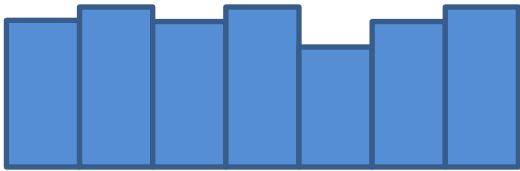




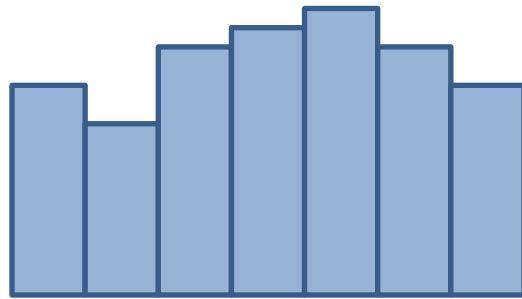
Gradient Domain Blending

James Hays

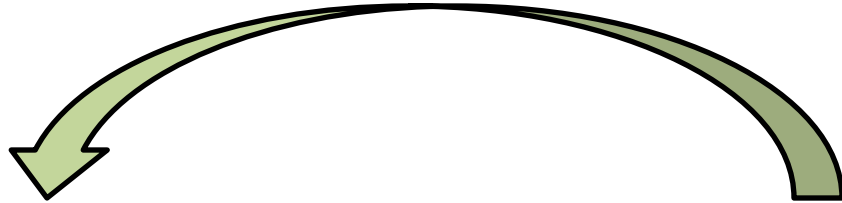
CS 129 Fall 2012

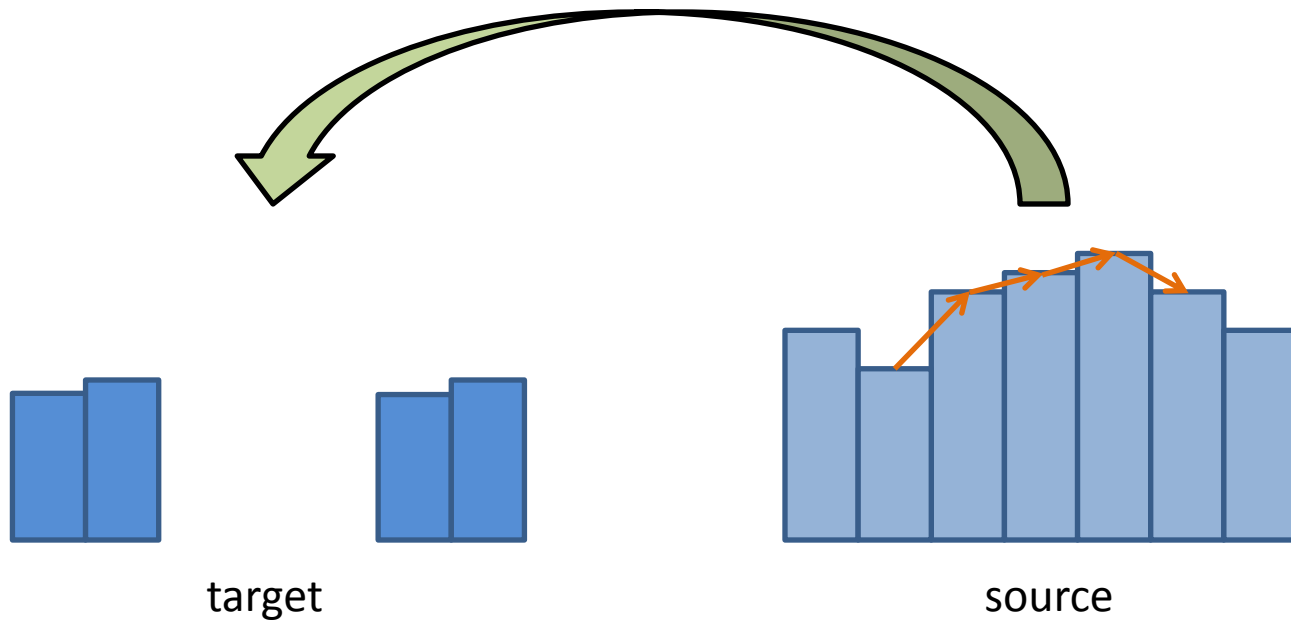


target



source





It is impossible to faithfully preserve the gradients

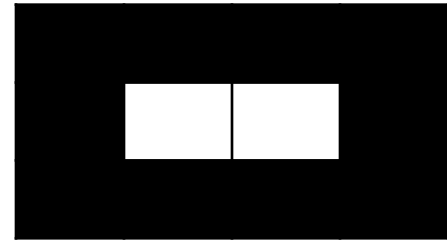
Simple 2d example

| | | | |
|----|----|----|----|
| .2 | .5 | .2 | .2 |
| .7 | .7 | .7 | .7 |
| .9 | .9 | .8 | .9 |

target, t

| | | | |
|----|----|----|----|
| .8 | .6 | .6 | .6 |
| .6 | .6 | .2 | .6 |
| .6 | .8 | .6 | .6 |

source, s



mask



| | | | |
|---|---|---|---|
| ? | ? | ? | ? |
| ? | ? | ? | ? |
| ? | ? | ? | ? |

output, x

What properties do we want x to have?

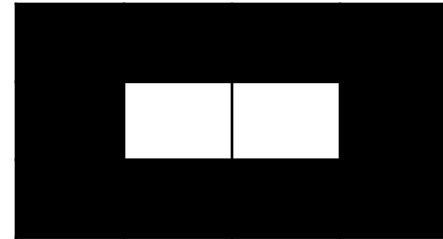
Simple 2d example

| | | | |
|----|----|----|----|
| .2 | .5 | .2 | .2 |
| .7 | .7 | .7 | .7 |
| .9 | .9 | .8 | .9 |

target, t

| | | | |
|----|----|----|----|
| .8 | .6 | .6 | .6 |
| .6 | .6 | .2 | .6 |
| .6 | .8 | .6 | .6 |

source, s



mask

| | | | |
|---|---|---|---|
| ? | ? | ? | ? |
| ? | ? | ? | ? |
| ? | ? | ? | ? |

output, x

- (1) For unmasked pixels, $x_i = t_i$
- (2) For masked pixels, we want the gradients at x_i to match the gradients at s_i

But how do we define the gradient? Instead of constraining one or many gradients, in this example we will use the Laplacian.

| | | |
|----|----|----|
| 0 | -1 | 0 |
| -1 | 4 | -1 |
| 0 | -1 | 0 |

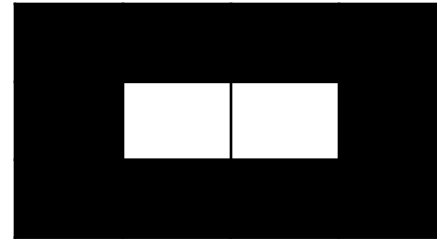
Simple 2d example

| | | | |
|----|----|----|----|
| .2 | .5 | .2 | .2 |
| .7 | .7 | .7 | .7 |
| .9 | .9 | .8 | .9 |

target, t

| | | | |
|----|----|----|----|
| .8 | .6 | .6 | .6 |
| .6 | .6 | .2 | .6 |
| .6 | .8 | .6 | .6 |

source, s



mask

| | | |
|----|----|----|
| 0 | -1 | 0 |
| -1 | 4 | -1 |
| 0 | -1 | 0 |

Laplacian

| | | | |
|---|---|---|---|
| ? | ? | ? | ? |
| ? | ? | ? | ? |
| ? | ? | ? | ? |

output, x

| | | | |
|---|---|---|----|
| 1 | 4 | 7 | 10 |
| 2 | 5 | 8 | 11 |
| 3 | 6 | 9 | 12 |

Pixel indexing

$$x_1 = t_1$$

$$x_2 = t_2$$

$$x_3 = t_3$$

$$x_4 = t_4$$

$$4x_5 - x_4 - x_2 - x_6 - x_8 = 4s_5 - s_4 - s_2 - s_6 - s_8$$

$$x_6 = t_6$$

$$x_7 = t_7$$

$$4x_8 - x_7 - x_5 - x_9 - x_{11} = 4s_8 - s_7 - s_5 - s_9 - s_{11}$$

$$x_9 = t_9$$

$$x_{10} = t_{10}$$

$$x_{11} = t_{11}$$

$$x_{12} = t_{12}$$

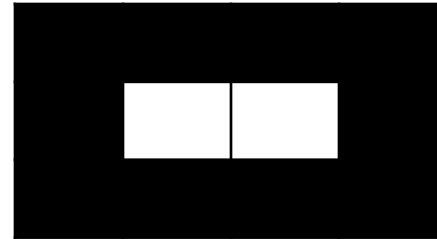
Simple 2d example

| | | | |
|----|----|----|----|
| .2 | .5 | .2 | .2 |
| .7 | .7 | .7 | .7 |
| .9 | .9 | .8 | .9 |

target, t

| | | | |
|----|----|----|----|
| .8 | .6 | .6 | .6 |
| .6 | .6 | .2 | .6 |
| .6 | .8 | .6 | .6 |

source, s



mask

| | | |
|----|----|----|
| 0 | -1 | 0 |
| -1 | 4 | -1 |
| 0 | -1 | 0 |

Laplacian

| | | | |
|---|---|---|---|
| ? | ? | ? | ? |
| ? | ? | ? | ? |
| ? | ? | ? | ? |

output, x

| | | | |
|---|---|---|----|
| 1 | 4 | 7 | 10 |
| 2 | 5 | 8 | 11 |
| 3 | 6 | 9 | 12 |

Pixel indexing

$$x_1 = 0.2$$

$$x_2 = 0.7$$

$$x_3 = 0.9$$

$$x_4 = 0.5$$

$$4x_5 - x_4 - x_2 - x_6 - x_8 = 0.2$$

$$x_6 = 0.9$$

$$x_7 = 0.2$$

$$4x_8 - x_7 - x_5 - x_9 - x_{11} = -1.6$$

$$x_9 = 0.8$$

$$x_{10} = 0.2$$

$$x_{11} = 0.7$$

$$x_{12} = 0.9$$

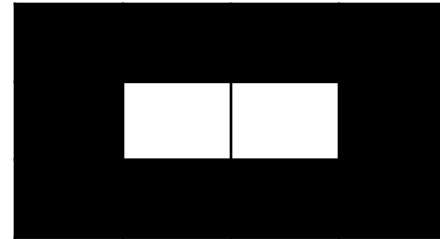
Simple 2d example

| | | | |
|----|----|----|----|
| .2 | .5 | .2 | .2 |
| .7 | .7 | .7 | .7 |
| .9 | .9 | .8 | .9 |

target, t

| | | | |
|----|----|----|----|
| .8 | .6 | .6 | .6 |
| .6 | .6 | .2 | .6 |
| .6 | .8 | .6 | .6 |

source, s



mask

| | | |
|----|----|----|
| 0 | -1 | 0 |
| -1 | 4 | -1 |
| 0 | -1 | 0 |

Laplacian

| | | | |
|---|---|---|---|
| ? | ? | ? | ? |
| ? | ? | ? | ? |
| ? | ? | ? | ? |

output, x

| | | | |
|---|---|---|----|
| 1 | 4 | 7 | 10 |
| 2 | 5 | 8 | 11 |
| 3 | 6 | 9 | 12 |

Pixel indexing

| | | | | | | | | | | |
|---|----|---|----|---|----|----|----|---|----|---|
| 1 | | | | | | | | | | |
| | 1 | | | | | | | | | |
| | | 1 | | | | | | | | |
| | | | 1 | | | | | | | |
| | -1 | | -1 | 4 | -1 | | -1 | | | |
| | | | | 1 | | | | | | |
| | | | | | 1 | | | | | |
| | | | | | | -1 | -1 | 4 | -1 | |
| | | | | | | | | 1 | | |
| | | | | | | | | | 1 | |
| | | | | | | | | | | 1 |

A

$$x = A \setminus b$$

*

=

| |
|---|
| ? |
| ? |
| ? |
| ? |
| ? |
| ? |
| ? |
| ? |
| ? |
| ? |
| ? |
| ? |

x

| |
|------|
| .2 |
| .7 |
| .9 |
| .5 |
| .2 |
| .9 |
| .2 |
| -1.6 |
| .8 |
| .2 |
| .7 |
| .9 |

b

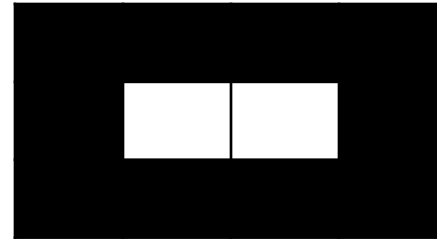
Simple 2d example

| | | | |
|----|----|----|----|
| .2 | .5 | .2 | .2 |
| .7 | .7 | .7 | .7 |
| .9 | .9 | .8 | .9 |

target, t

| | | | |
|----|----|----|----|
| .8 | .6 | .6 | .6 |
| .6 | .6 | .2 | .6 |
| .6 | .8 | .6 | .6 |

source, s



mask

| | | |
|----|----|----|
| 0 | -1 | 0 |
| -1 | 4 | -1 |
| 0 | -1 | 0 |

Laplacian

| | | | |
|----|-----|-----|----|
| .2 | .5 | .2 | .2 |
| .7 | .62 | .18 | .7 |
| .9 | .9 | .8 | .9 |

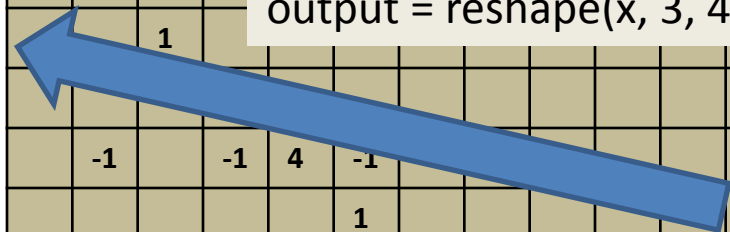
output, x

| | | | |
|---|---|---|----|
| 1 | 4 | 7 | 10 |
| 2 | 5 | 8 | 11 |
| 3 | 6 | 9 | 12 |

Pixel indexing

| | | | | | | | | | |
|---|---|---|----|----|---|----|---|---|---|
| 1 | | | | | | | | | |
| | 1 | | | | | | | | |
| | | 1 | | | | | | | |
| | | | -1 | -1 | 4 | -1 | | | |
| | | | | | | 1 | | | |
| | | | | | | | 1 | | |
| | | | | | | | | 1 | |
| | | | | | | | | | 1 |

output = reshape(x, 3, 4)



*

=

| |
|-----|
| .2 |
| .7 |
| .9 |
| .5 |
| .62 |
| .9 |
| .2 |
| .18 |
| .8 |
| .2 |
| .7 |
| .9 |

x

| |
|------|
| .2 |
| .7 |
| .9 |
| .5 |
| .2 |
| -1.6 |
| .8 |
| .2 |
| .7 |
| .9 |

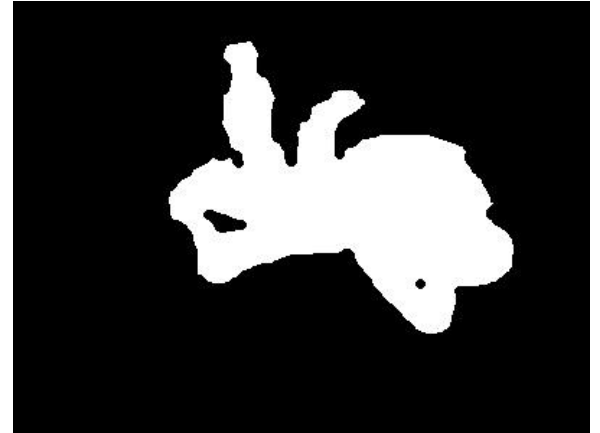
b



target



source



mask



no blending



gradient domain blending

What's the difference?



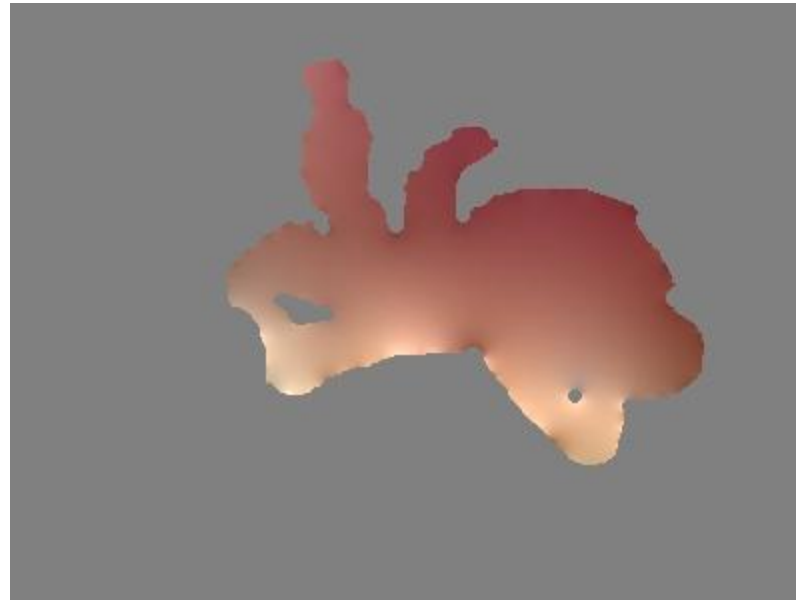
gradient domain blending



no blending

-

=



What's the difference?



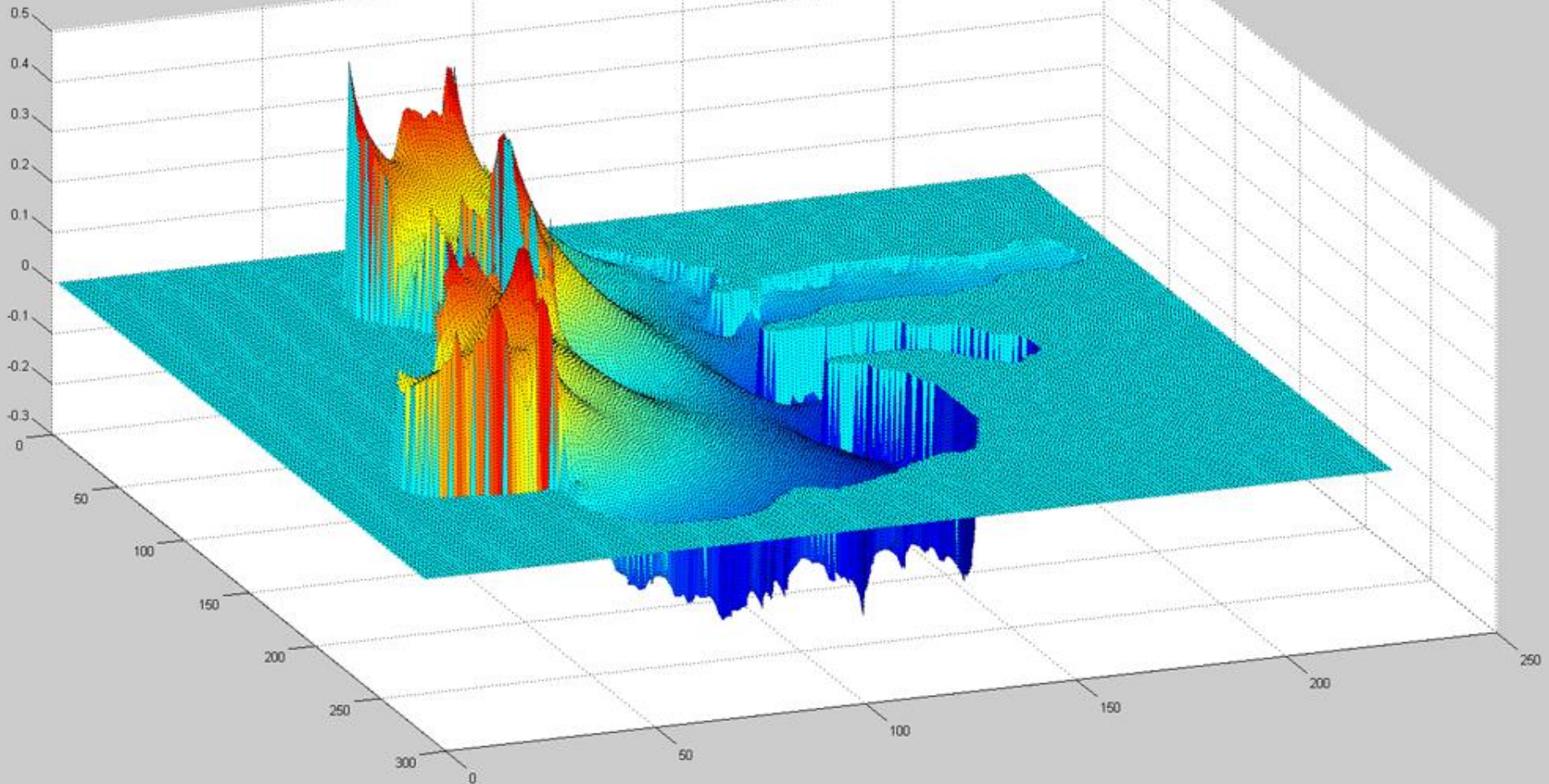
gradient domain blending

-



no blending

=



What's the difference?



gradient domain blending

-



no blending

=

