

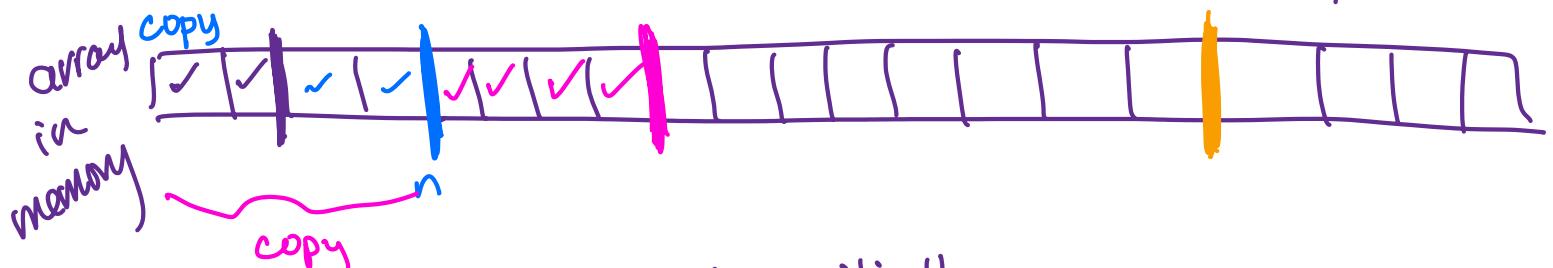
## Lecture 12 – ArrayLists and Runtime

Summarize Worst-Case Runtimes (in terms of number of elements in the list)

	LinkList (immutable)	MutableList (Link)	ArrayList
size	Constant (if keep field, otherwise linear to compute)		
addFirst	Constant	constant	for now, linear
addLast	linear	constant	usually constant
get(index)	linear	linear	constant

What's with "usually constant"?

unless array is full, then linear



Create an array with 2 cells initially  
• each of the first two addLasts costs constant time

What is the cost of addLast?

- constant if array has space
- otherwise linear in #elts

} By worst case, addLast is linear, even though usually constant

What if instead we ask for the time to make  $K$  calls to addLast?

what's the average time needed per call among the  $K$  calls?

$$\frac{\text{total cost of } K \text{ calls}}{K}$$

this is where the amount of resizing matters

$K$  times

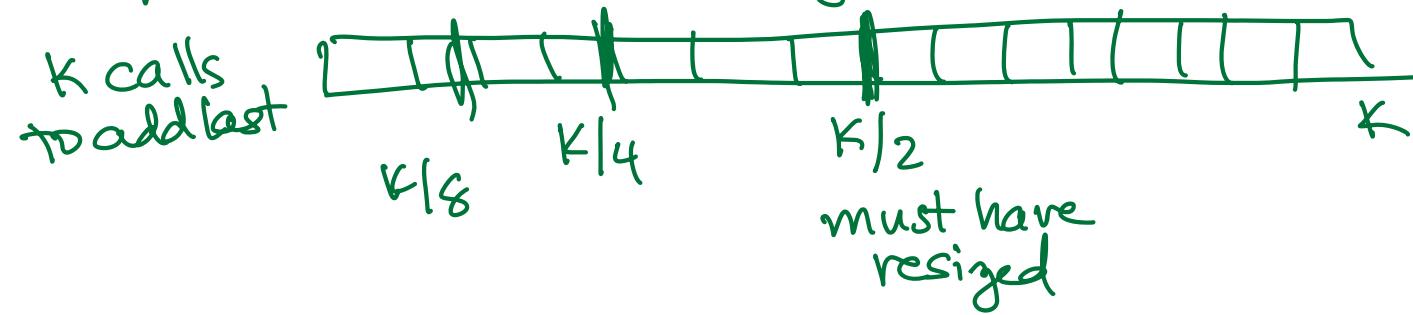
{ addLast  
addLast  
:  
addLast

if we add 1 cell per resize, then each call to addLast is linear time.

total cost is  $\frac{O(K) * K}{K}$  — each call  
set linear time per call

average it out

Now let's double the size when out of room



total cost of getting to k elements

$$\dots + \frac{k}{8} + \frac{k}{4} + \frac{k}{2} + k \quad \text{cost for each insert}$$

Sums to  $k * 2$  in total costs

---

amortized cost is  $\frac{2k}{k}$  avg to 2 constant  $O(1)$

addLast has constant amortized time

over many calls to addLast

## Runtime of AddLast/AddFirst with Resizing

```

public class ArrList {
    String[] theArray; // the underlying array that stores the elements
    int eltcount; // how many elements are in the array
    int end; // the last USED slot in the array

    private void resize(int newSize) {
        // make the new array
        String[] newArray = new String[newSize];
        // copy items from the current theArray to newArray
        for (int index = 0; index < theArray.length; index++) {
            newArray[index] = this.theArray[index];
        }
        // change this.theArray to refer to the new, larger array
        this.theArray = newArray;
    }

    public void addLast(String newItem) {
        if (this.isFull()) {
            // add capacity to the array
            this.resize(this.theArray.length + 1);
            // now that the array has room, add the item
            this.addLast(newItem);
        } else {
            if (!(this.isEmpty())) {
                this.end = this.end + 1;
            }
            this_eltcount = this_eltcount + 1;
            this.theArray[this.end] = newItem;
        }
    }
}

```

<pre> public class ArrTest {     ArrList flavors = new ArrList(2);     flavors.addLast("mint")     flavors.addLast("grape")     new Course("cs1410", 200)     flavors.addLast("lemon")     flavors.addLast("cherry") }  ----- - <u>environment</u> flavors → @1221 </pre>	@1221	<b>ArrList</b> theArray: @1222 end: 1      eltcount: 2
	@1222	"mint"
	@1223	"grape"
	@1224	Course("cs1410", 200)
	@1225	
	@1226	
	@1227	
	@1228	

**How many resizes get done across N calls to addLast? How does this affect runtime?**

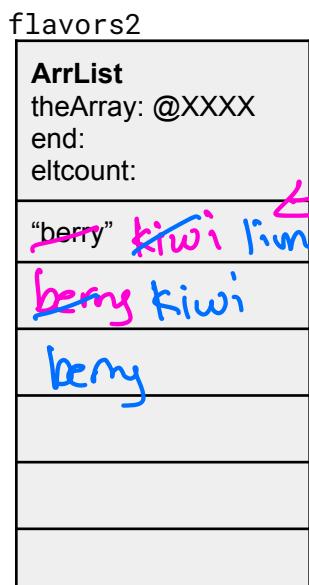
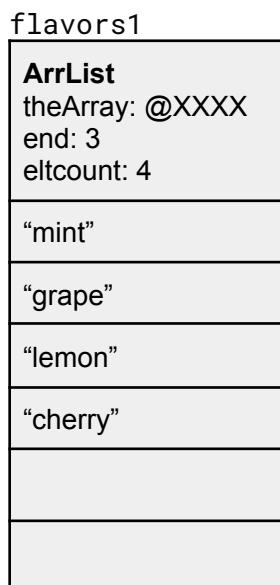
```
ArrList flavors = new ArrList(2);
```

	Resize by 1	Resize by 2	Resize by double
flavors.addLast("mint")			
flavors.addLast("grape")			
flavors.addLast("lemon")			
flavors.addLast("cherry")			
flavors.addLast("mango")			
flavors.addLast("orange")			
flavors.addLast("coffee")			

**Enabling AddFirst – Leave space at front and end of the array to avoid resizing**

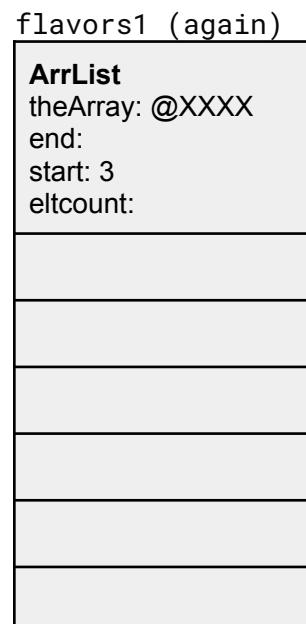
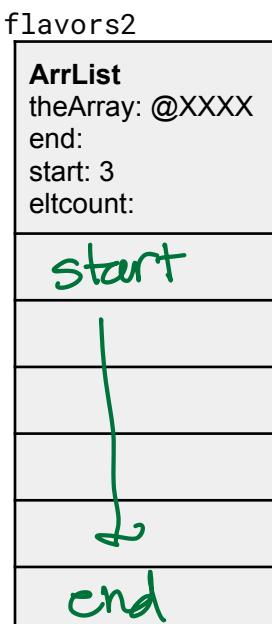
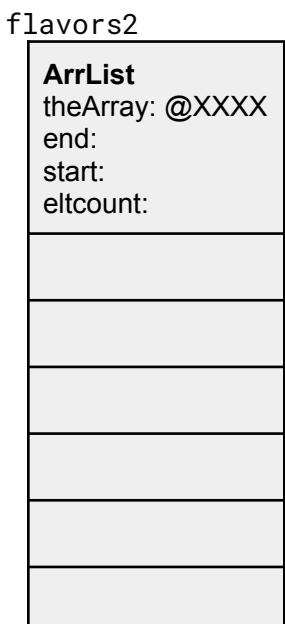
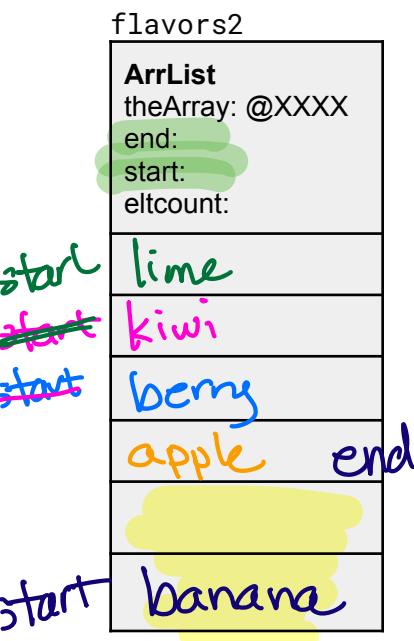
```
public class ArrTest1 {  
    ArrList flavors1 = new ArrList(6);  
    flavors.addLast("mint")  
    flavors.addLast("grape")  
    flavors.addLast("lemon")  
    flavors.addLast("cherry")  
}
```

```
public class ArrTest2 {  
    ArrList flavors2 = new ArrList(6);  
    flavors.addLast("berry")  
    flavors.addFirst("kiwi")  
    flavors.addFirst("lime")  
    flavors.addLast("apple")  
}
```



Kiwi needs to be here.  
suggests that to addFirst,  
we move everything  
down by 1 slot

(lots of copying)  
ensues!



addFirst("banana")  
what needs to happen?

class ArrList {

int start ← where first elts is

int end ← where last elts is

public addLast ()  
if ( $\text{end} + 1 == \text{start}$ )  
  \ loops - array is full, must resize

assumes end & start in  
middle of the array

$(\text{end} + 1) \% \text{capacity} == \text{start}$

↑  
# of slots