

Single-Parameter Ascending Auctions

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Ausubel and Milgrom observed that the Vickrey auction, while elegant in theory, is not prevalent in practice. We discuss some advantages of open-outcry, ascending (*a.k.a.* English) auctions over sealed-bid auctions. We then characterize ascending auctions in general, and describe several specific instances.

“The Lovely but Lonely Vickrey Auction” is the title of a paper by two prominent economists, Ausubel and Milgrom,¹ who note that the Vickrey auction is indeed lovely in theory but not especially prevalent in practice.^{2,3} On the contrary, most auction houses sell their wares via an open-outcry, ascending (*a.k.a.* English) auction.

Why is this?

One likely reason is the fact that bidders rarely have a precise number in mind that articulates what a good might be worth to them. For example, it is not obvious to me how I can assign a monetary value—my willingness to pay—to my enjoyment of a piece of art that hangs on my wall? And for companies bidding on contracts with inherent monetary values, it may be computationally intensive to determine these values.

On the other hand, even without knowledge of a precise value, it may still be possible to answer (so-called **demand**) queries of the form, “Are you willing to pay x for a good?”, which require only a bound on this value. Such auctions require less deliberation on the part of bidders, making them less challenging to enter, and hence, more inviting to bidders.⁴ Moreover, even when the bidders values happen to be known, these auctions reveal less information about those values to other bidders and the auctioneer.

Second, and arguably even more powerful, bidders tend to engage in bidding wars during English auctions. Even when bidders know their precise values for the goods at hand, they still might bid beyond those values. This behavior is rooted in our psychology, as “losses loom larger than gains”.⁵ Applied to auctions, this maxim suggests that a bidder can become attached to a good while she is winning that good, and might therefore be willing to bid higher than her value to hold on to her tentative winnings. Furthermore, some might associate shame with losing, and pride with winning, especially when auction results are made public.

Remark. It has been said that “the only thing worse than losing an auction is winning.” Winning bidders often regret having won

¹ Lawrence M. Ausubel and Paul Milgrom. The Lovely but Lonely Vickrey Auction. Discussion Papers 03-036, Stanford Institute for Economic Policy Research, August 2004

² A notable exception were stamp auctions during the 19th century, in which bids were sent via post to auctioneers in sealed envelopes.

David Lucking-Reiley. Vickrey auctions in practice: From nineteenth-century philately to twenty-first-century e-commerce. *Journal of Economic Perspectives*, 14(3):183–192, September 2000

³ A second, more recent notable exception is online ad auctions!

⁴ Remember, attracting bidders is essential to running a profitable auction!

⁵ Amos Tversky and Daniel Kahneman. Loss aversion in riskless choice: A reference-dependent model. *The Quarterly Journal of Economics*, 106(4):1039–1061, 1991

an auction, because upon winning, it is revealed to them that their bid was greater than everyone else's bid, and hence everyone else's value (assuming no overbidding). If a bidder is unsure of his own value, even if it is not definitively greater than his bid, he may still experience **buyer's remorse**, a feeling of post-purchase regret, stemming, for example, from the fact that other alternatives are no longer available, because of a reduction in purchasing power.

Finally, if there are any doubts about an auctioneer's integrity, an English auction is preferable to a sealed-bid auction. Since it is more transparent, bidders can trust the outcome of an open-outcry mechanism much more readily than that of a sealed-bid mechanism. Although auctioneers can, and sometimes do, hire shill (i.e., fake) bidders to artificially raise the price of a good, it is riskier to do so in an open-outcry than in a sealed-bid environment, as these shill bidders would be on display for all to witness.

In sum, the following three phenomena help explain why English auctions are more common than Vickrey auctions:

1. greater transparency
2. potentially more revenue, because bidding wars can arise, and simpler auction formats are more attractive to bidders
3. requires less deliberation on the part of bidders to determine their values, and reveals less information about the bidders' values to other bidders and the auctioneer alike

Since the Vickrey auction is rarely used in practice, an alternative model of auctions is needed. In search of such an alternative, we now turn our attention to indirect mechanisms, specifically ascending auctions, in which prices are adjusted over time.

For our purposes, an ascending auction is an iterative algorithm that operates as follows:

- The auction proceeds in discrete rounds, $t \in \{0, \dots\}$.
- At each round t , the auction maintains a **state** $\mathbf{s}^t = (\mathbf{x}^t, \mathbf{p}^t)$, consisting of the current (tentative) allocation \mathbf{x}^t and price vector \mathbf{p}^t .
- An **allocation** \mathbf{x}^t at round t is an assignment of goods to bidders.
- **Prices** are per good (as opposed to per bundle: e.g.,⁶), and can only increase as the auction proceeds (i.e., $\mathbf{p}^{t+1} \geq \mathbf{p}^t$, for all $t \in \{0, \dots\}$). The amount by which the price increases at round t is called the **price increment**, and it is denoted ϵ^t . So, if the price of good j increases during round $t + 1$, then $p_j^{t+1} = p_j^t + \epsilon^t$. In general, the price increment need not be constant across rounds.

⁶ David C. Parkes. iBundle: An efficient ascending price bundle auction. In *Proceedings of the 1st ACM Conference on Electronic Commerce*, pages 148–157, New York, NY, USA, 1999. Association for Computing Machinery

- Given the current state, queries can take the form of **demand queries**, in which bidders are asked what bundle of goods they prefer, or **value queries** (as in sealed-bid auctions), in which bidders are asked their value(s) for a bundle(s) of goods.
- The final allocation and prices may be any (even randomized) function of the auction's history (i.e., the sequence of states).
- Initially, the good(s) is (are) allocated to the seller, while prices are initialized at reserve values, often zero (e.g., $\mathbf{p}^0 = \mathbf{0}$).

An ascending auction is further specified by a set of rules:

- **Allocation and pricing (i.e., payment) rules** determine the next state (i.e., allocation and price vector), given the bidders' replies to their queries. An example allocation rule might be to allocate each good to a bidder that demands it. An example pricing rule might be to increase prices on all overdemanded goods (i.e., goods for which demand exceeds supply).
- The auction's **termination rule** determines when the auction ends, which in the case of a single good auction is when prices are high enough that no good is overdemanded.
- An **information revelation policy** determines what part of the state is revealed to each bidder. For example, the current prices might be revealed to all bidders, while the tentative winners might be revealed only to the tentative winners themselves.
- There may be some additional **activity rules**, such as a bidder cannot exit the auction and then re-enter again later. The auction may also terminate if none of the bidders' replies to their queries are valid, meaning they do not satisfy the activity rules.
- Although unlikely in auctions with value queries, ties are common in auctions with demand queries, especially when the price increment is large. Thus, all auctions need a **tie-breaking rule**.

We depict the rules for three ascending auctions for a single good in the tables below: an English auction, an eBay auction, and a Japanese auction (a demand query version of the English auction with an activity rule that forbids bidders from coming and going).⁷

The eBay auction design is modelled after the English auction. Both employ value queries, and under ideal conditions (i.e., limited strategizing by bidders), yield something very close to the outcome of a Vickrey auction, namely, an efficient allocation, and a payment near the second-highest value. The primary difference between them is the termination rule. The eBay auction ends at a fixed time, while the English auction continues until quiescence.⁸

⁷ We also contrast these designs with two descending auctions, the second of which is reverse: i.e., run by a buyer, with suppliers bidding to produce goods, rather than run by a seller, with buyers bidding to consume goods.

⁸ An alternative auction design developed by Amazon mimicked the English auction even more closely, as it, too, proceeded until quiescence. You will explore this design in your homework.

We do not elaborate on how the price increment ϵ^t at round t is determined, as it may be at the discretion of a seasoned auctioneer (i.e., heuristic!). We do note, however, that Japanese auctions are also known as clock auctions, as the incremental price increases are usually constant, and thus analogous to a ticking clock.

| Rules | English Auction |
|------------------------|---|
| Information Revelation | All (even bidding) information is public |
| Value Queries | "Name your bid above $\$x$?", where $\$x \geq p^t + \epsilon^t$? (The parameter ϵ^t is set by the auctioneer) |
| Allocation Rule | A highest bidder |
| Pricing Rule | The highest bid |
| Activity Rule | Bids can only increase |
| Termination Rule | At most one reply |
| Tie-breaking | In favor of earlier bidders |

| Rules | eBay Auction |
|------------------------|---|
| Information Revelation | The current price and the tentative winner are public Bids are private |
| Value Queries | "Name your bid above $\$x$?", where $\$x \geq p^t + \epsilon$? |
| Allocation Rule | The highest bidder |
| Pricing Rule | The second-highest bid plus ϵ |
| Activity Rule | None (so bids can oscillate up and down) |
| Termination Rule | At a set time, or after a set number of rounds |
| Tie-breaking | In favor of earlier bidders |

| Rules | Japanese Auction |
|------------------------|---|
| Information Revelation | All (even bidding) information is public |
| Demand Queries | Raise your hand if $\$x$ is acceptable, where $\$x = p^t + \epsilon^t$ (The parameter ϵ^t is often a constant clock tick) |
| Allocation Rule | A random bidder with her hand up (If no bidders have their hands up, it is a tie) |
| Pricing Rule | The broadcast price, $\$x$ |
| Activity Rule | You gotta be in it to win it (Once a bidder's hand goes down, he forfeits) |
| Termination Rule | At most one hand up |
| Tie-breaking | Uniform at random among last remaining bidders |

The Dutch sell flowers, which are perishable goods that must be sold quickly, in descending clock auctions. The initial price in an ascending auction is low (typically, zero), while the initial price in a descending auction is very high: a price no buyer is willing to pay.

| Rules | Dutch Auction |
|------------------------|--|
| Information Revelation | Price information is public Once any value information is revealed, the auction ends |
| Demand Queries | Put your hand up as soon as $\$x$ is acceptable, where $\$x = p^t - \epsilon$ (The parameter ϵ is often a constant clock tick) |
| Allocation Rule | A random bidder with her hand up (If two bidders put their hands up, it is a tie) |
| Pricing Rule | The broadcast price, $\$x$ |
| Activity Rule | None |
| Termination Rule | At least one hand up |

A Reverse Auctions

In a reverse auction, there is one buyer (the auctioneer) and many sellers. In a descending, reverse auction, the buyer initializes the price very high—at a price at least one seller is sure to accept—and gradually decreases it, until at most one bidder (i.e., seller) remains.

| Rules | Reverse Auction |
|------------------------|--|
| Information Revelation | All (even bidding) information is public |
| Demand Queries | Hold your hands up if $\$x$ is acceptable, where $\$x = p^t - \epsilon$ (The parameter ϵ is often a constant clock tick) |
| Allocation Rule | A random bidder with her hand up (If no bidders have their hands up, it is a tie) |
| Pricing Rule | The broadcast price, $\$x$ |
| Activity Rule | Once a bidder's hand goes down, he forfeits |
| Termination Rule | At most one hand up |

It is also possible to imagine an ascending, reverse auction, where the price is initialized at a very low price at which no seller is willing to transact, so no sellers hands are raised. And then the price is incremented, until at least one seller raises his hand.

References

- [1] Lawrence M. Ausubel and Paul Milgrom. The Lovely but Lonely Vickrey Auction. Discussion Papers 03-036, Stanford Institute for Economic Policy Research, August 2004.
- [2] David Lucking-Reiley. Vickrey auctions in practice: From nineteenth-century philately to twenty-first-century e-commerce. *Journal of Economic Perspectives*, 14(3):183–192, September 2000.
- [3] David C. Parkes. iBundle: An efficient ascending price bundle auction. In *Proceedings of the 1st ACM Conference on Electronic*

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- [4] Amos Tversky and Daniel Kahneman. Loss aversion in riskless choice: A reference-dependent model. *The Quarterly Journal of Economics*, 106(4):1039–1061, 1991.