

Project 3 questions?

Interest Points and Instance Recognition

Computer Vision

CS 143, Brown

James Hays

Last time

- Detecting corner-like points in an image

Today

- Local invariant features
 - Detection of interest points
 - (Harris corner detection)
 - Scale invariant blob detection: LoG
 - Description of local patches
 - SIFT pipeline for invariant local features

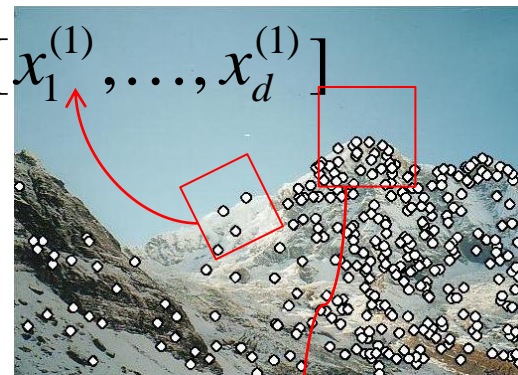
Local invariant features: outline

1) Detection: Identify the interest points



2) Description: Extract vector feature descriptor surrounding each interest point.

$$\mathbf{x}_1 = [x_1^{(1)}, \dots, x_d^{(1)}]$$



$$\mathbf{x}_2 = [x_1^{(2)}, \dots, x_d^{(2)}]$$

3) Matching: Determine correspondence between descriptors in two views



Goal: interest operator repeatability

- We want to detect (at least some of) the same points in both images.

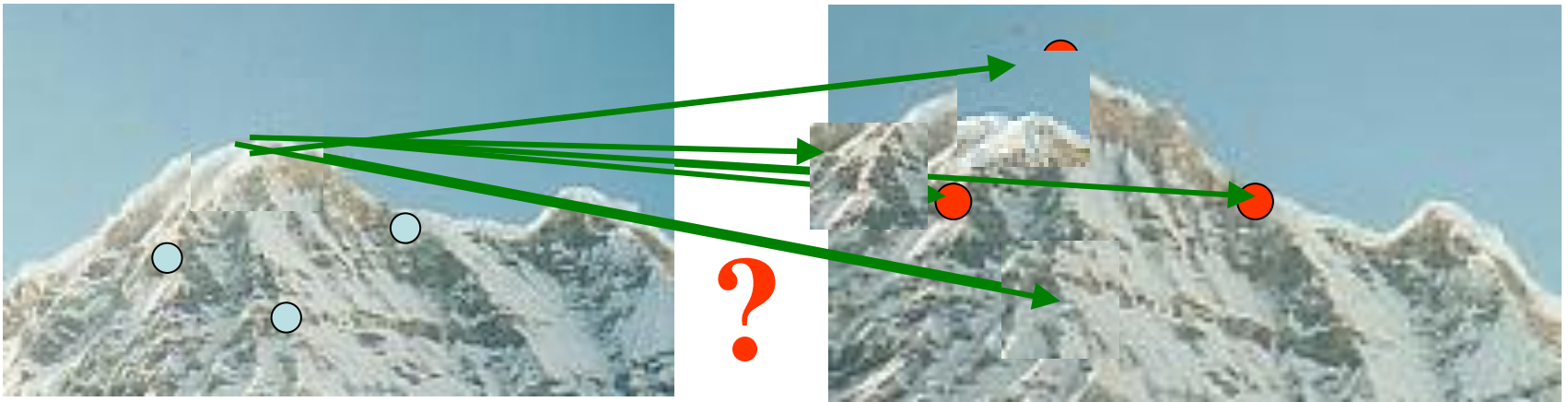


No chance to find true matches!

- Yet we have to be able to run the detection procedure *independently* per image.

Goal: descriptor distinctiveness

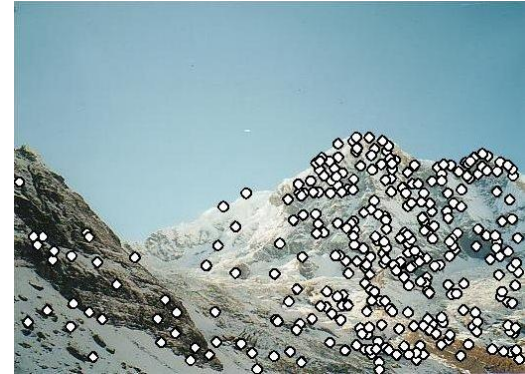
- We want to be able to reliably determine which point goes with which.



- Must provide some invariance to geometric and photometric differences between the two views.

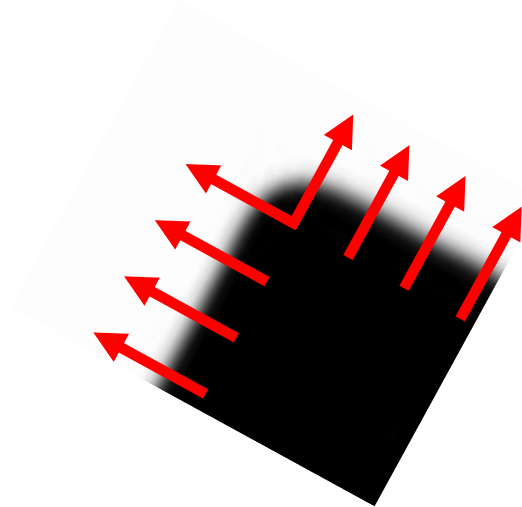
Local features: main components

- 1) Detection: Identify the interest points
- 2) Description: Extract vector feature descriptor surrounding each interest point.
- 3) Matching: Determine correspondence between descriptors in two views



Recall: Corners as distinctive interest points

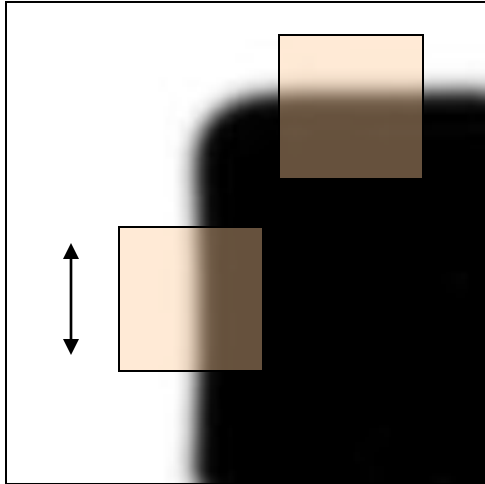
Since M is symmetric, we have $M = X \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix} X^T$



$$Mx_i = \lambda_i x_i$$

The *eigenvalues* of M reveal the amount of intensity change in the two principal orthogonal gradient directions in the window.

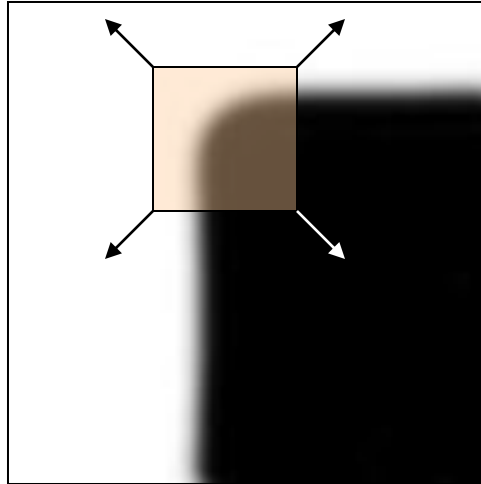
Recall: Corners as distinctive interest points



“edge”:

$$\lambda_1 \gg \lambda_2$$

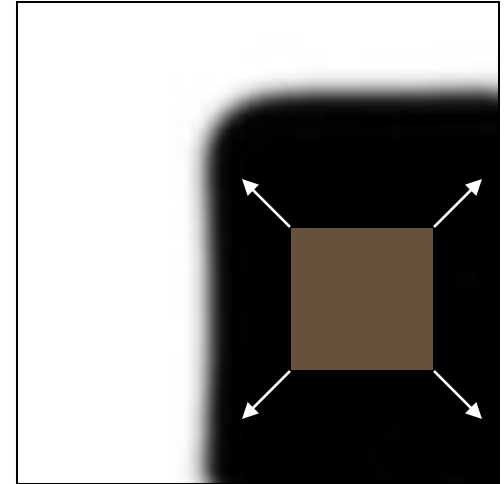
$$\lambda_2 \gg \lambda_1$$



“corner”:

λ_1 and λ_2 are large,

$$\lambda_1 \sim \lambda_2;$$



“flat” region

λ_1 and λ_2 are small;

One way to score the corneriness:

$$f = \frac{\lambda_1 \lambda_2}{\lambda_1 + \lambda_2}$$

Harris Detector [Harris88]

- Second moment matrix
(autocorrelation matrix)

$$\mu(\sigma_I, \sigma_D) = g(\sigma_I) * \begin{bmatrix} I_x^2(\sigma_D) & I_x I_y(\sigma_D) \\ I_x I_y(\sigma_D) & I_y^2(\sigma_D) \end{bmatrix}$$

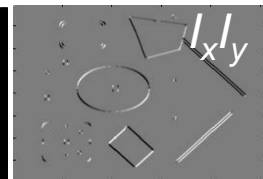
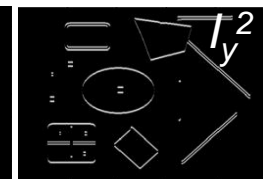
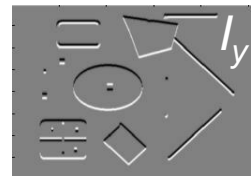
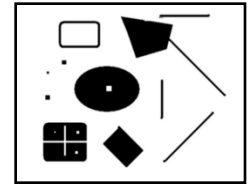
$$\det M = \lambda_1 \lambda_2$$

$$\text{trace } M = \lambda_1 + \lambda_2$$

2. Square of
derivatives

3. Gaussian
filter $g(\sigma_I)$

1. Image
derivatives

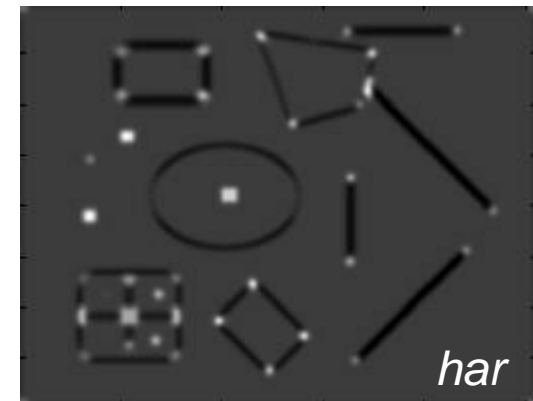


4. Cornerness function – both eigenvalues are strong

$$har = \det[\mu(\sigma_I, \sigma_D)] - \alpha [\text{trace}(\mu(\sigma_I, \sigma_D))]^2 =$$

$$g(I_x^2)g(I_y^2) - [g(I_x I_y)]^2 - \alpha [g(I_x^2) + g(I_y^2)]^2$$

5. Non-maxima suppression



Properties of the Harris corner detector

Rotation invariant? Yes

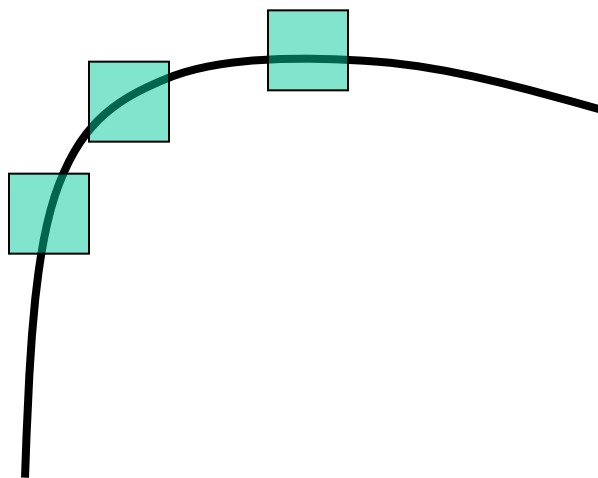
$$M = X \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix} X^T$$

Scale invariant?

Properties of the Harris corner detector

Rotation invariant? Yes

Scale invariant? No



All points will be
classified as **edges**

Corner !

Scale invariant interest points

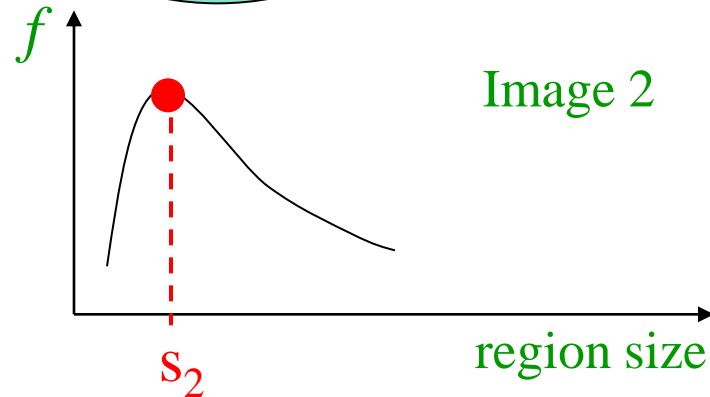
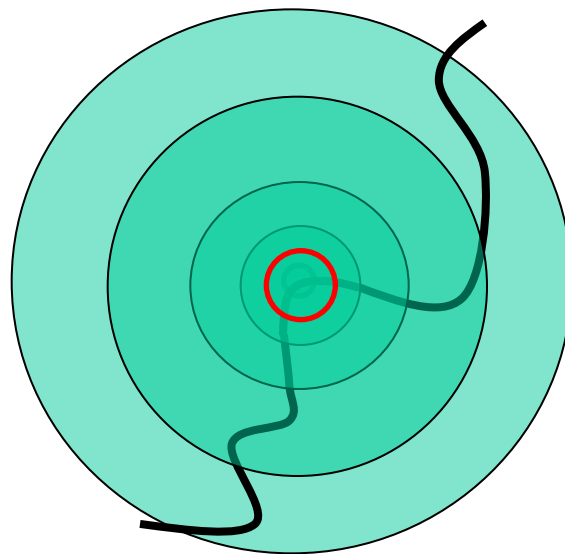
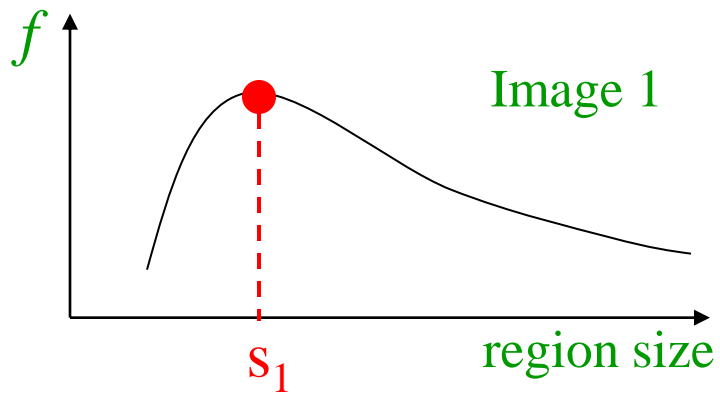
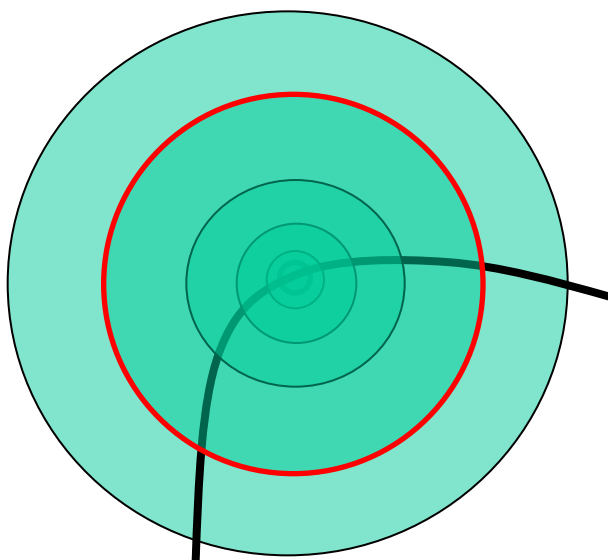
How can we independently select interest points in each image, such that the detections are repeatable across different scales?



Automatic scale selection

Intuition:

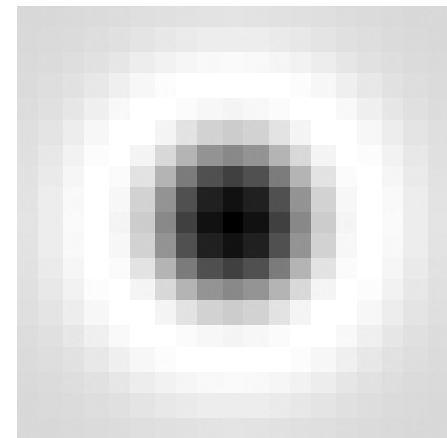
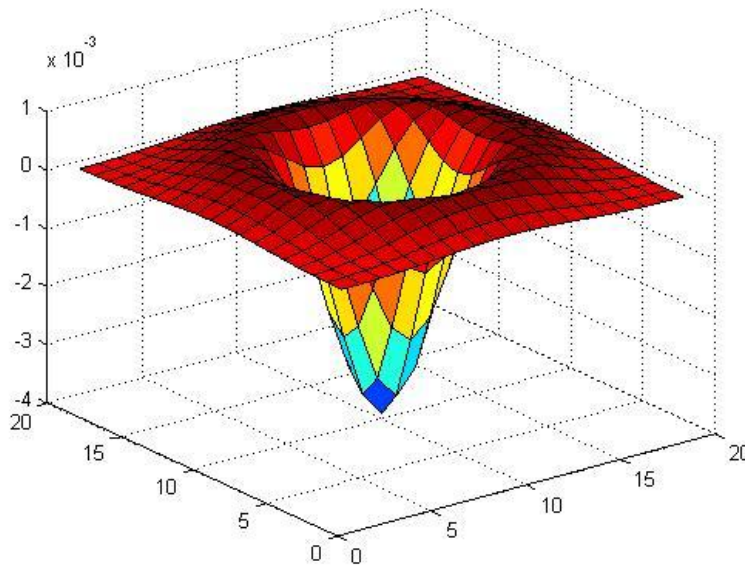
- Find scale that gives local maxima of some function f in both position and scale.



What can be the “signature” function?

Blob detection in 2D

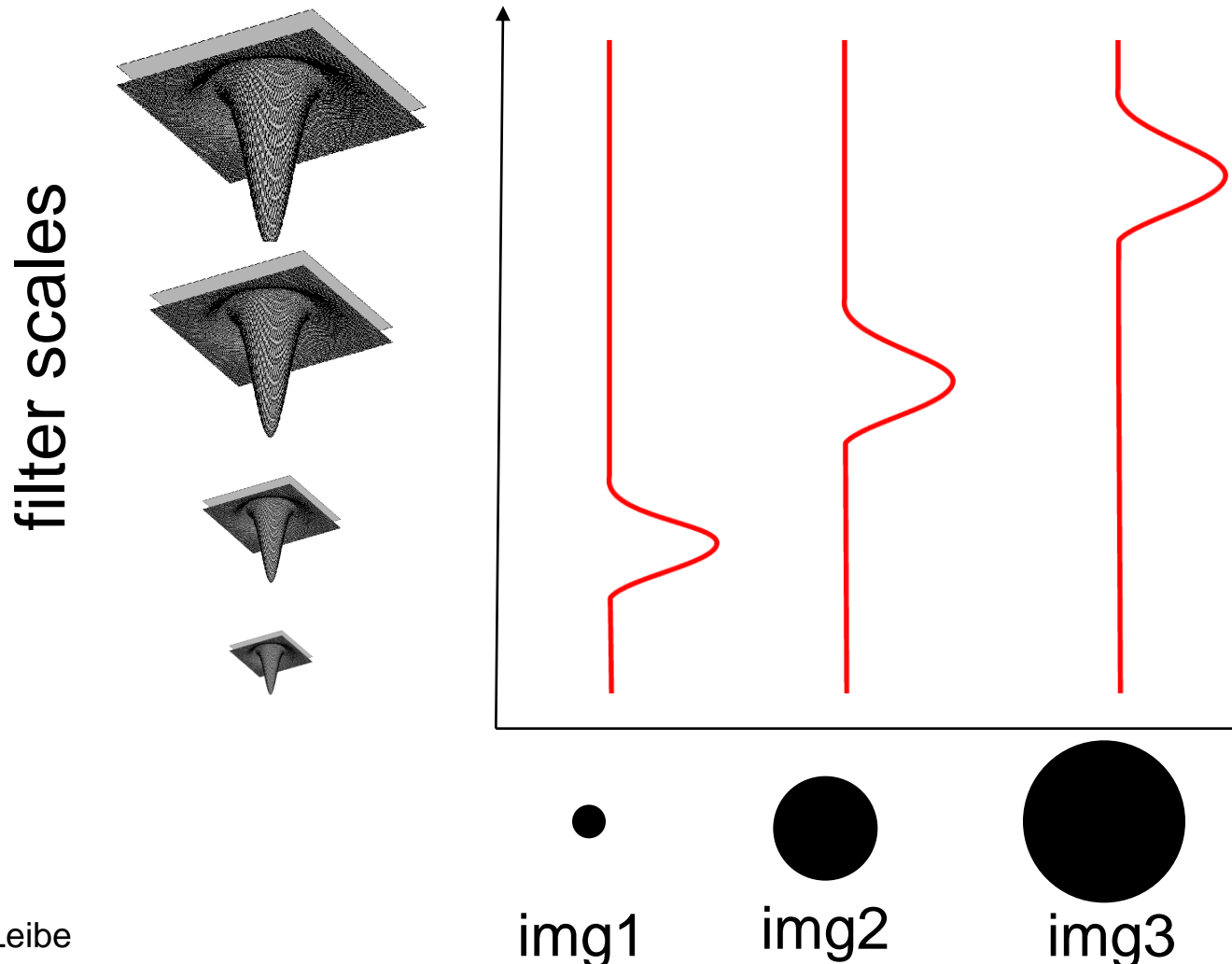
Laplacian of Gaussian: Circularly symmetric operator for blob detection in 2D



$$\nabla^2 g = \frac{\partial^2 g}{\partial x^2} + \frac{\partial^2 g}{\partial y^2}$$

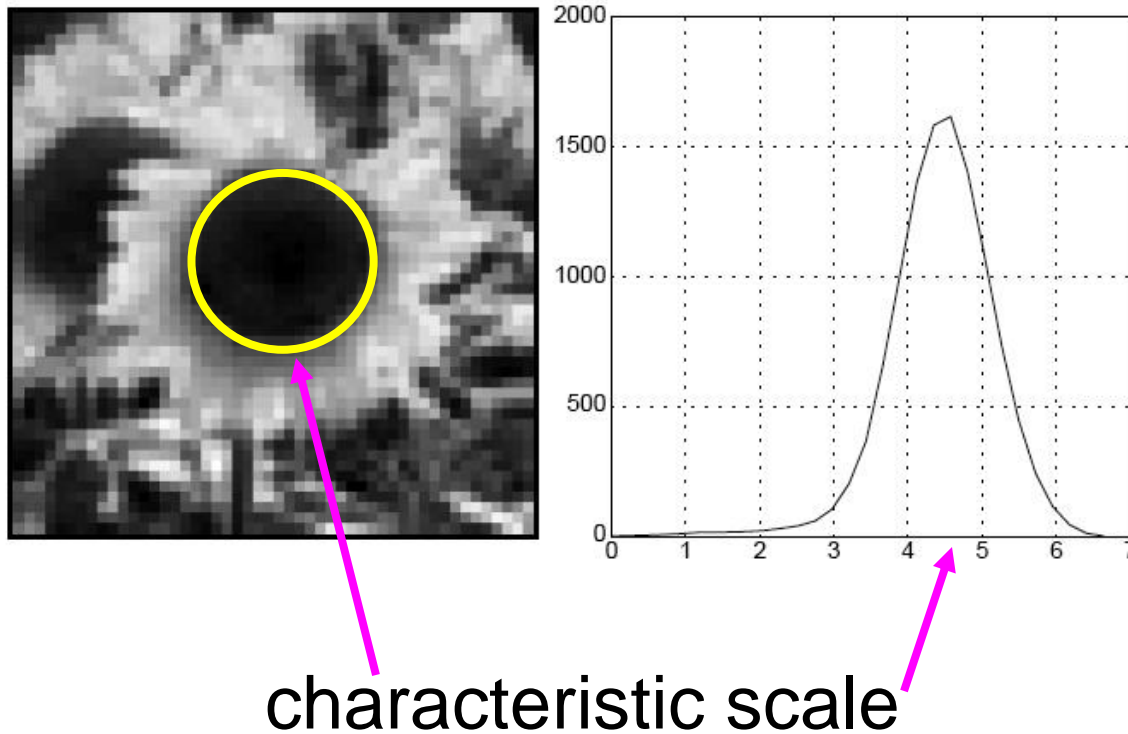
Blob detection in 2D: scale selection

Laplacian-of-Gaussian = “blob” detector $\nabla^2 g = \frac{\partial^2 g}{\partial x^2} + \frac{\partial^2 g}{\partial y^2}$



Blob detection in 2D

We define the *characteristic scale* as the scale that produces peak of Laplacian response

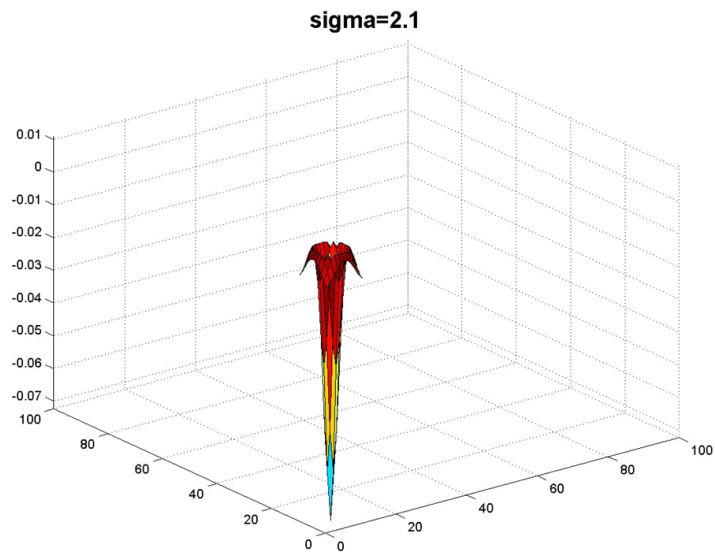
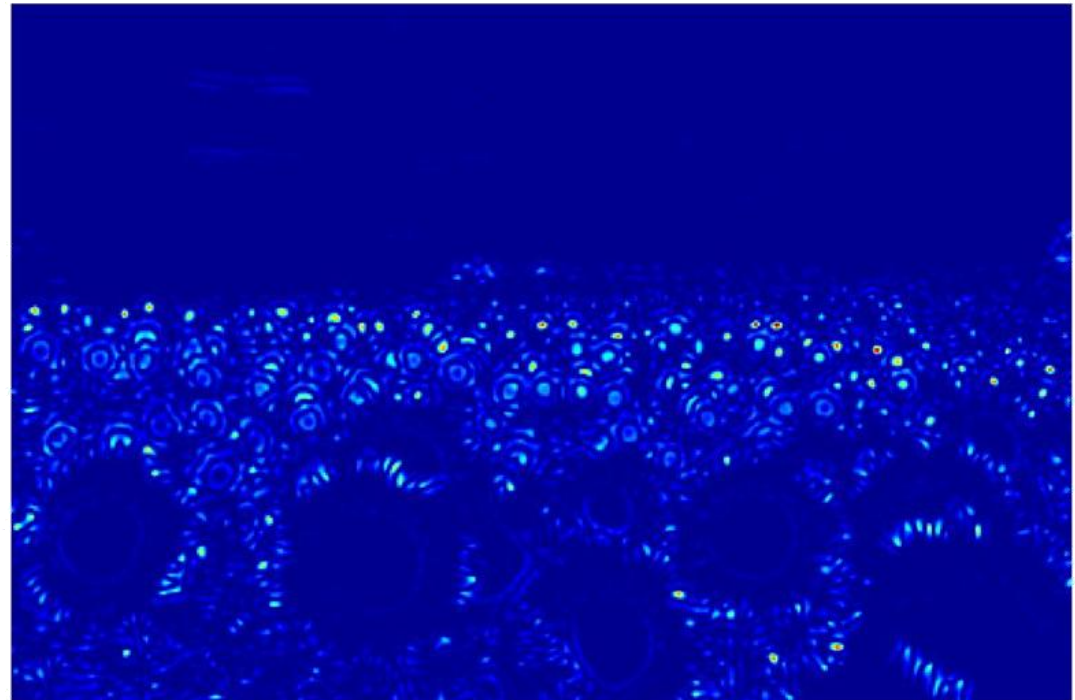
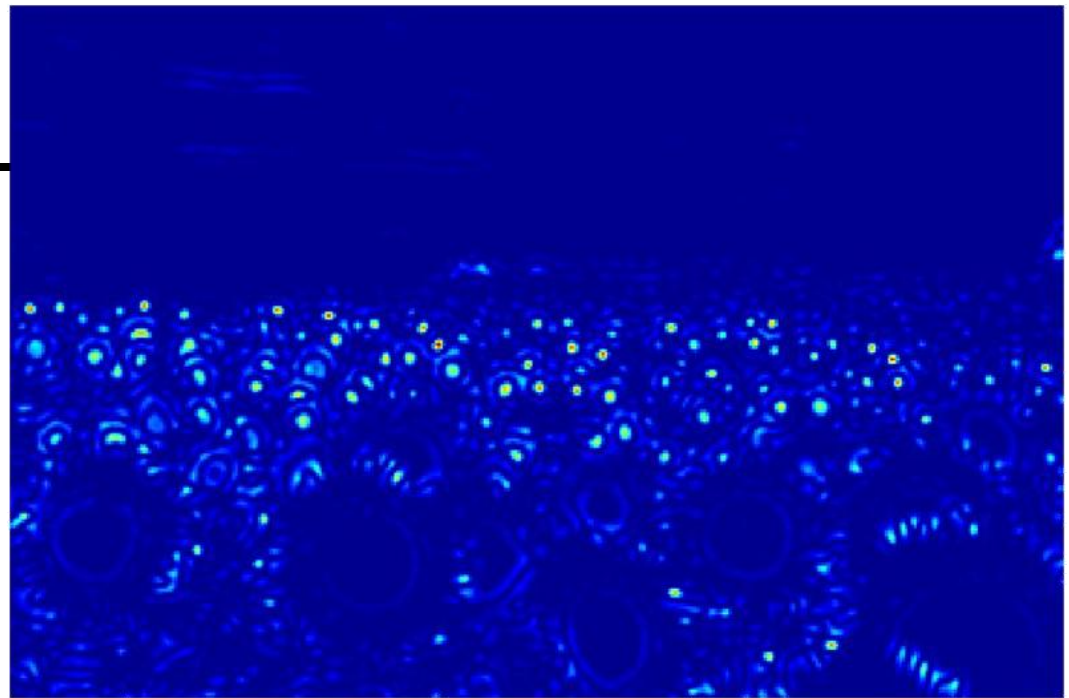


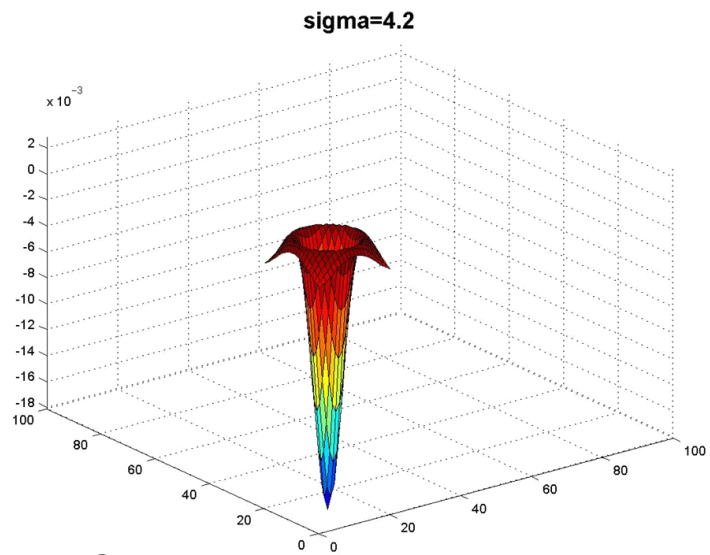
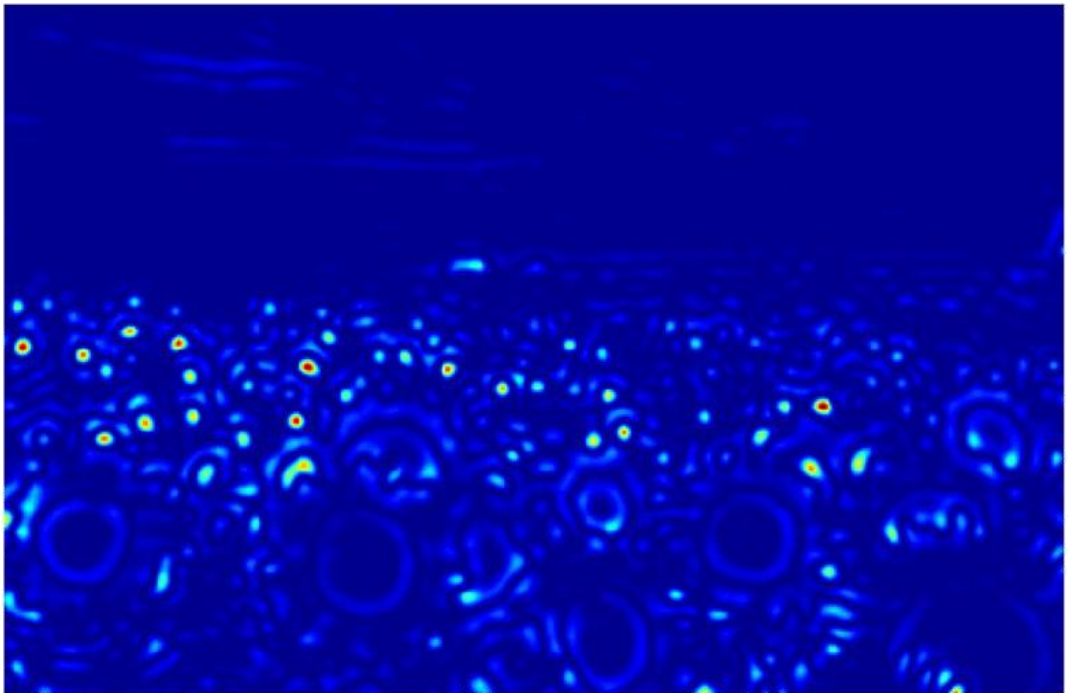
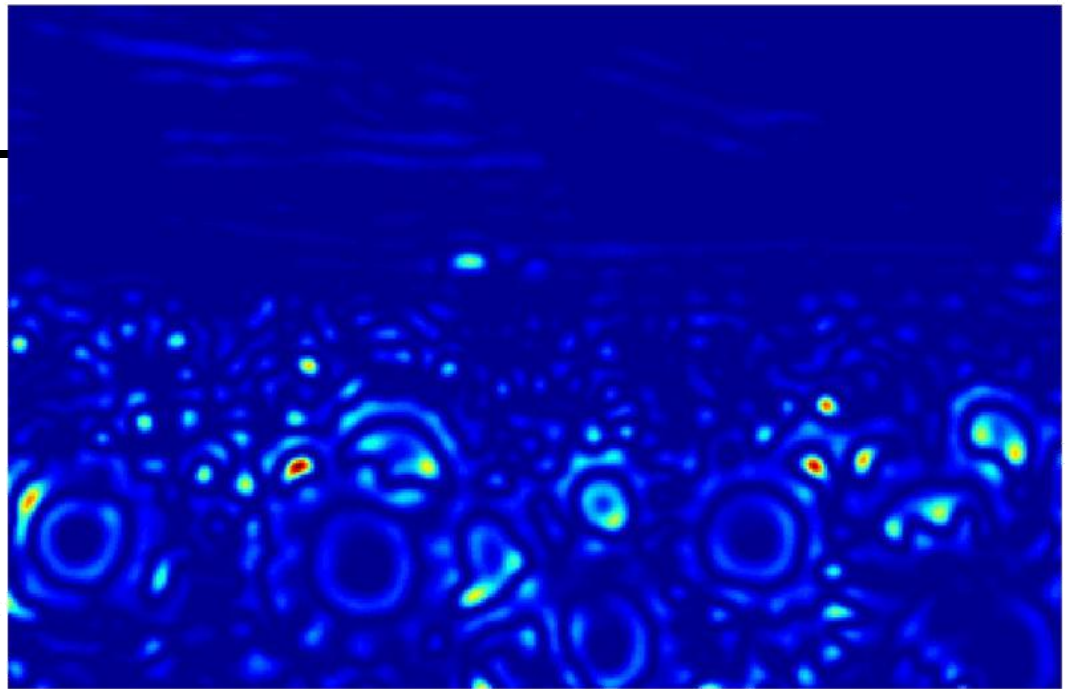
Example

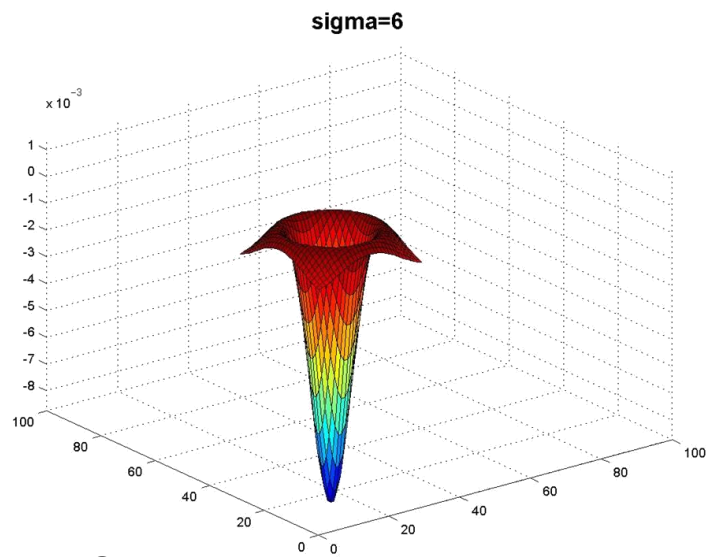
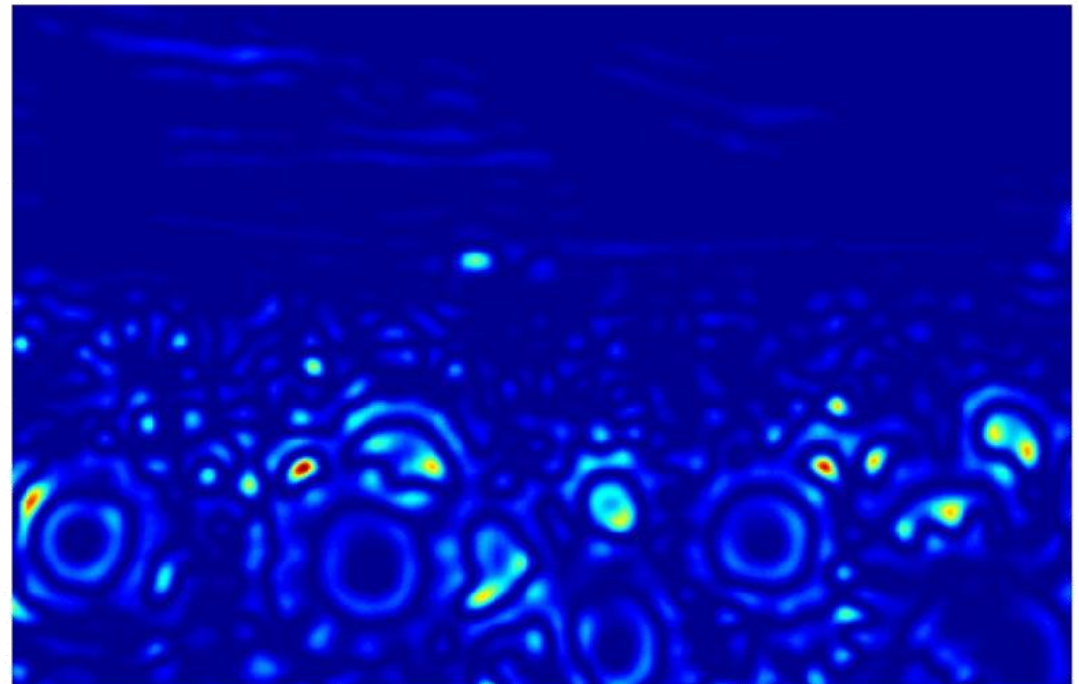
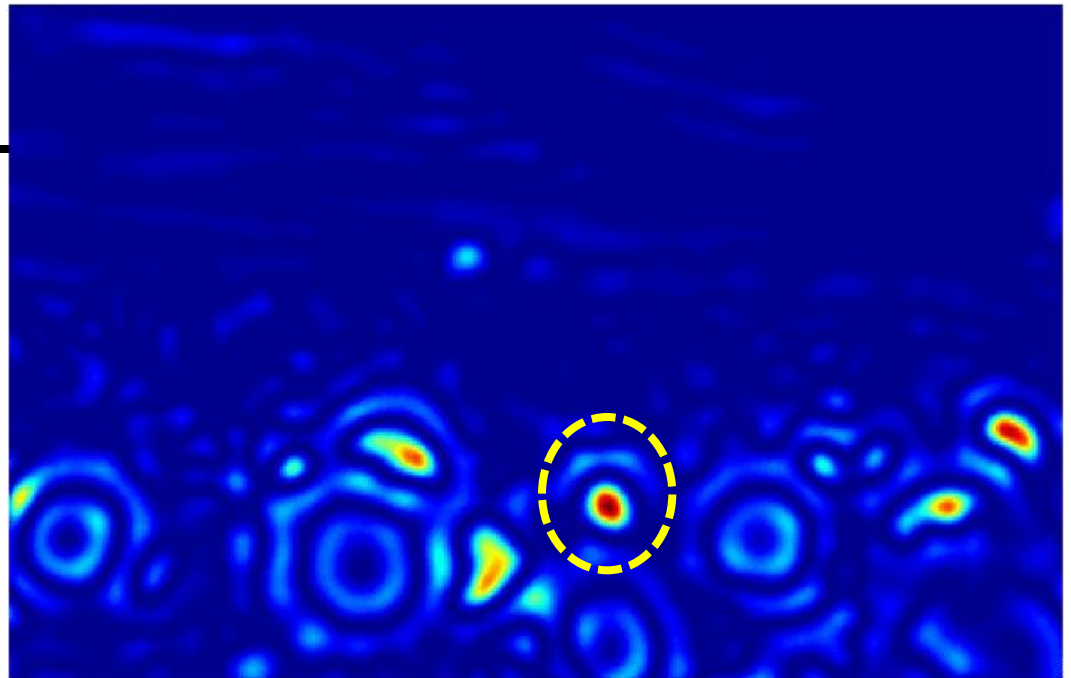
Original image
at $\frac{3}{4}$ the size

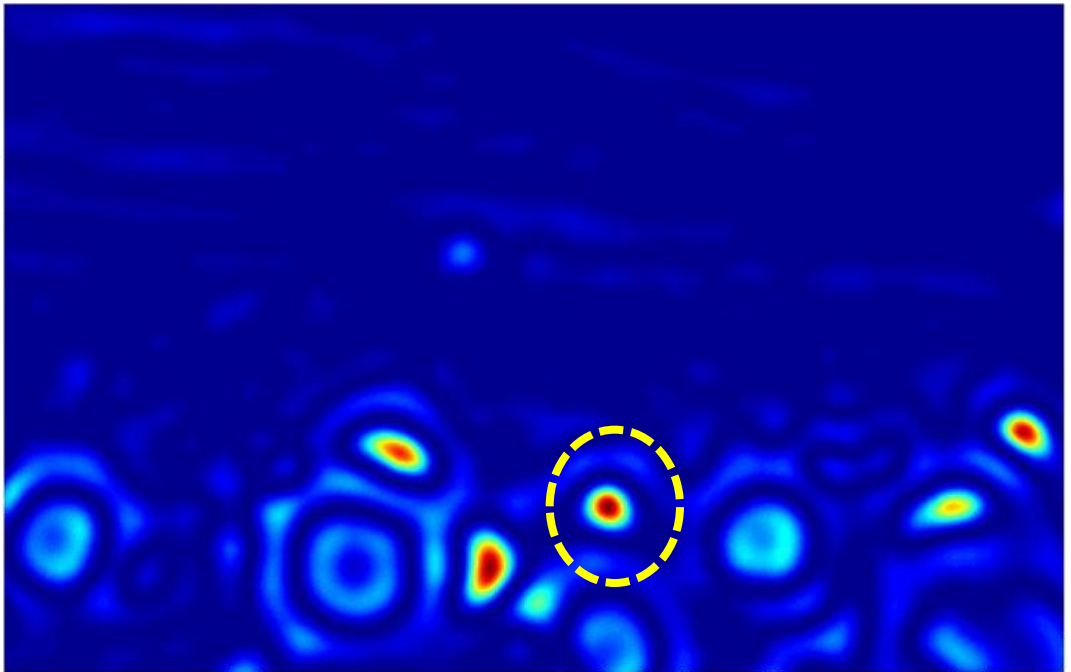
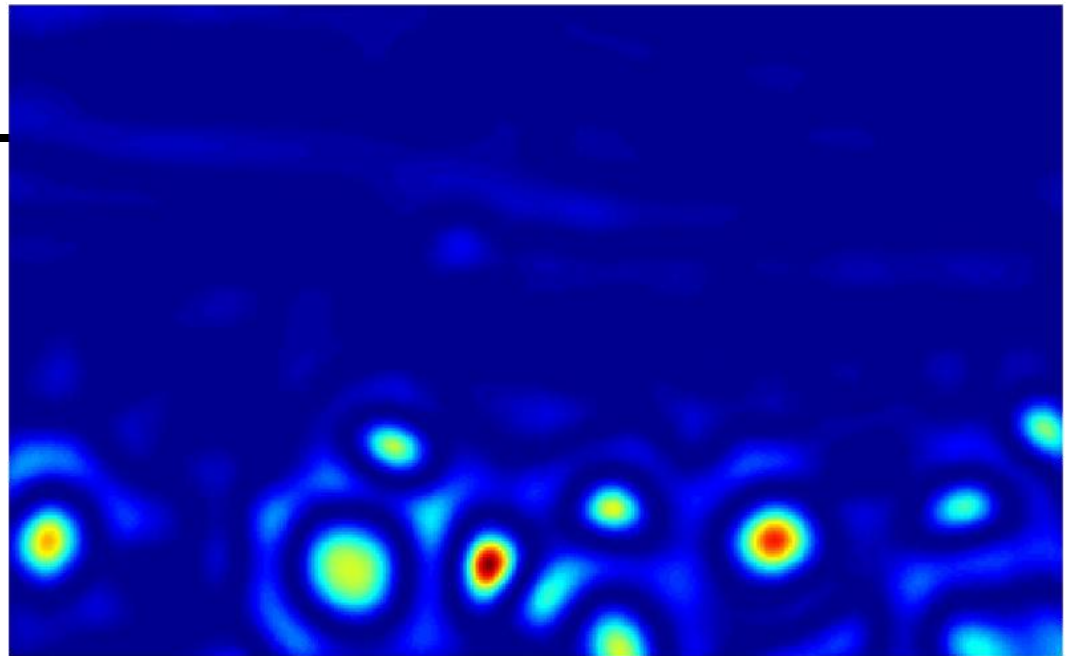
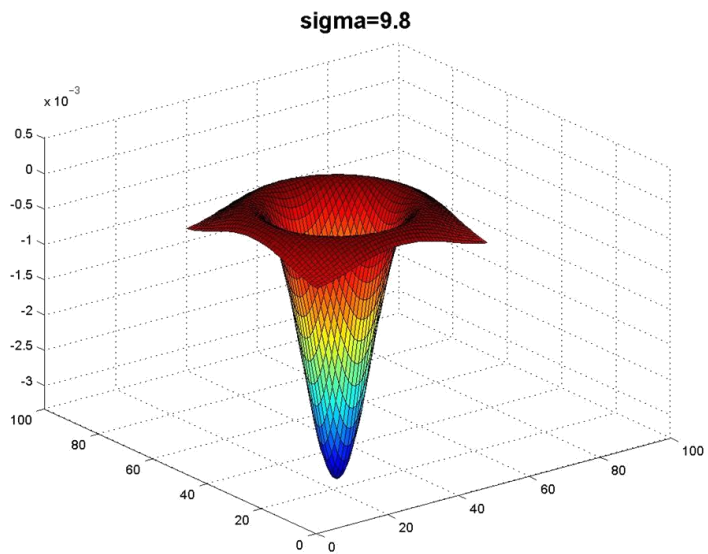


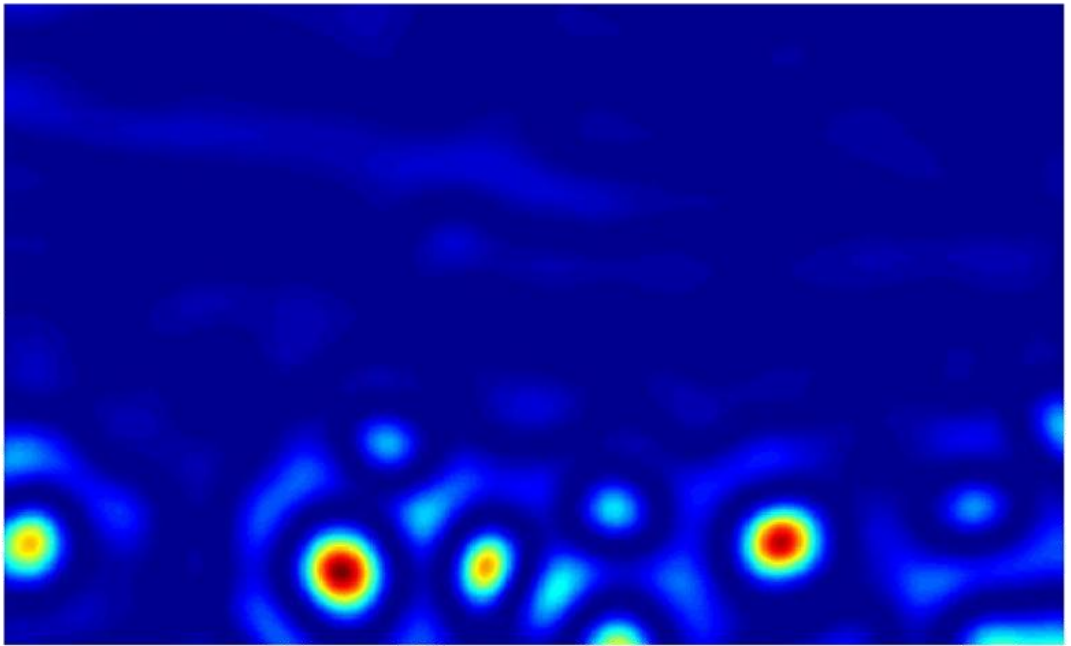
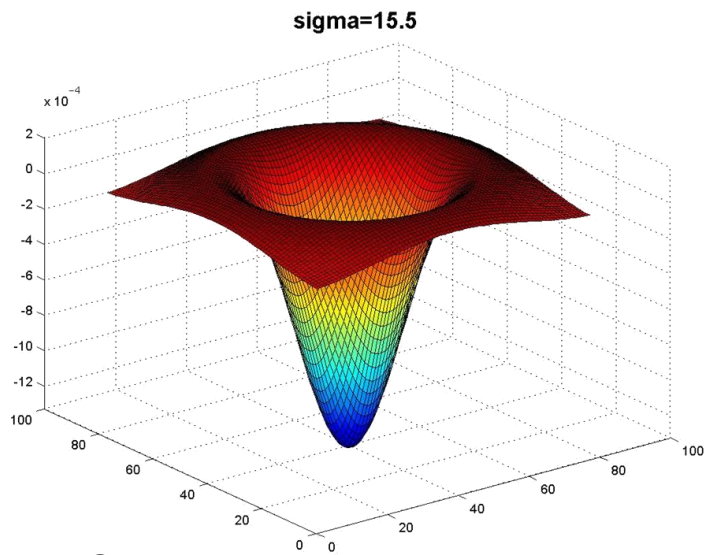
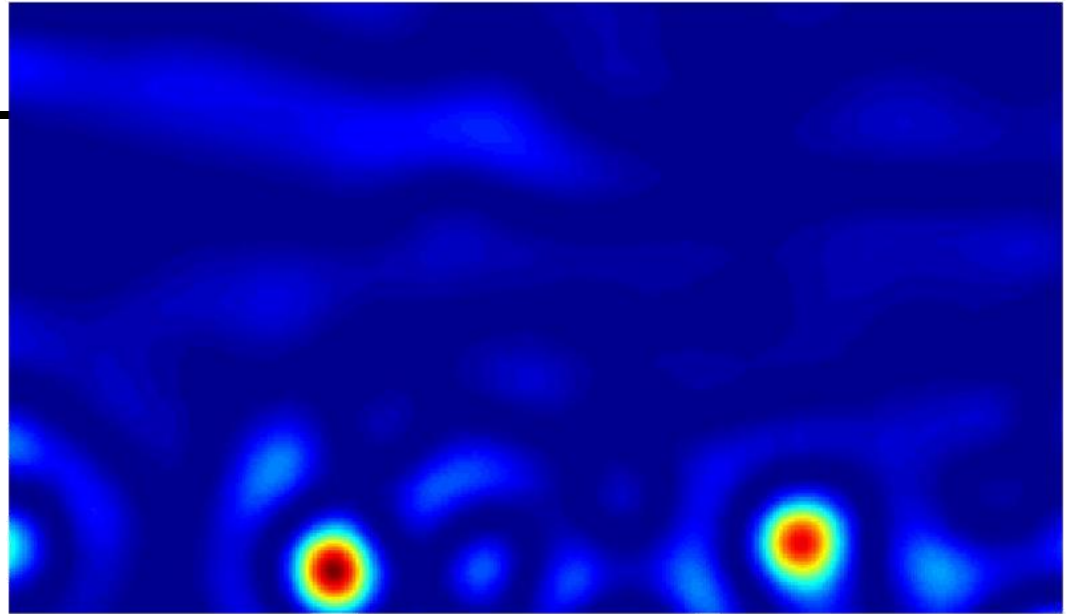
Original image
at $\frac{3}{4}$ the size





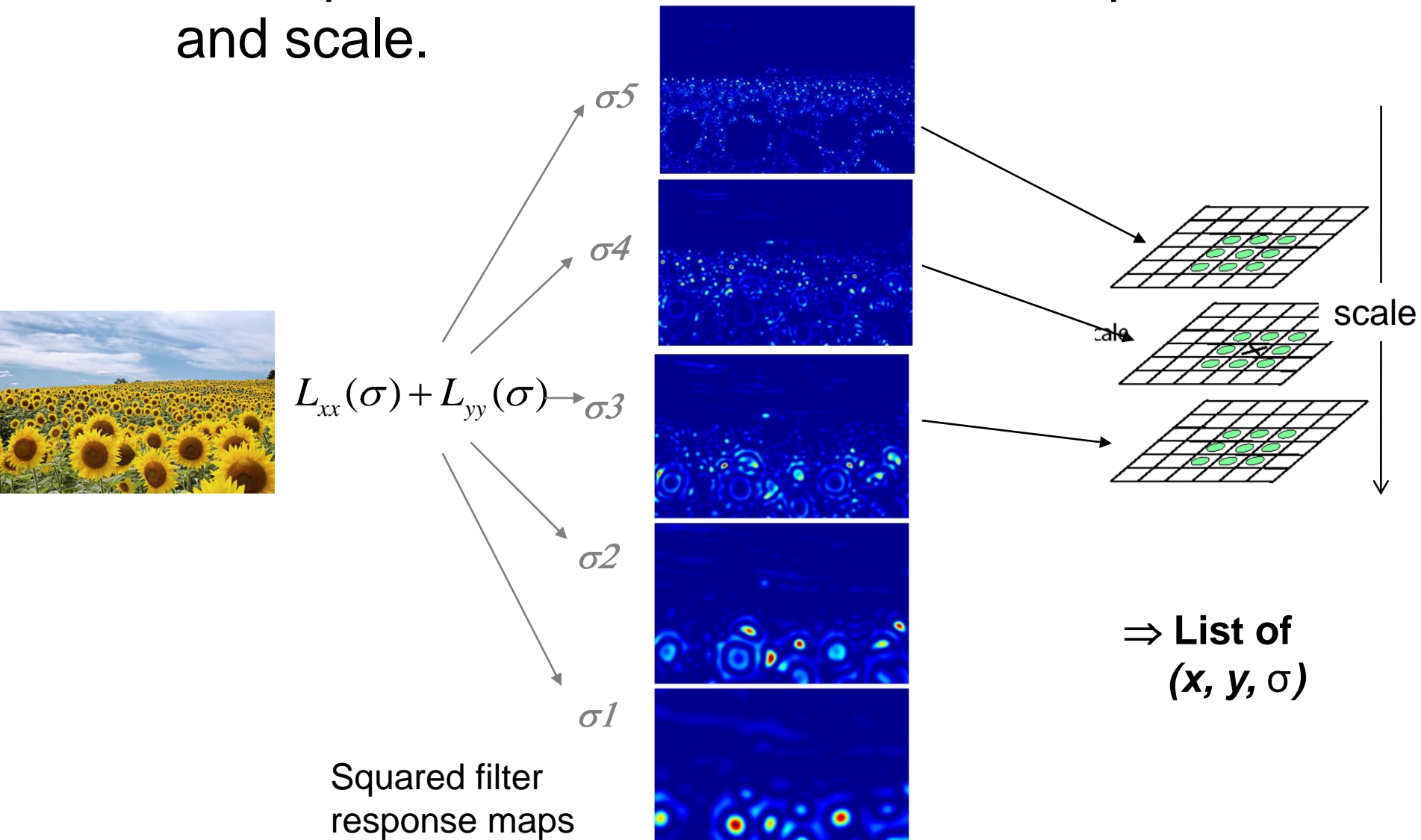




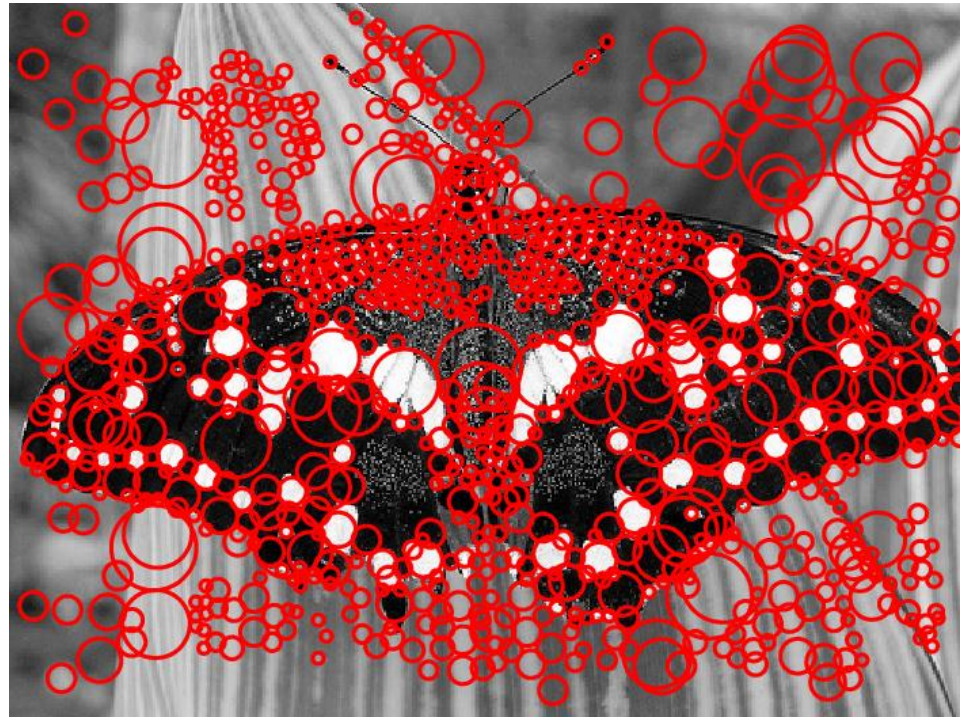


Scale invariant interest points

Interest points are local maxima in both position and scale.



Scale-space blob detector: Example



Technical detail

We can approximate the Laplacian with a difference of Gaussians; more efficient to implement.

$$L = \sigma^2 G_{xx}(x, y, \sigma) + G_{yy}(x, y, \sigma)$$

(Laplacian)

$$DoG = G(x, y, k\sigma) - G(x, y, \sigma)$$

(Difference of Gaussians)

$I(k\sigma)$

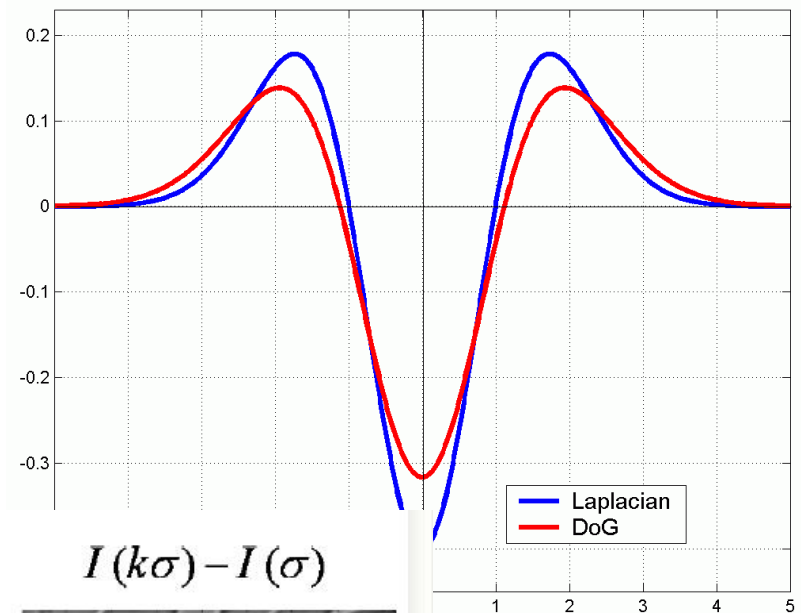
$I(\sigma)$



-



=

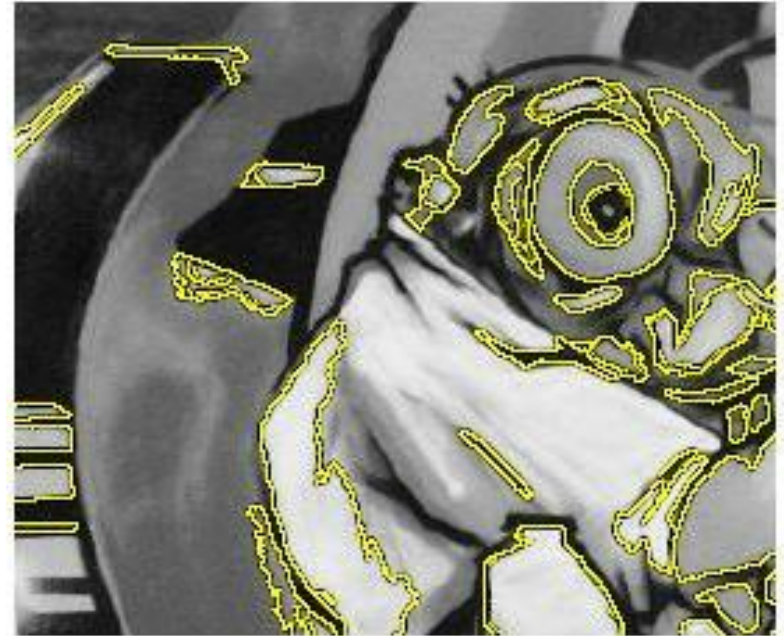


Maximally Stable Extremal Regions [Matas '02]

- Based on Watershed segmentation algorithm
- Select regions that stay stable over a large parameter range

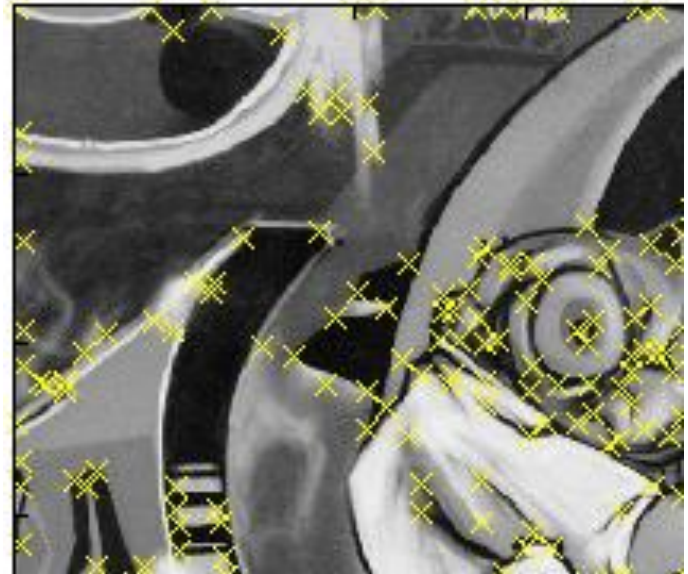


Example Results: MSER

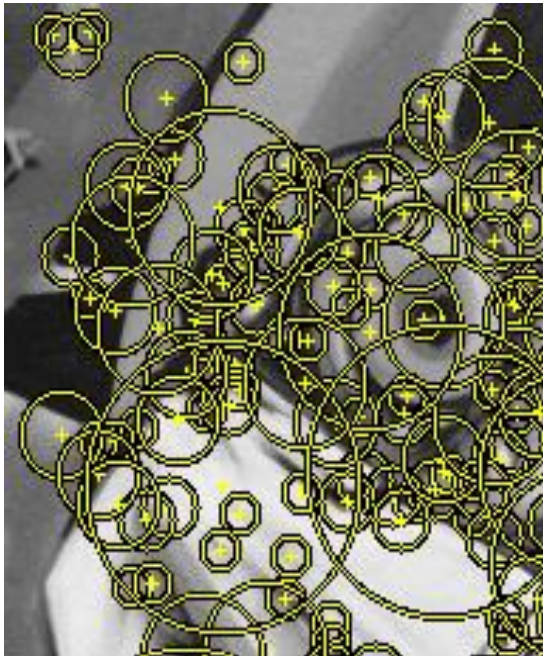


Comparison

Harris



LoG



MSER



Comparison of Keypoint Detectors

Table 7.1 Overview of feature detectors.

Feature Detector	Corner	Blob	Region	Rotation invariant	Scale invariant	Affine invariant	Repeatability	Localization accuracy	Robustness	Efficiency
Harris	✓			✓			+++	+++	+++	++
Hessian		✓		✓			++	++	++	+
SUSAN	✓			✓			++	++	++	+++
Harris-Laplace	✓	(✓)		✓	✓		+++	+++	++	+
Hessian-Laplace	(✓)	✓		✓	✓		+++	+++	+++	+
DoG	(✓)	✓		✓	✓		++	++	++	++
SURF	(✓)	✓		✓	✓		++	++	++	+++
Harris-Affine	✓	(✓)		✓	✓	✓	+++	+++	++	++
Hessian-Affine	(✓)	✓		✓	✓	✓	+++	+++	+++	++
Salient Regions	(✓)	✓		✓	✓	(✓)	+	+	++	+
Edge-based	✓			✓	✓	✓	+++	+++	+	+
MSER			✓	✓	✓	✓	+++	+++	++	+++
Intensity-based			✓	✓	✓	✓	++	++	++	++
Superpixels			✓	✓	(✓)	(✓)	+	+	+	+

Choosing a detector

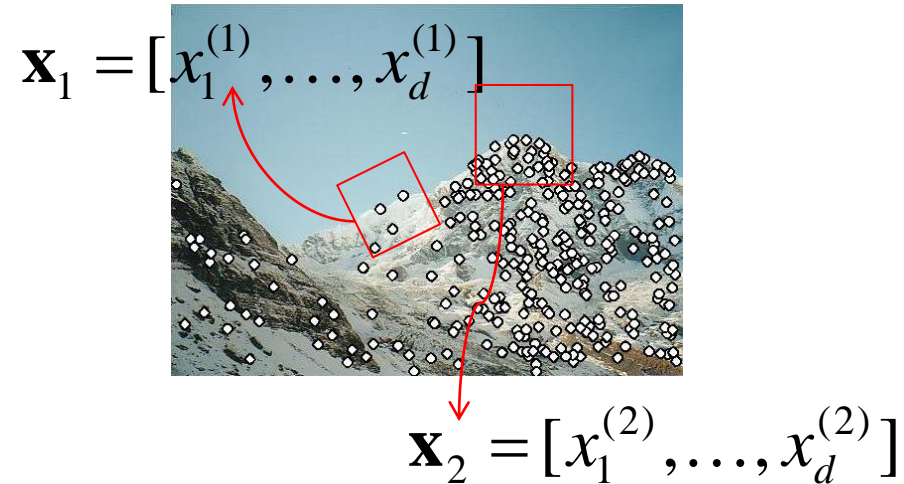
- What do you want it for?
 - Precise localization in x-y: Harris
 - Good localization in scale: Difference of Gaussian
 - Flexible region shape: MSER
- Best choice often application dependent
 - Harris-/Hessian-Laplace/DoG work well for many natural categories
 - MSER works well for buildings and printed things
- Why choose?
 - Get more points with more detectors
- There have been extensive evaluations/comparisons
 - [Mikolajczyk et al., IJCV'05, PAMI'05]
 - All detectors/descriptors shown here work well

- For most local feature detectors, executables are available online:
 - <http://robots.ox.ac.uk/~vgg/research/affine>
 - <http://www.cs.ubc.ca/~lowe/keypoints/>
 - <http://www.vision.ee.ethz.ch/~surf>

Local features: main components

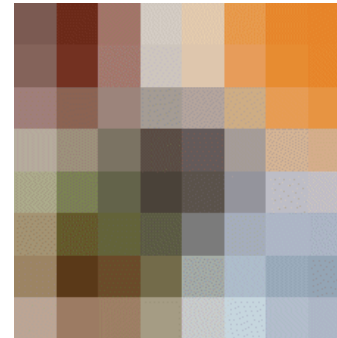
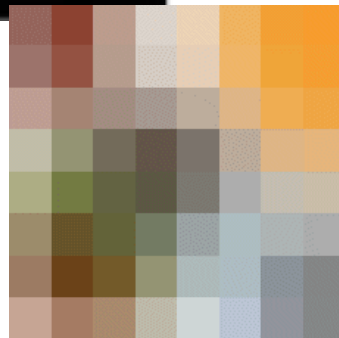
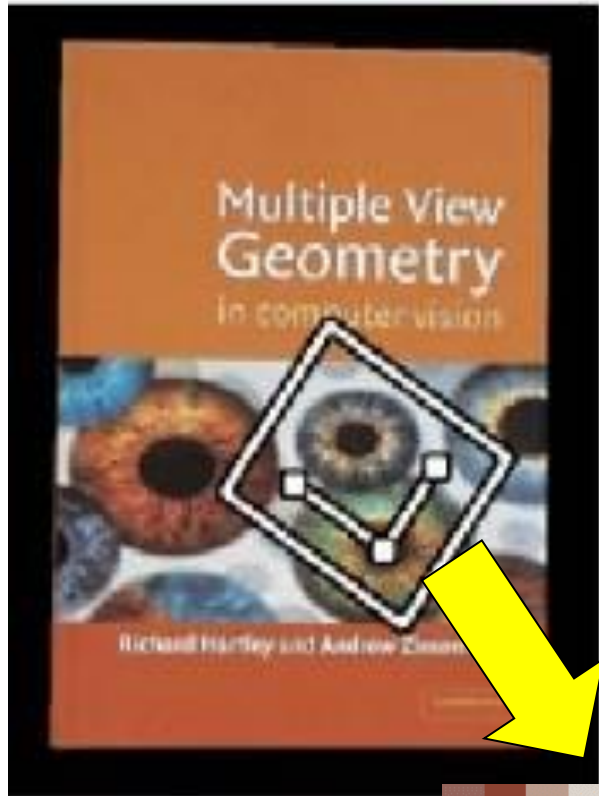
1) Detection: Identify the interest points

2) Description: Extract vector feature descriptor surrounding each interest point.



3) Matching: Determine correspondence between descriptors in two views

Geometric transformations



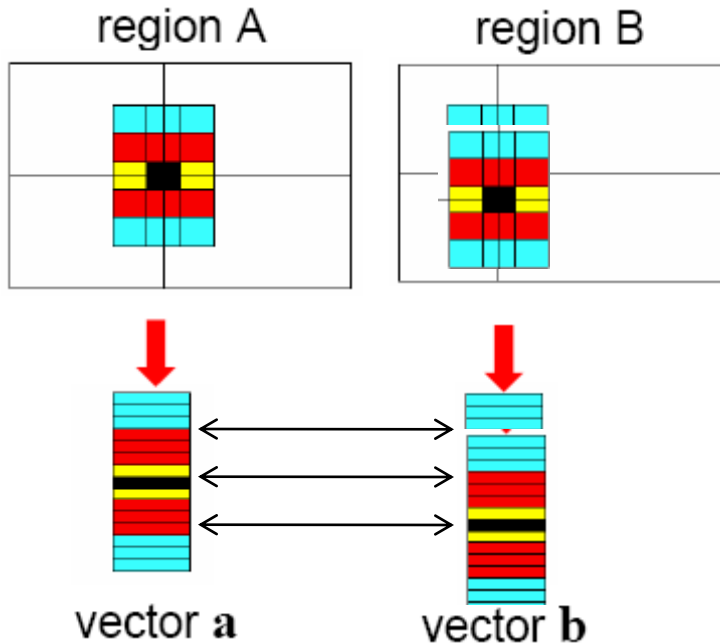
e.g. scale,
translation,
rotation

Photometric transformations



Figure from T. Tuytelaars ECCV 2006 tutorial

Raw patches as local descriptors

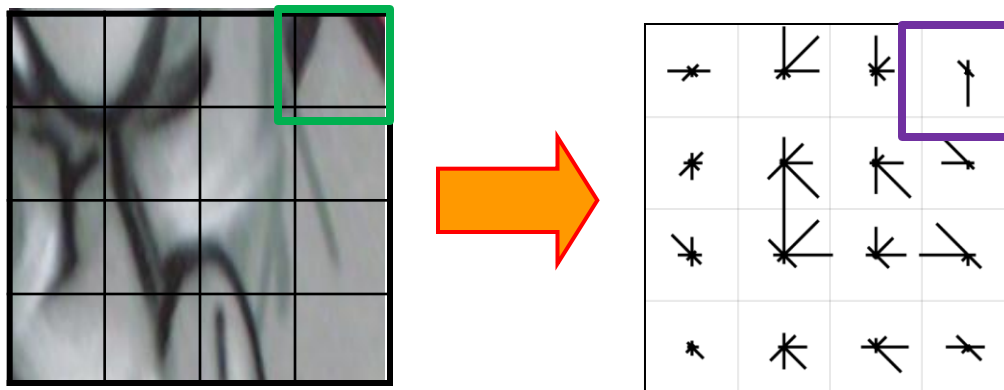
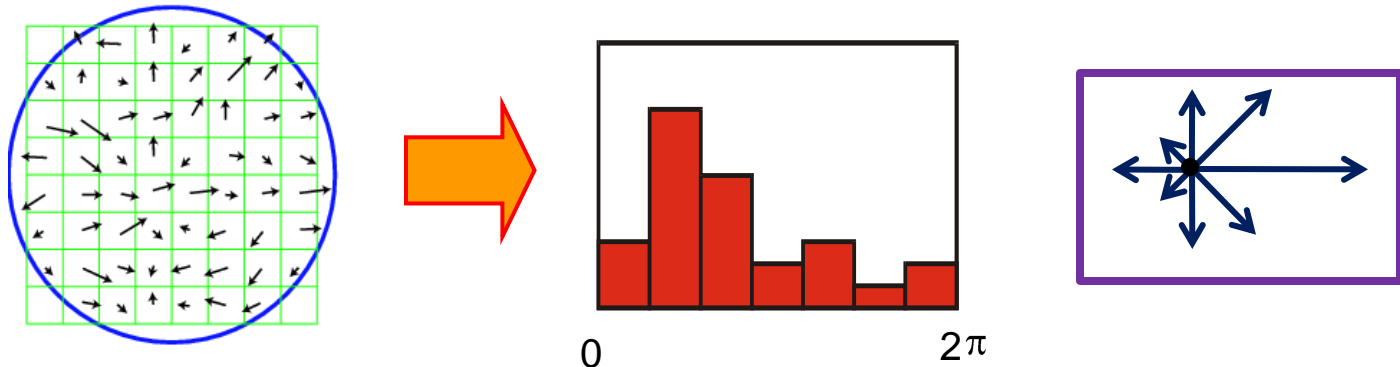


The simplest way to describe the neighborhood around an interest point is to write down the list of intensities to form a feature vector.

But this is very sensitive to even small shifts, rotations.

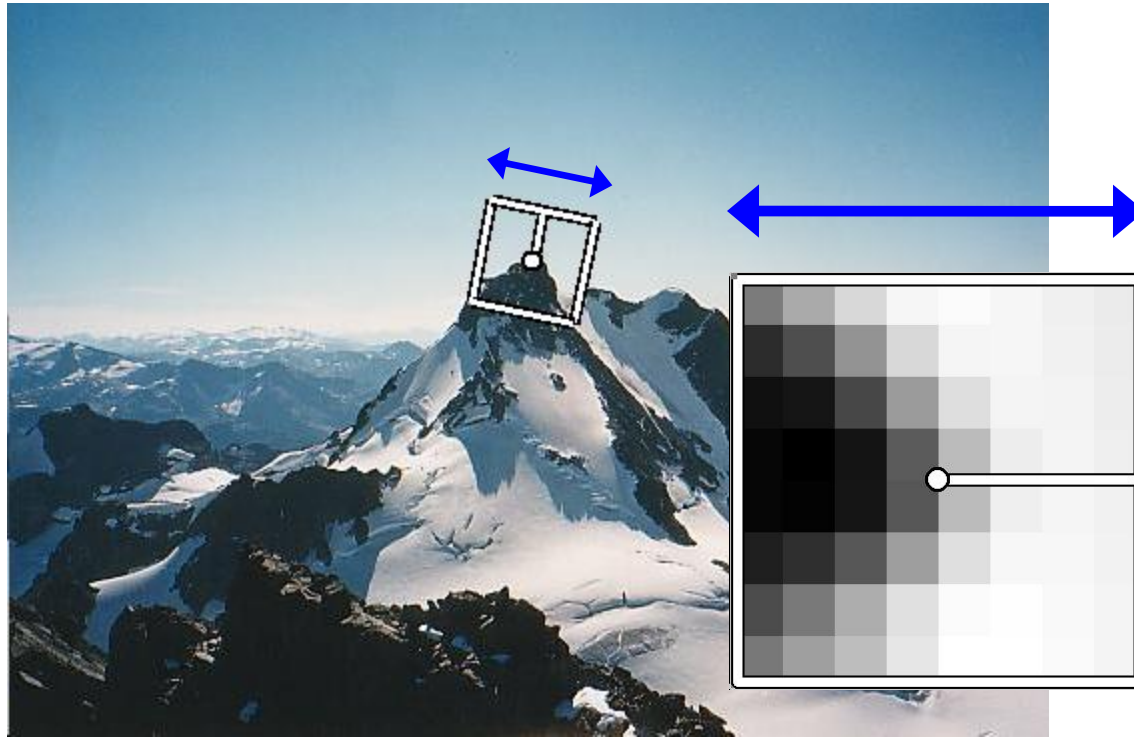
SIFT descriptor [Lowe 2004]

- Use histograms to bin pixels within sub-patches according to their orientation.



*Why subpatches?
Why does SIFT
have some
illumination
invariance?*

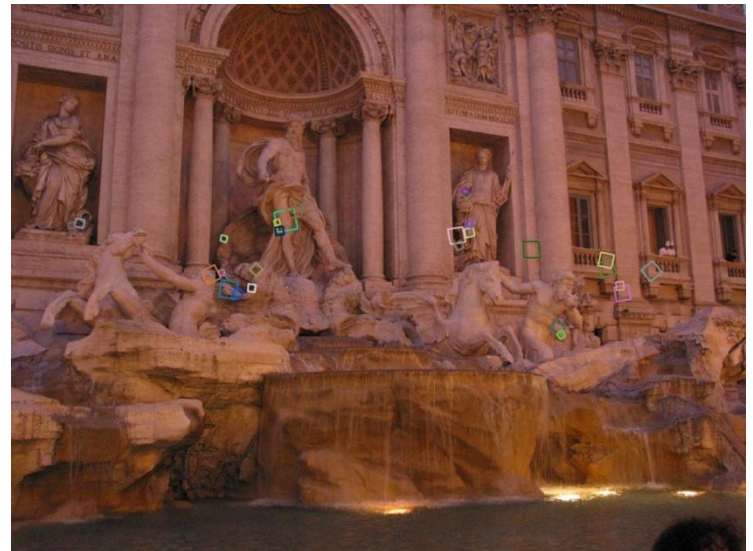
Making descriptor rotation invariant



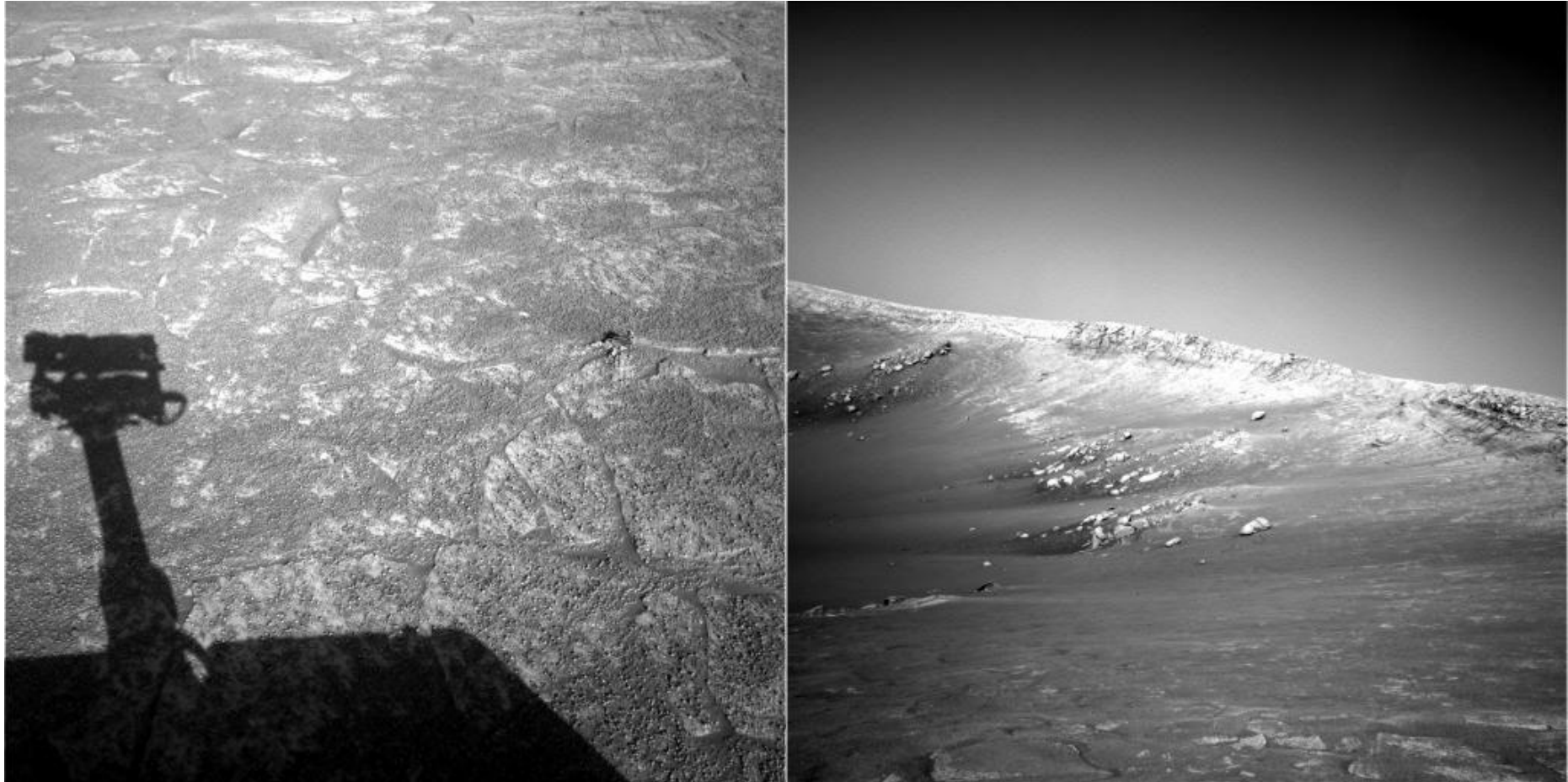
- Rotate patch according to its dominant gradient orientation
- This puts the patches into a canonical orientation.

SIFT descriptor [Lowe 2004]

- Extraordinarily robust matching technique
 - Can handle changes in viewpoint
 - Up to about 60 degree out of plane rotation
 - Can handle significant changes in illumination
 - Sometimes even day vs. night (below)
 - Fast and efficient—can run in real time
 - Lots of code available
 - http://people.csail.mit.edu/albert/ladypack/wiki/index.php/Known_implementations_of_SIFT

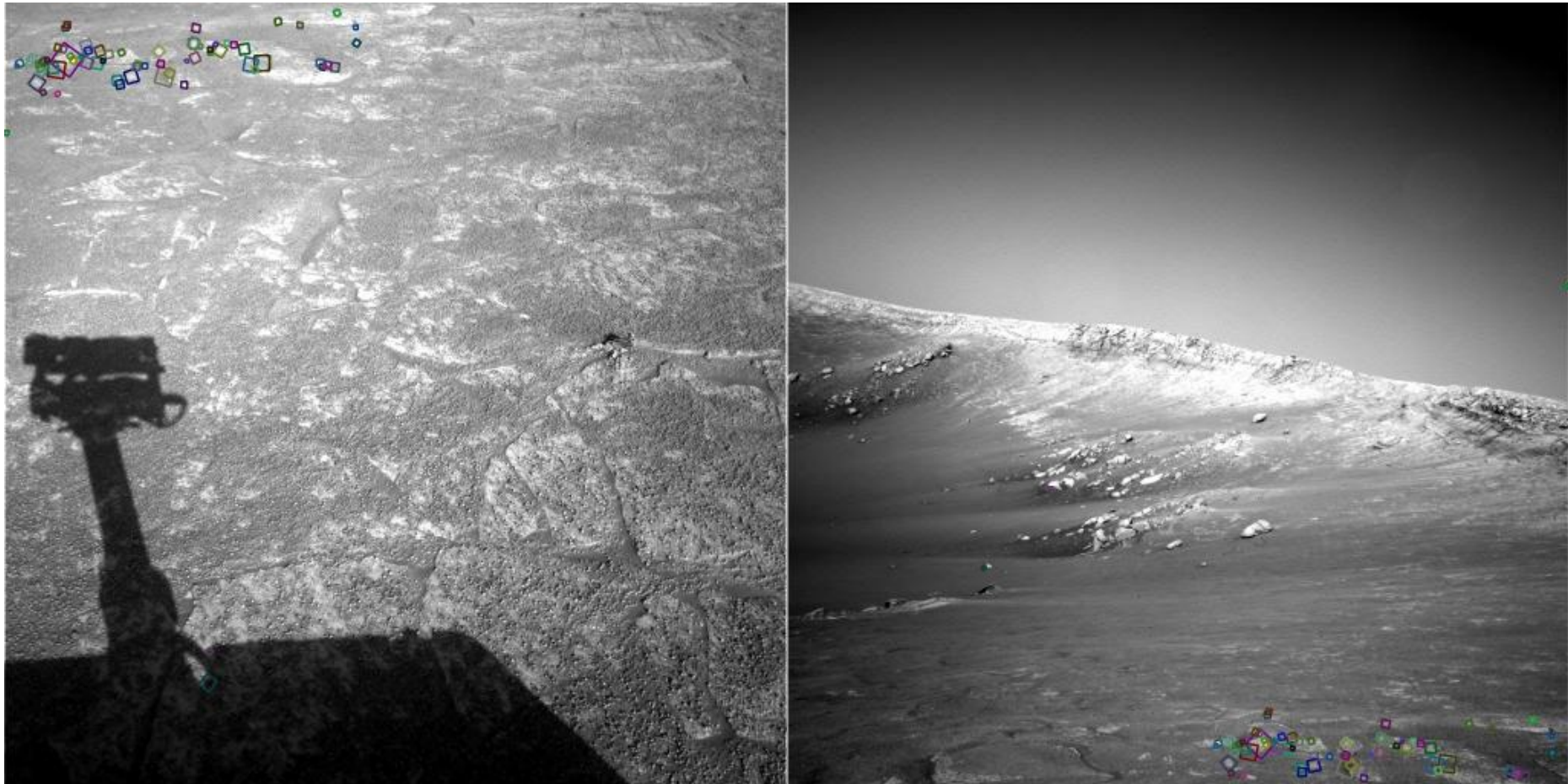


Example



NASA Mars Rover images

Example



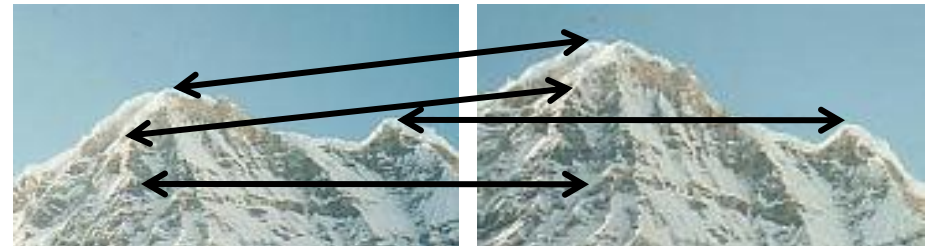
NASA Mars Rover images
with SIFT feature matches
Figure by Noah Snively

SIFT properties

- Invariant to
 - Scale
 - Rotation
- Partially invariant to
 - Illumination changes
 - Camera viewpoint
 - Occlusion, clutter

Local features: main components

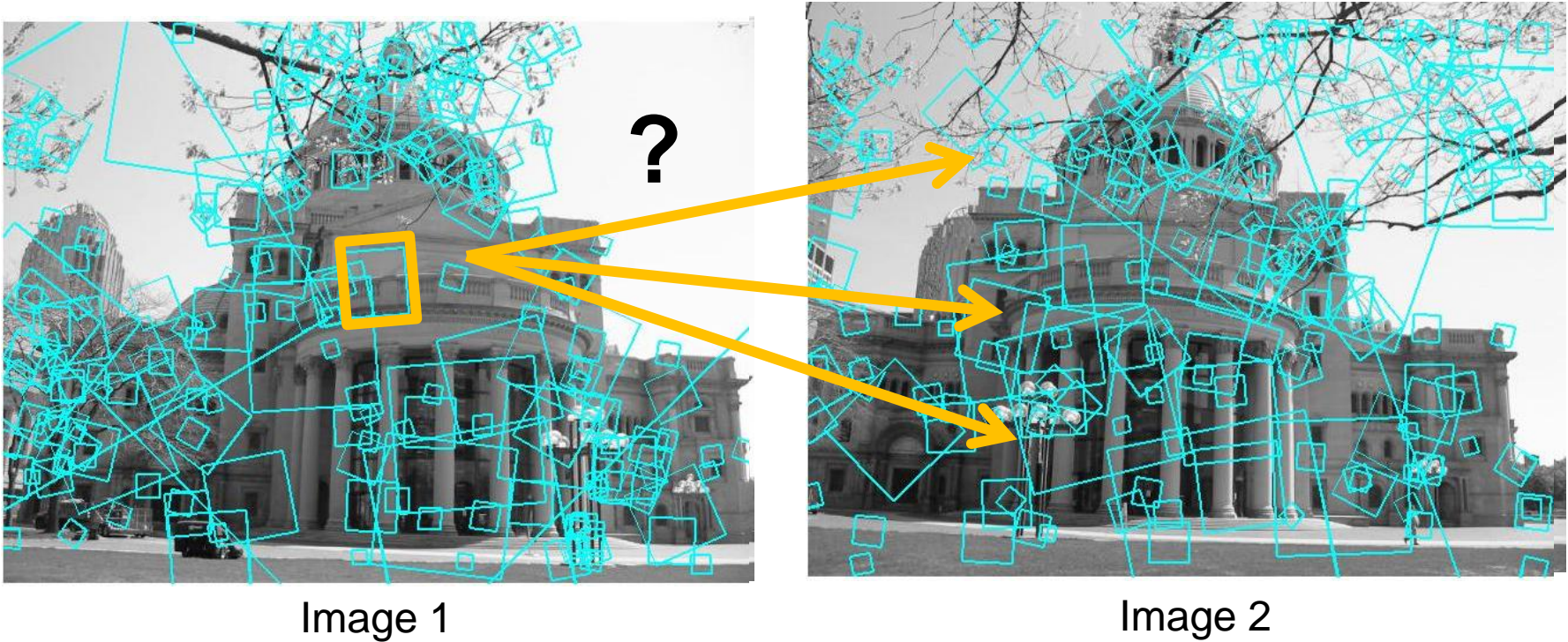
- 1) Detection: Identify the interest points
- 2) Description: Extract vector feature descriptor surrounding each interest point.
- 3) Matching: Determine correspondence between descriptors in two views



Matching local features



Matching local features



To generate **candidate matches**, find patches that have the most similar appearance (e.g., lowest SSD)

Simplest approach: compare them all, take the closest (or closest k , or within a thresholded distance)

Ambiguous matches



Image 1



Image 2

At what SSD value do we have a good match?

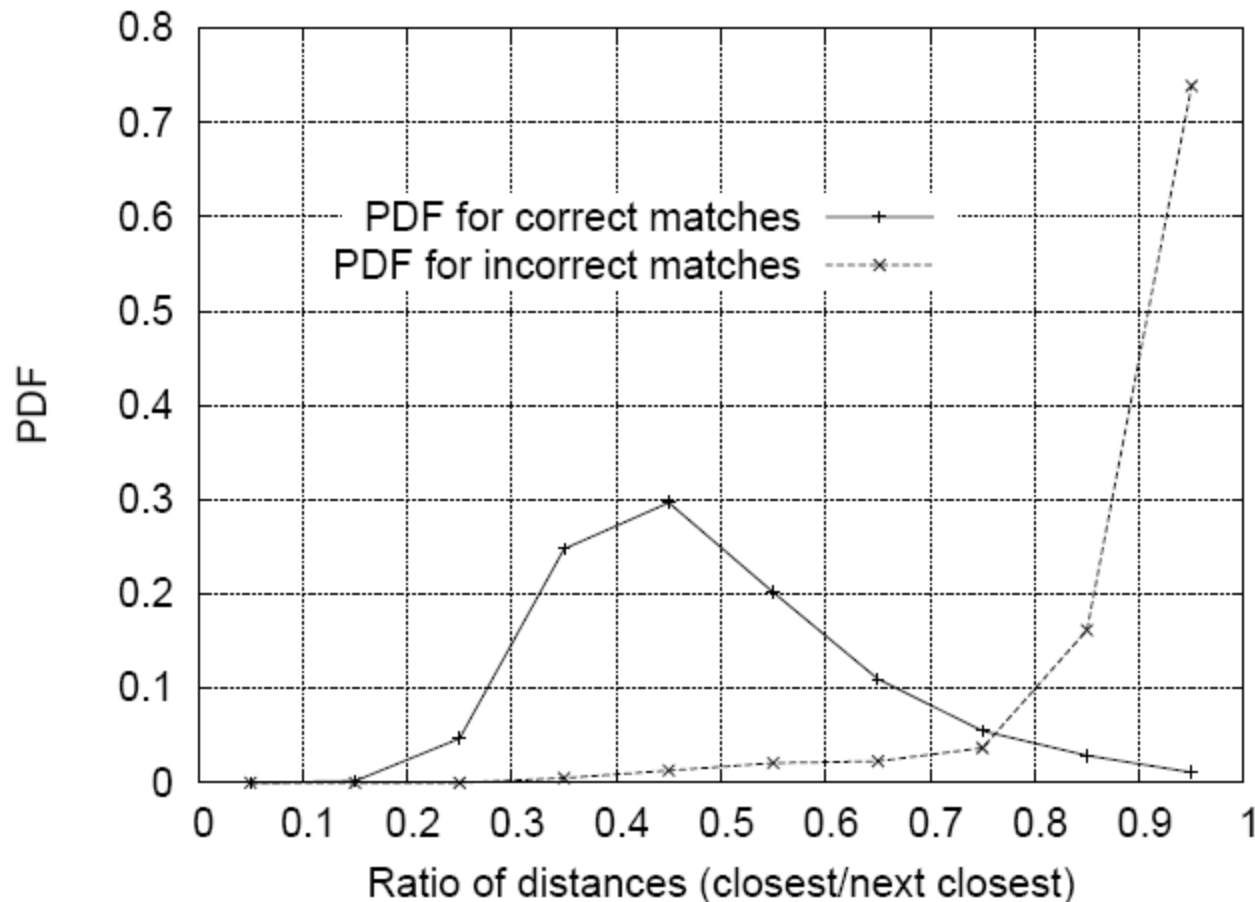
To add robustness to matching, can consider **ratio** :
distance to best match / distance to second best match

If low, first match looks good.

If high, could be ambiguous match.

Matching SIFT Descriptors

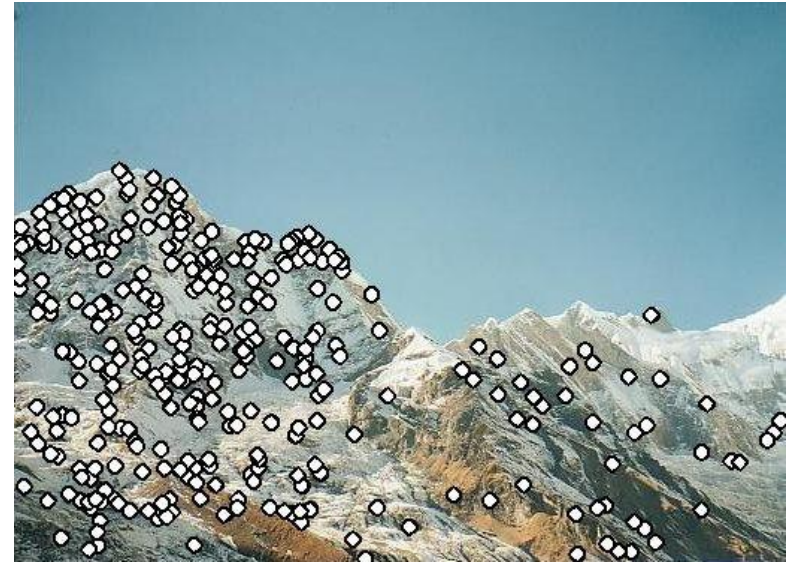
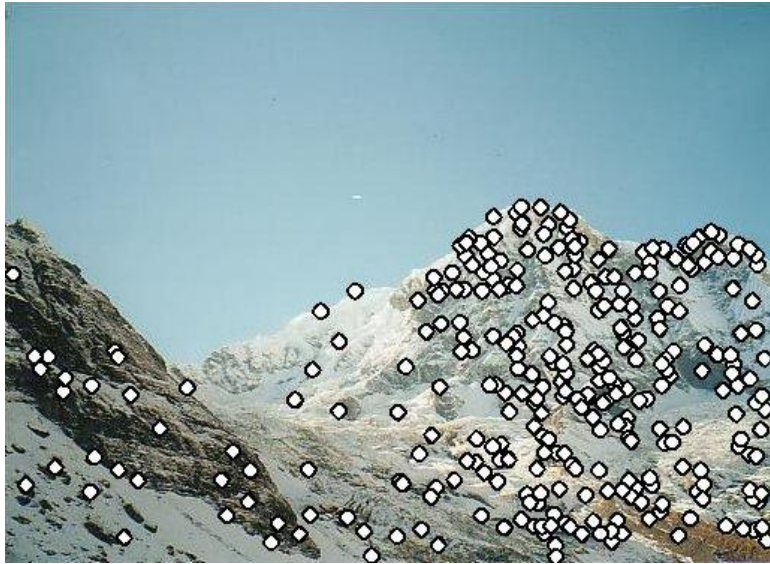
- Nearest neighbor (Euclidean distance)
- Threshold ratio of nearest to 2nd nearest descriptor



Recap: robust feature-based alignment

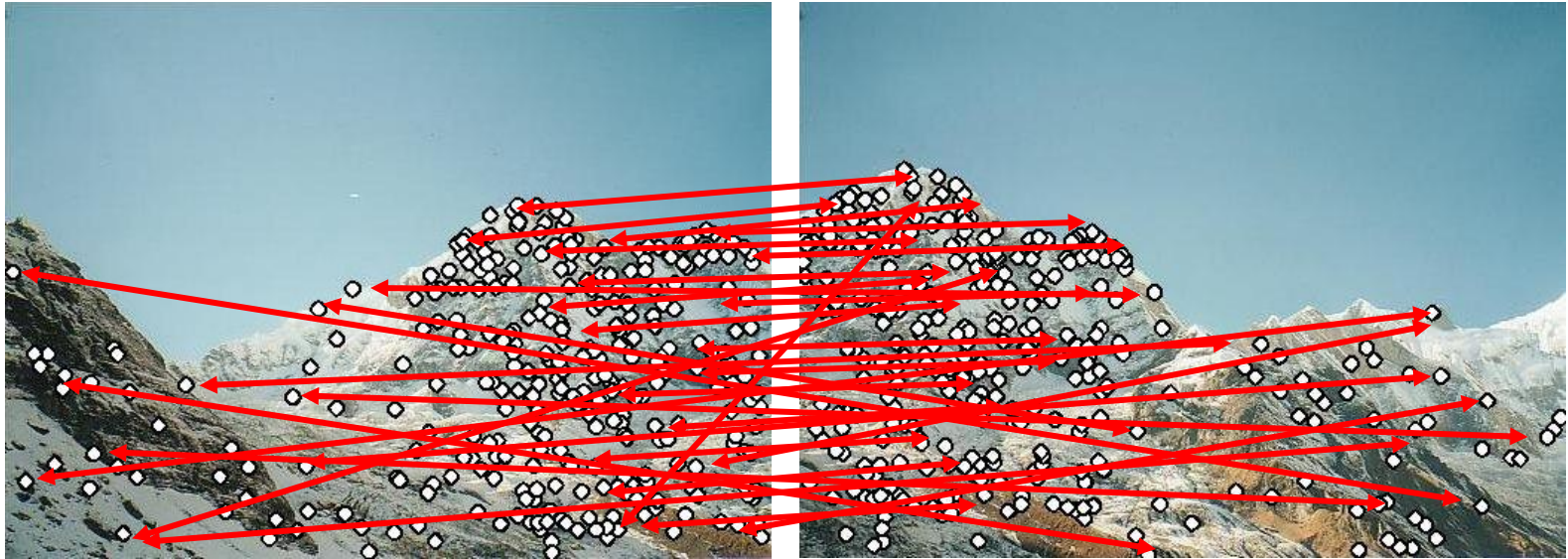


Recap: robust feature-based alignment



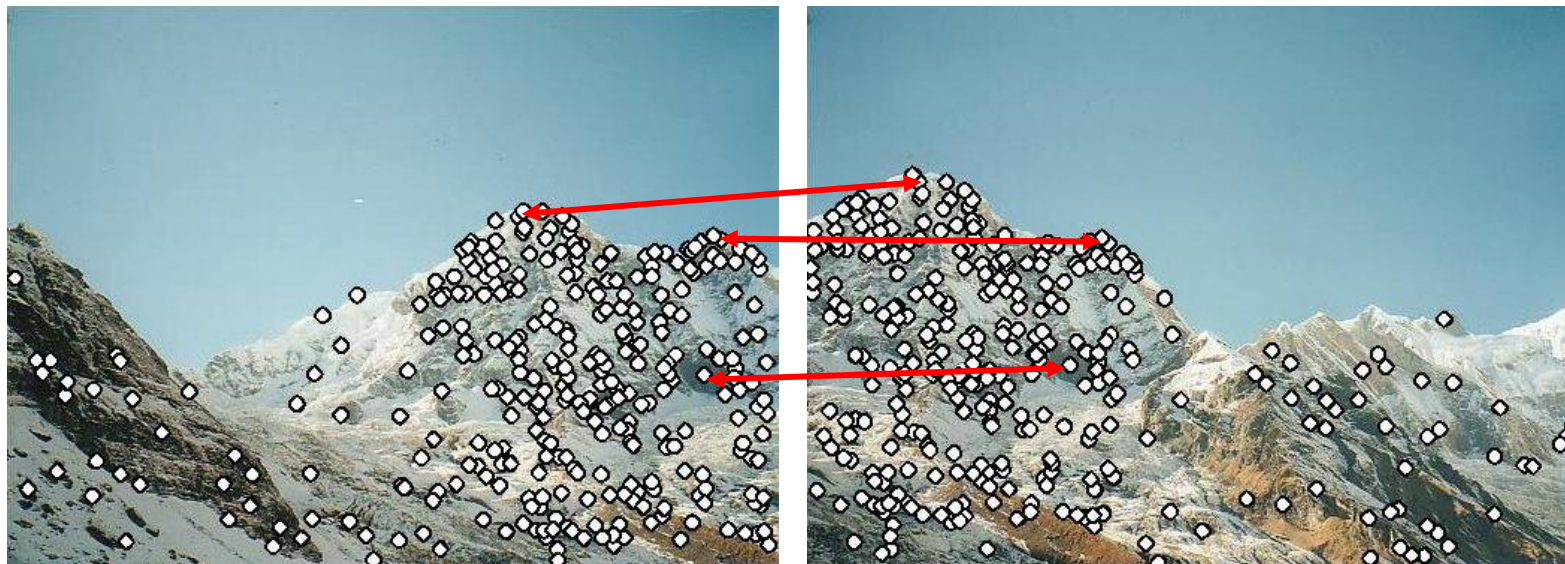
- Extract features

Recap: robust feature-based alignment



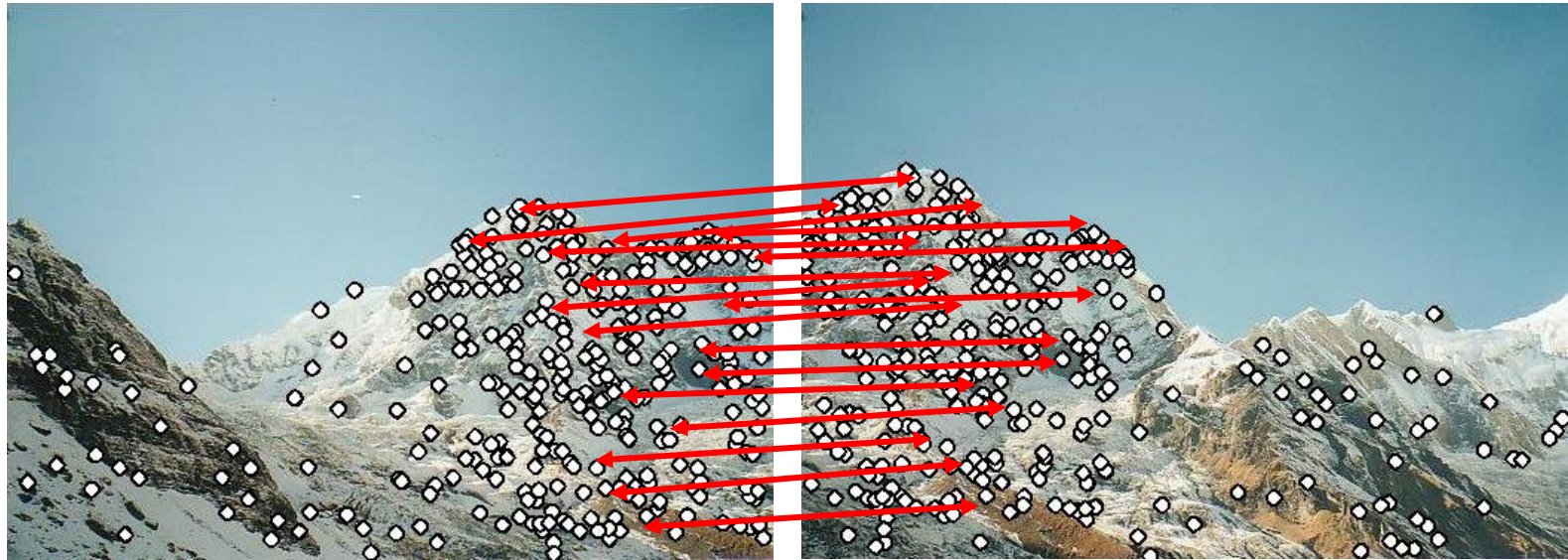
- Extract features
- Compute *putative matches*

Recap: robust feature-based alignment



- Extract features
- Compute *putative matches*
- Loop:
 - *Hypothesize* transformation T (small group of putative matches that are related by T)

Recap: robust feature-based alignment



- Extract features
- Compute *putative matches*
- Loop:
 - *Hypothesize* transformation T (small group of putative matches that are related by T)
 - *Verify* transformation (search for other matches consistent with T)

Recap: robust feature-based alignment



- Extract features
- Compute *putative matches*
- Loop:
 - *Hypothesize* transformation T (small group of putative matches that are related by T)
 - *Verify* transformation (search for other matches consistent with T)

Applications of local invariant features

- Wide baseline stereo
- Motion tracking
- Panoramas
- Mobile robot navigation
- 3D reconstruction
- Recognition
- ...

Automatic mosaicing



<http://www.cs.ubc.ca/~mbrown/autostitch/autostitch.html>

Wide baseline stereo



[Image from T. Tuytelaars ECCV 2006 tutorial]

Recognition of specific objects, scenes



Schmid and Mohr 1997



Sivic and Zisserman, 2003



Rothganger et al. 2003



Lowe 2002

Summary

- Interest point detection
 - Harris corner detector
 - Laplacian of Gaussian, automatic scale selection
- Invariant descriptors
 - Rotation according to dominant gradient direction
 - Histograms for robustness to small shifts and translations (SIFT descriptor)