

## Lecture 12 – ArrayLists and Runtime

Summarize Worst-Case Runtimes (in terms of number of elements in the list)

(LIKE HW2)

	LinkedList	MutableList (Link)	ArrayList
size			
addFirst			
addLast			
get(index)	$O(N)$ LINEAR	$O(N)$ LINEAR	$O(1)$ CONSTANT

So far we've seen three ways to look at lists...

LinkedList (or ImmutableList)

- Has a chain of nodes with (at least) a "next" field
- Each node could be at any spot in memory

For get() => Need to follow "chain" of nodes (or Links) to get a specific item

=> Linear runtime over the size of the list =>  $O(N)$

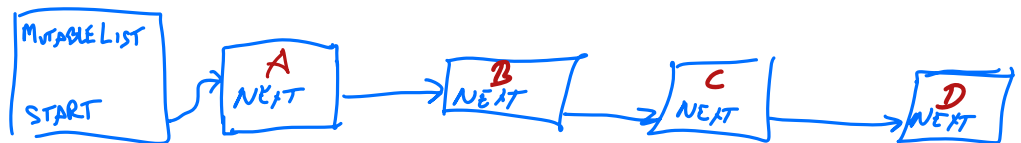
SAY WE HAVE LIST WITH STRINGS ['A', 'B', 'C', 'D']



MutableList (like HW2)

- Same "chain" of nodes
- MutableList class has "start" field that points to nodes
- MutableList might have other fields like in HW2 (end, etc.)

For get() => same as LinkedList =>  $O(N)$

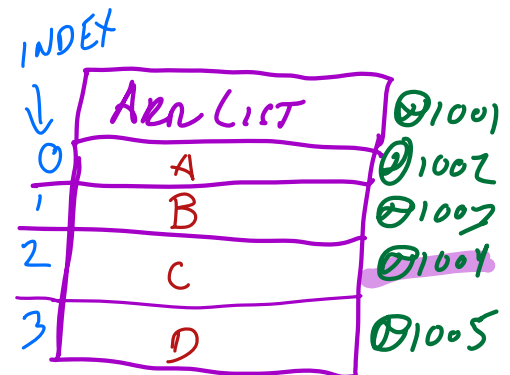


ArrayList (ArrayList in Java)

- Relies on arrays: at start, reserve a fixed number of consecutive memory slots
- When array is full, resize by creating a new array and copying over all elements

For get() => Since the array elements are always in contiguous memory slots, can look up the i'th element just based on the starting address value.

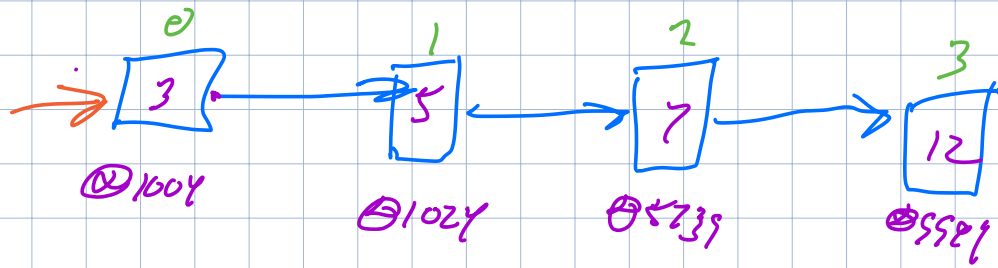
=> Just add to the starting address => constant time =>  $O(1)$



Ex.

$$\text{GET}(2) = \underset{\substack{\uparrow \\ \text{START}}}{01001} + \underset{\substack{\uparrow \\ \text{INDEX}}}{2} + 1$$

(3, 5, 7, 12]



GET(3)

## Runtime of AddLast/AddFirst with Resizing

```
public class ArrList {
    String[] theArray; // the underlying array that stores the elements
    int eltcnt;        // how many elements are in the array
    int end;           // the last USED slot in the array

    private void resize(int newSize) {
        // make the new array
        String[] newArray = new String[newSize];
        // copy items from the current theArray to newArray
        for (int index = 0; index < theArray.length; index++) {
            newArray[index] = this.theArray[index];
        }
        // change this.theArray to refer to the new, larger array
        this.theArray = newArray;
    }

    public void addLast(String newItem) {
        if (this.isFull()) {
            // add capacity to the array
            this.resize(this.theArray.length + 1);
            // now that the array has room, add the item
            this.addLast(newItem);
        } else {
            if (!(this.isEmpty())) {
                this.end = this.end + 1;
            }
            this.eltcnt = this.eltcnt + 1;
            this.theArray[this.end] = newItem;
        }
    }
}
```

⇒ WORST CASE RUNTIME??

For now, we make a new array 1 larger than the previous one each time we resize. We could call this the "resize policy" (This isn't a very good one, we'll learn a practical one soon.)

ADDLAST

```
public class ArrTest {
    ArrList flavors = new ArrList(2);
    flavors.addLast("mint")
    flavors.addLast("grape")
    new Course("cs1410", 200)
    ① flavors.addLast("lemon") ← RESIZE!
    ② flavors.addLast("cherry")
}
```

environment

flavors → @1221

@1221

ArrList

theArray: @1222

end: 1 2 3

eltcount: 1 2 3 4

@1222

"mint"

@1223

"grape"

@1224

Course("cs1410", 200)

@1225

MINT

@1226

GRAPE

@1227

LEMON

@1228

MINT

GRAPE

LEMON

CHERRY

### What's the worst case runtime of addLast?

It's a big more nuanced before, because it depends on if the array is full:

If array is full => resize => linear time operation (copy)

If array is not full => constant time (add to a slot)

⇒ As developers, we want to think about how often we "pay the cost" of resizing

How many resizes get done across N calls to addLast? How does this affect runtime?

```
ArrayList flavors = new ArrayList(2);
```

	<u>Resize by 1</u>	Resize by 2	Resize by double
flavors.addLast("mint")	CONST	CONST	
flavors.addLast("grape")	CONST	CONST	
flavors.addLast("lemon")	RESIZE	RESIZE (1x)	
flavors.addLast("cherry")	RESIZE	CONST	
flavors.addLast("mango")	RESIZE	RESIZE	
flavors.addLast("orange")	RESIZE	CONST	
flavors.addLast("coffee")	RESIZE	RESIZE	

Each resize is linear time due to the copy

For N calls, resize N/2 times => halved runtime cost => still linear runtime  $O(N)$

Overall, It's helpful to think about the amortized cost, which is the runtime across multiple calls to a method.

What happens in practice (as a general rule)

=> When you resize, double the size of the array

SEE NEXT PAGE

## ADD 2 ON EACH RESIZE

0	MINT
1	GRAPE

ADD LAST (LEMON)  
(RESIZE)

0	MINT
1	GRAPE
2	LEMON
3	CHERRY

New size: 4  
Items copied: 2  
addLast's before  
next resize: 2

ADD LAST (MANGO)  
(RESIZE)

0	MINT
1	GRAPE
2	LEMON
3	CHERRY
4	MANGO
5	ORANGE

New size: 6  
Items copied: 4  
addLast's before  
next resize: 2

ADD LAST (COFFEE)  
(RESIZE)

0	MINT
1	GRAPE
2	LEMON
3	CHERRY
4	MANGO
5	ORANGE
6	COFFEE
7	CHOCOLATE

New size: 8  
Items copied: 6  
addLast's before  
next resize: 2

### FOR THIS VERSION

SIZE 4 6 8 10

ITEMS COPIED 2 4 6 8

ADDS BEFORE RESIZE 2 2 2 2

Number of copies still grows linearly as array size grows  
=> linear runtime! => O(N)

## DOUBLE ARRAY ON RESIZE

0	MINT
1	GRAPE

ADD LAST (LEMON)  
(NEED TO RESIZE)

0	MINT
1	GRAPE
2	LEMON
3	CHERRY

New size: 4  
Items copied: 2  
addLast's before  
next resize: 2

ADD LAST (MANGO)  
(NEEDS TO RESIZE)

0	MINT
1	GRAPE
2	LEMON
3	CHERRY
4	MANGO
5	ORANGE
6	COFFEE
7	CHOCOLATE

New size: 8  
Items copied: 4  
addLast's before  
next resize: 4

SIZE	4	8	16	32	64
ITEMS COPIED	2	4	8	16	32
ADDS BEFORE RESIZE	2	4	8	16	32

By doubling the array each time we resize, we pay effectively pay a fixed portion of the cost equal to the number of items we add. Thus, if we divide up the total cost of copying over all elements in the array, the cost to add is constant!