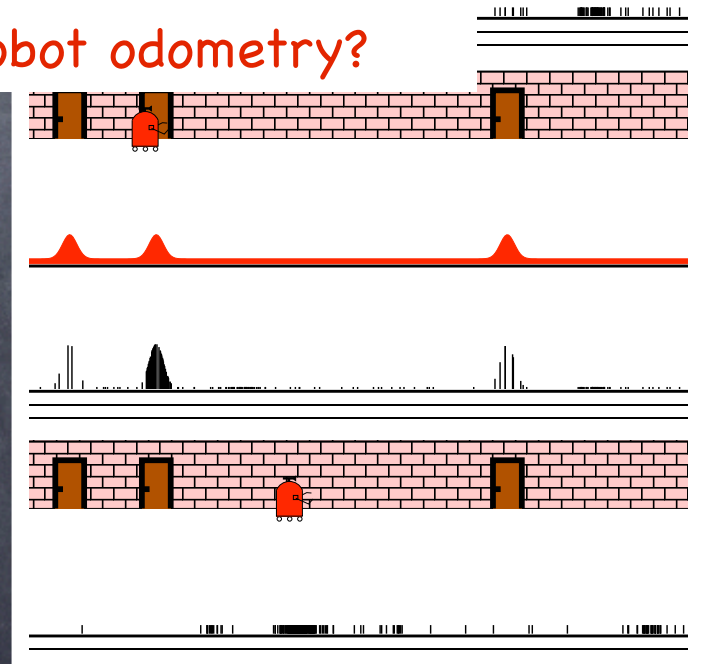
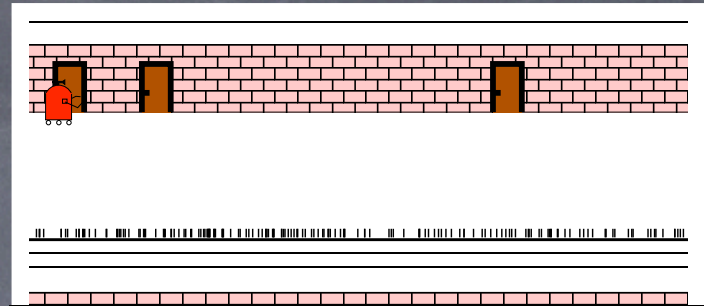
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How to evaluate the likelihood of a pose given robot observations?

How to predict a new belief given robot odometry?

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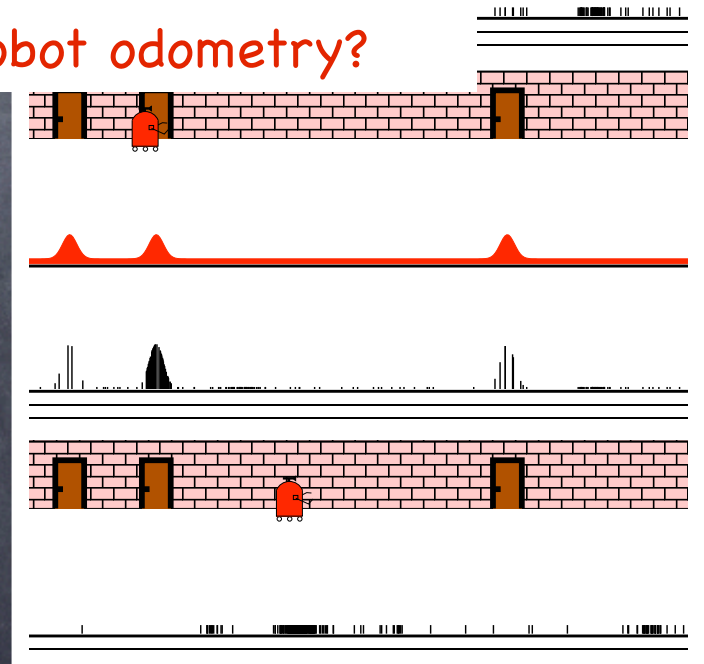
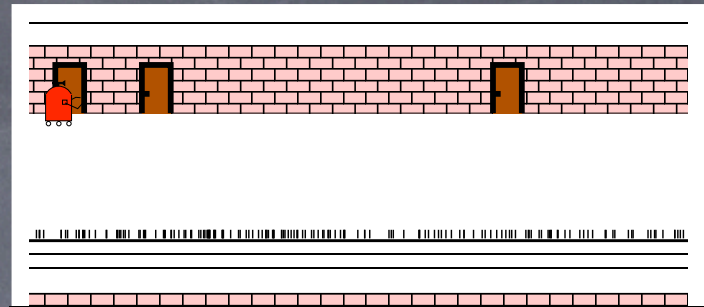
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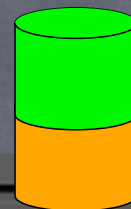
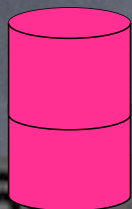
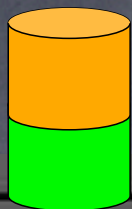
How to predict a new belief given robot odometry?

- recursive Markovian inference over time with predict-update loop
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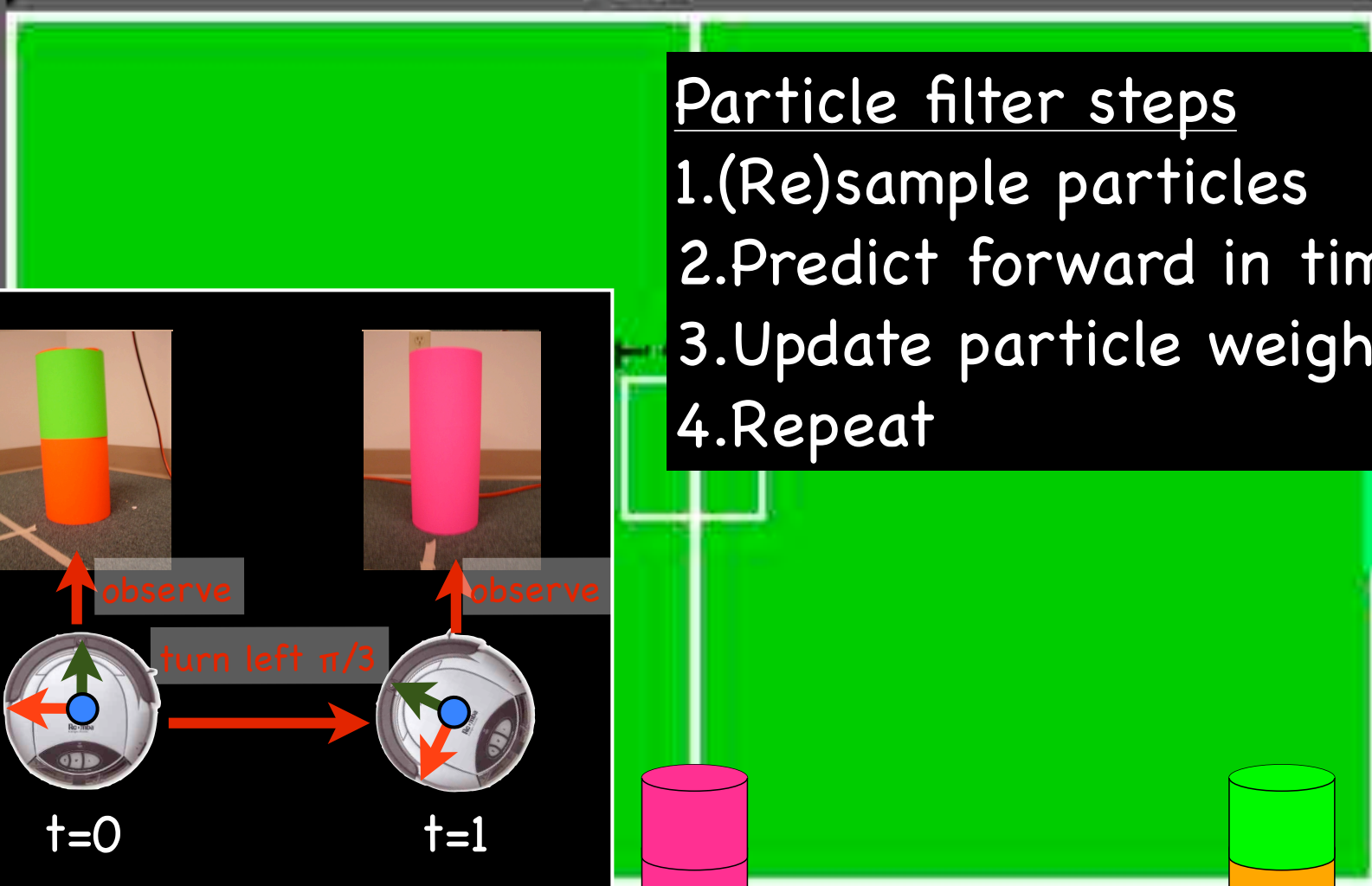
What are we still missing to compute localization?



suppose the robot starts by seeing this landmark, then turns left, and then sees another landmark



380



Particle filter steps

1. (Re)sample particles
2. Predict forward in time
3. Update particle weights
4. Repeat



observe



observe

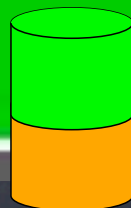
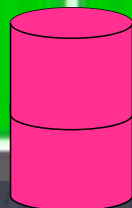


t=0

turn left $\pi/3$

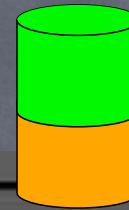
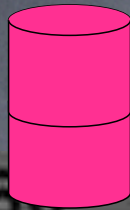
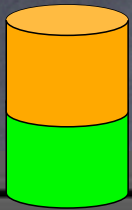


t=1



260

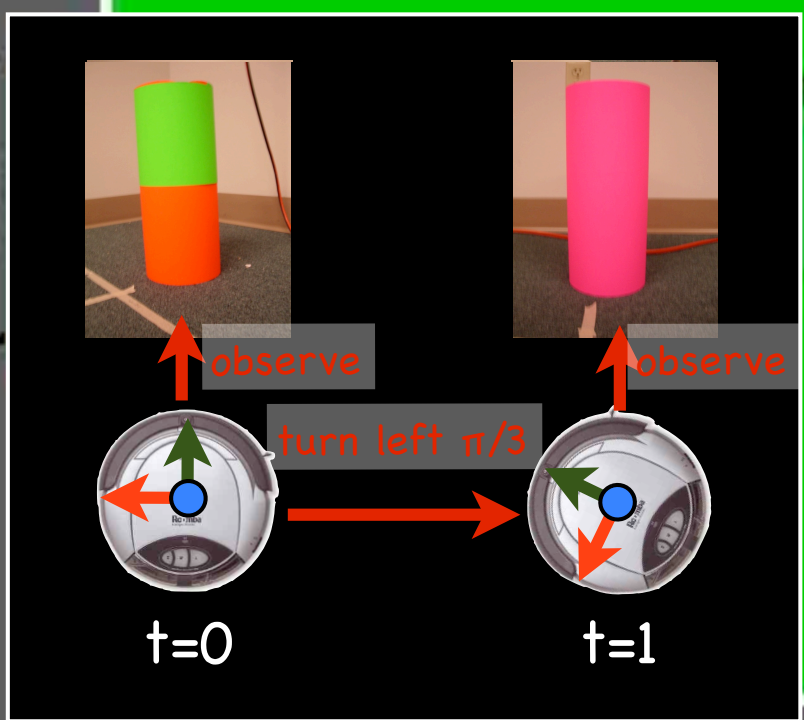
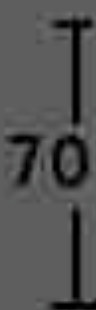
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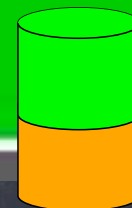
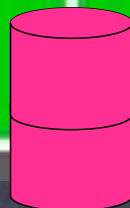
Initially, the robot has no observations

Particle filter steps

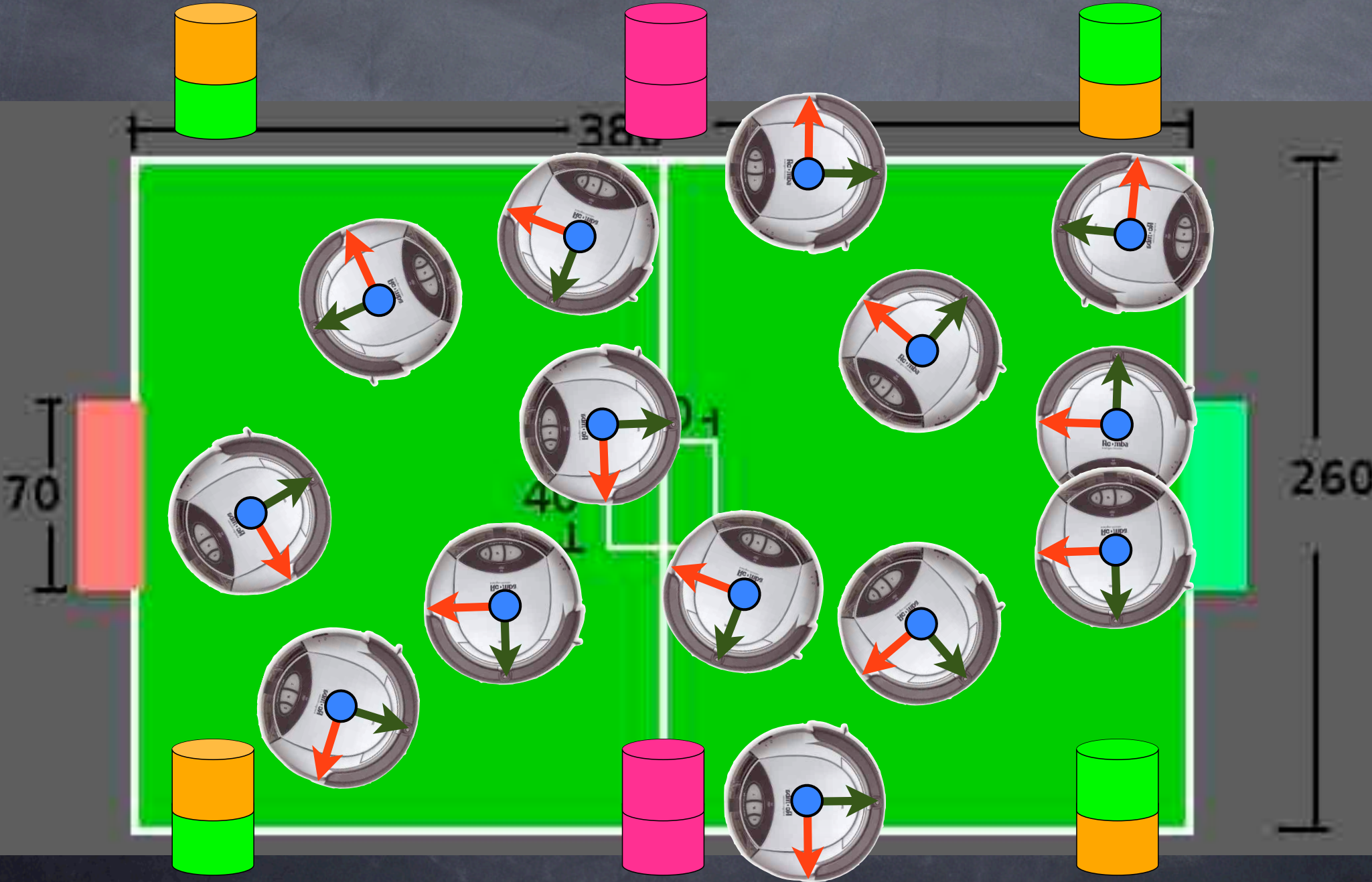
1. (Re)sample particles
2. Predict forward in time
3. Update particle weights
4. Repeat



What should happen during initial sampling?



poses sampled from a uniform distribution across pitch



poses sampled from a uniform distribution across pitch

Particle filter steps

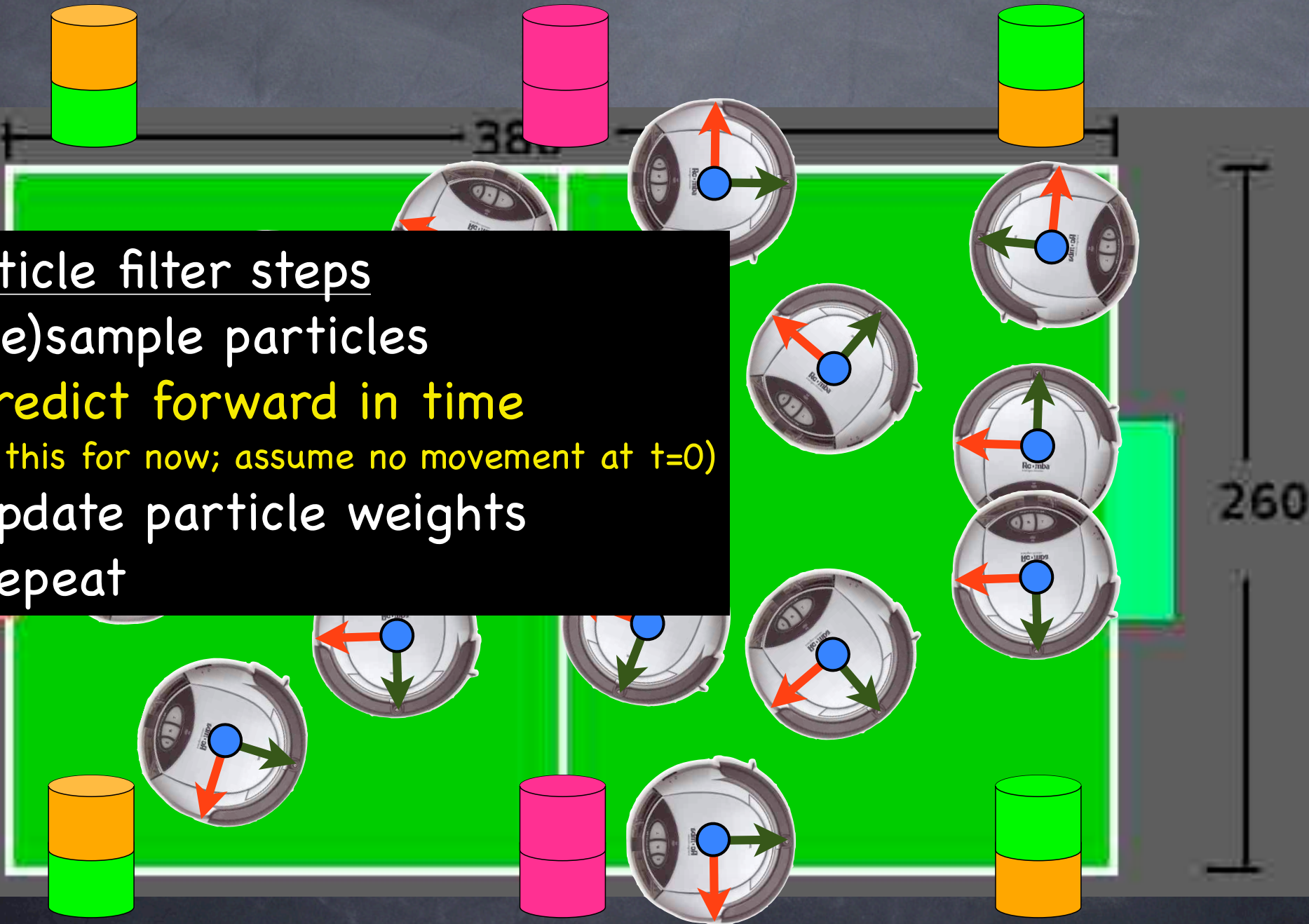
1. (Re)sample particles

2. Predict forward in time

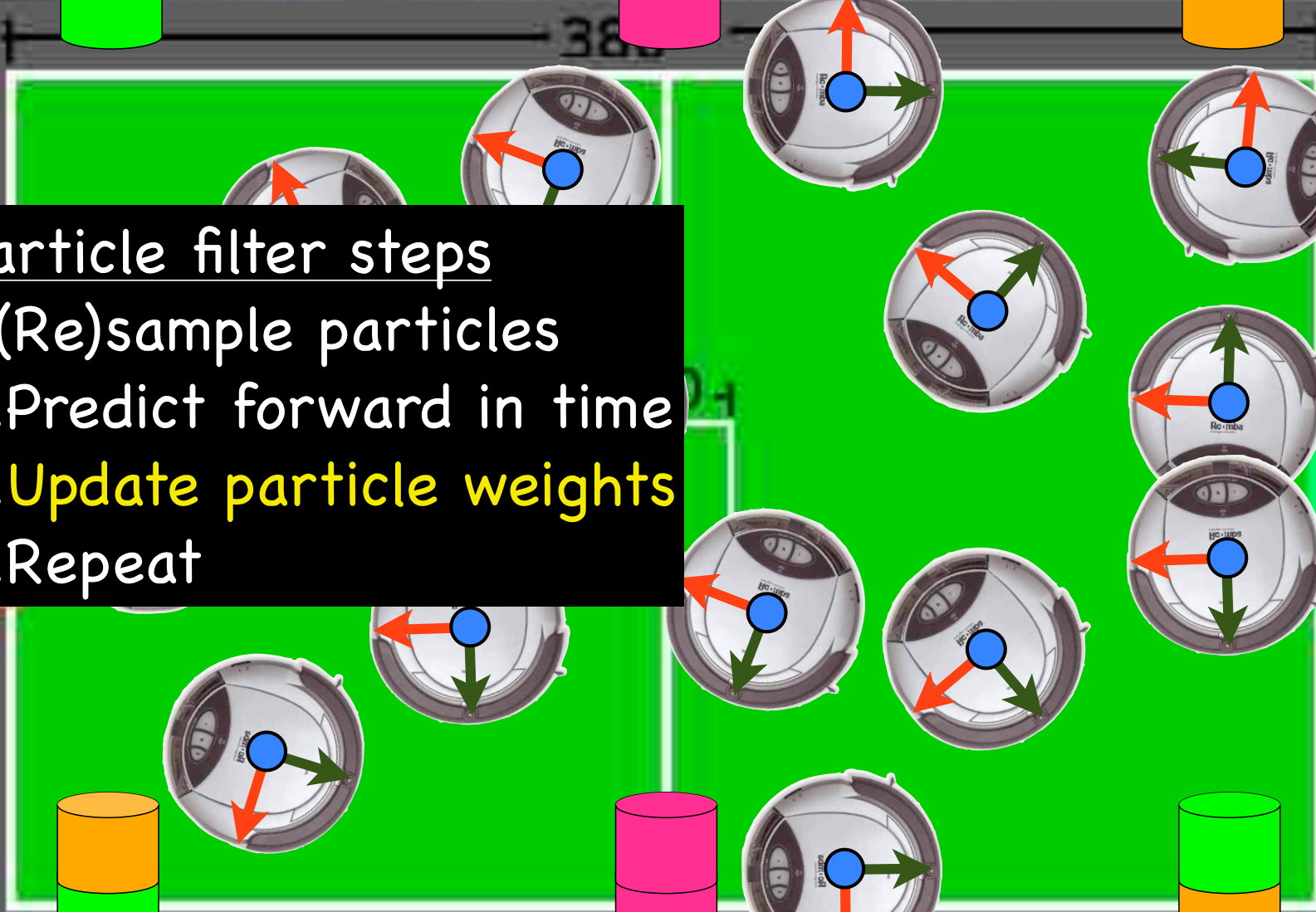
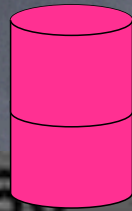
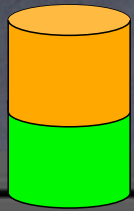
(skip this for now; assume no movement at $t=0$)

3. Update particle weights

4. Repeat

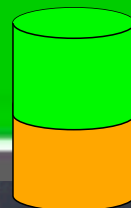
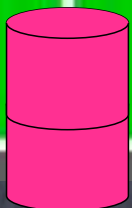
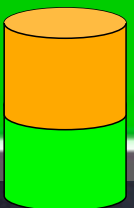


poses sampled from a uniform distribution across pitch

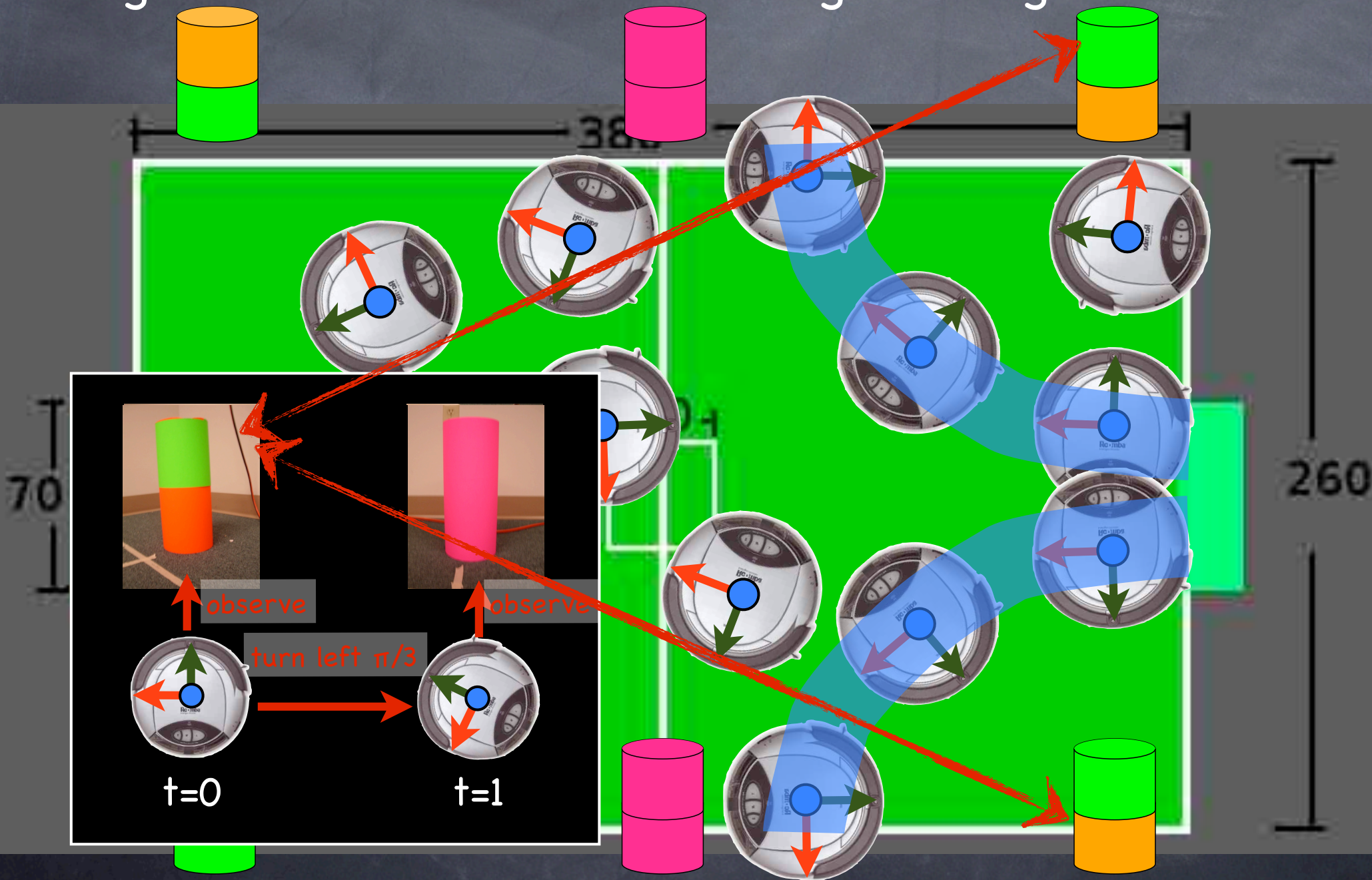


Particle filter steps

1. (Re)sample particles
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4. Repeat



remember from previous example: poses seeing green/
orange landmark should receive higher weights



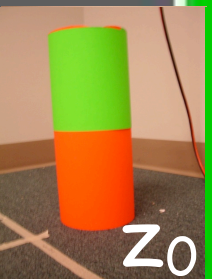
note: belief for particle filter are pose samples weighted by probability (noted by size of ellipse)



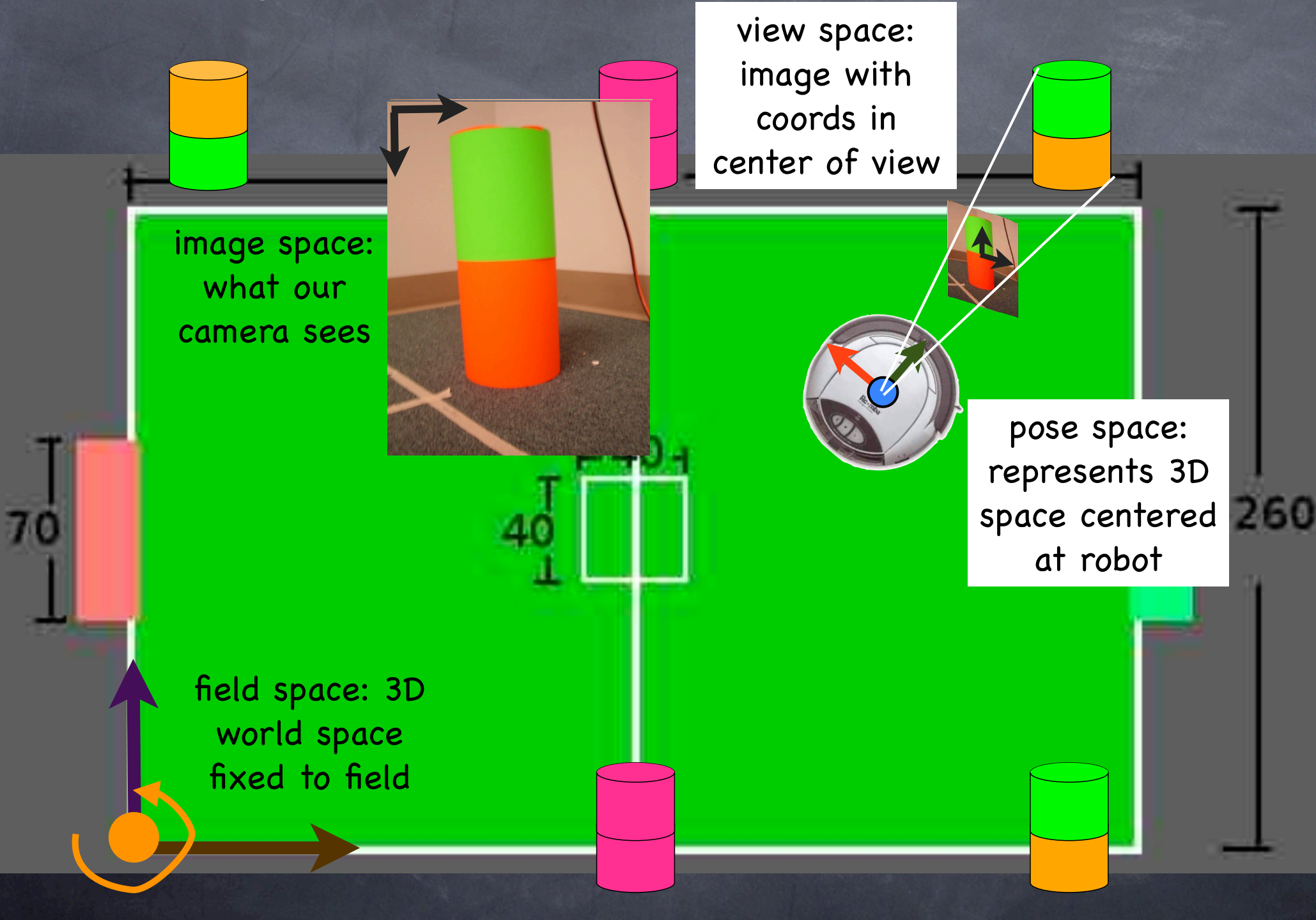
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How to evaluate the likelihood of each pose sample?

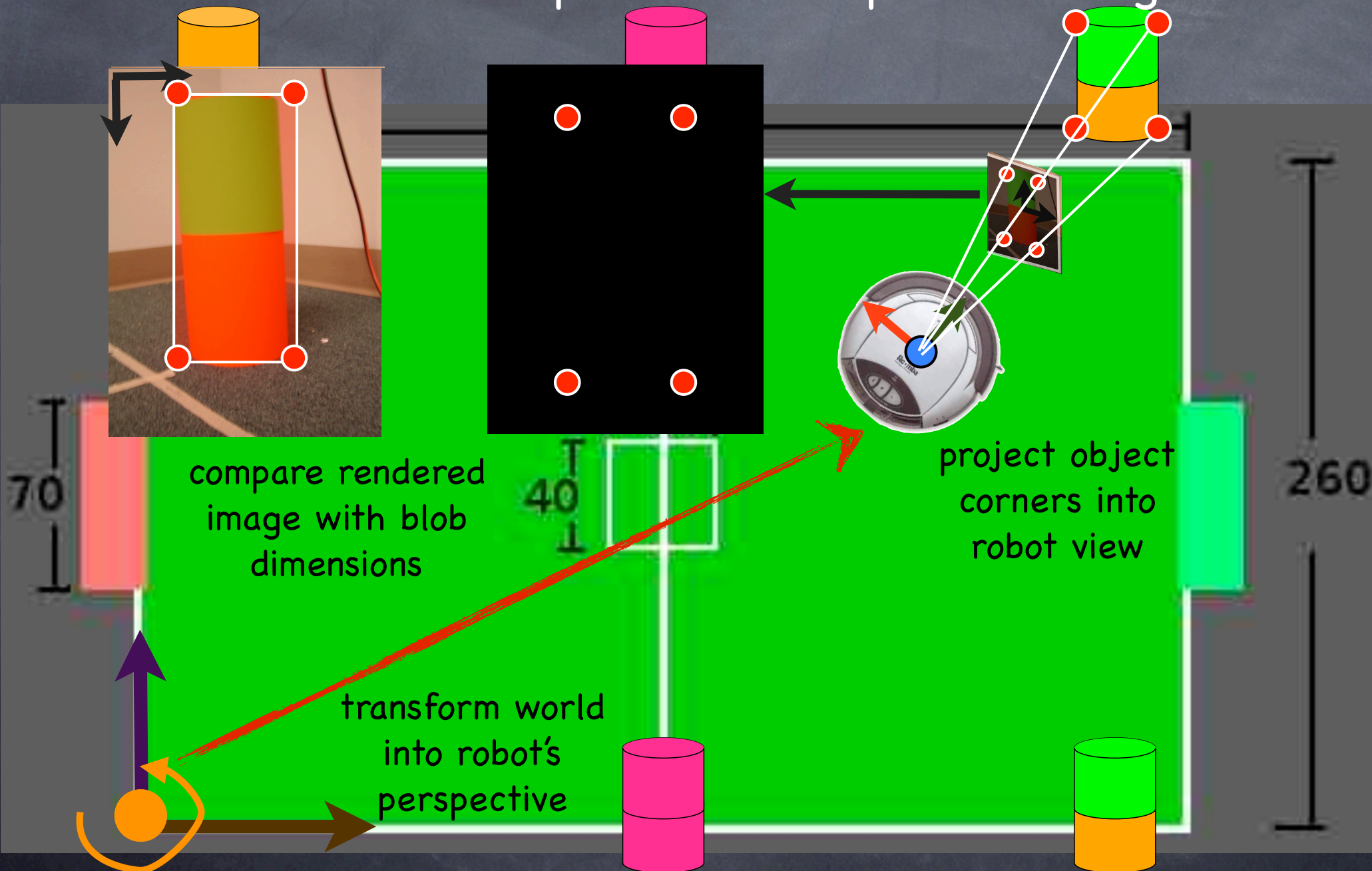
$p(x_0|z_0)$



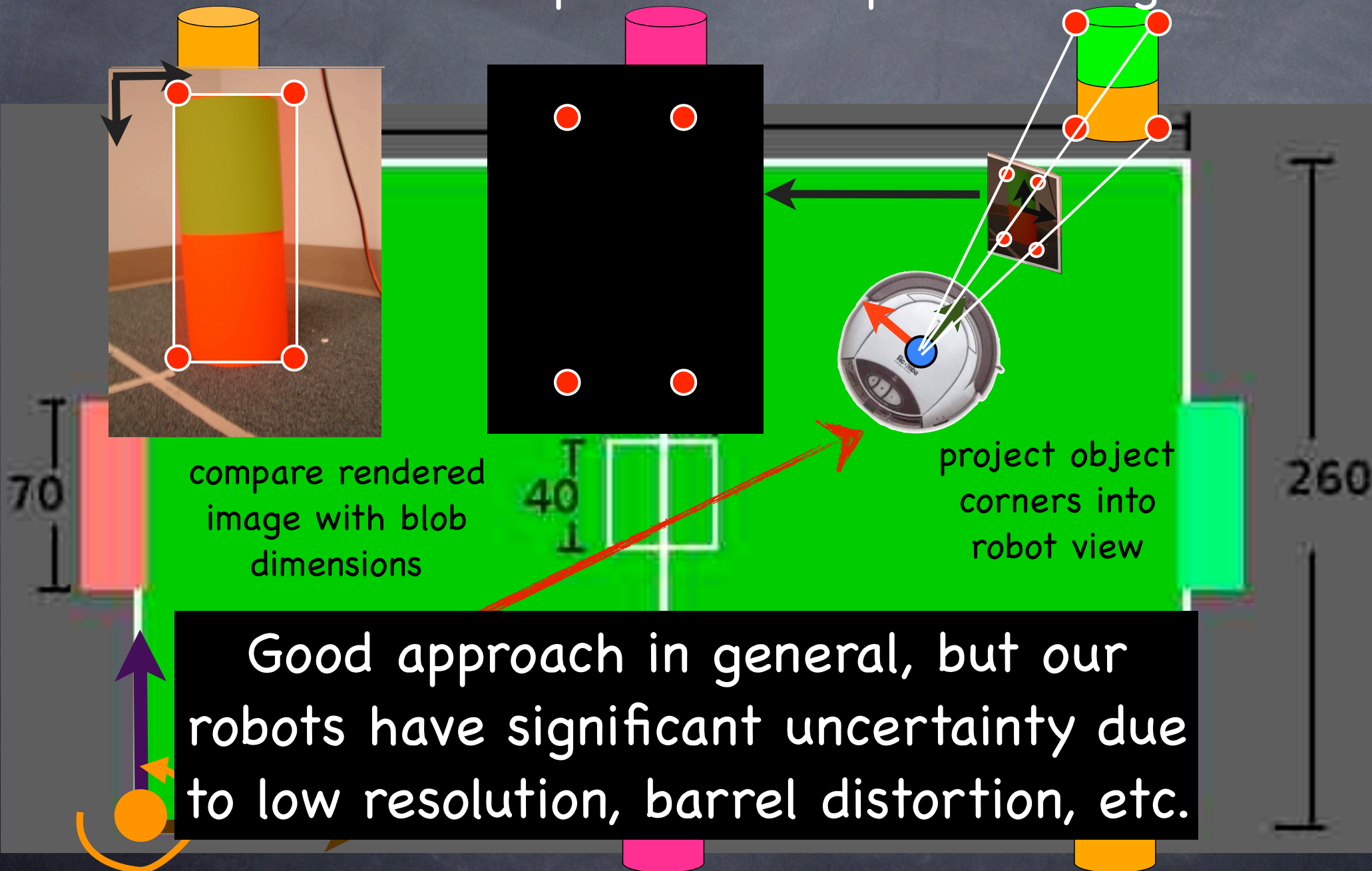
consider again the robot's coordinate spaces



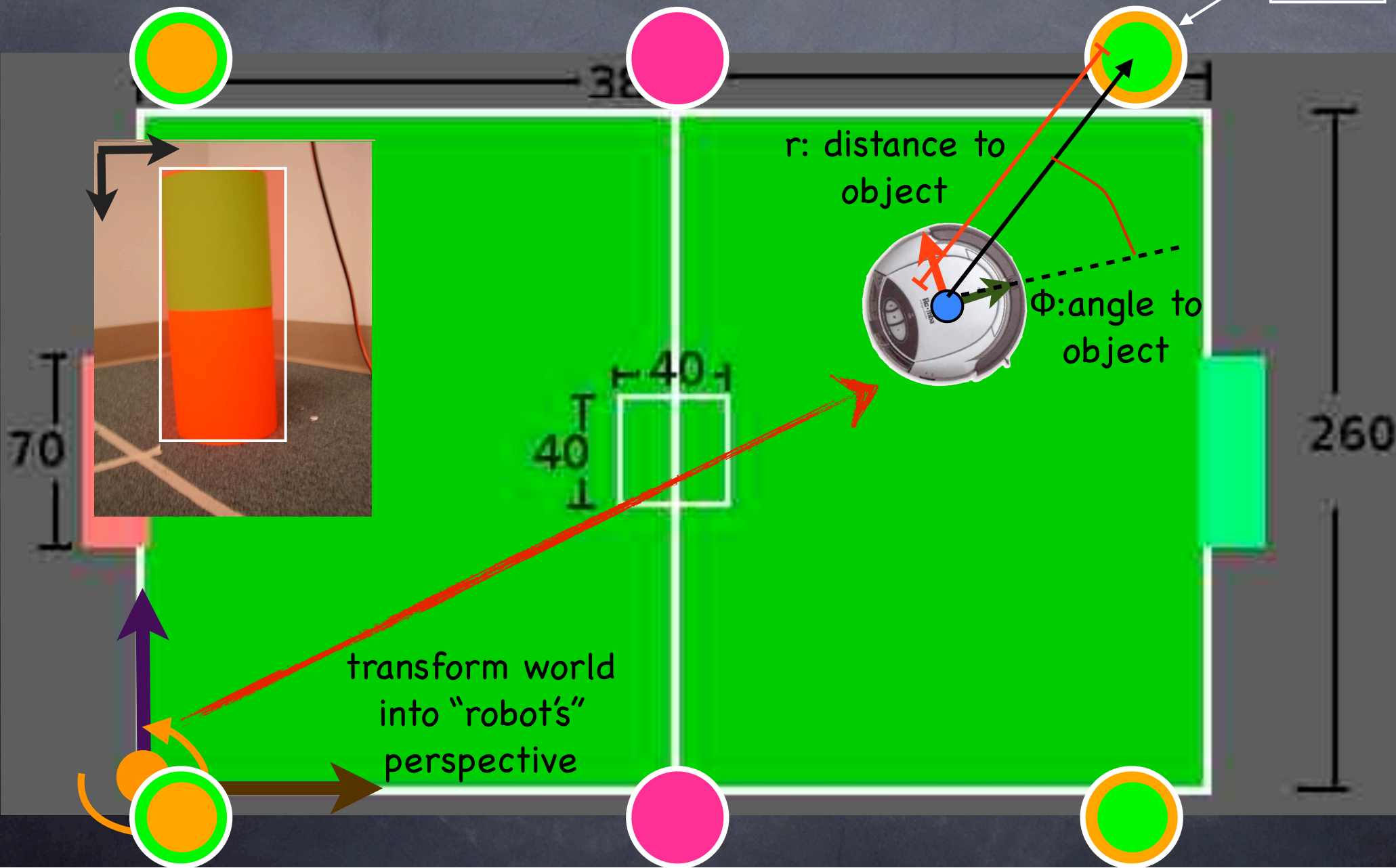
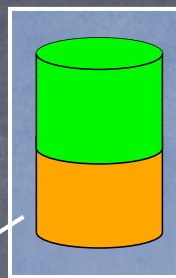
To evaluate a pose, we could graphically render what should be seen at the pose and compare to image



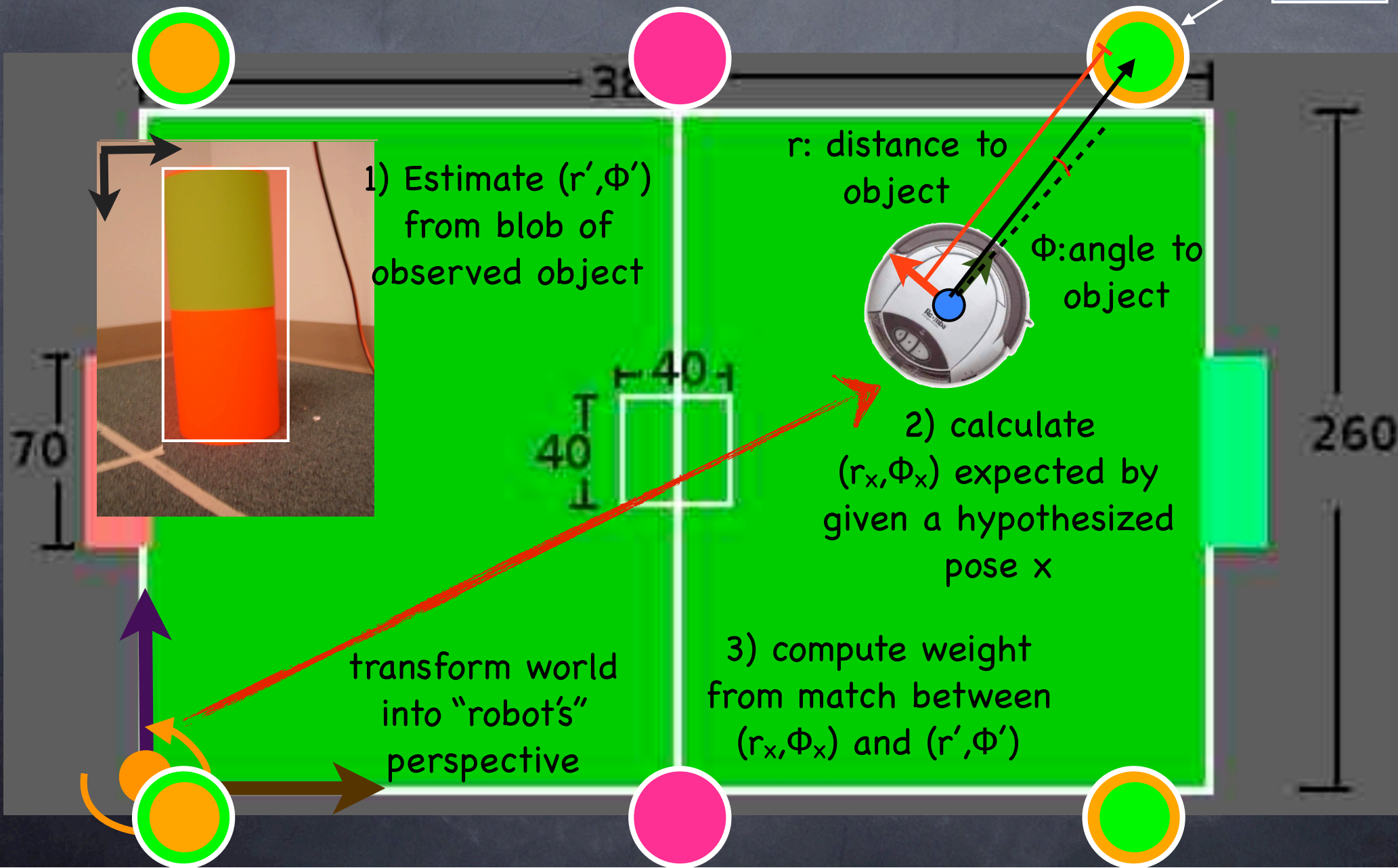
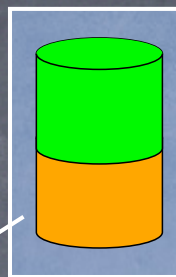
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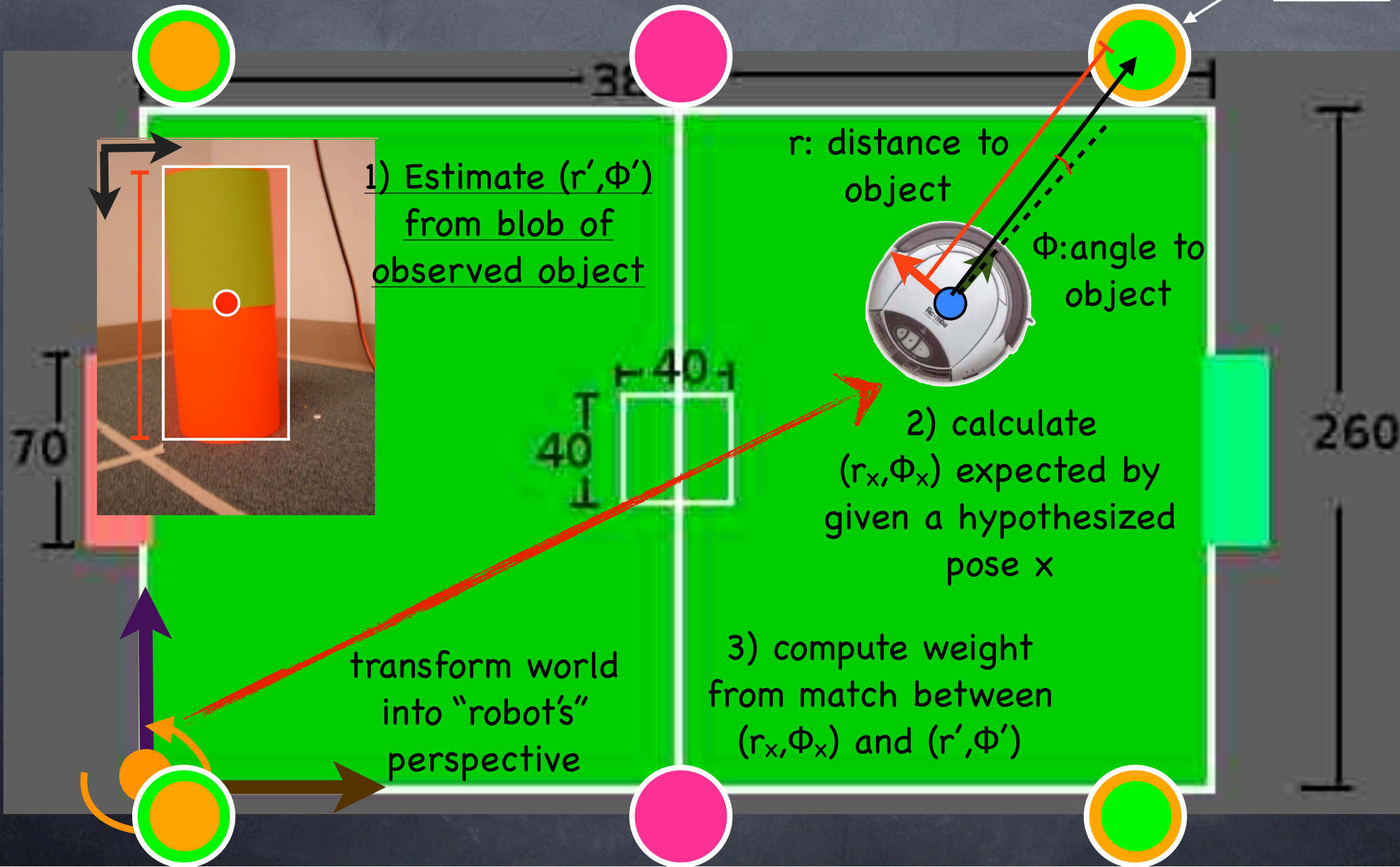
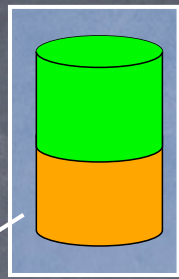
Instead, we will compare the range and bearing of objects in robot pose coordinates



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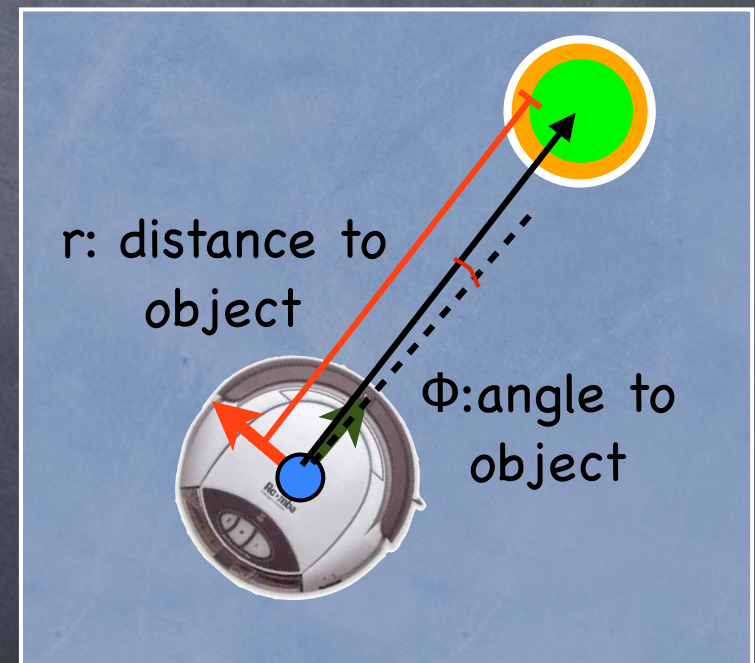
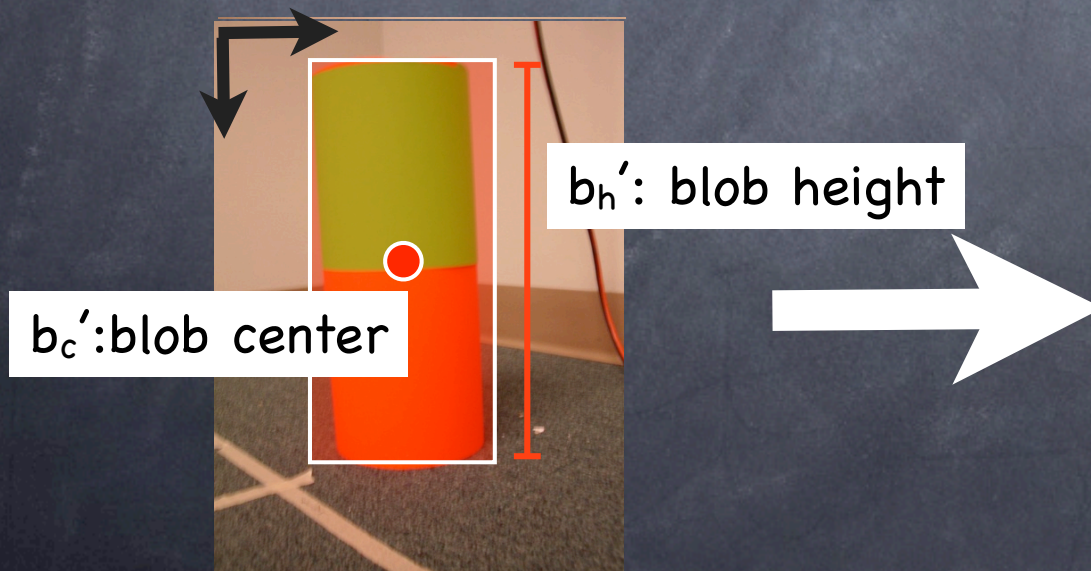


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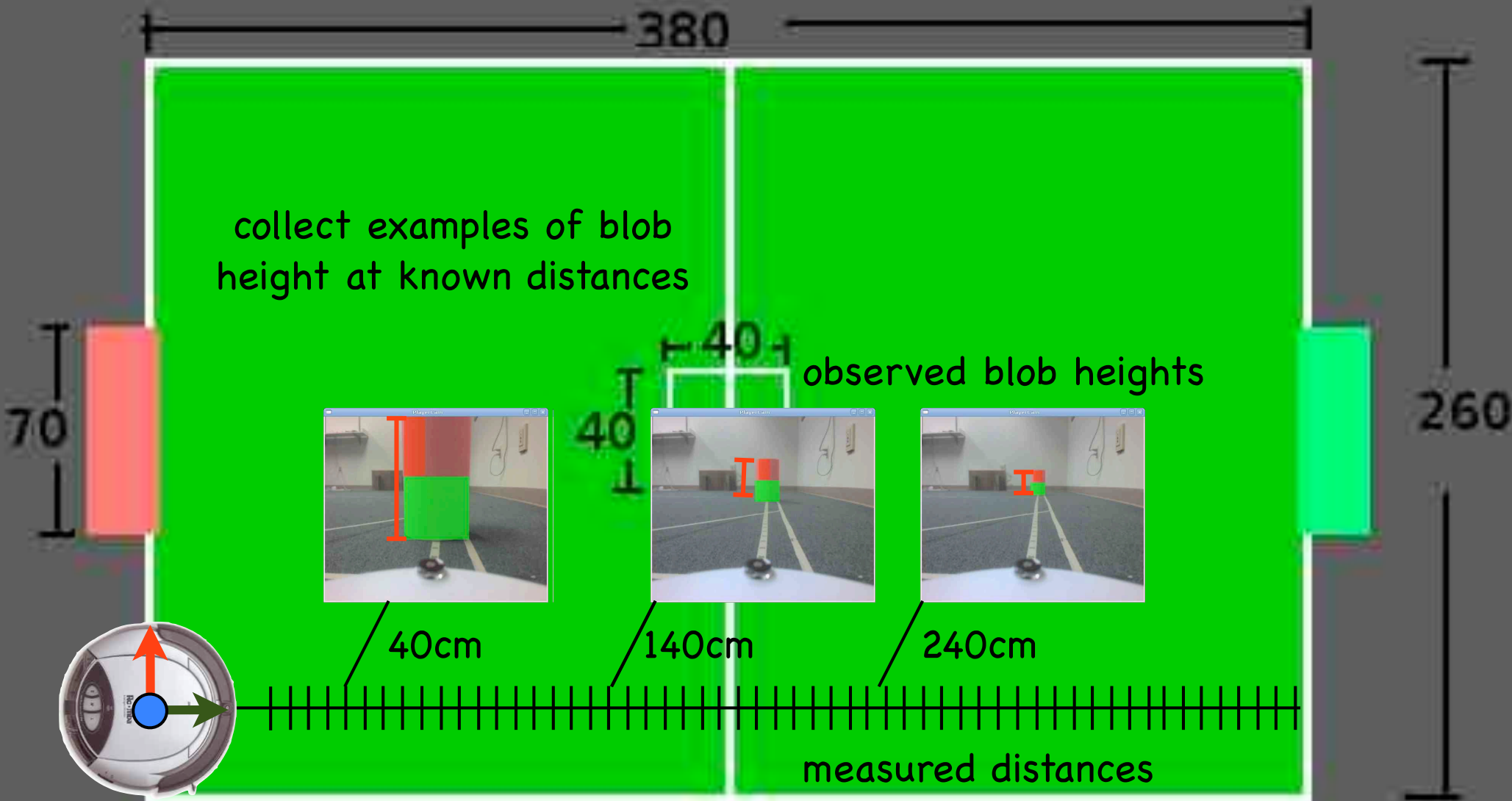
Estimating range and distance from blob

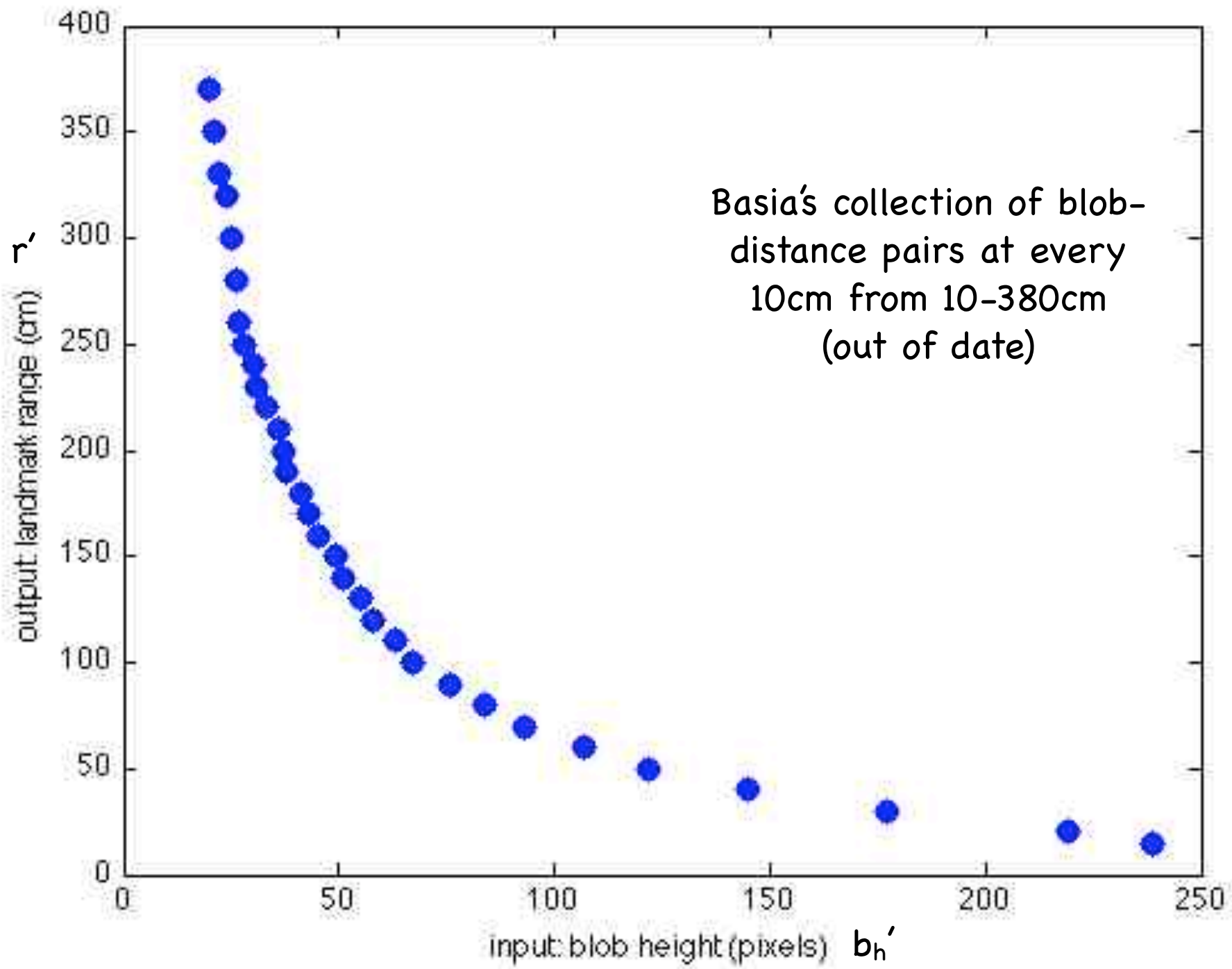
- Construct two functions:
 - Predict object distance from blob height
 - Predict object angle from blob center

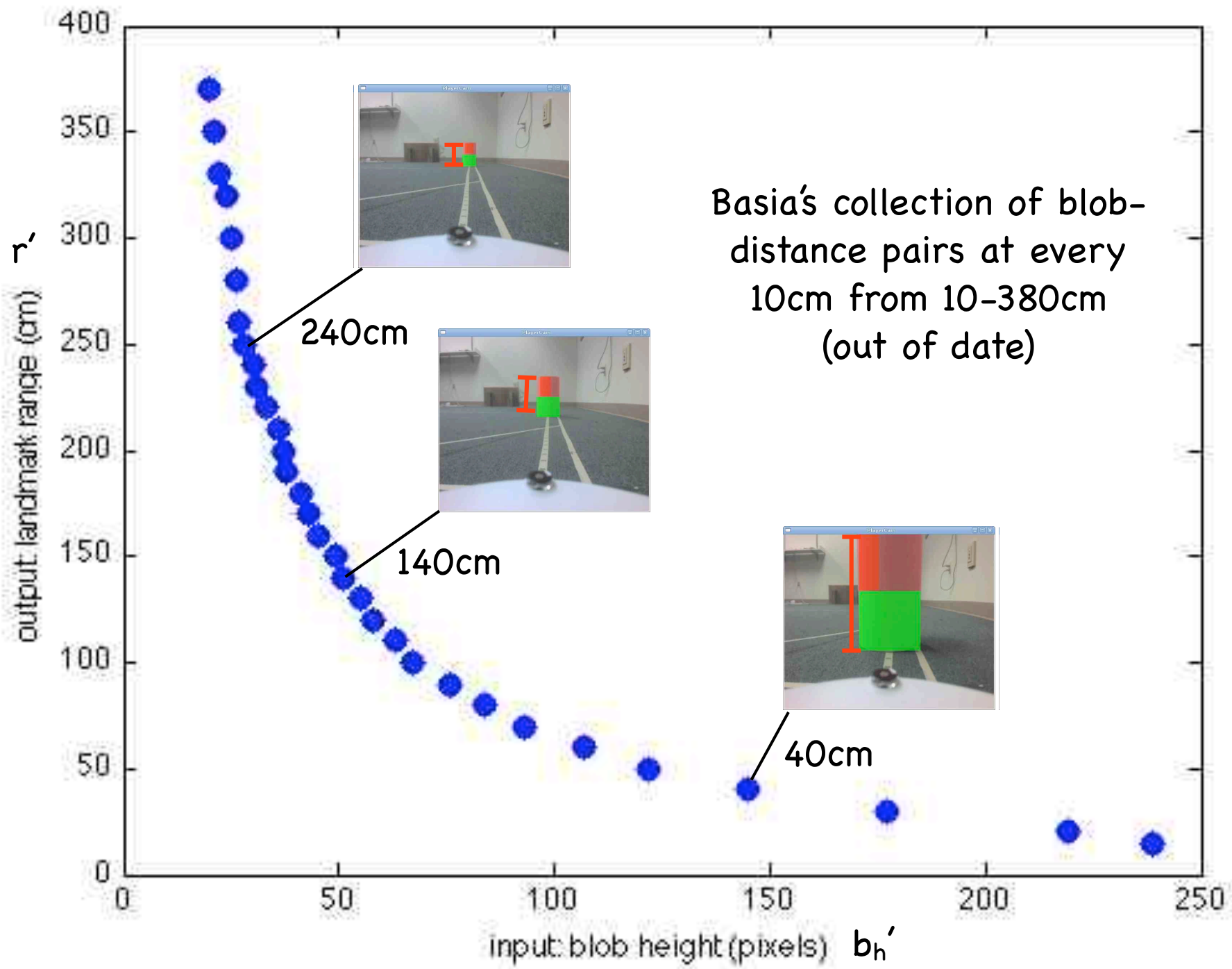


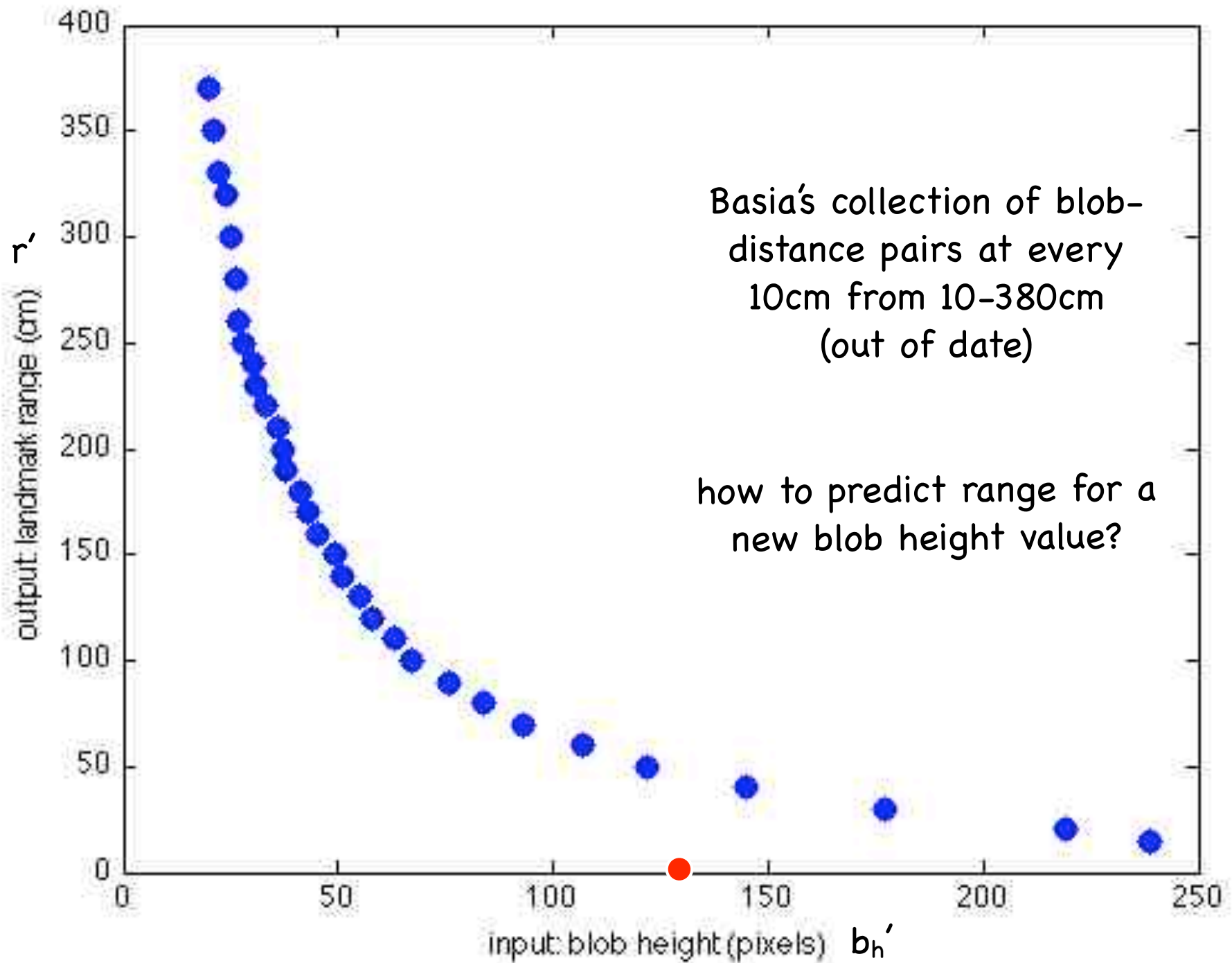
Estimating distance from examples

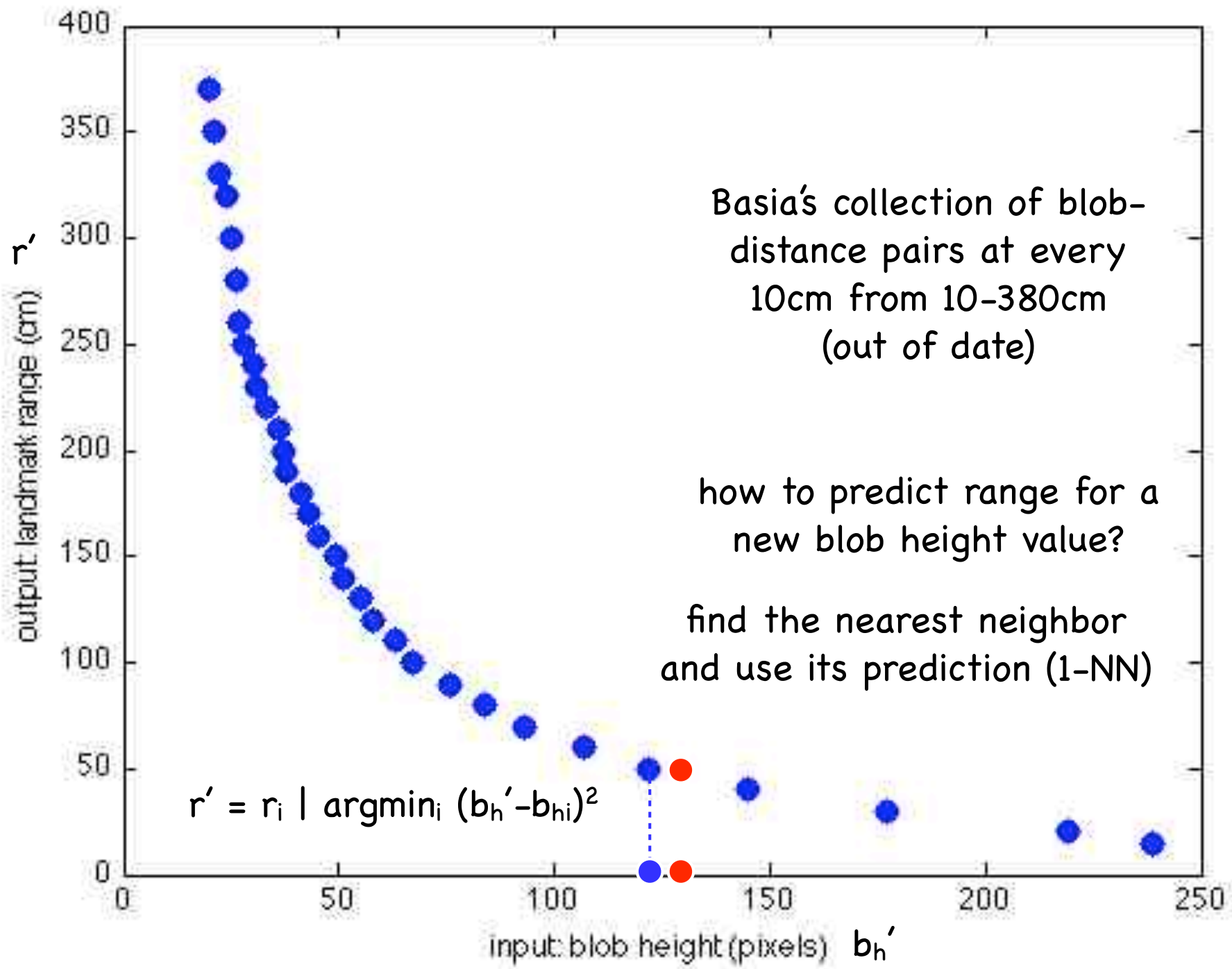
collect examples of blob height at known distances



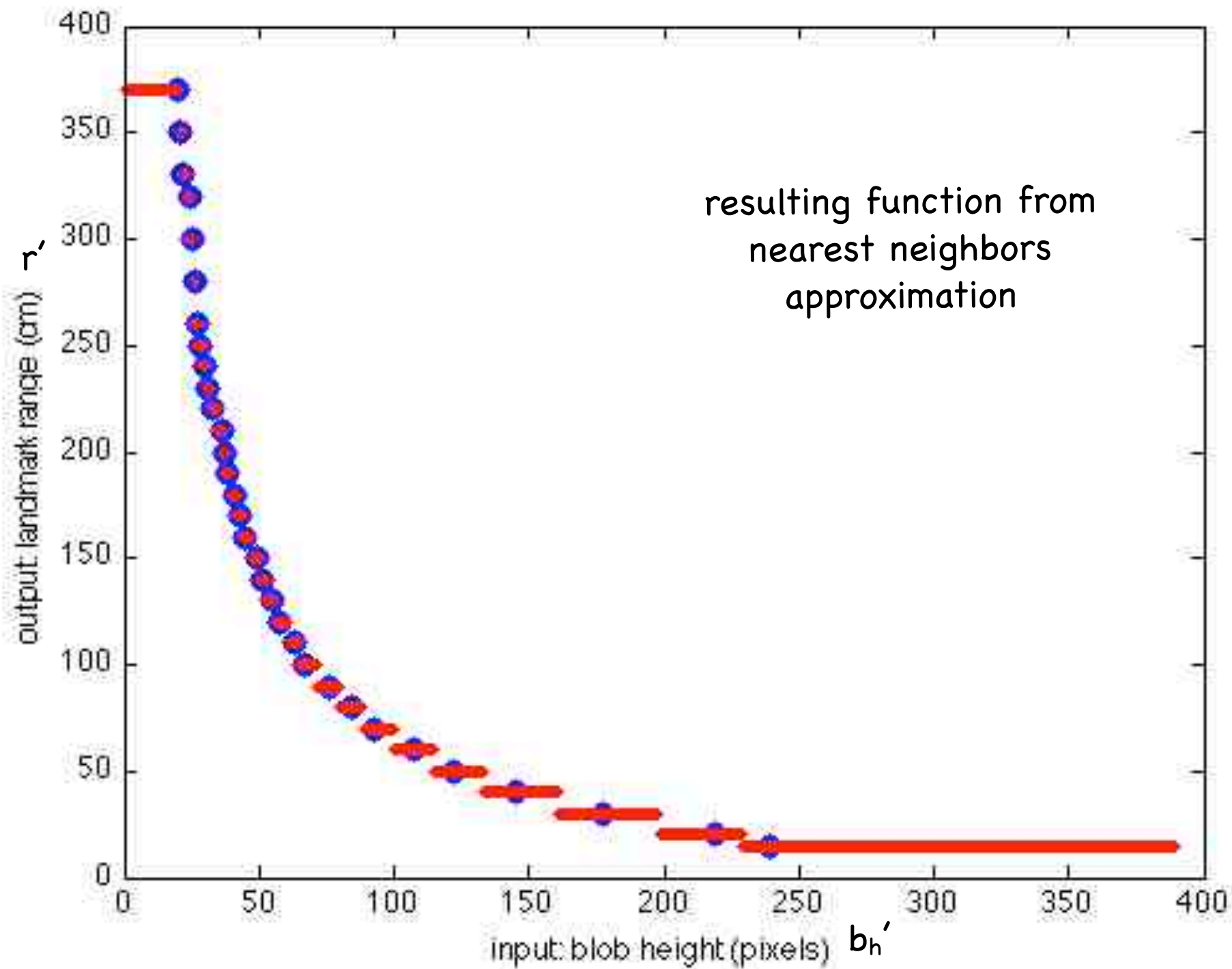


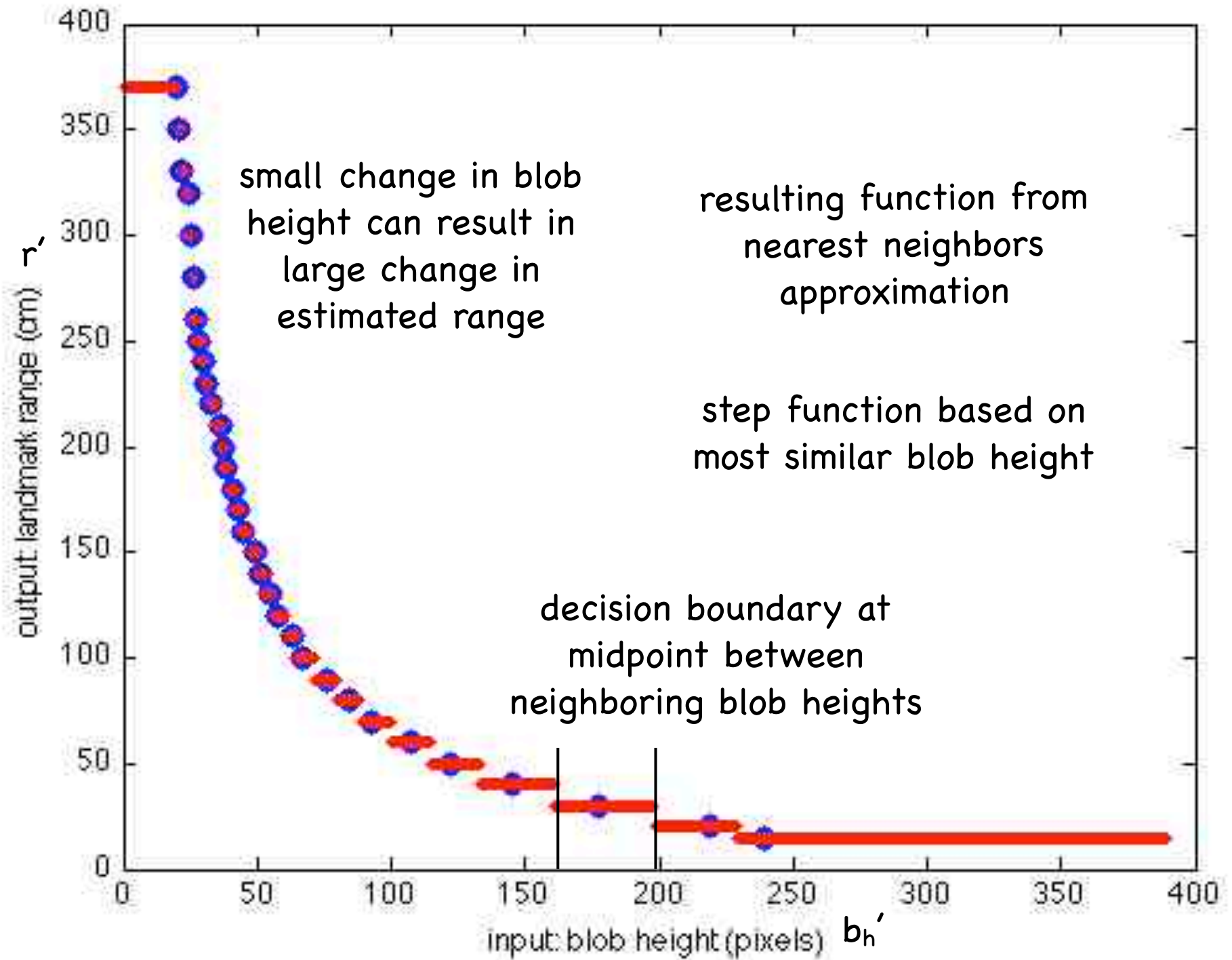


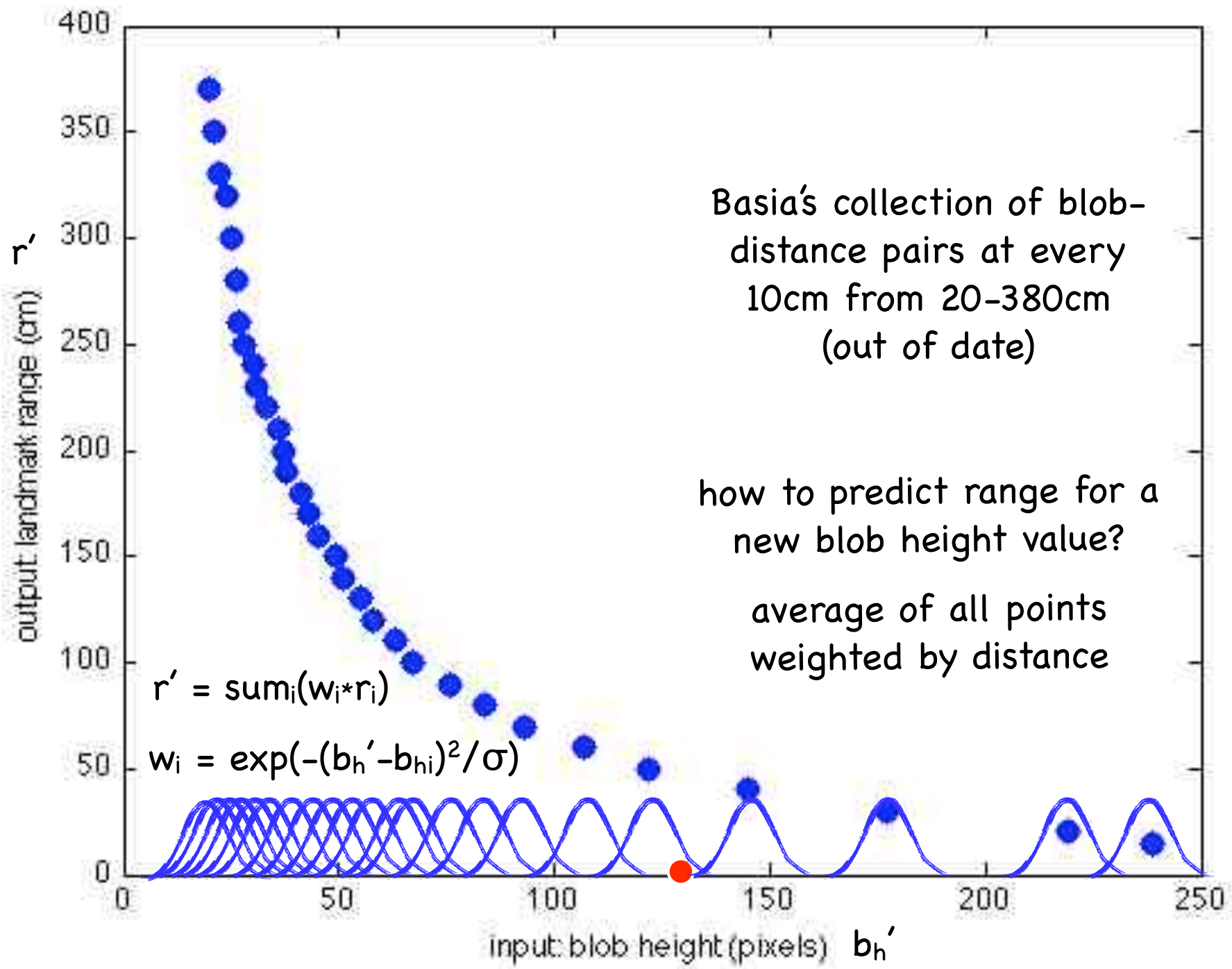


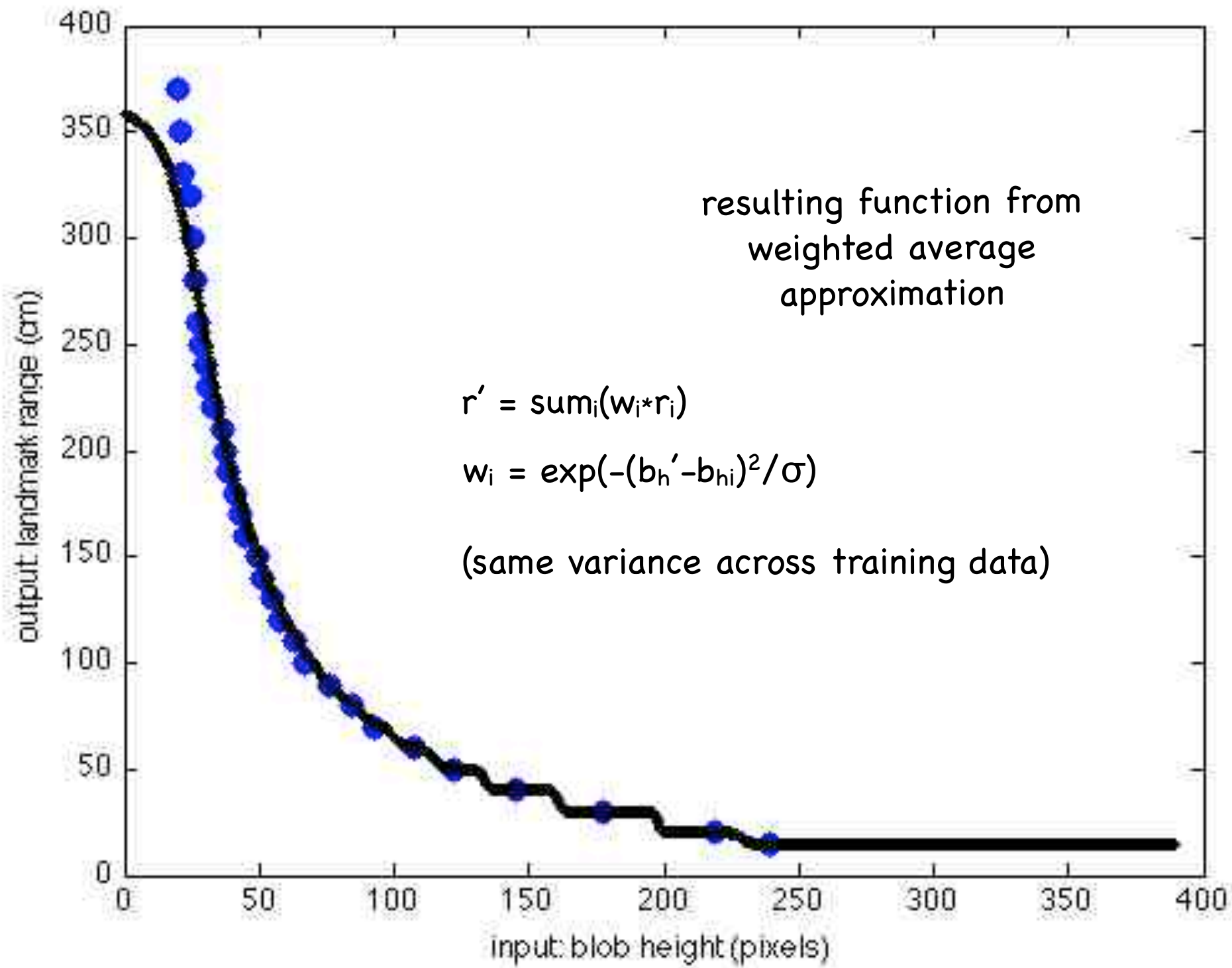


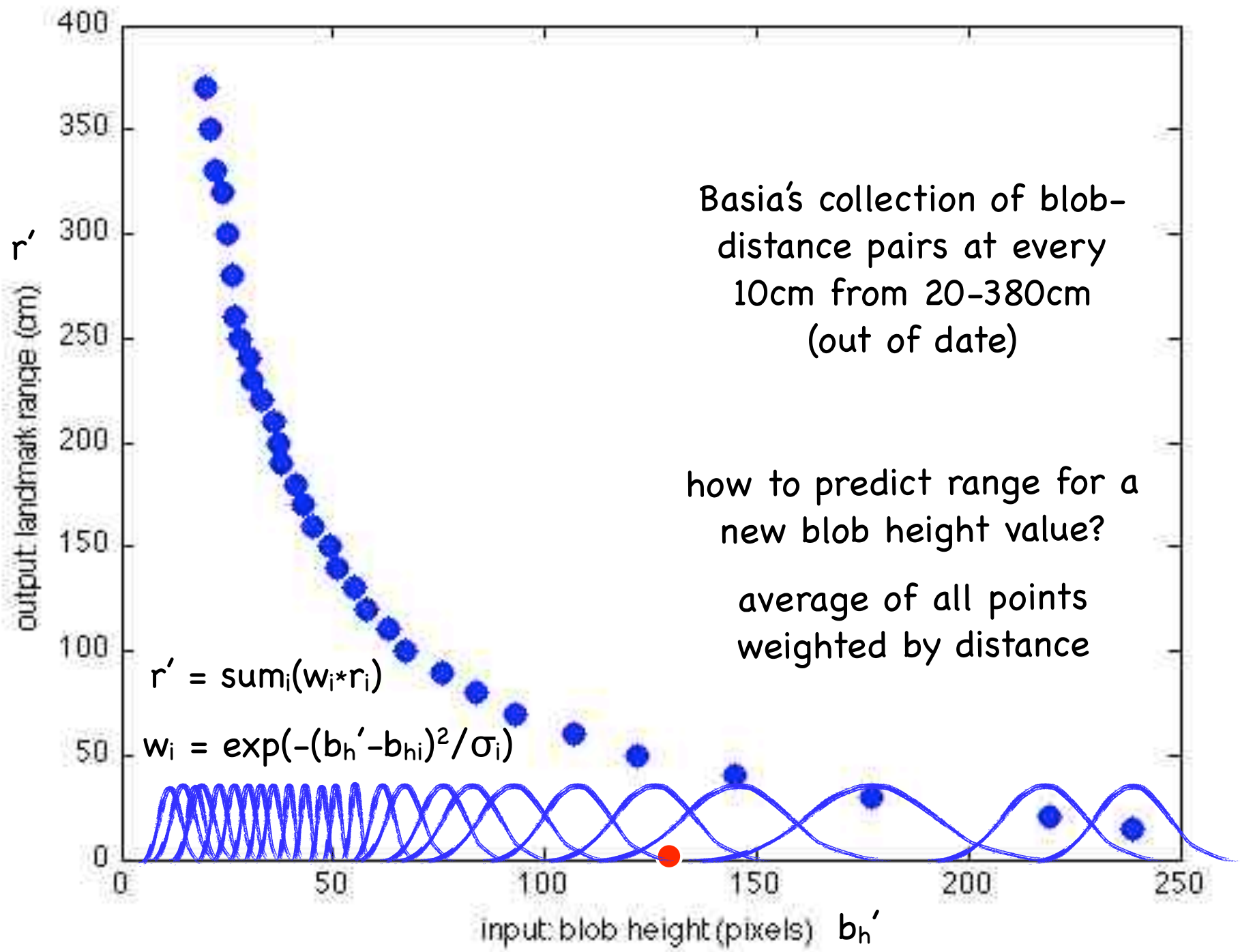
resulting function from
nearest neighbors
approximation

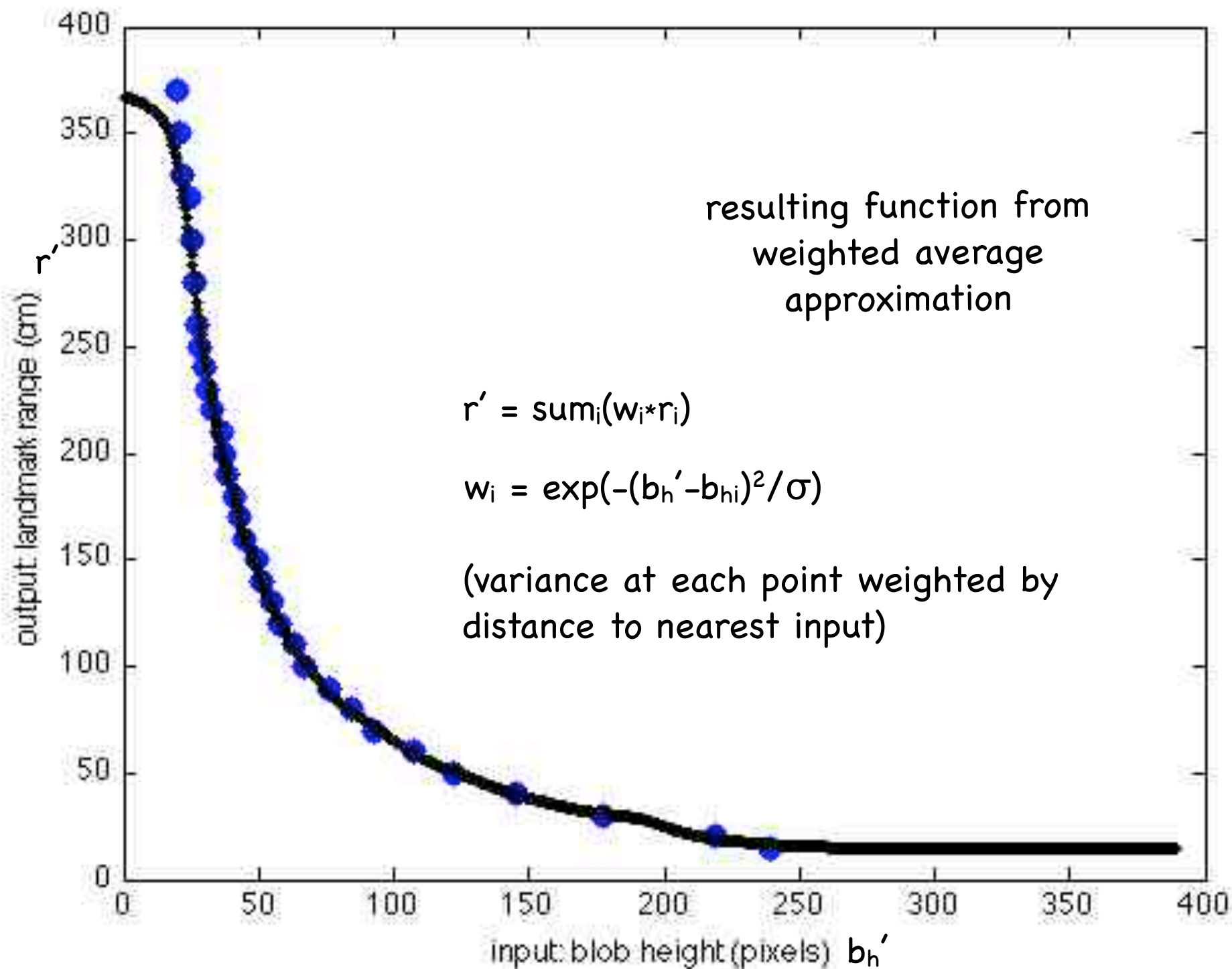


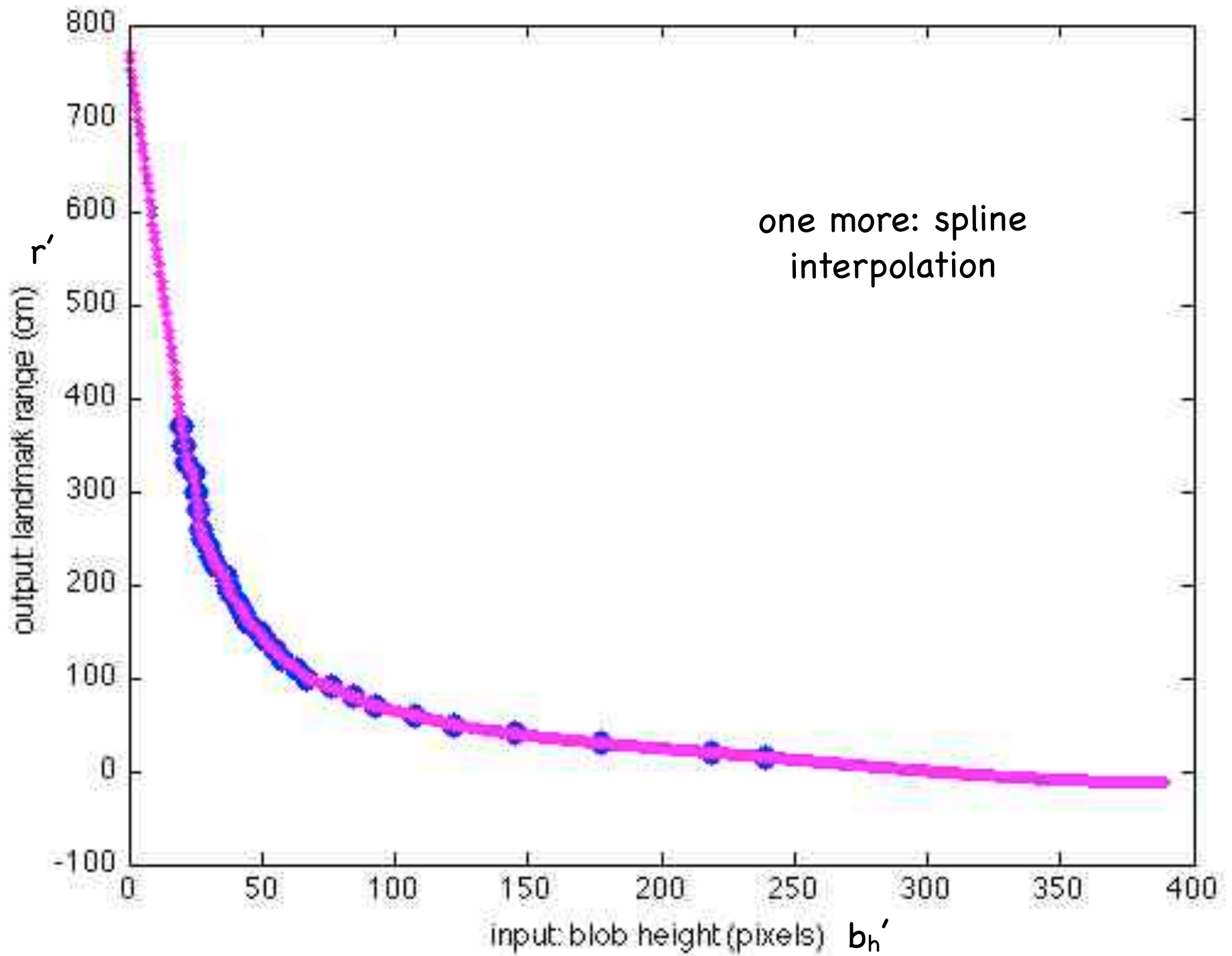






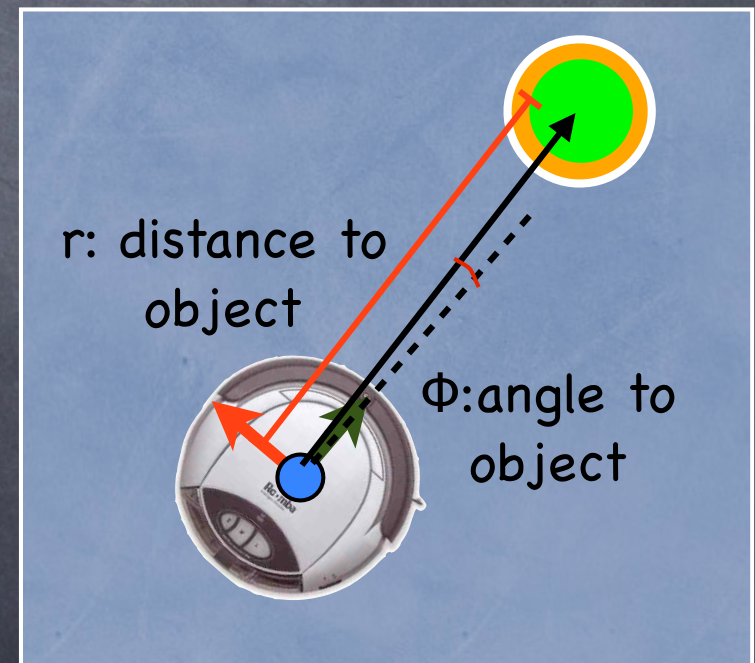
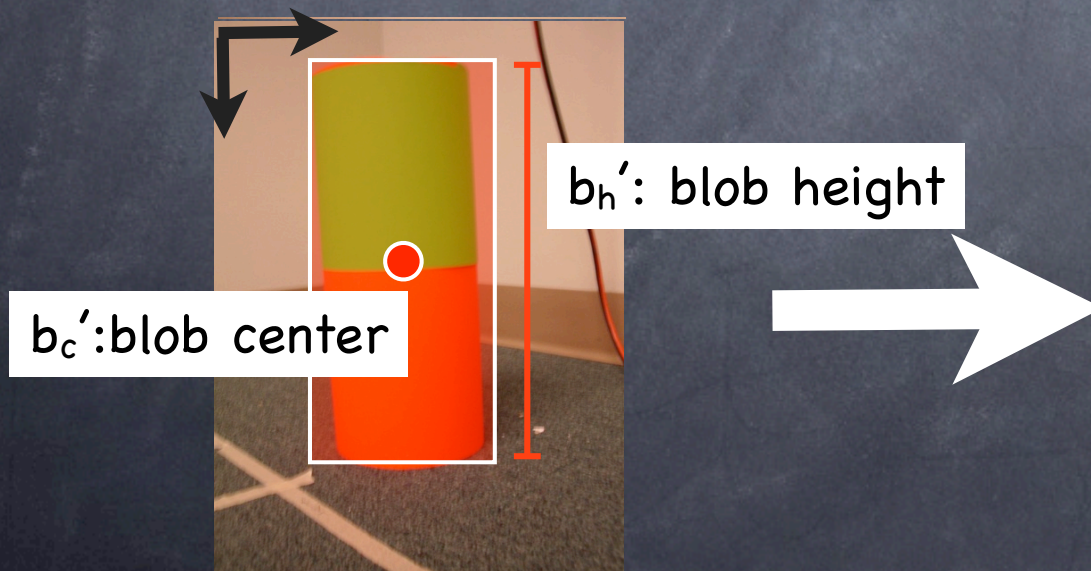




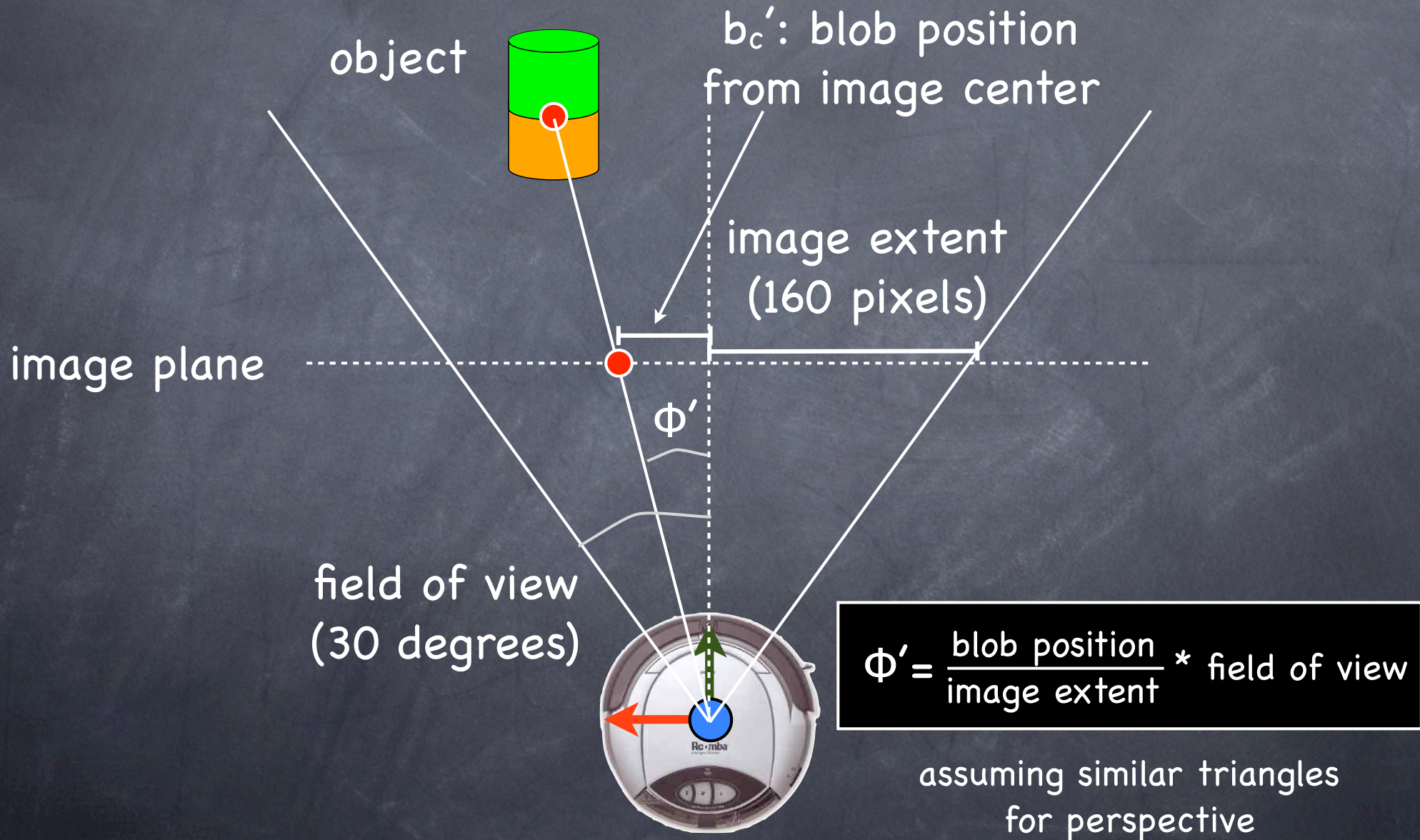


Estimating range and distance from blob

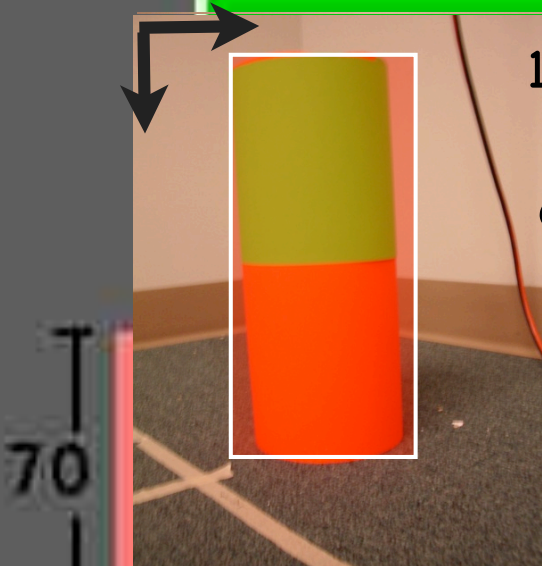
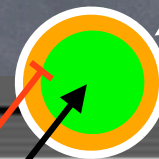
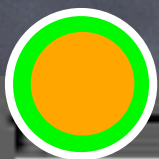
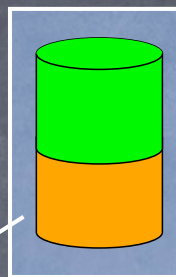
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Approximating bearing



Instead, we will compare the range and bearing of objects in robot pose coordinates



1) Estimate (r', Φ') from blob of observed object

r : distance to object

Φ : angle to object



2) calculate (r_x, Φ_x) expected by given a hypothesized pose x

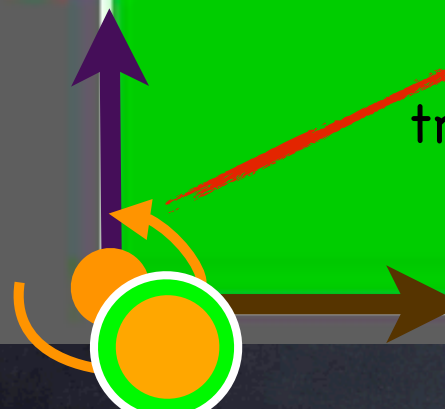
transform world into "robot's" perspective

3) compute weight from match between (r_x, Φ_x) and (r', Φ')

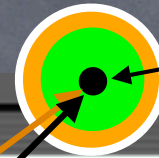
70

40
40

260



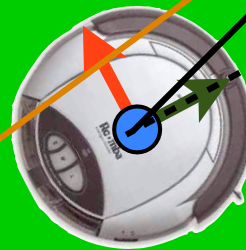
take every landmark and project it into robot pose coordinates



$$\begin{bmatrix} p_x^w \\ p_y^w \\ 1 \end{bmatrix}$$

Each landmark has a 2D location

Remember: we can translate and rotate any 2D point into new coordinates



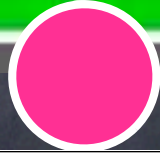
p^w : 2D location of landmark center in field coordinates

70

40

260

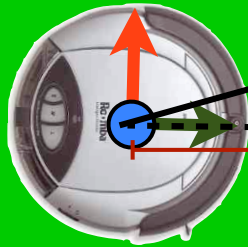
$$\begin{bmatrix} p_x^r \\ p_y^r \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} p_x^w \\ p_y^w \\ 1 \end{bmatrix}$$



p^r : 2D location of landmark center in robot coordinates

view from robot
coordinates

p_x^r
 p_y^r
1

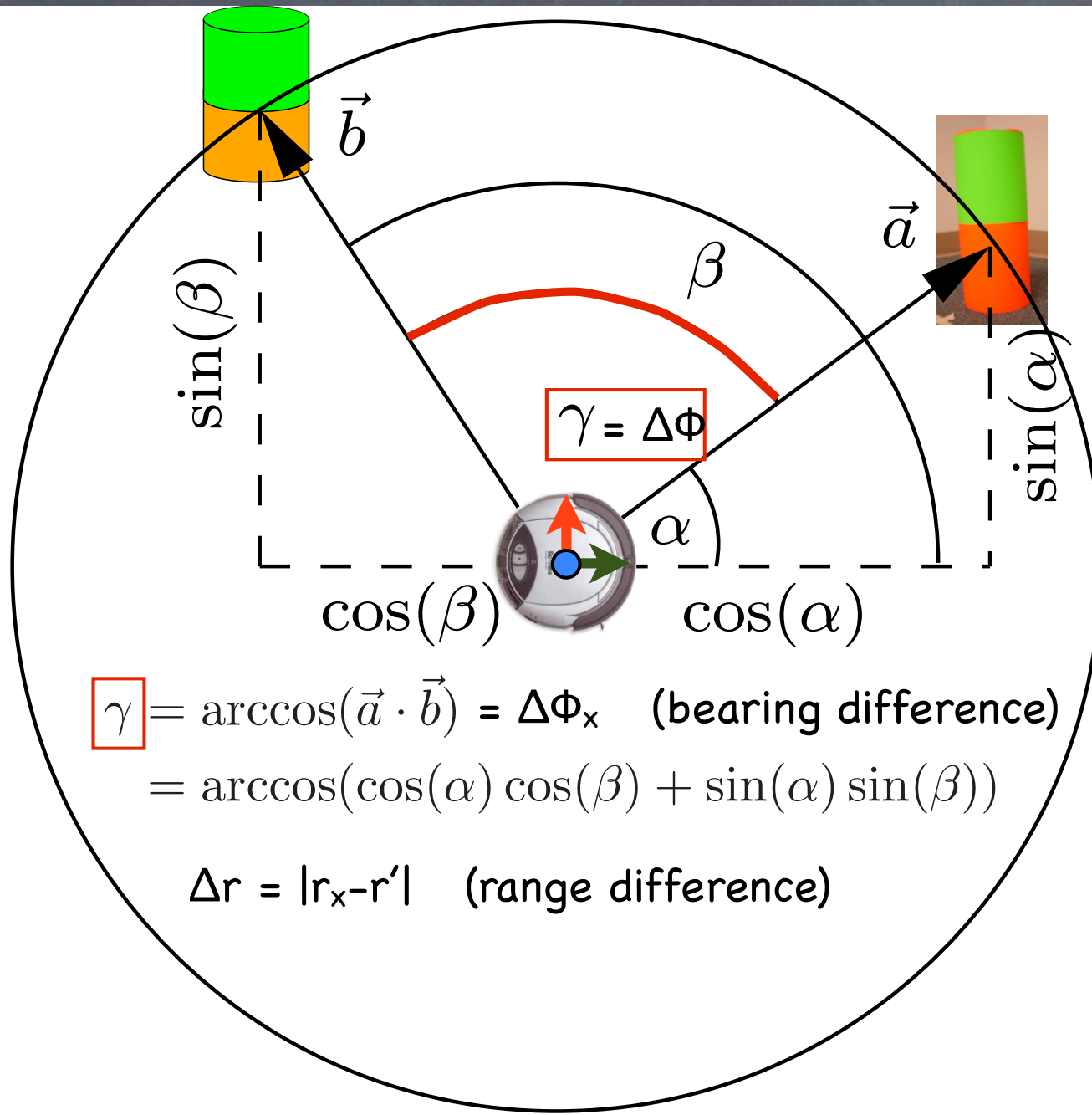


$r_x = \text{sqrt}((p_x^r)^2 + (p_y^r)^2)$
distance of vector to object

$\Phi_x = \text{atan}(p_y^r / p_x^r)$
bearing of vector to object

p^r : 2D location of
landmark center in
field coordinates






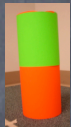
$$\boxed{\gamma} = \arccos(\vec{a} \cdot \vec{b}) = \Delta\Phi_x \quad (\text{bearing difference})$$

$$= \arccos(\cos(\alpha) \cos(\beta) + \sin(\alpha) \sin(\beta))$$

$$\Delta r = |r_x - r'| \quad (\text{range difference})$$

$$l(z = \text{cylinder} | x) \approx$$

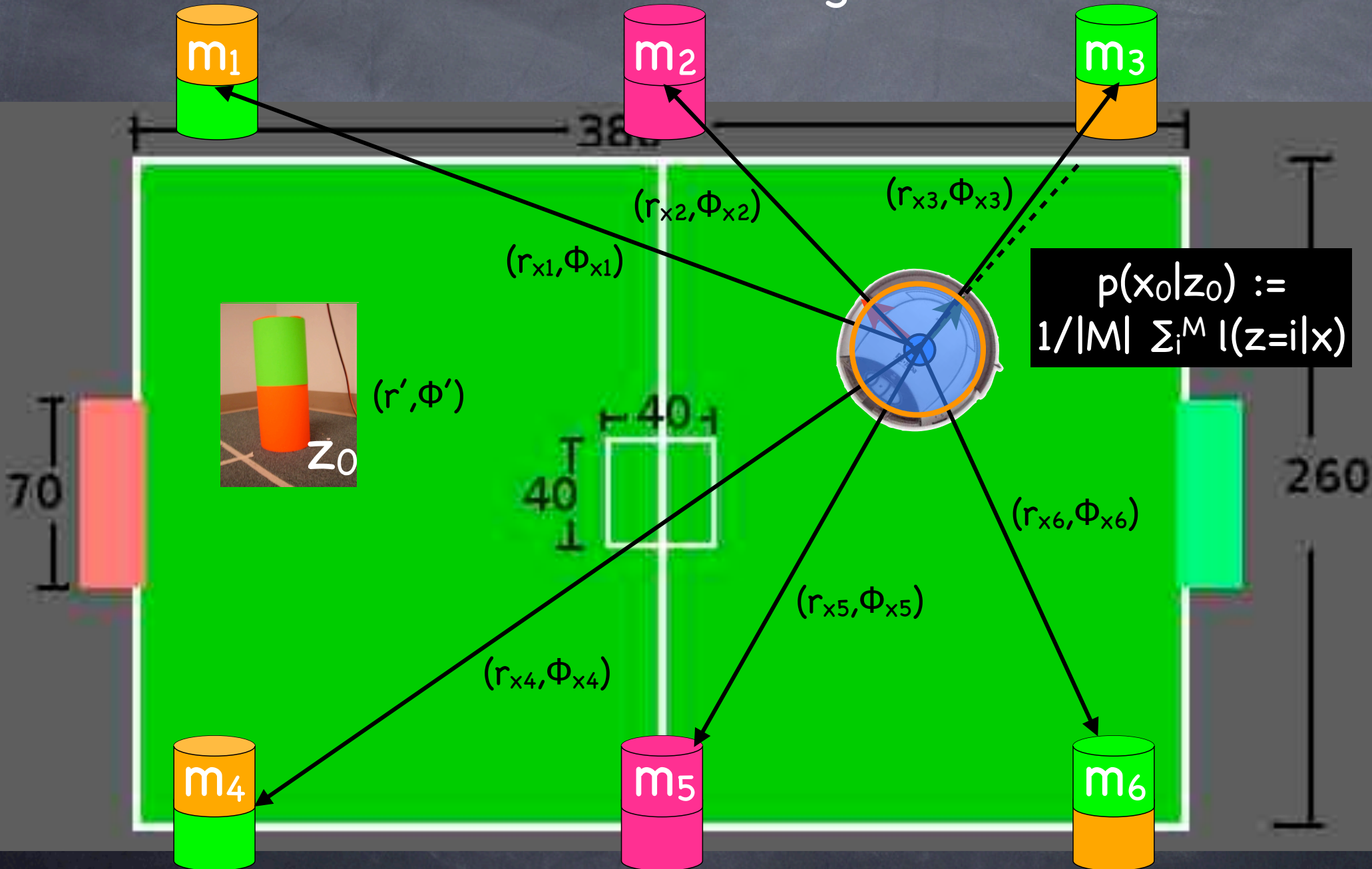
"low", if  out
 view and
 $-30^\circ < \Phi_x < 30^\circ$

"high", if  in
 view and
 $-30^\circ < \Phi_x < 30^\circ$

$$\exp(-\Delta\Phi * \Delta r),$$

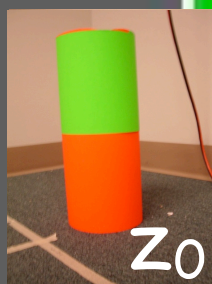
otherwise

for multiple landmarks, approximate by computing likelihood for each and then average



evaluate every pose sample

$$p(x_0|z_0) := \frac{1}{|M|} \sum_{i=1}^M I(z=i|x)$$



Particle filter recap

posterior

likelihood

dynamics

prior

$$p(\mathbf{x}_k | \mathbf{Z}_k) = \alpha p(\mathbf{Z}_k | \mathbf{x}_k) \int p(\mathbf{x}_k | \mathbf{x}_{k-1}) p(\mathbf{x}_{k-1} | \mathbf{Z}_{k-1})$$

"belief
at t=k"

"update"

"predict"

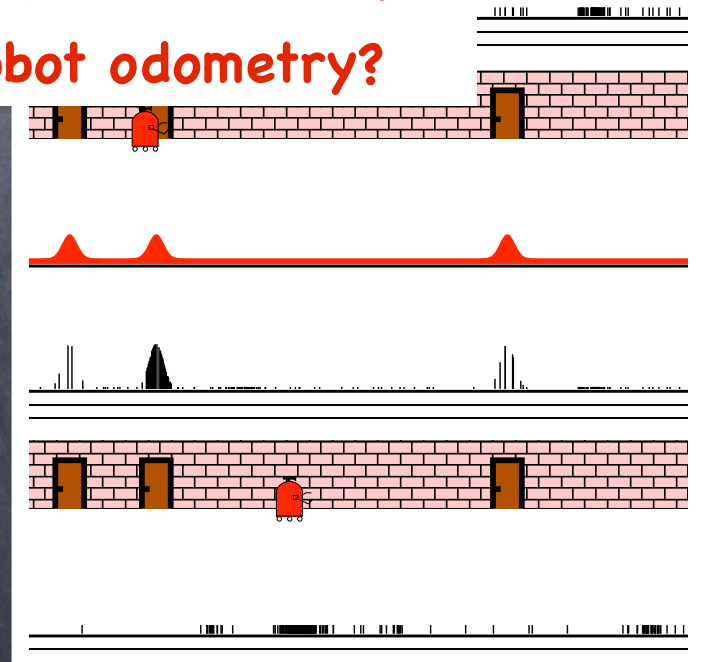
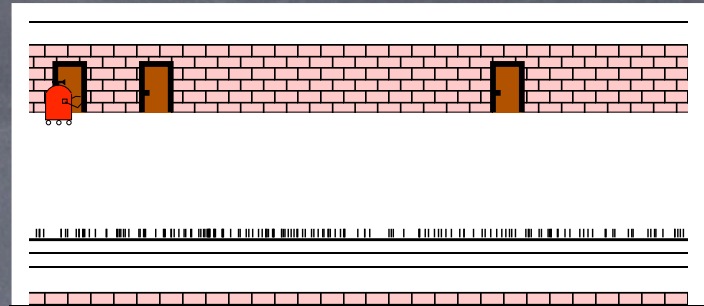
"belief
at t=k-1"

How to evaluate the likelihood of a pose given robot observations?

How to predict a new belief given robot odometry?

- recursive Markovian inference over time with predict-update loop
- Particle filter algorithms predict-update with sample set of poses

What are we still missing to compute localization?

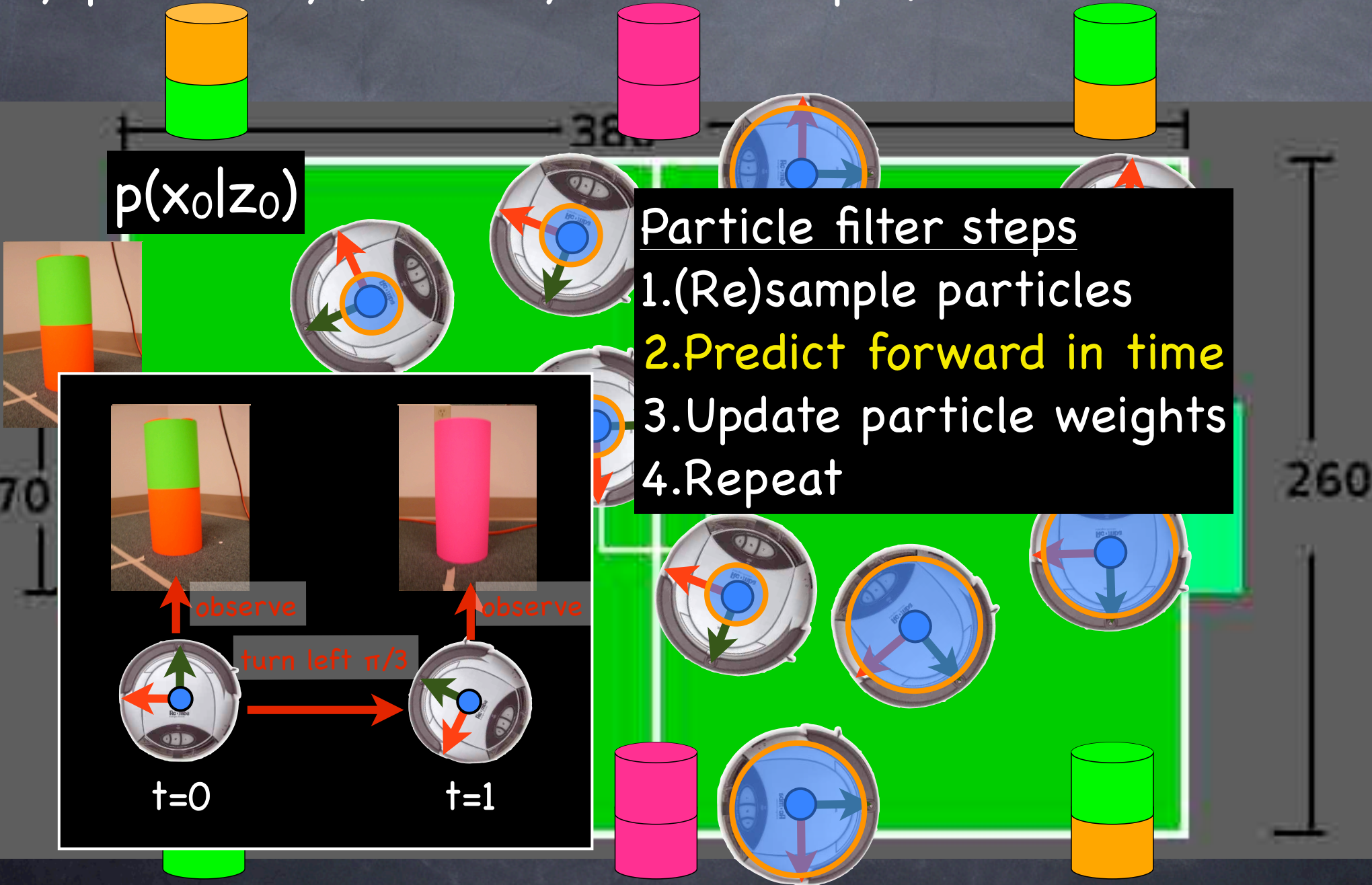
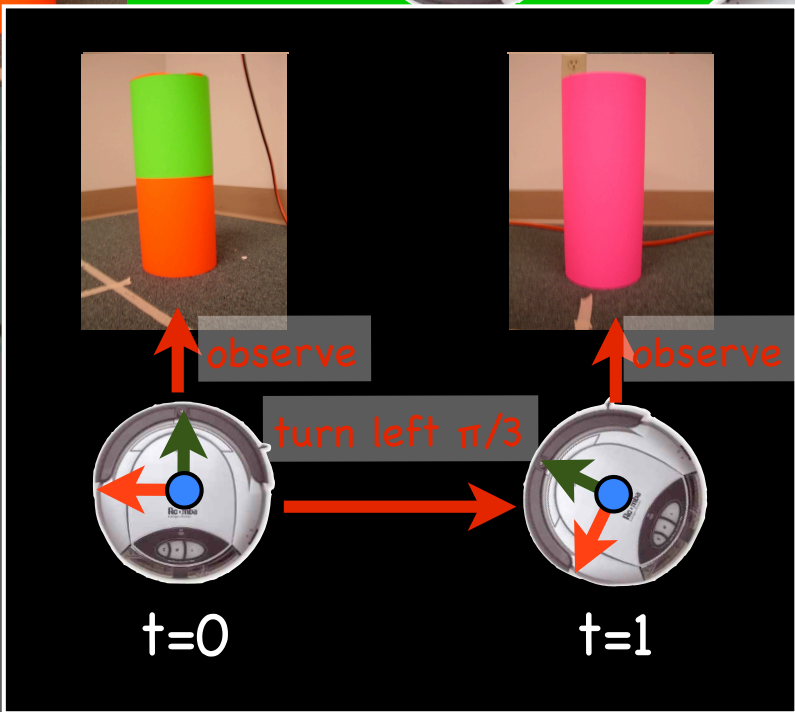


note: belief for particle filter are pose samples weighted by probability (noted by size of ellipse)

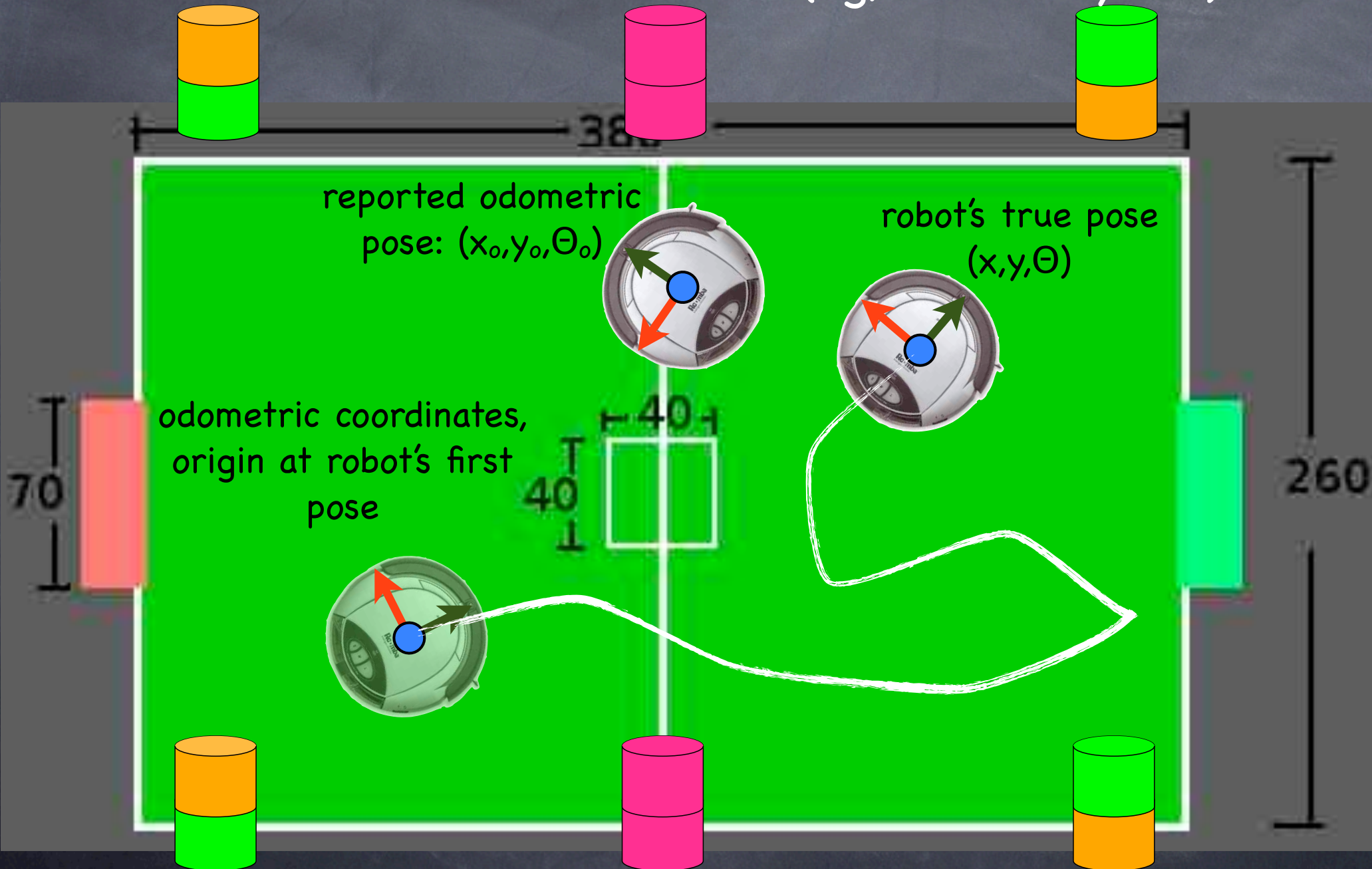
$$p(x_0|z_0)$$

Particle filter steps

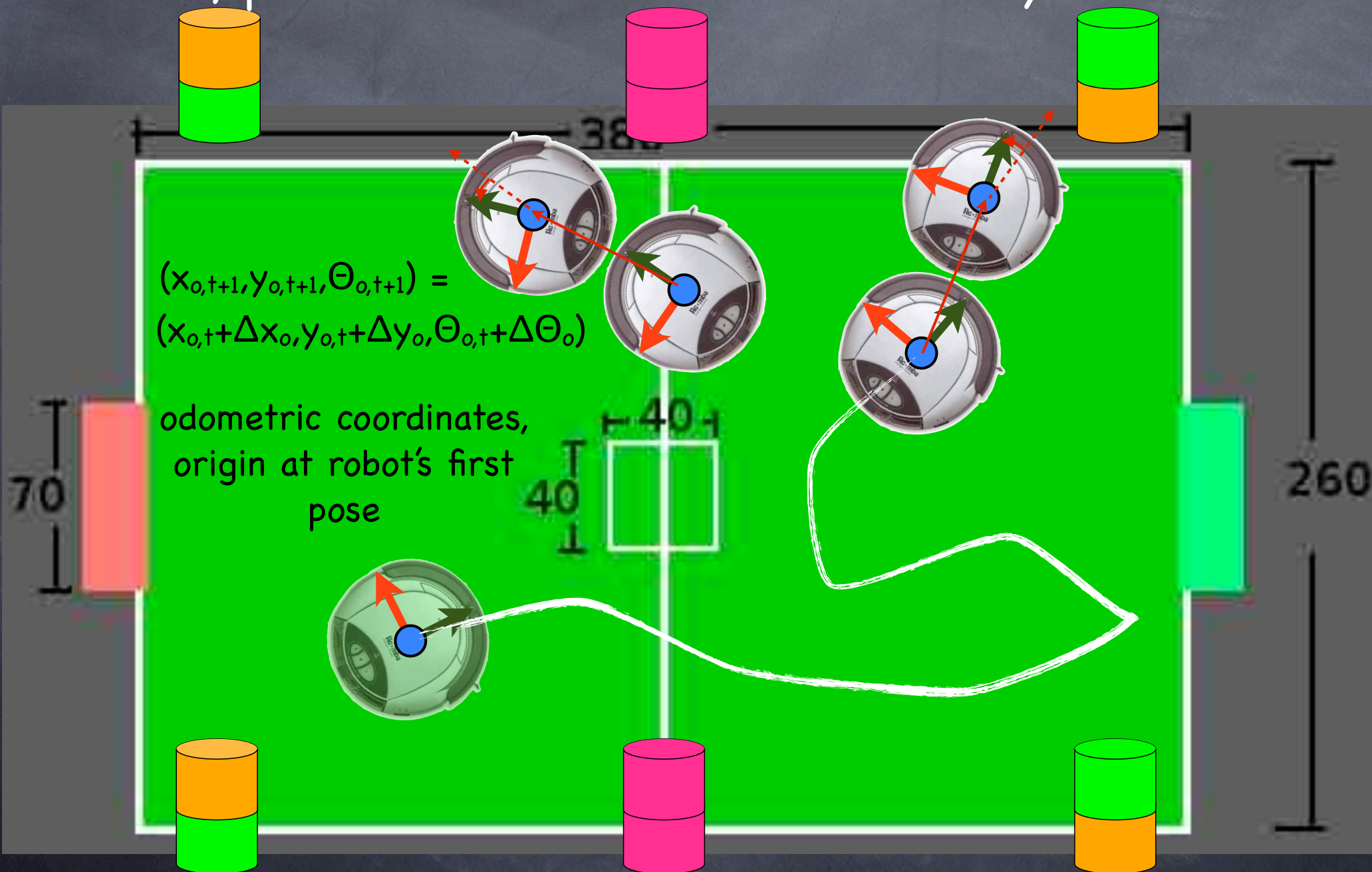
1. (Re)sample particles
2. Predict forward in time
3. Update particle weights
4. Repeat



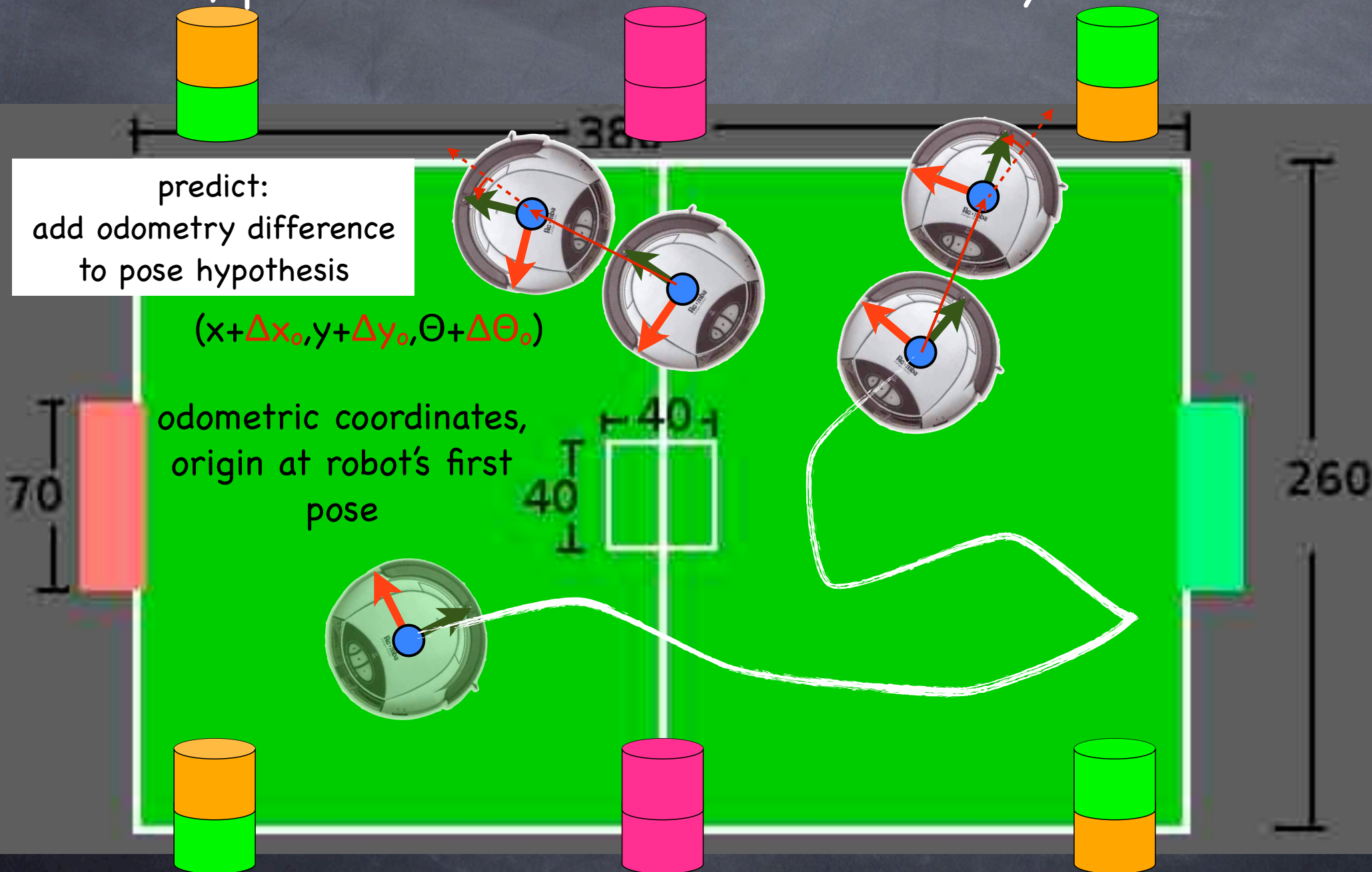
Player reports a pose estimate in odometric coordinates, we cannot trust this localization (eg, odometry lab)



odometry error due to accumulated noise over time;
however, poses close in time are reasonably accurate

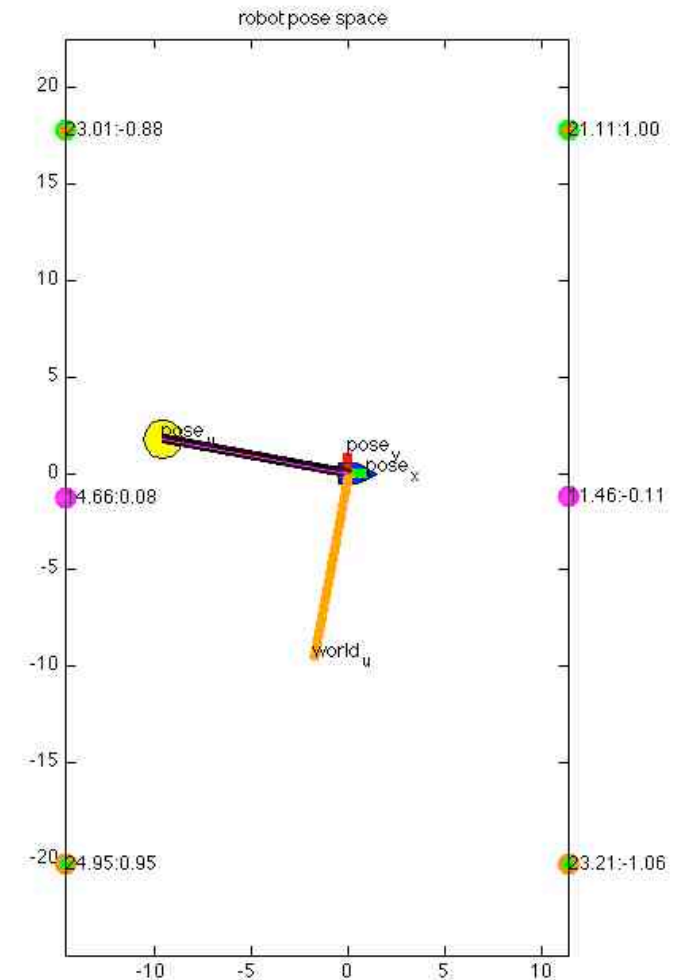
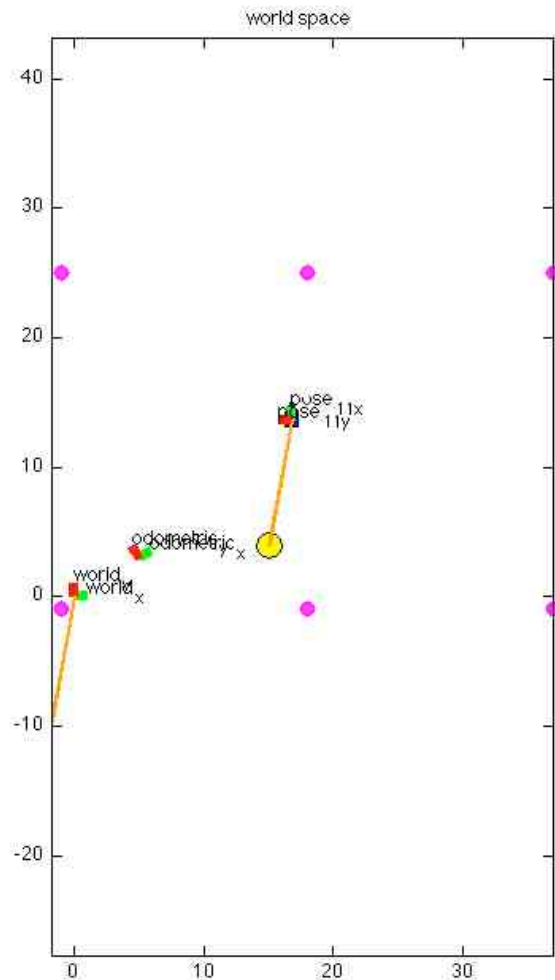


odometry error due to accumulated noise over time;
however, poses close in time are reasonably accurate



matlab example

field_coordinate_transform.m



matlab example

[/course/cs148/pub/range_function_approximation.m](#)

