

# Today's agenda:

- ① classic retrieval (keyword-based)
- ② neural retrieval
- ③ RAG
- ④ General examples of compound AI systems + challenges

## Classic IR / BM25

- scope: large corpus of text documents (e.g., Wikipedia - potentially split into passages)
- input: textual query (e.g., question)
- output: Top-K RANKING of relevant docs

### \* simple case: "single-term" queries

- build term document matrix
- each cell says how many times a term appears in a doc (perhaps w/ reweighting)
- if query has a single term, just return K documents w/ largest weights for a single term

\* "against" has dif-  
weights for d4, d7

|         | d1 | d2 | d3 | d4 | d5 | d6 | d7 | d8 | d9 | d10 |
|---------|----|----|----|----|----|----|----|----|----|-----|
| against | 0  | 0  | 0  | 1  | 0  | 0  | 3  | 2  | 3  | 0   |
| age     | 0  | 0  | 0  | 1  | 0  | 3  | 1  | 0  | 4  | 0   |
| agent   | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0   |
| ages    | 0  | 0  | 0  | 0  | 0  | 2  | 0  | 0  | 0  | 0   |
| ago     | 0  | 0  | 0  | 2  | 0  | 0  | 0  | 0  | 3  | 0   |
| agree   | 0  | 1  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0   |
| ahead   | 0  | 0  | 0  | 1  | 0  | 0  | 0  | 0  | 0  | 0   |
| ain't   | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0   |
| air     | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0   |
| aka     | 0  | 0  | 0  | 1  | 0  | 0  | 0  | 0  | 0  | 0   |

\* what about "multi-term" queries?

$$\text{Relevance Score}(\text{query}, \text{doc}) = \sum_{\text{term} \in \text{query}} \text{Weight}_{\text{doc}, \text{term}}$$

\* core questions in classical IR:

- How do we best tokenize queries / documents?
- How do we best WEIGHT term-document pair?

\* Intuitions behind term-document weightings:

### 1) FREQUENCY

- if term  $t$  occurs frequently in document  $d$  - doc is more likely to be relevant for queries w/  $t$

### 2) NORMALIZATION

- if term  $t$  is rare overall, any document  $d$  including  $t$  is likely very relevant
- if  $d$  is overall short and contains  $t \rightarrow$  probably important

TF-IDF: Term-Document weighting

•  $N = | \text{collection} |$

•  $df(\text{term}) = \left| \{ \text{doc} \in \text{collection} : \text{term} \in \text{doc} \} \right|$   
     $\nearrow$  which docs contain  $t$   
    , term freq

$$\text{TF}(\text{term}, \text{doc}) = \log(1 + \text{freq}(\text{term}, \text{doc}))$$

↳ grows sublinearly w/ frequency

$$\text{IDF}(\text{term}) = \log \left( \frac{N}{\text{df}(\text{term})} \right)$$

inverse doc frequency

\* if many docs contain term, IDF will be smaller

↳ grows sublinearly w/  $1/\text{DF}$

\* accounts for normalization

$$\text{TF.IDF}(\text{term}, \text{doc}) = \text{TF}(\text{term}, \text{doc}) \times \text{IDF}(\text{term})$$

$$\text{TF.IDF}(\text{query}, \text{doc}) = \sum_{\text{term} \in \text{query}} \text{TFIDF}(\text{term}, \text{doc})$$

\* BM25: Inspired from TFIDF, but better

→ change: term frequency saturates to constant value  
and penalizes LONGER docs

$$\text{IDF}(\text{term}) = \log \left( 1 + \frac{N - \text{df}(\text{term}) + 0.5}{\text{df}(\text{term}) + 0.5} \right)$$

$$\text{TF}(\text{term}, \text{doc}) = \frac{\text{freq}(\text{term}, \text{doc}) \cdot (k+1)}{\text{freq}(\text{term}, \text{doc}) + k \cdot (1 - b + b \cdot \frac{|\text{doc}|}{\text{avg doc len}})}$$

\* k, b are params

• Efficient Retrieval: Inverted Indexing

raw collection: docs → terms

term doc matrix: terms → docs

↳ could be very sparse!

\* inverted index: sparse representation of term-doc matrix (maps each unique term  $t$  to "posting list")

↳ posting list contains list of docs where term appears, + frequency of term  $t$  in each doc

\* Intents of calculating TF, IDF:

- when we see a query:

- for each term:

→  $df(\text{term})$  stored in inverted index

→  $tf(\text{term}, \text{doc})$  stored

→ can calculate TF, IDF

\* until 2019, when BERT-based ranking came out - BM25 was easy to deploy, strong, baseline

- JUDGING IR SYSTEMS:

1) effective (good accuracy) and efficient

^  
various measures

- latency per query
- throughput (queries/sec)
- space for index
- HW required
- scaling to larger indexes

→ success and MRR

- let rank  $\{1, 2, 3 \dots\}$  be position in returned top-k of 1<sup>st</sup> RELEVANT DOC

success @k =  $\begin{cases} 1 & \text{if rank} \leq k \\ 0 & \text{otherwise} \end{cases}$

→ if user needs returned list to contain anything in top-k

reciprocal rank at k =  $\begin{cases} 1/\text{rank} & \text{if rank} \leq k \\ 0 & \text{otherwise} \end{cases}$

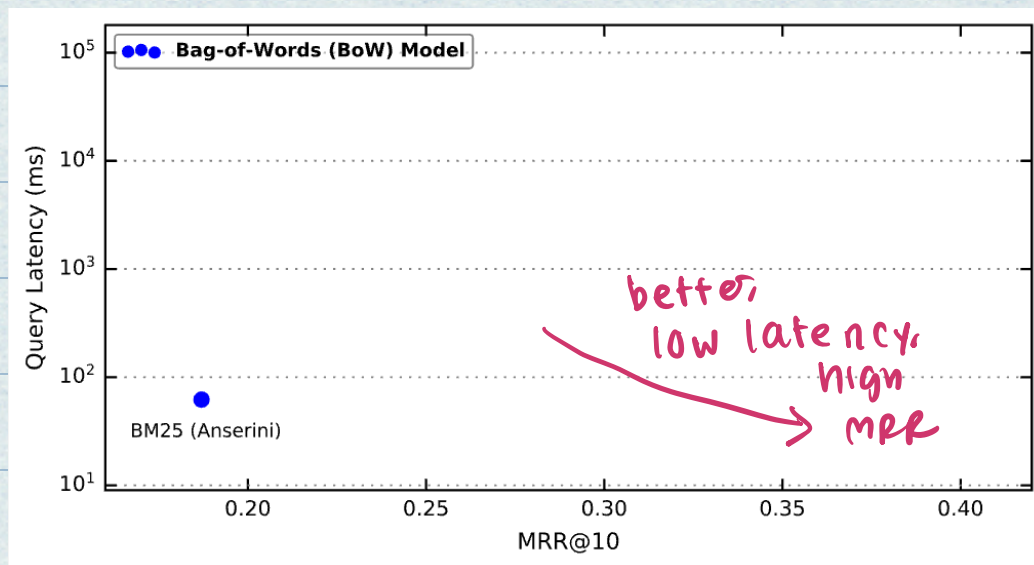
→ does not position

→ MRR → mean of this across queries

→ look at  $k=1, 5, 100, 1000 \dots$

→ for bm25, we get:

low latency, but, low MRR?



- how do we increase MRR (accuracy)

for some

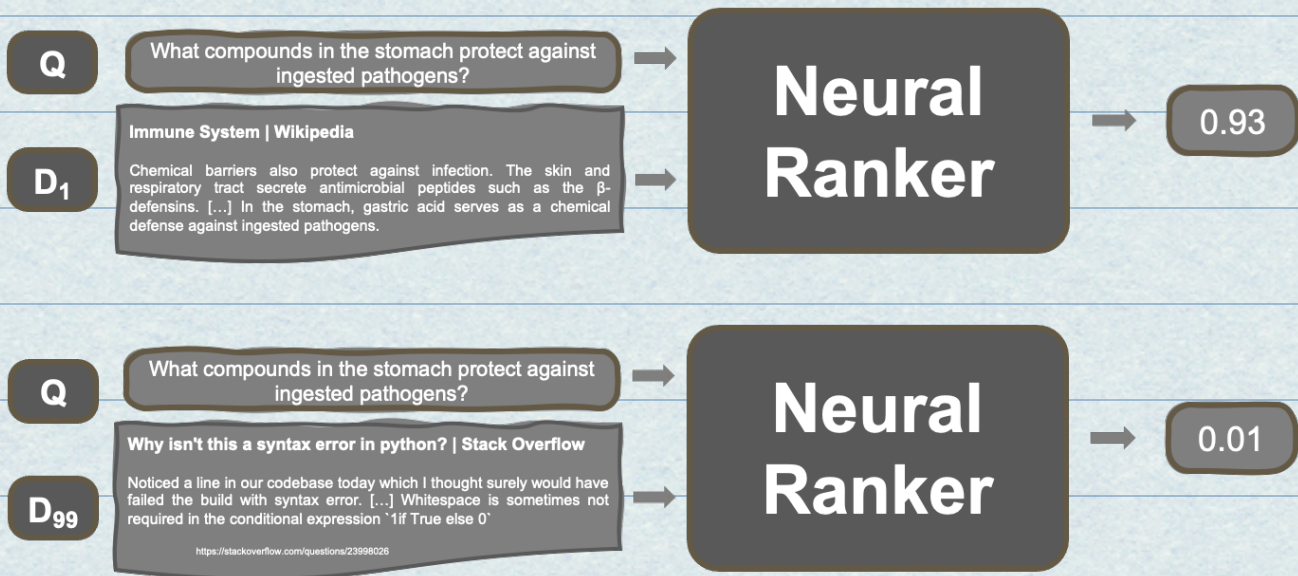
cost of query latency?

\*ms moco: dataset widely used

for retrieval (Bing queries, 9 mil. passed)

what would input and output of neural ranking be?

- if neural retriever were a blackbox:



Om

- input = query,  
document

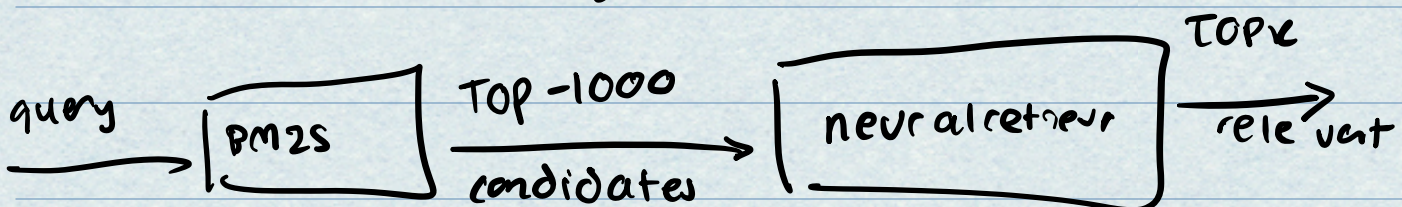
- Output = score (relevance, higher = more relevant)

- TOPK docs = ranked ordering of docs  
according to score

\* if we have 9 billion passages, and each  
query.doc pair inference takes 1ms  $\rightarrow$  still 9s  
per query (unacceptable!)

IDEA:

- do reranking:



\* potential problem: if BM2S misses

some docs, we won't get them in  
our ans ("artificial recall ceiling")

## HOW DO WE CAPTURE QUERY-DOCUMENT RELEVANCE?

1. Tokenize query and document
2. Embed tokens into static vector

repr

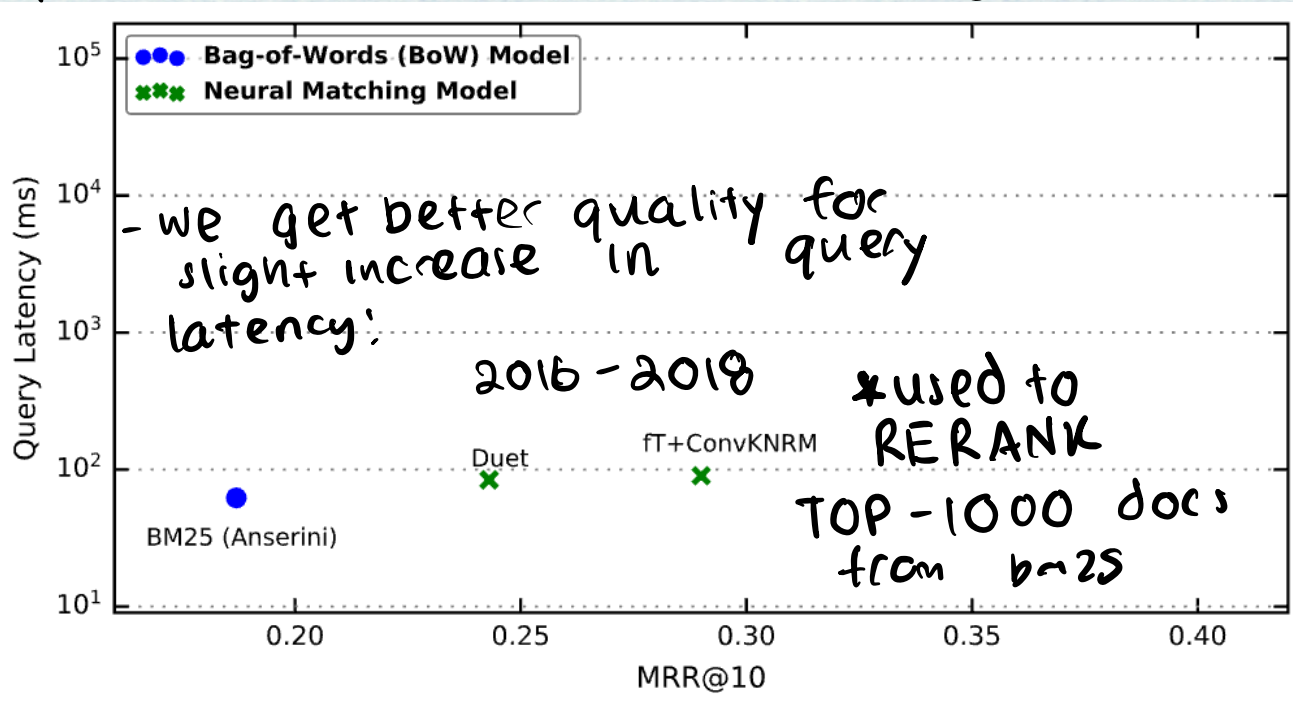
3. Build query-document interaction  
matrix

↳ similarity scores b/w each

pair of word embeddings across

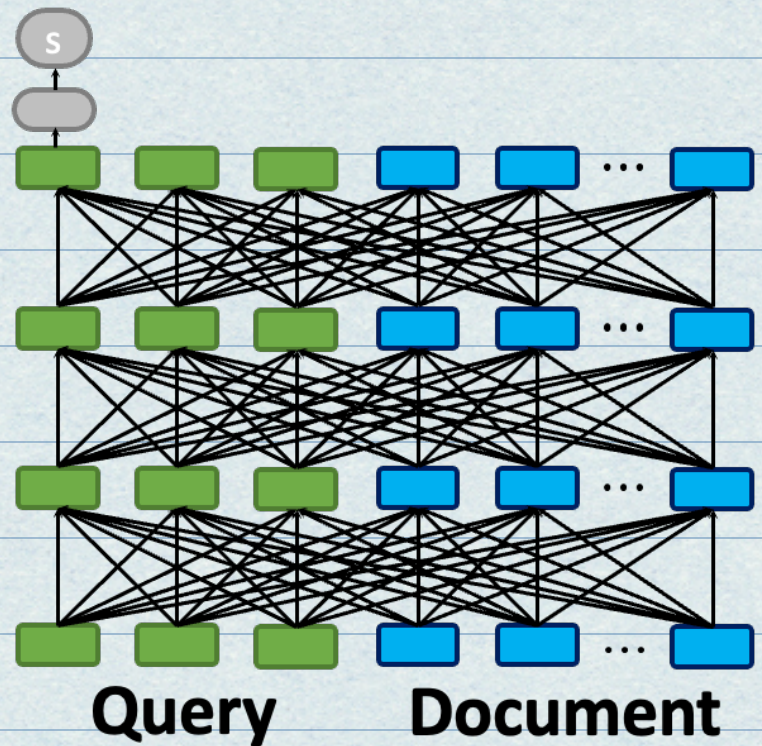
query/doc, such as cosine similarity

4. Reduce dense matrix to a single score

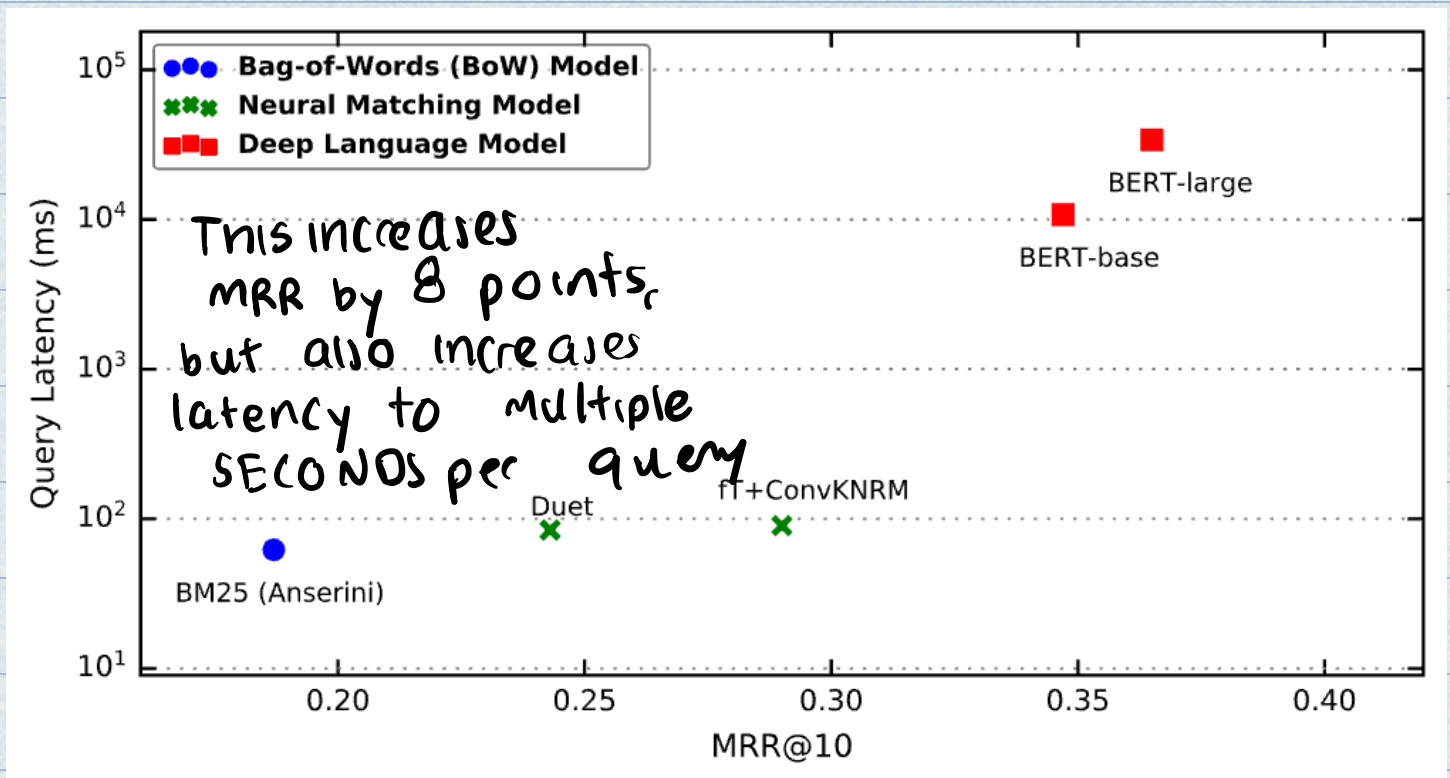


# POST 2018: All-to-All interaction w/ BERT

1. Feed BERT the query and document as one sentence w/ two segments
2. Run this through BERT layers
3. Extract final output embedding



- use custom linear layer to reduce to single score



How do we INCREASE quality but keep latency low?

\* Bert rankers slow as computations are redundant:

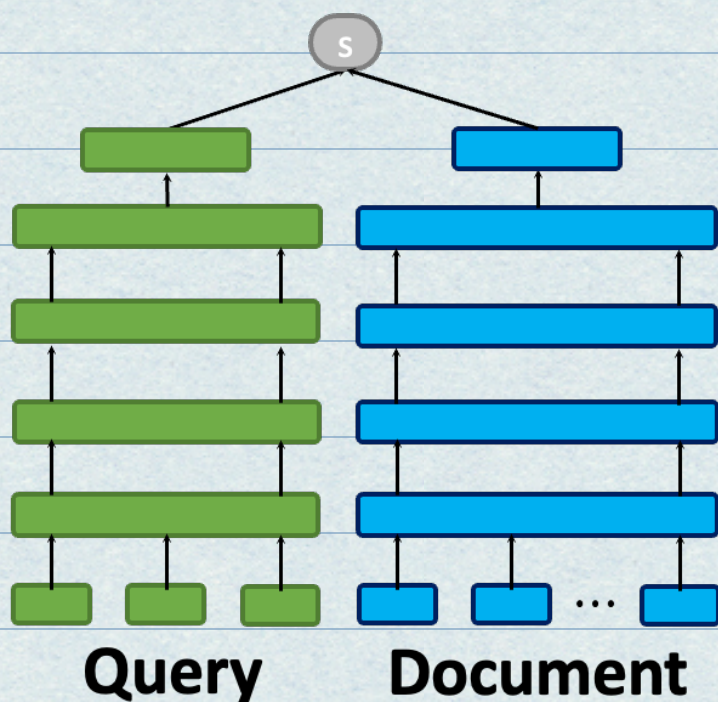
- repr. query (1000 times for 1000 docs)
- repr. doc (for EACH inference)
- matching

\* can we precompute document representations? and "cache" these for use across queries?

### REPRESENTATION SIMILARITY:

- tokenize query / doc
- independently encode query / doc
- use dot product to estimate similarity

- doc reprs can be precomputed!
- query reprs can be reused across dot products



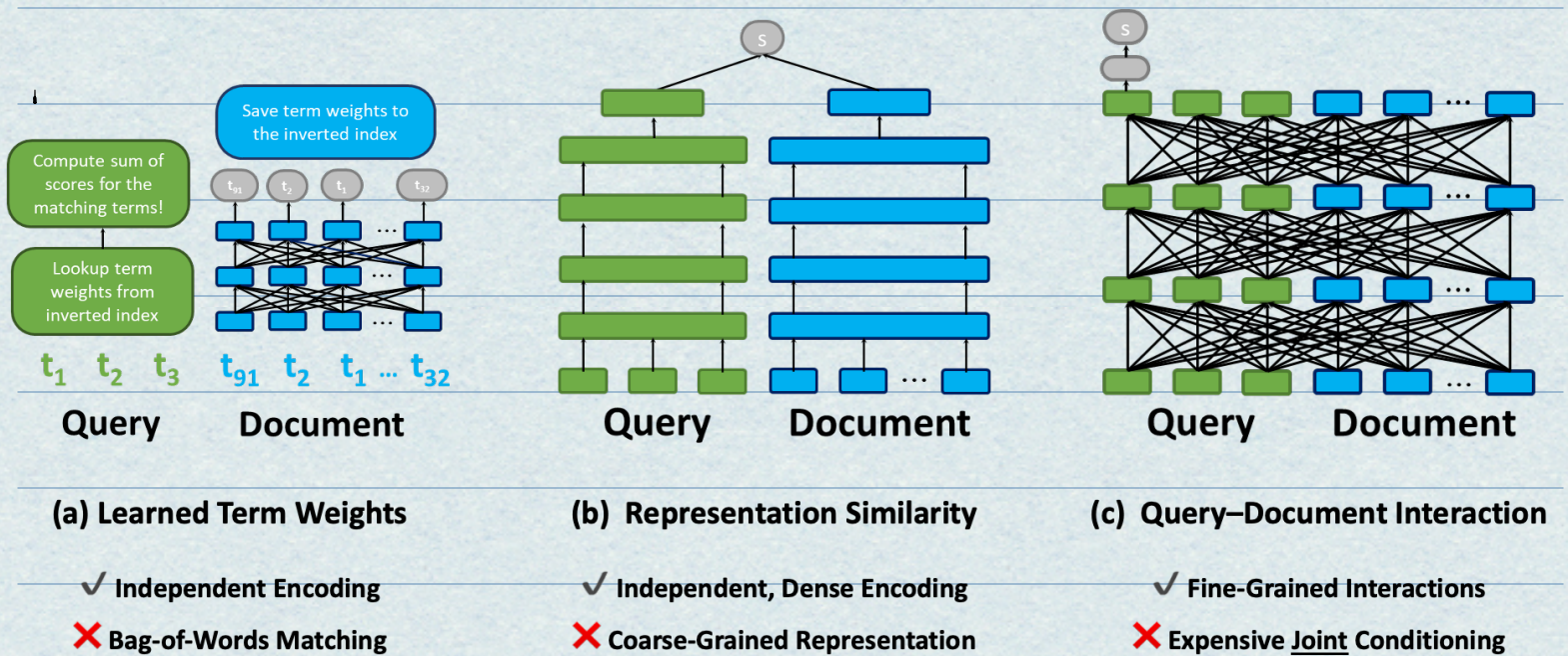
- Downsides of JUST doing representation similarity:

- single-vector repr could be coarse-grained

- no FINE-GRAINED interaction

↳ e.g. btwn individual tokens in query to doc

## SUMMARY SO FAR



- we didn't

look at this

specifically

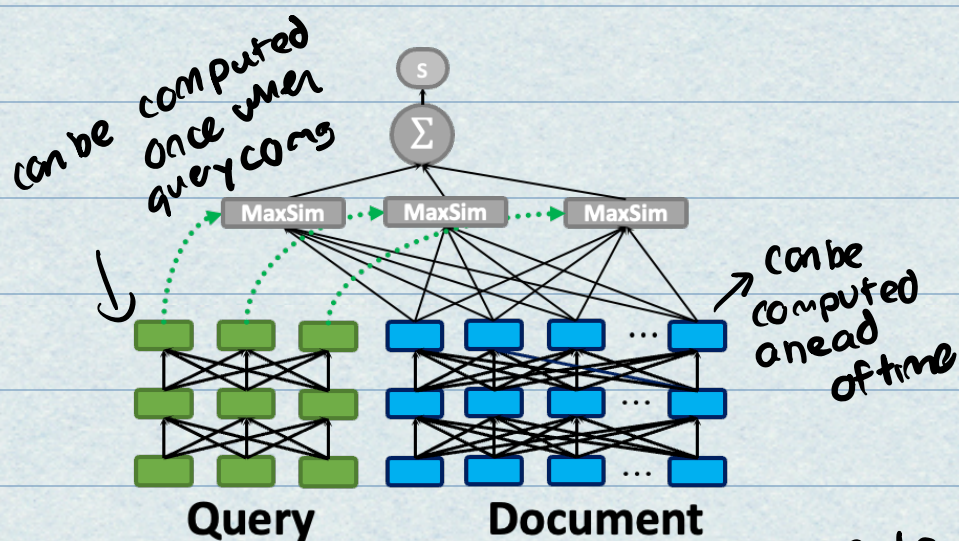
but this is

like bm25 w/

better weights

**LATE INTERACTION:** keep precomputation, but have fine-grained interactions (ColBERT, Khattab & Zaharia)

- insight: feed BERT into query / each doc, but KEEP output embeddings corresponding to each token (don't feed in output to final linear layer)
  - ↳ recall model produces  $1 \times d$  vector per token
- now for each query token embedding, compute max similarity score across all doc embeddings
- sum all these partial scores.

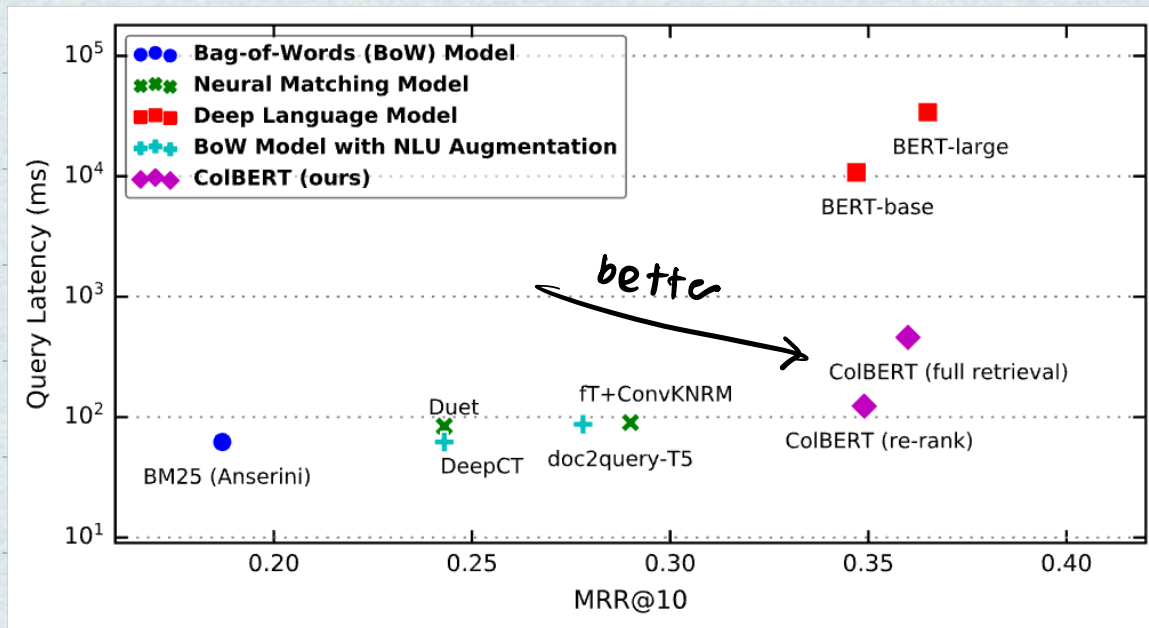


- note that ColBERT

(d) Late Interaction represents Doc as  $N \times d$  matrix (rather than a single vector)  
(i.e., ColBERT)

Omar Khattab and Matei Zaharia. "ColBERT: Efficient and effective passage search via contextualized late interaction over BERT." SIGIR'20.

- w/ late interaction, we can resolve mismatches from before!



RAG: LLMs struggle on knowledge-intensive tasks

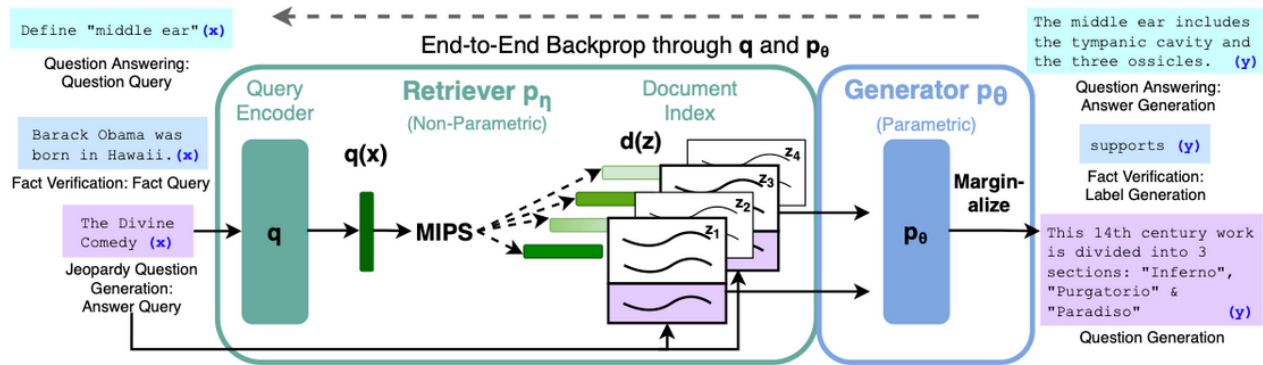
1. retrieve docs relevant to input from an external DB (either retriever OR vector DB)
2. Augment LLM input w/ retrieved docs.
3. Generate response on augmented input

- we need:

- LM
- retrieval model (turn query into embeddings)
- DB w/ representations of docs - to search on query with

Early RAG approaches: fine-tune pre-trained LM  
and query encoder:  
(doc encoder frozen)

During fine-tuning, jointly train retriever (query encoder) and language model



Lewis et al '21 <https://arxiv.org/pdf/2005.11401>

- can change weights of LM OR  
query encoder via backprop