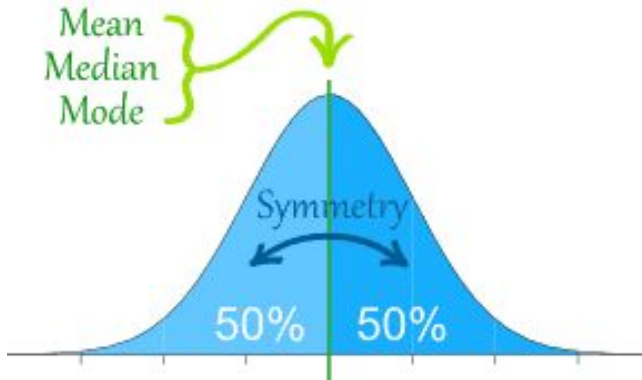


# Normal Distribution

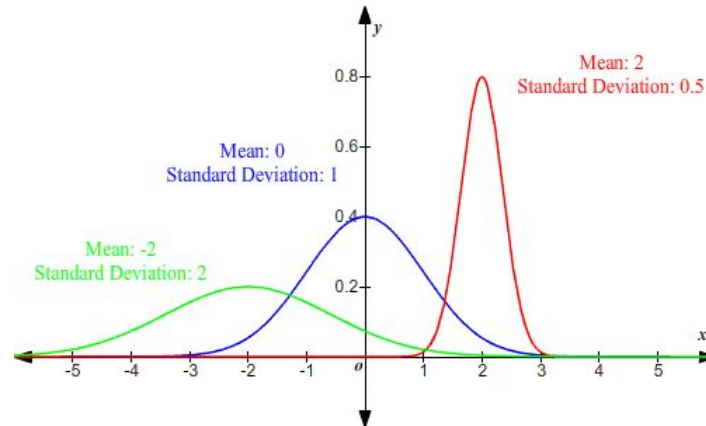
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# The Normal Distribution

- A bell-shaped curve, whose shape depends on two things
  - Mean, Median, and Mode: the center of the curve
  - Variance: the spread (i.e., the height and width) of the curve



[Image source](#)

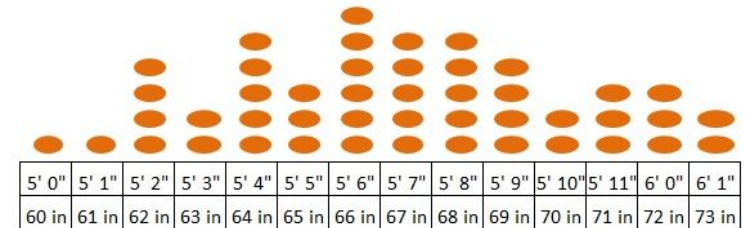


[Image source](#)

# Are data normally normally distributed?



46 students in a statistics class  
at Simon Fraser University.



# Are data normally normally distributed?



Sample mean: 66.78

Sample standard deviation: 3.37

- $(66.78 - 1 \times 3.37, 66.78 + 1 \times 3.37)$
- $(66.78 - 2 \times 3.37, 66.78 + 2 \times 3.37)$
- $(66.78 - 3 \times 3.37, 66.78 + 3 \times 3.37)$

How many of the measurements lie within these intervals?

- 30 lie in  $(63.4, 70.2) = 65.2 \%$
- 45 lie in  $(60.0, 73.5) = 97.8 \%$
- 46 lie in  $(56.7, 76.9) = 100 \%$

# Standard Normal

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# Women's heights in the US

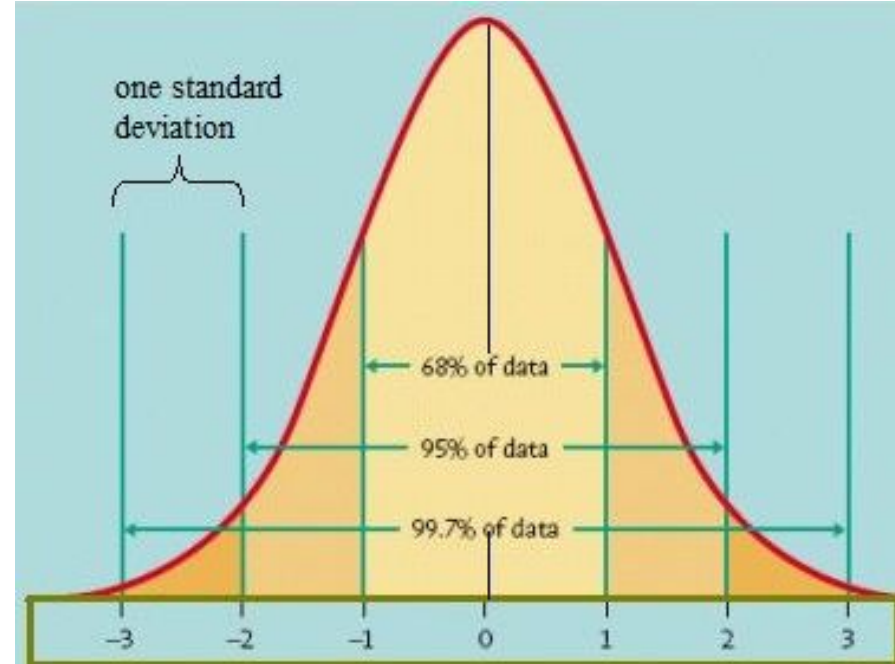
- In the US, women's heights are normally distributed with a mean of 65 inches and a standard deviation of 3.5 inches.
- I am 63.25 inches tall. How many standard deviations below the mean am I?
- How many standard deviations above the mean is 6 feet (72 inches)?
- What percentage of women in the US are shorter than me?
- What percentage of women in the US are taller than 6 feet?

# Women's heights in the US (cont'd)

- To find the percentages, all we have to do is integrate.
  - The percentage of women in the US who are shorter than me is simply the area under the normal curve  $N(65, 3.5)$  from  $-\infty$  to 63.25.
  - Likewise, the percentage of women in the US who are taller than 72 inches is simply the area under the normal curve  $N(65, 3.5)$  from 72 to  $\infty$ .
- **Big problem:** Integrating a normal distribution is not easy!
- Strategy: to answer queries such as the ones about women's heights, pose the equivalent query in terms of the **standard normal** instead.

# The Standard Normal Distribution

- Mean is 0.
- Standard deviation is 1.
- The data are symmetrically dispersed around the bell
- About 68% of the data lie within 1 standard deviation of the mean. About 95% of the data lie within 2 standard deviation of the mean.



[Image Sources](#)



# Standard Normal Table

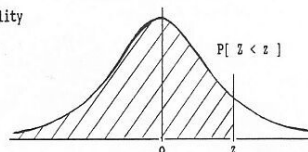
In the olden days (back when I was a student), we used the standard normal table to answer queries.

- $P[-1 \leq Z \leq 1] =$   
 $P[Z \leq 1] - P[Z \leq -1] =$   
 $P[Z \leq 1] - (1 - P[Z \leq 1])$
- $P[-1 \leq Z \leq 1] = .8413 - (1 - .8413) = 68.26\%$
- $P[-2 \leq Z \leq 2] = .9773 - (1 - .9773) = 95.46\%$
- $P[-3 \leq Z \leq 3] = .9986 - (1 - .9986) = 99.72\%$

STANDARD STATISTICAL TABLES

1. Areas under the Normal Distribution

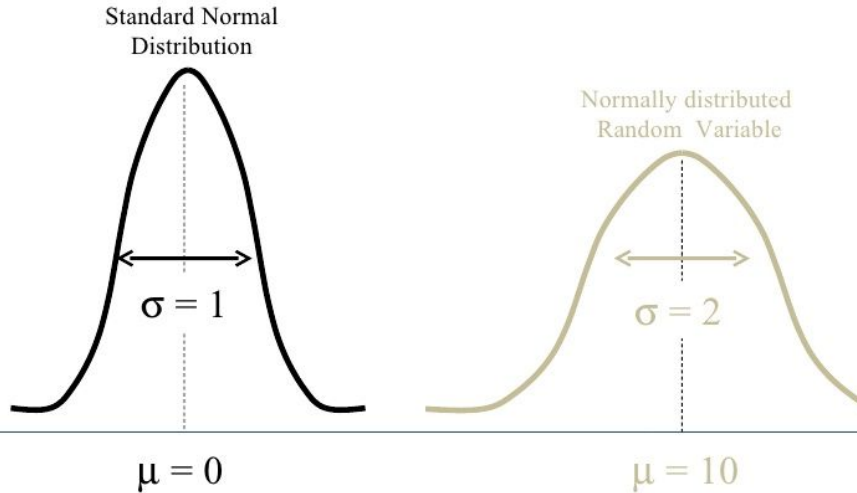
The table gives the cumulative probability up to the standardised normal value  $z$  i.e.

$$P[Z < z] = \int_{-\infty}^z \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{1}{2}z^2\right) dz$$


$z$	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5159	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7854
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	<b>0.8413</b>	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8804	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	<b>0.9773</b>	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9865	0.9868	0.9871	0.9874	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9924	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9980	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
$z$	3.00	3.10	3.20	3.30	3.40	3.50	3.60	3.70	3.80	3.90
$P$	<b>0.9986</b>	0.9990	0.9993	0.9995	0.9997	0.9998	0.9998	0.9999	0.9999	1.0000

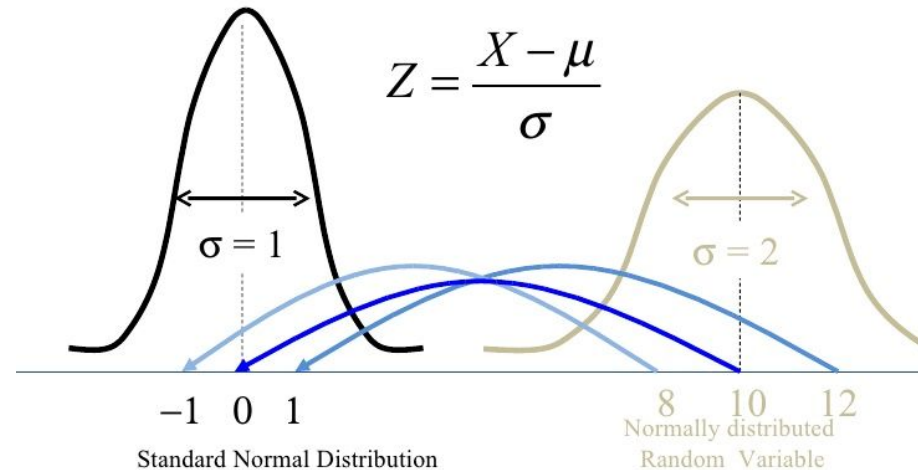
# z-transformation

We use the formula for Z transformation:  $Z = \frac{X - \mu}{\sigma}$



In sum, the Z formula transforms the original normal distribution in two ways:

1. The numerator of the formula,  $(X - \mu)$ , shifted the distribution so it is centered on 0.
2. By dividing by the standard deviation of the original distribution, it compressed the width of the distribution so it has a standard deviation equal to 1.



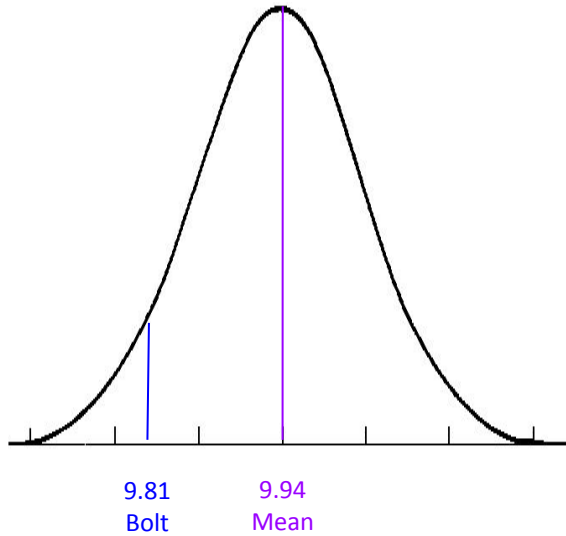
# z-transformation

- Standard units are the number of standard deviations away from the mean
  - Some values will be negative, corresponding to values below the mean
  - Some values will be positive, corresponding to values above the mean
- The z-transformation transforms a normally distributed random variable with mean  $\mu$  and standard deviation  $\sigma$  into a standard normal random variable, meaning it has mean 0 and standard deviation 1.
- First shift the value, by computing how far away it is from the mean, and then compute the ratio of that deviation to the standard deviation.
- The resulting z-score represents the number of standard deviations away from the mean (0) that a shifted value is.

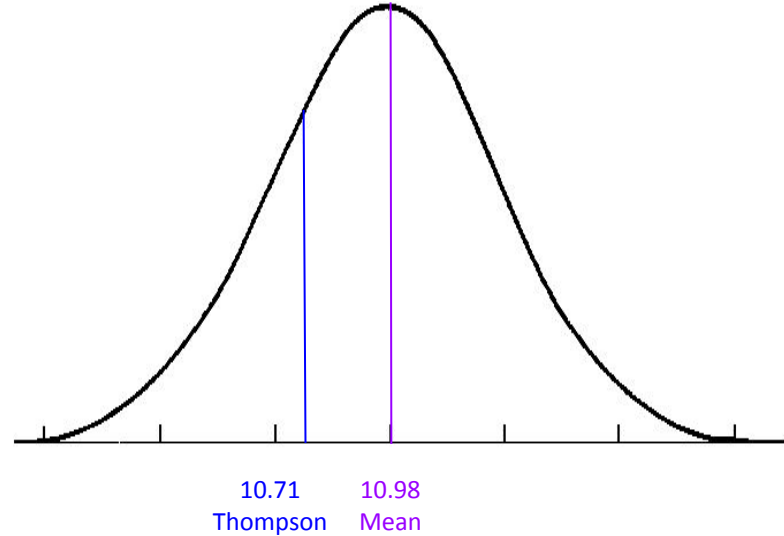
# Standardization Example

- In the 2016 summer Olympics:
  - Usain Bolt won the gold medal in the men's 100M race with a time of 9.81 seconds.
  - Elaine Thompson won the gold medal in the women's 100M race with a time of 10.71 seconds.
- Statistics for the races:
  - The average time for men was 9.94 seconds, with a standard deviation of 0.08 seconds.
  - The average time for women was 10.98 seconds, with a standard deviation of 0.34 seconds.
- Which racer did better in comparison to the rest of their field?

# Visualizing Runner Times



Standard deviation = 0.08



Standard deviation = 0.34

# 2016 Olympic Runners (cont'd)

- We cannot compare these data easily unless we first standardize them.
- Indeed, by applying the z-transformation, all the units cancel, so we are comparing “apples to apples” instead of “apples to oranges.”
- First, we can see how Usain Bolt did relative to his competition.
  - $Z = (9.81 \text{ sec} - 9.94 \text{ sec}) / 0.08 \text{ sec} = -1.63$
- Second, we can see how Elaine Thompson did relative to her competition.
  - $Z = (10.71 \text{ sec} - 10.98 \text{ sec}) / 0.34 \text{ sec} = -0.79$
- More extreme z-scores imply rarer events. So, the runner with the more extreme z-score performed better comparatively.
  - As measured by z-scores, Usain Bolt performed better relative to his field than Elaine Thompson did relative to hers.

# Back to Women's heights in the US

Apply the z-transformation:

- $Z = (63.25 - 65) / 3.5 = -\frac{1}{2}$
- $Z = (72 - 65) / 3.5 = 2$

Therefore, I am  $\frac{1}{2}$  a standard deviation below the mean.

Women who are 6 feet tall are two standard deviations above the mean.

# Standard Normal Table

The probability a woman in the US is shorter than me at 63.25 inches is equal to the probability a z-score is less than or equal to  $-\frac{1}{2}$ .

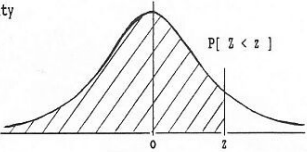
- In the textbook,  $P[Z \leq -\frac{1}{2}] = 1 - P[Z \leq \frac{1}{2}] = 1 - 0.6915 = 0.3085$ .
- In R: `pnorm(-1/2) = 0.31`

Hence, about 31% of women in the US are shorter than me.

STANDARD STATISTICAL TABLES

1. Areas under the Normal Distribution

The table gives the cumulative probability up to the standardised normal value  $z$  i.e.

$$P[Z < z] = \int_{-\infty}^z \frac{1}{\sqrt{2\pi}} \exp(-\frac{1}{2}z^2) dz$$


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2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9980	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
z	3.00	3.10	3.20	3.30	3.40	3.50	3.60	3.70	3.80	3.90
P	0.9986	0.9990	0.9993	0.9995	0.9997	0.9998	0.9998	0.9999	0.9999	1.0000



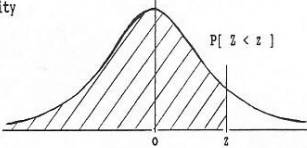
# Standard Normal Table

The probability a woman in the US is taller than 72 inches is equal to the probability a z-score is greater than 2.

STANDARD STATISTICAL TABLES

1. Areas under the Normal Distribution

The table gives the cumulative probability up to the standardised normal value  $z$  i.e.

$$P[Z < z] = \int_{-\infty}^z \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{1}{2}z^2\right) dz$$


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2.2	0.9861	0.9865	0.9868	0.9871	0.9874	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9924	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9980	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
$z$	3.00	3.10	3.20	3.30	3.40	3.50	3.60	3.70	3.80	3.90
$P$	0.9986	0.9990	0.9993	0.9995	0.9997	0.9998	0.9998	0.9999	0.9999	1.0000

# Standard Normal Table

The probability a woman in the US is taller than 72 inches is equal to the probability a z-score is greater than 2.

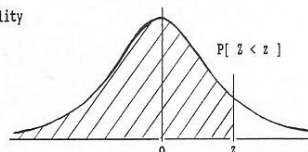
- In the textbook,  $P[Z \leq 2] = 0.9773$ .  
So  $P[Z > 2] = 1 - .9773 = .0227$
- In R: `pnorm(2, lower.tail = FALSE) = 0.023`

Hence, about 2.3% of women in the US are taller than 72 inches.

STANDARD STATISTICAL TABLES

1. Areas under the Normal Distribution

The table gives the cumulative probability up to the standardised normal value  $z$  i.e.

$$P[Z < z] = \int_{-\infty}^z \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{1}{2}z^2\right) dz$$


z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5159	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7854
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8804	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9773	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9865	0.9868	0.9871	0.9874	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9924	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9980	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
z	3.00	3.10	3.20	3.30	3.40	3.50	3.60	3.70	3.80	3.90
P	0.9986	0.9990	0.9993	0.9995	0.9997	0.9998	0.9998	0.9999	0.9999	1.0000

# Exercise:

What percentage of women in the US are shorter than you?