



Topic 9

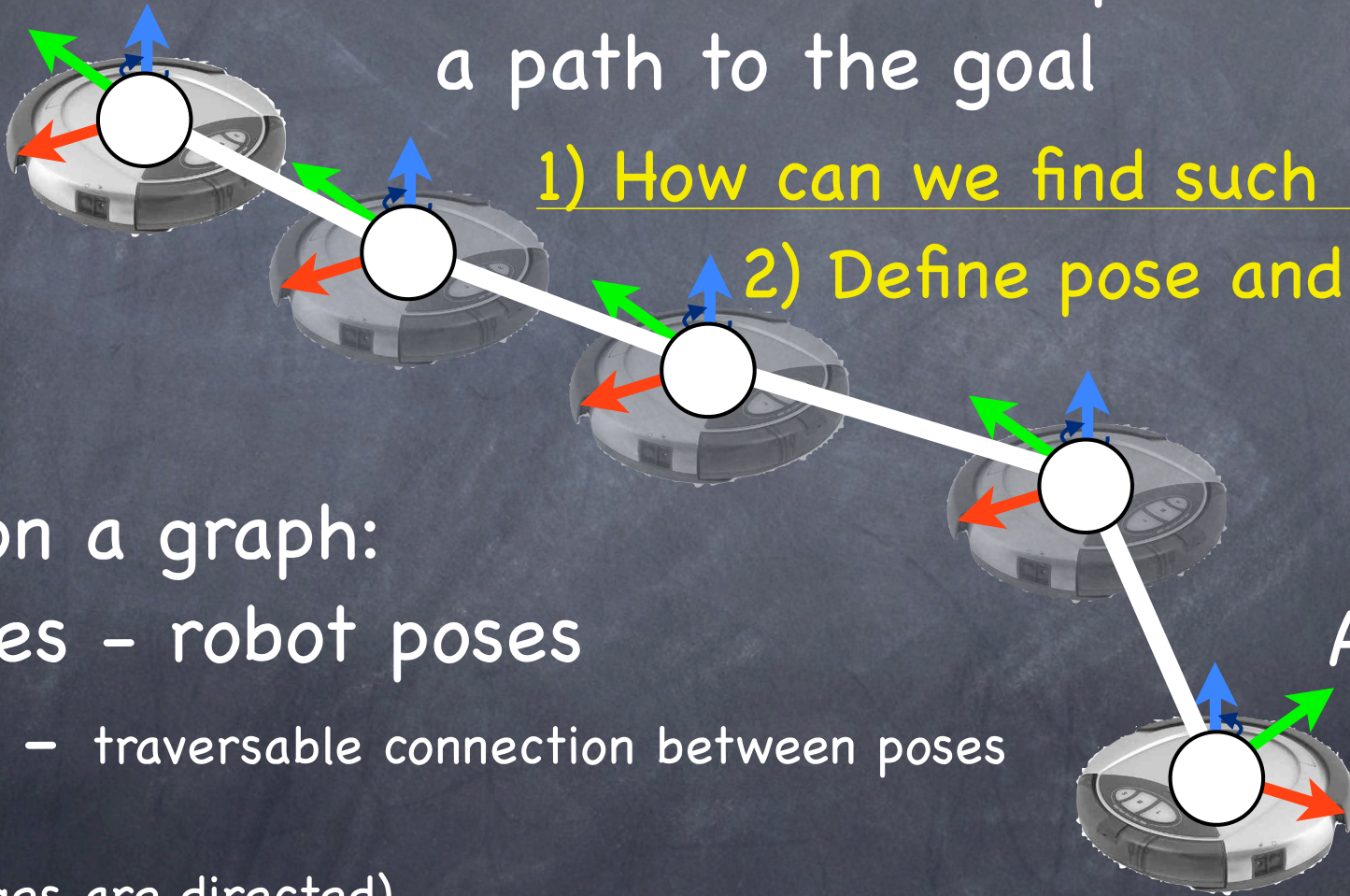
Potential fields:

Follow your
potential

Path Planning

B: Goal

Find intermediate poses forming a path to the goal



1) How can we find such paths?

2) Define pose and controls?

Path on a graph:

vertices - robot poses

edges - traversable connection between poses

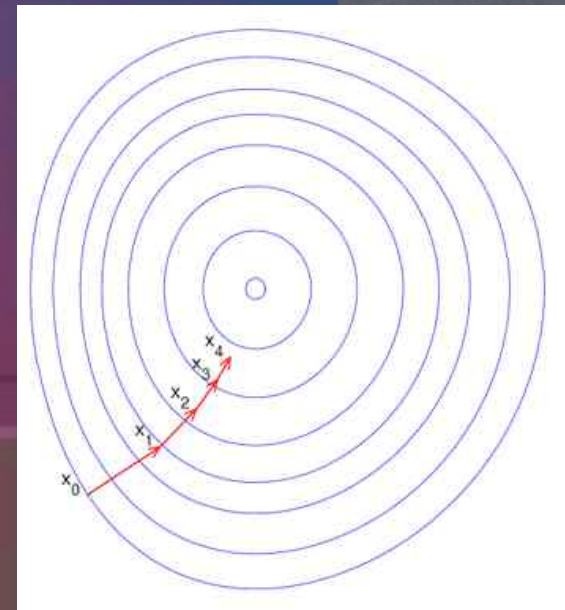
(note edges are directed)

A: Start

Approaches to path planning

- Search (fixed graph)
 - DFS, BFS, Dijkstra, A*
- Search (explore graph):
 - Probabilistic Road Maps
 - Rapidly-exploring Random Trees
- Optimization (local search):
 - Potential fields, gradient descent

Potential field



Energy potential converges at goal



volcanic



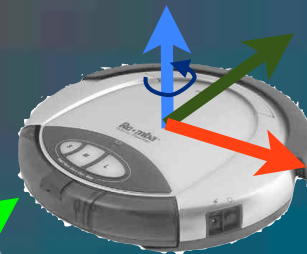
on fire



heating up



a little warmer



cold

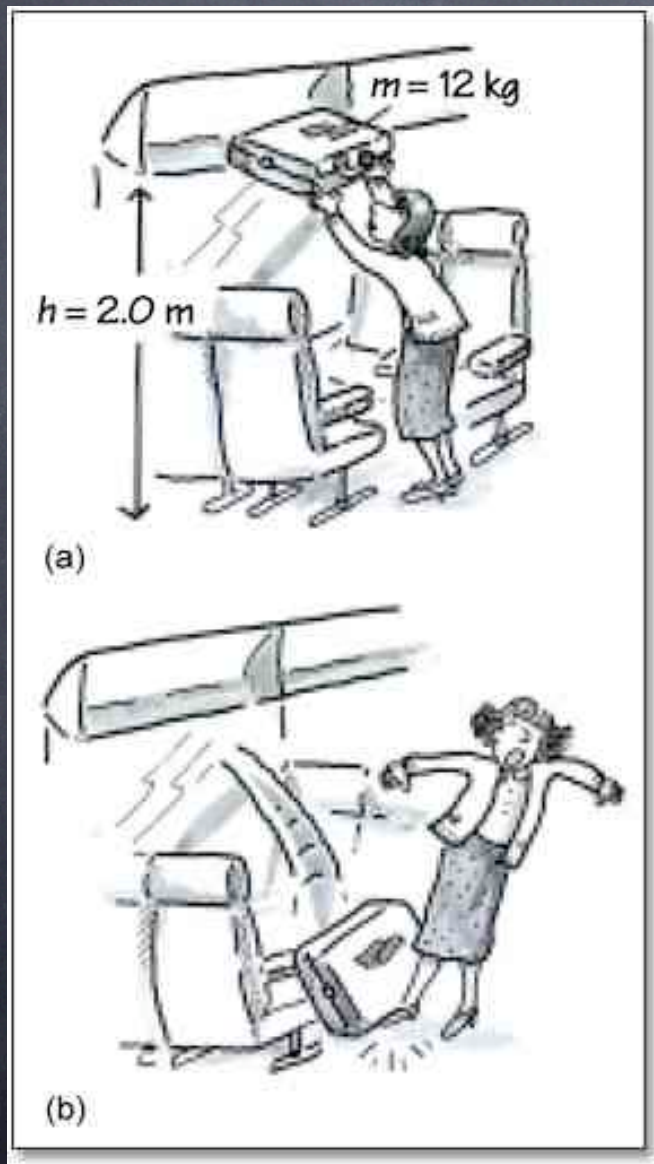


colder

How do we define this potential?

260

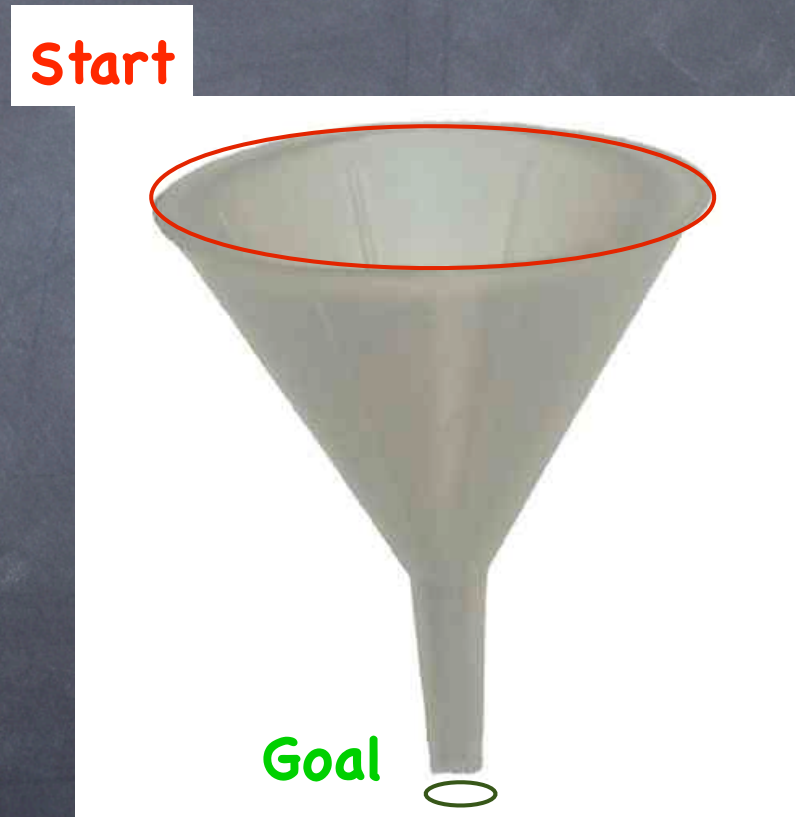
Potential Energy



- Energy stored in a physical system
- For objects acting only w.r.t. gravity
 - $PE = \text{mass} * \text{height} * \text{gravity}$

Convergent Potentials

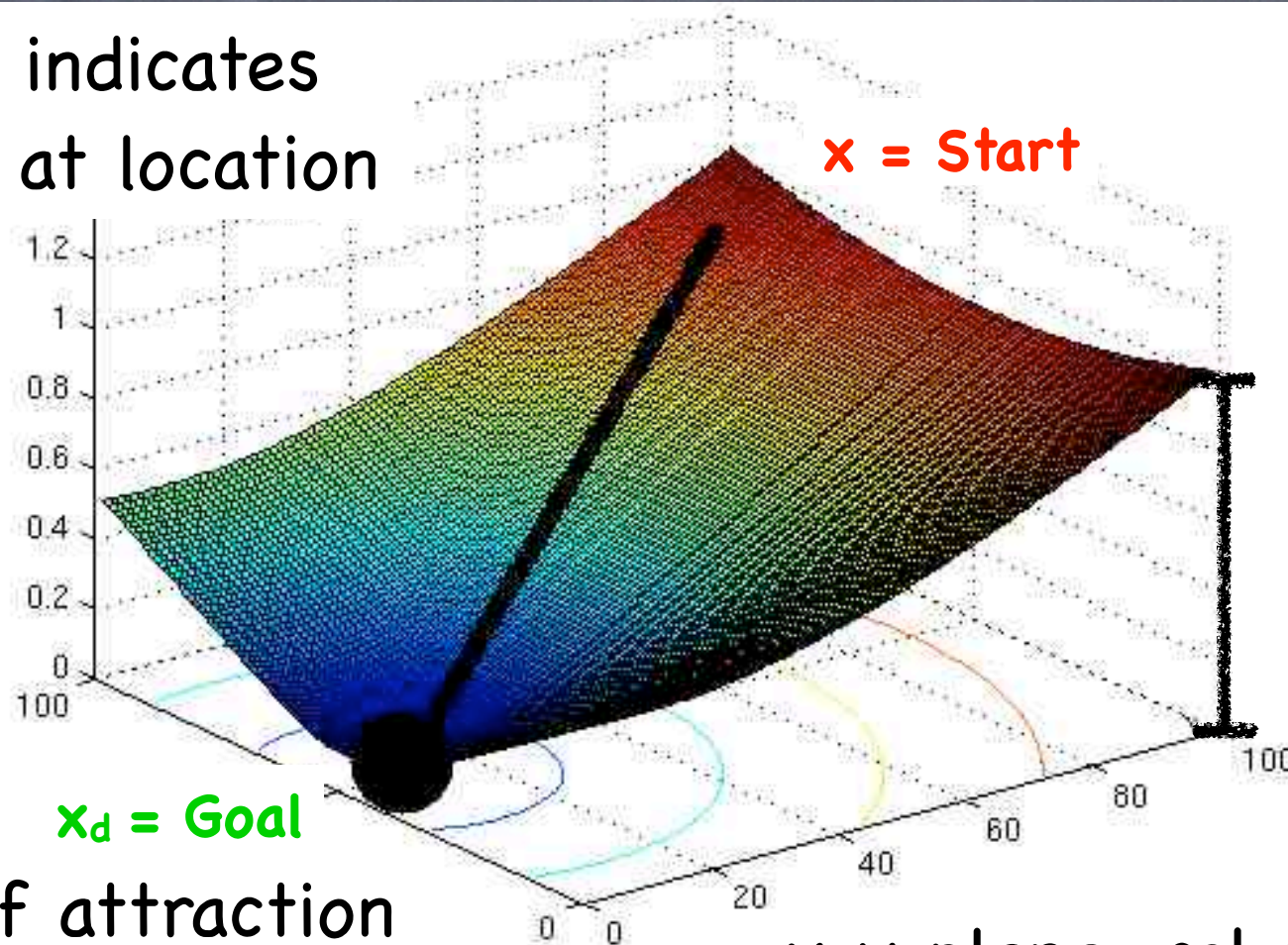
let's call these "attractor landscapes"



basin of attraction

2D potential navigation

z: height indicates potential at location



basin of attraction

x-y plane: robot position

"Cone" Attractor



$x_d = \text{Goal}$
"Attractor"

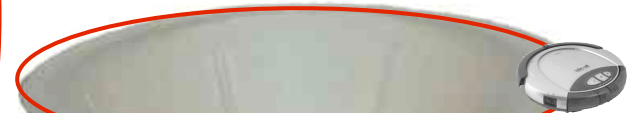
$$u = w(x_d - x) / \|x_d - x\|$$

$x = \text{Start}$



top view

Start



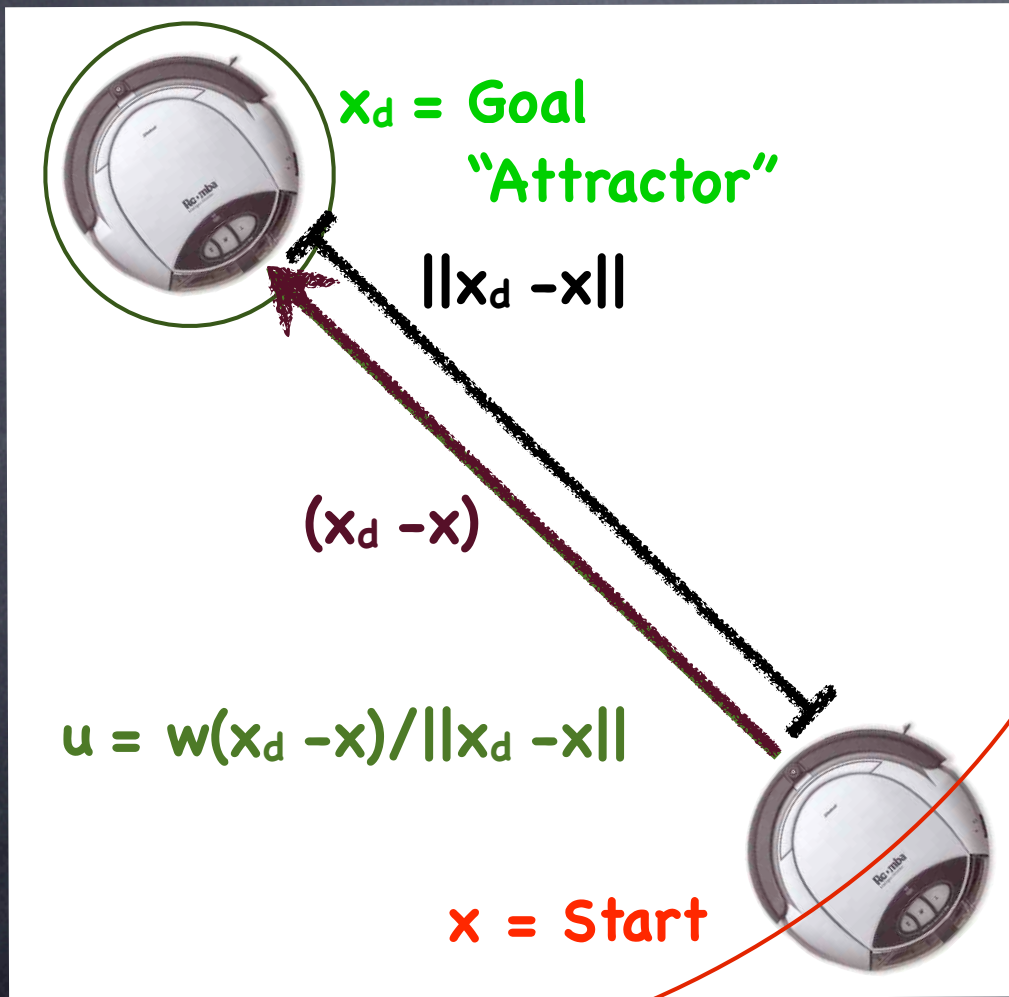
Goal



side view

w : weight
 $(x_d - x)$: direction
 $\|x_d - x\|$: distance

"Cone" Attractor



top view

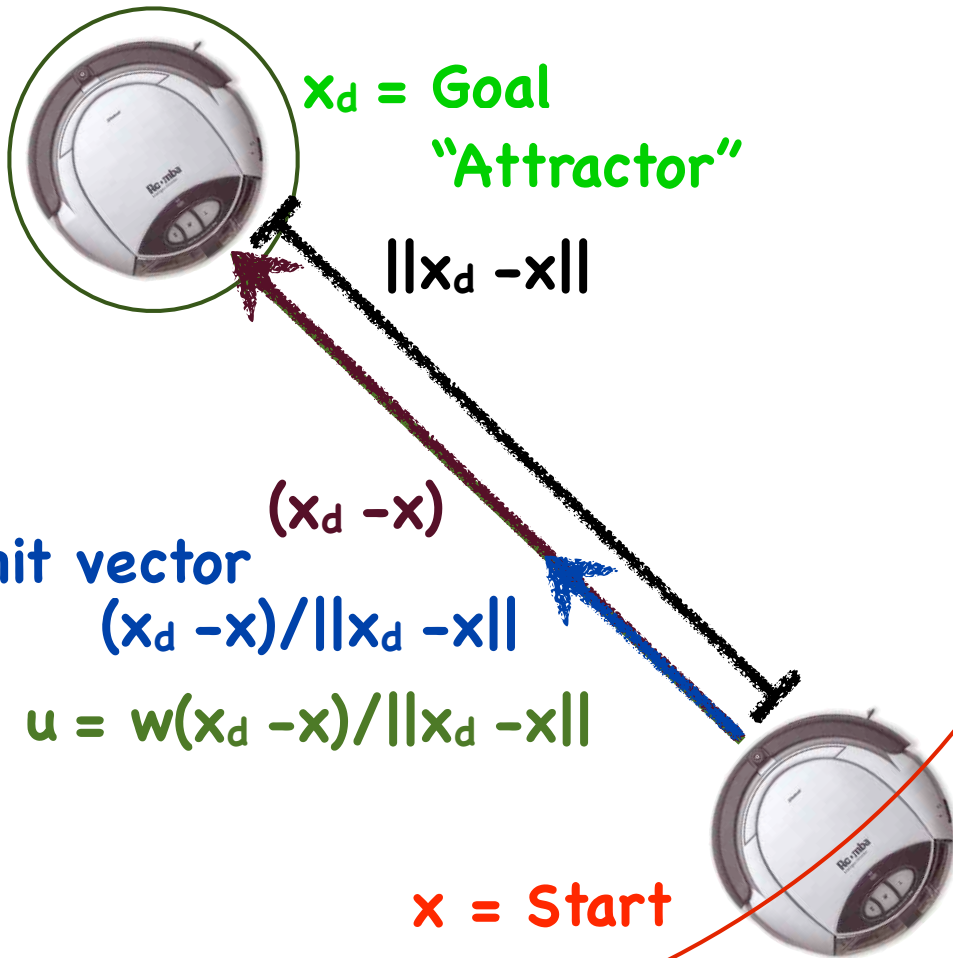
w: weight
 $(x_d - x)$: direction
 $\|x_d - x\|$: distance

Start



side view

"Cone" Attractor



top view

Start



side view

w: weight

$(x_d - x)$: direction

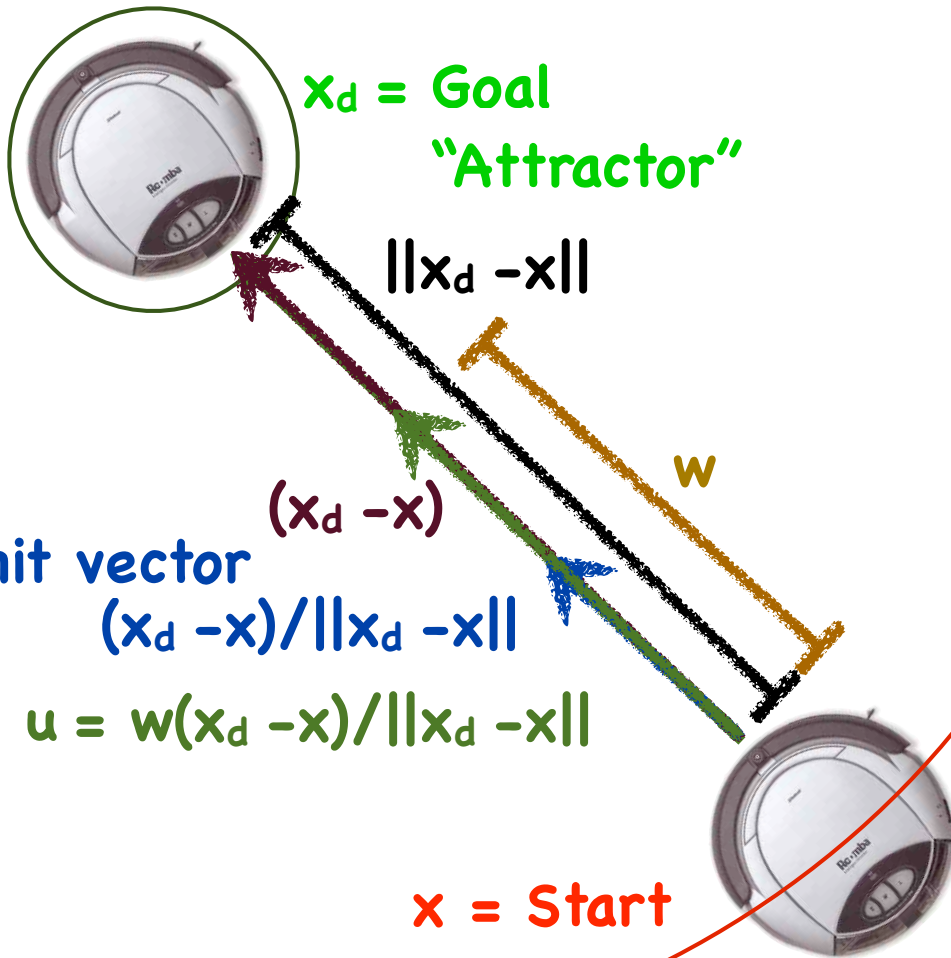
$\|x_d - x\|$: distance

"Cone" Attractor

w: weight

$(x_d - x)$: direction

$\|x_d - x\|$: distance



Start



Goal

top view

side view

"Bowl" Attractor



$x_d = \text{Goal}$

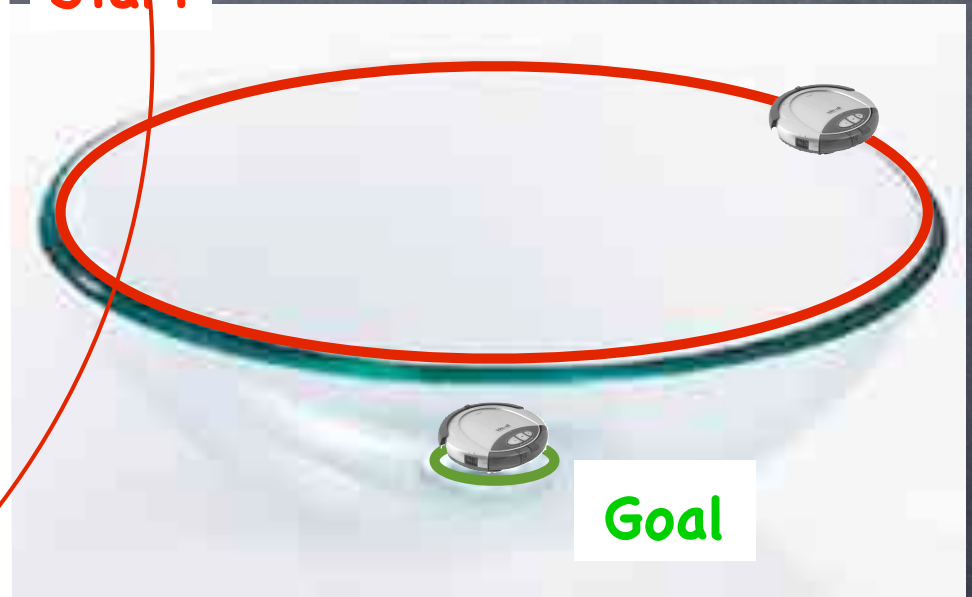
$$u = \exp(-\|x_d - x\|/w) (x_d - x)$$



$x = \text{Start}$

top view

Start

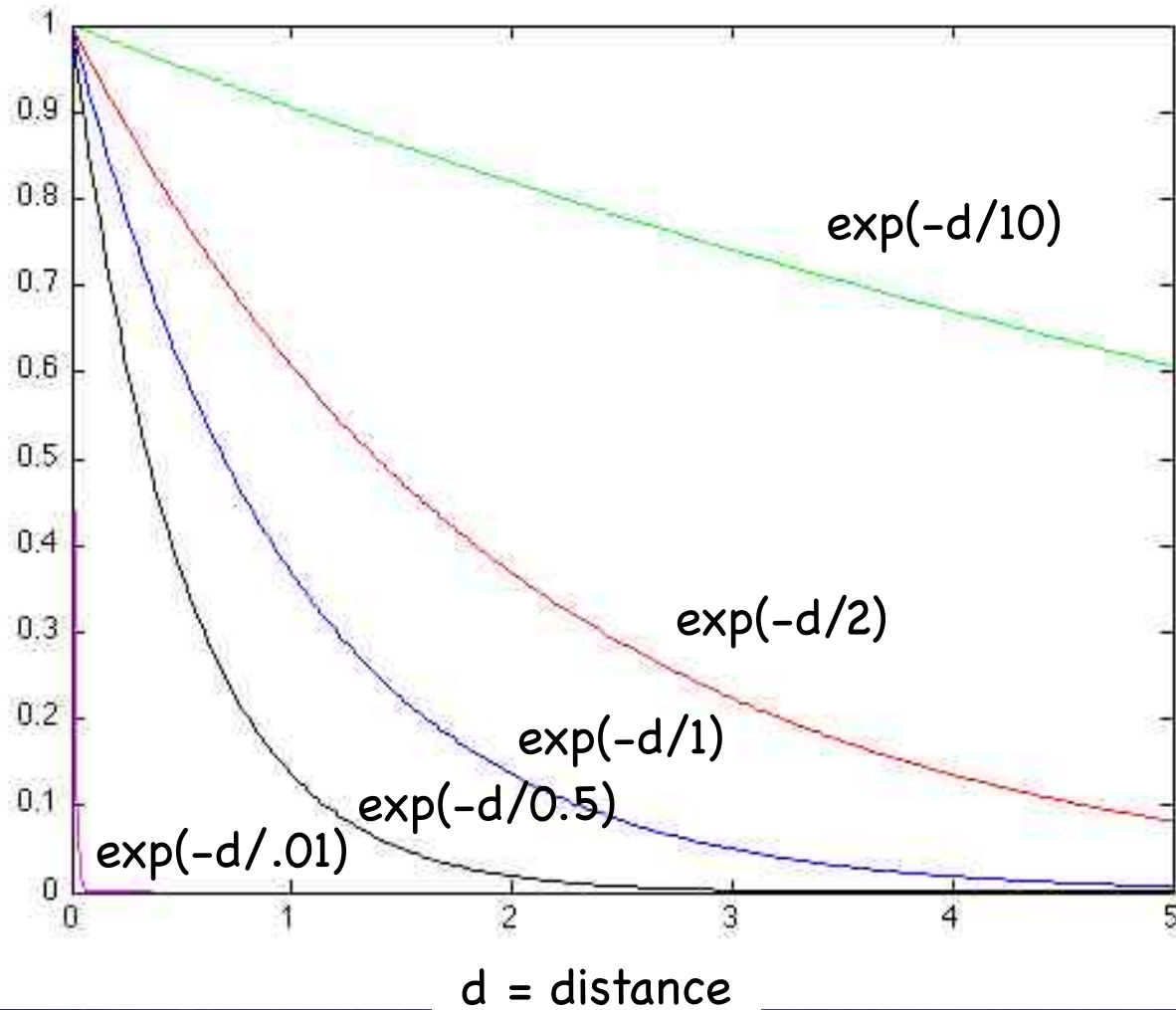


Goal

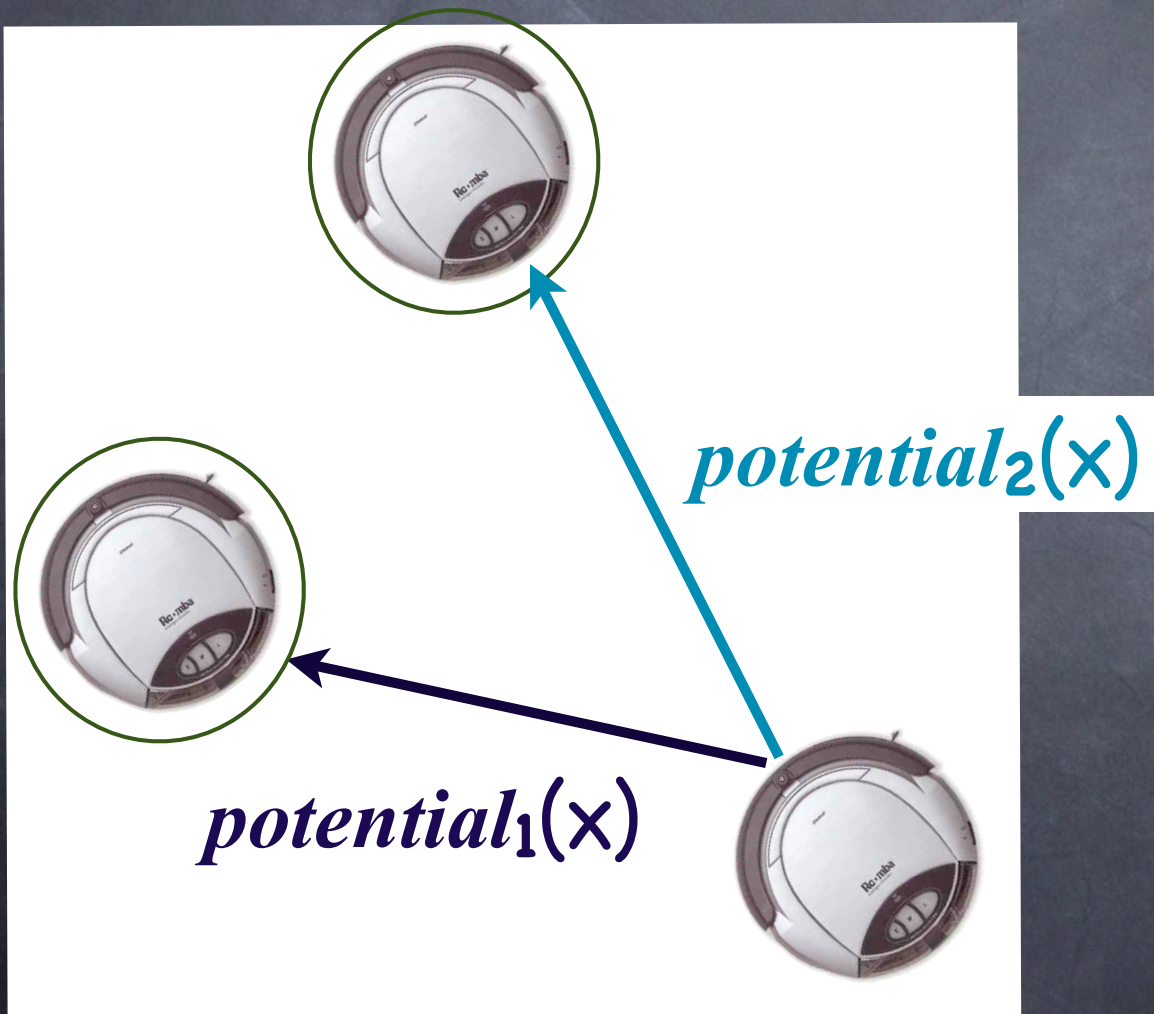
side view

$$\exp(-d/w)$$

$\exp(-d/w)$:
influence of
potential



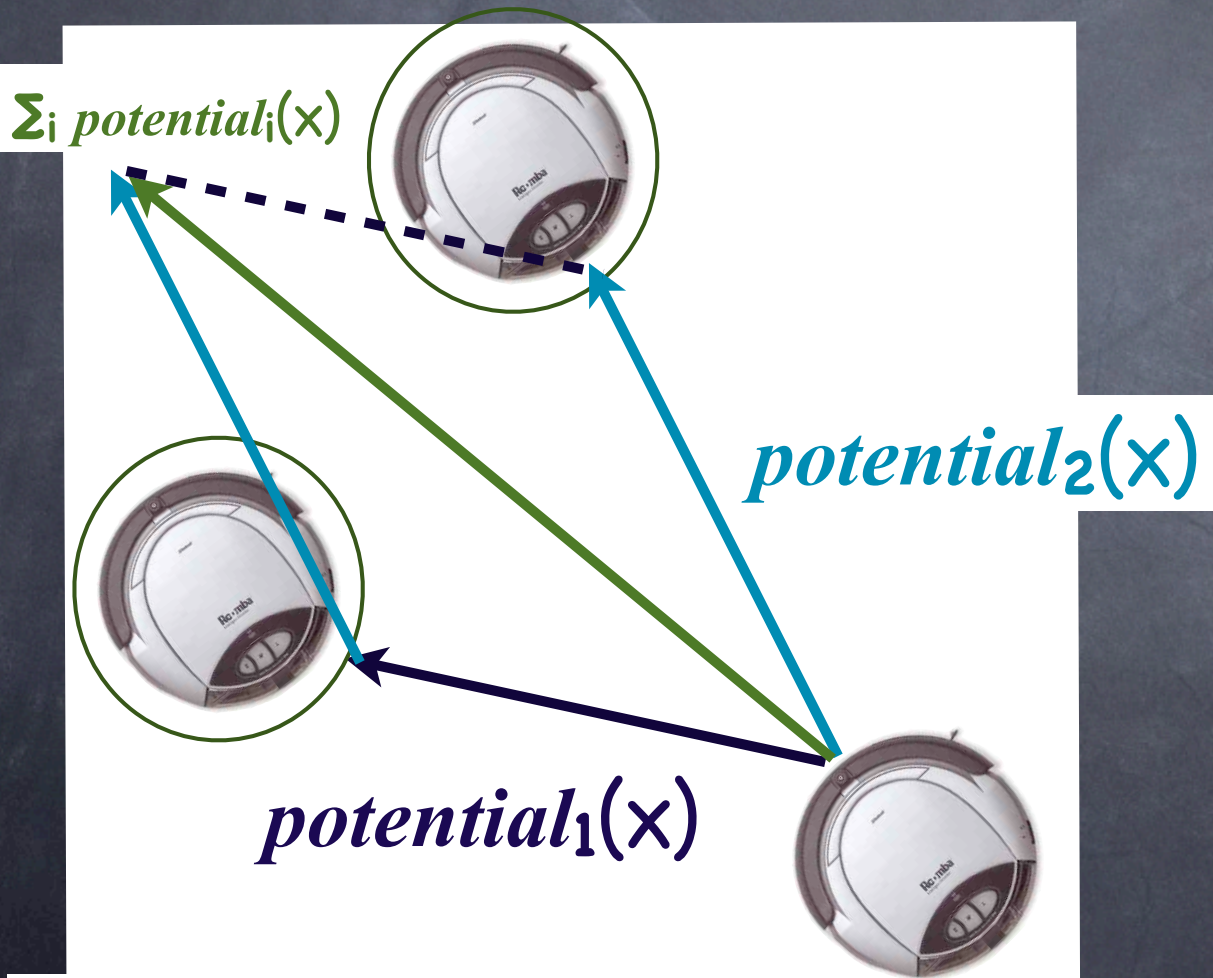
Multiple potentials



- Output of potential field is a vector

- How to combine or select between multiple potentials?

Multiple potentials



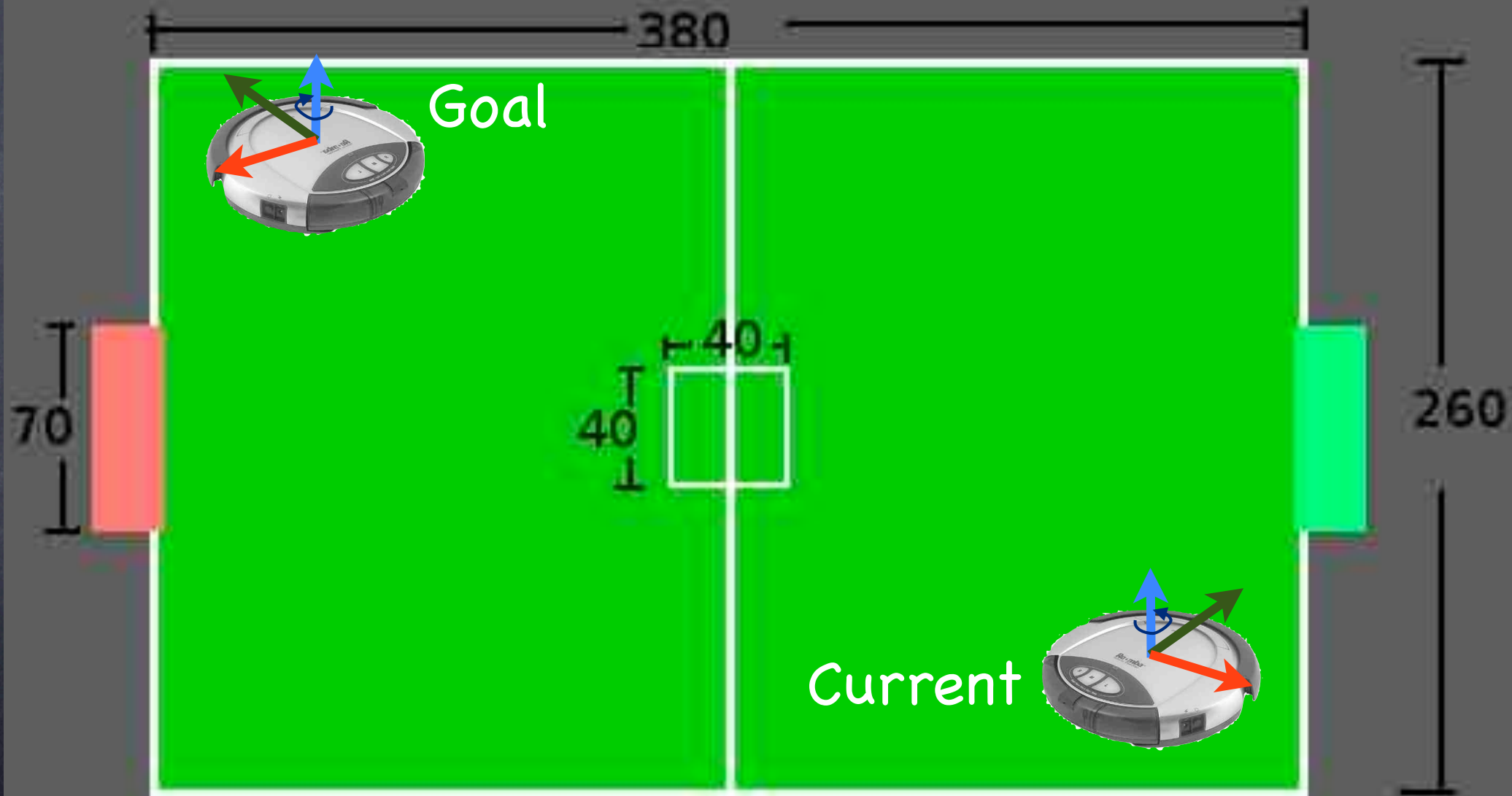
- Output of potential field is a vector

- Combine multiple potentials through vector summation

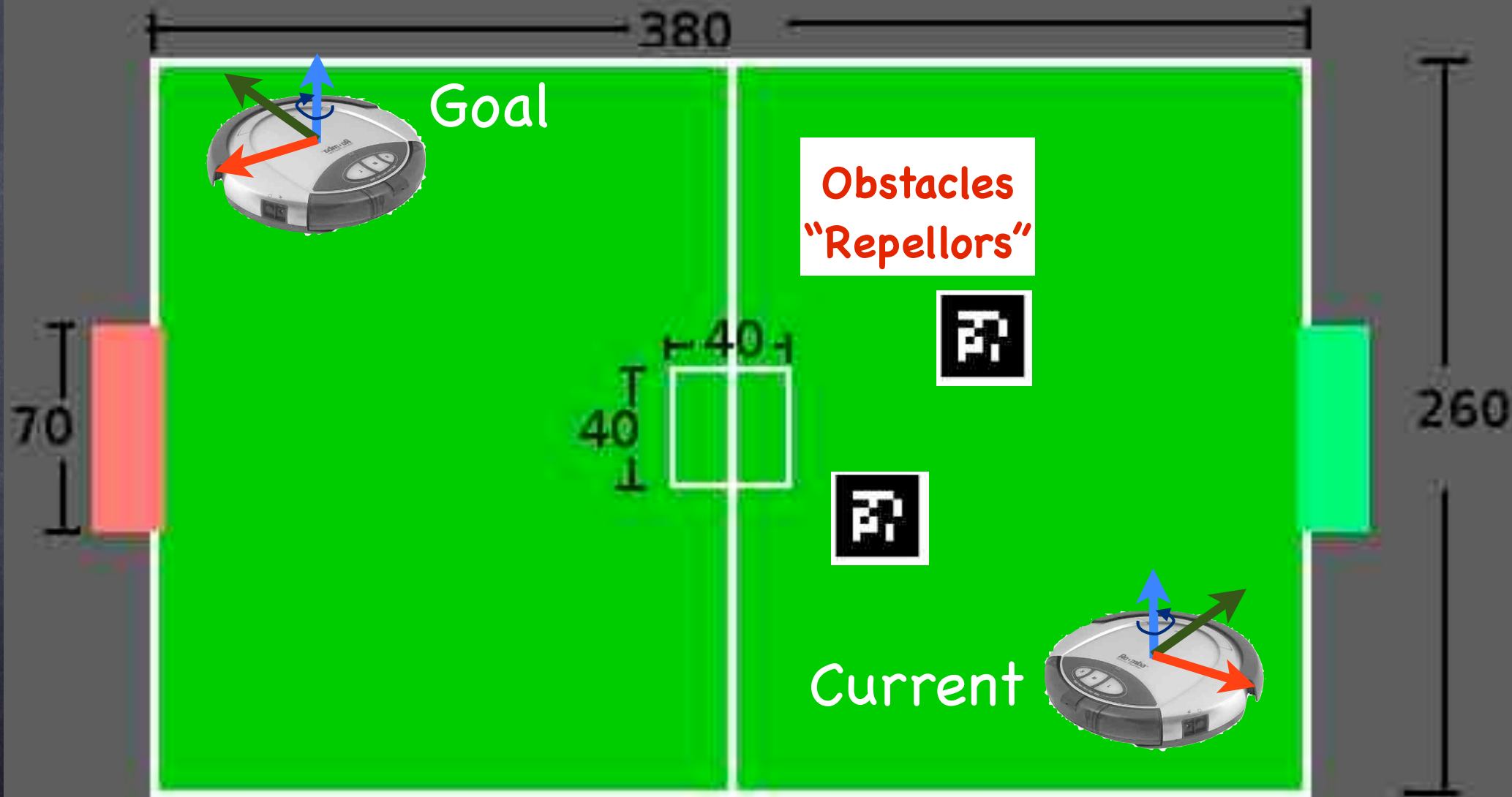
$$u = \sum_i potential_i(x)$$

or $u = potential_1(x) + potential_1(x)$

describe performance for this case

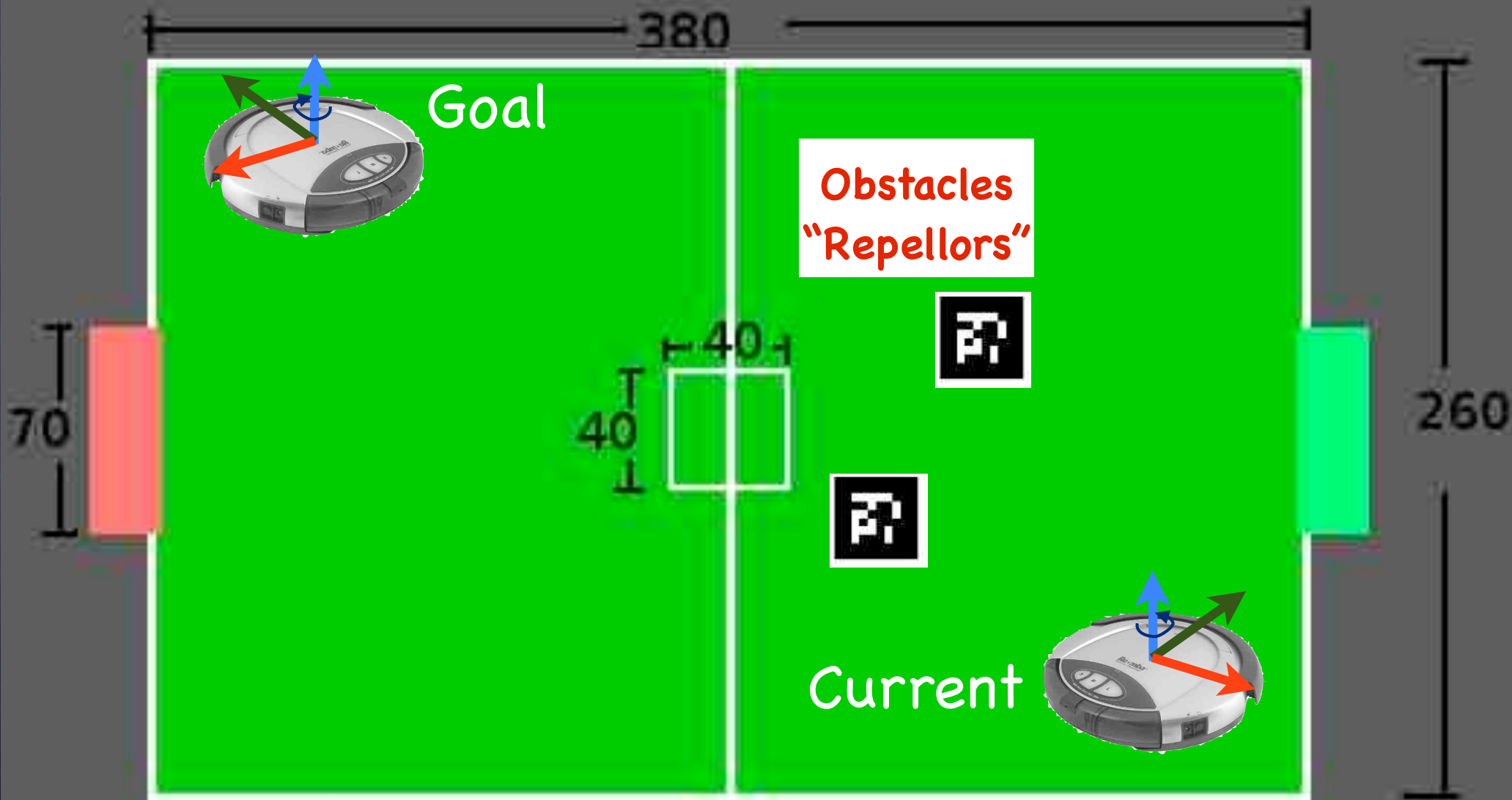


describe performance for this case



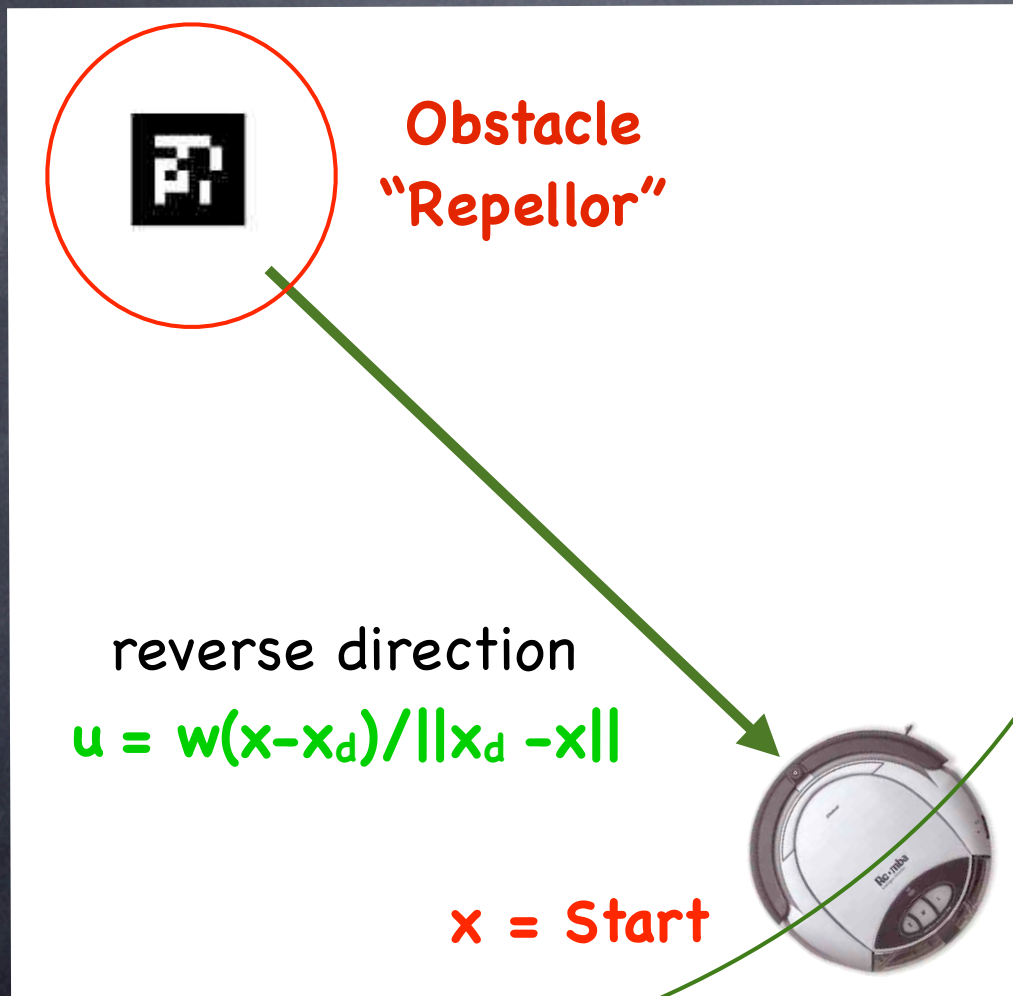
describe performance for this case

how do we deal with repellers?



"Cone" Repellor

potential problems

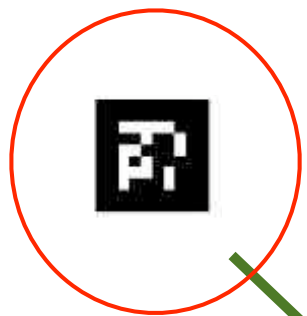


top view



side view

"Bowl" Repellor



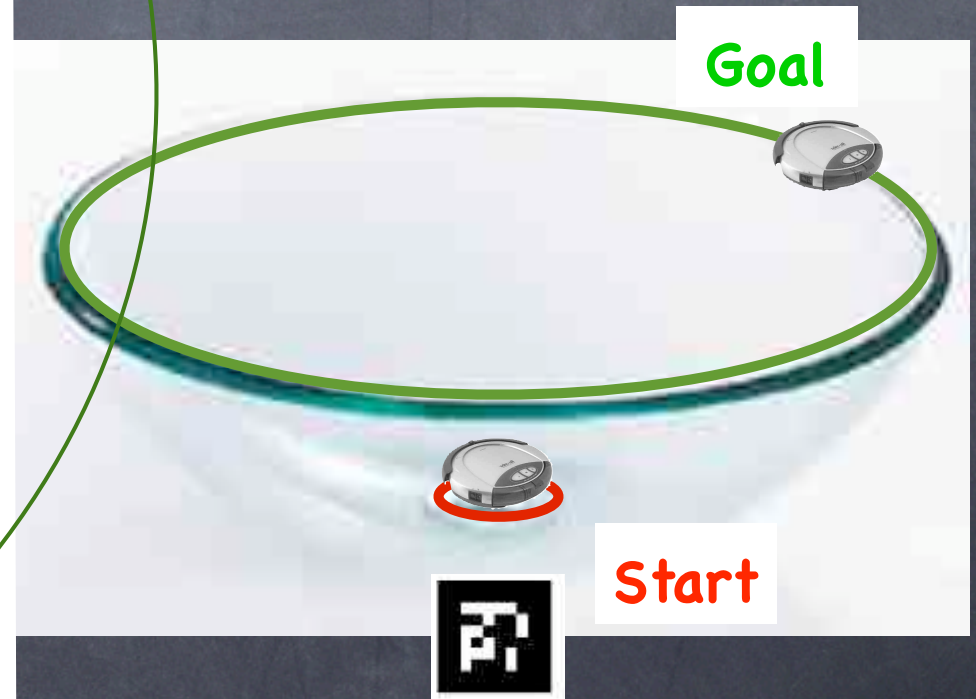
Obstacle
"Repellor"

$$u = \exp(-\|x-x_d\|/w) (x_d - x)$$

$x = \text{Start}$

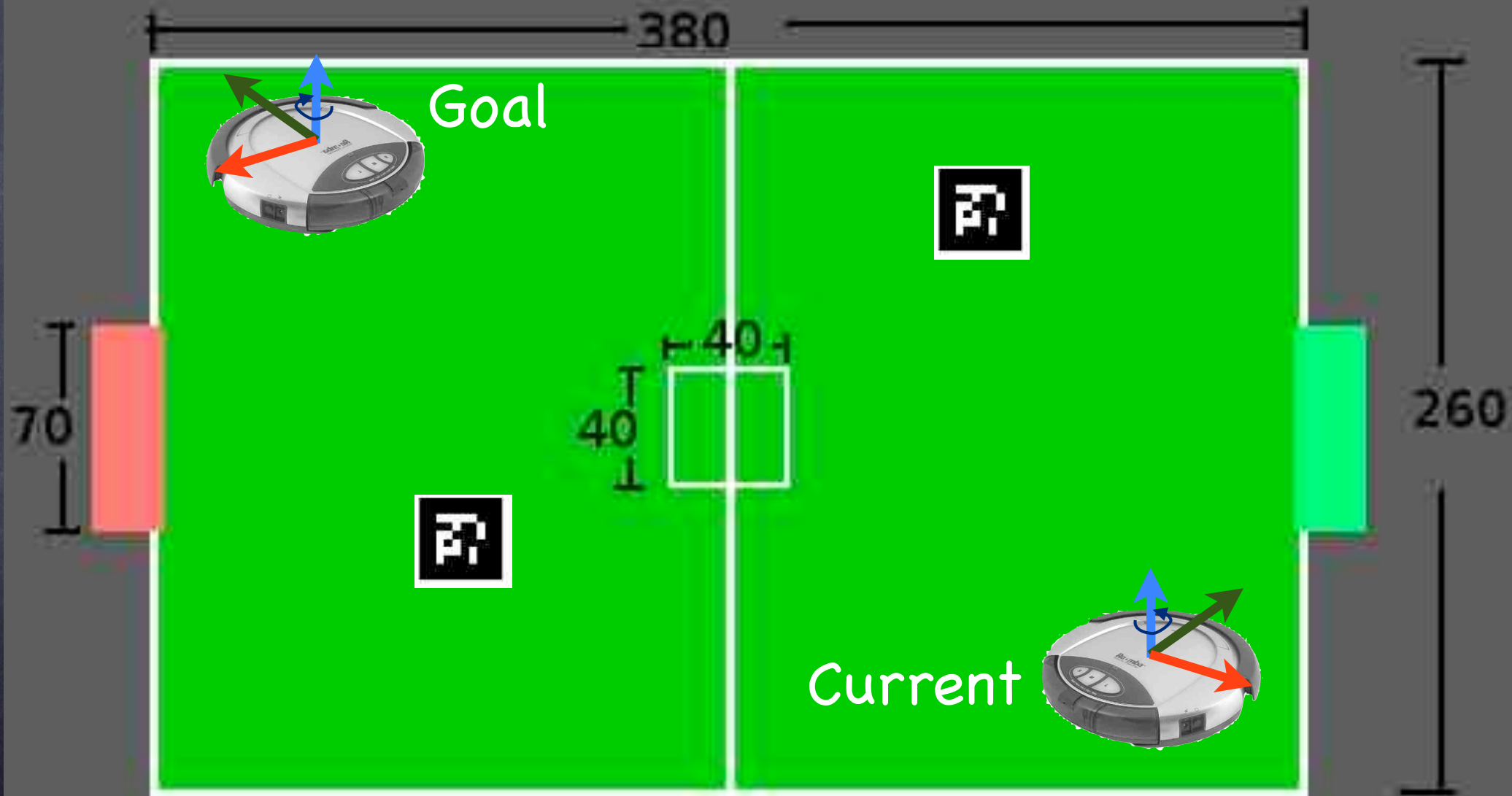


top view

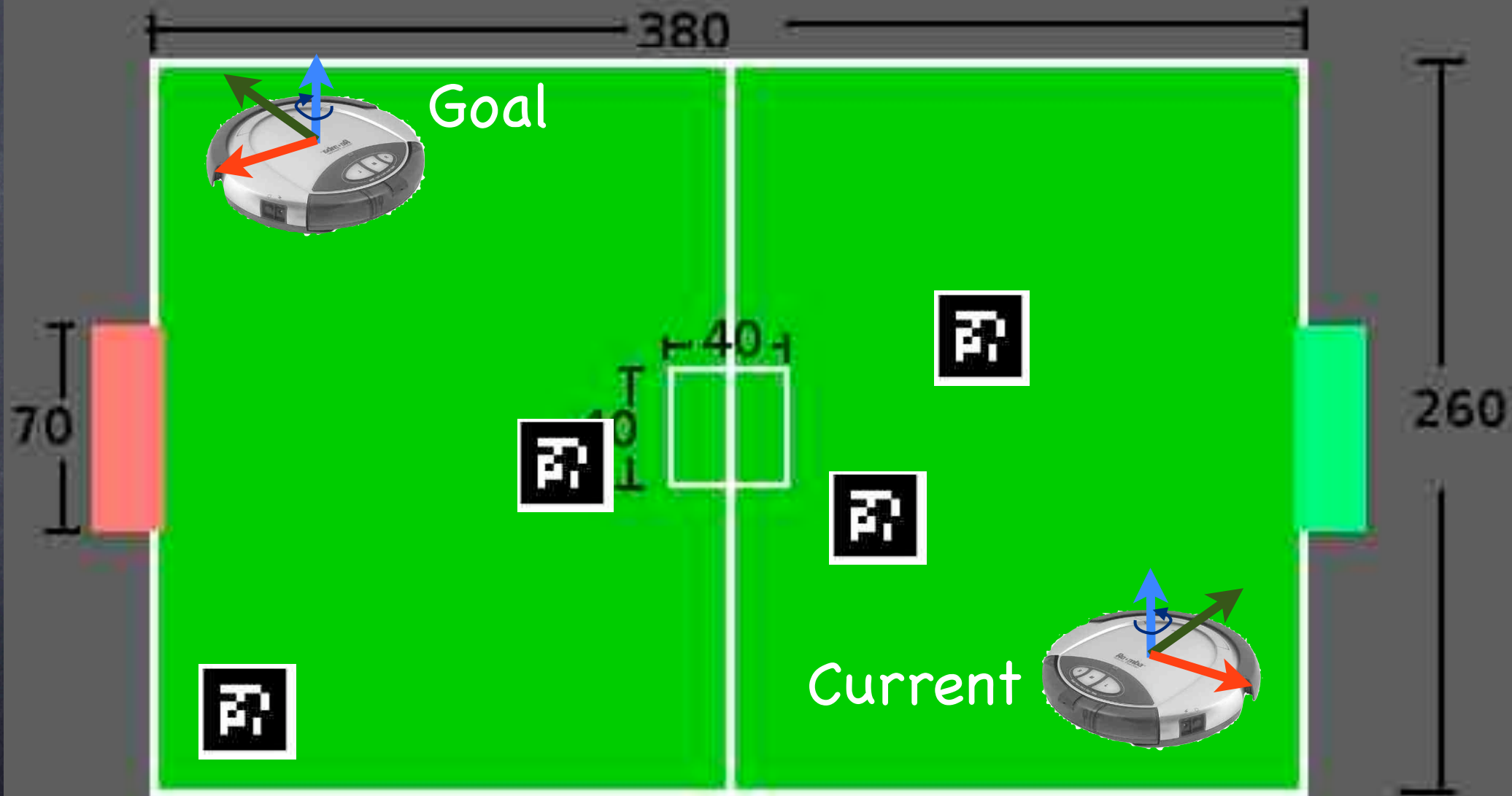


side view

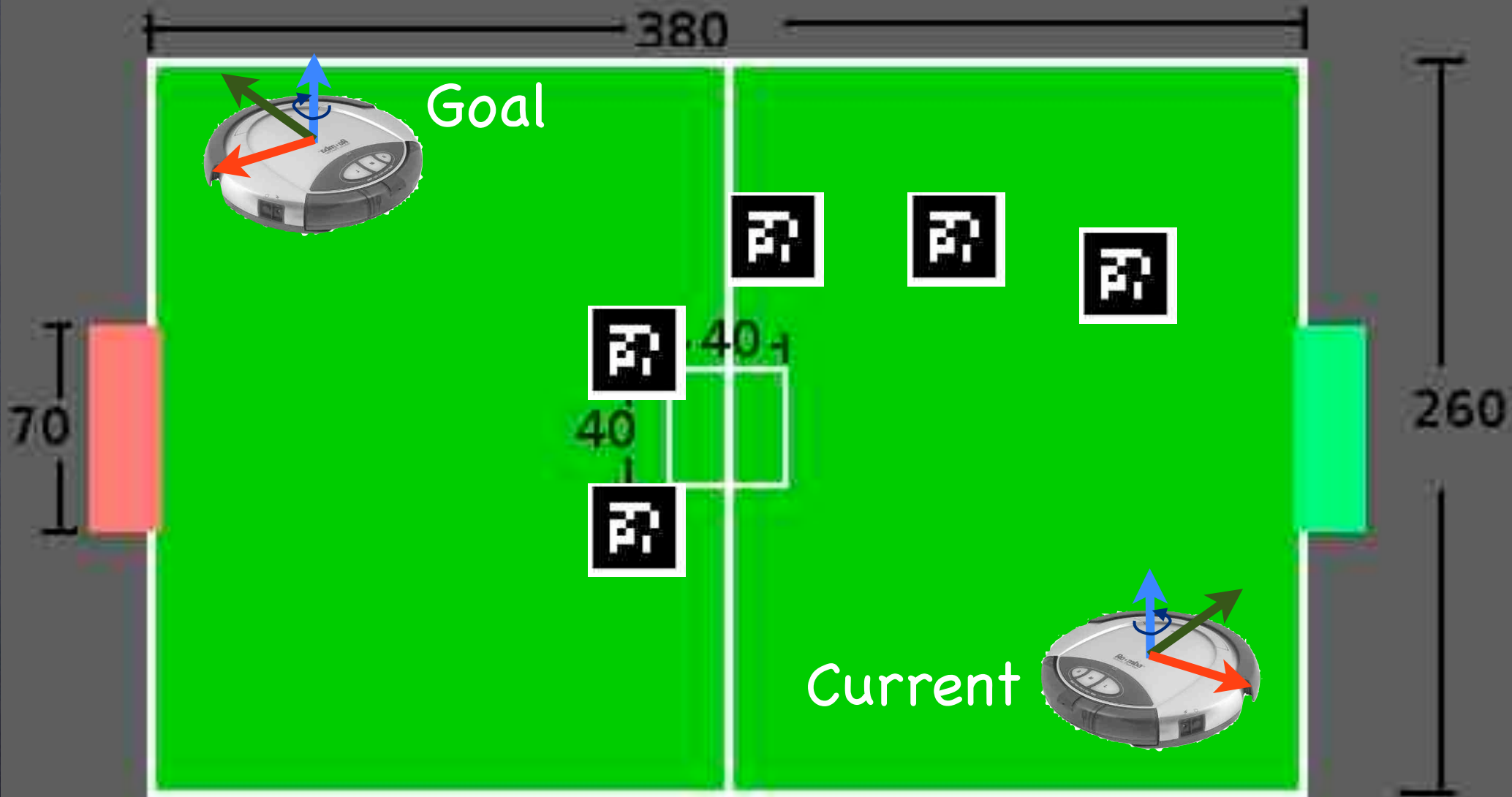
describe performance for this case



describe performance for this case



describe performance for this case



matlab example

👁 [/course/cs148/pub/pfield.m](#)

