

Some Tools and Techniques for Managing Uncertain Data

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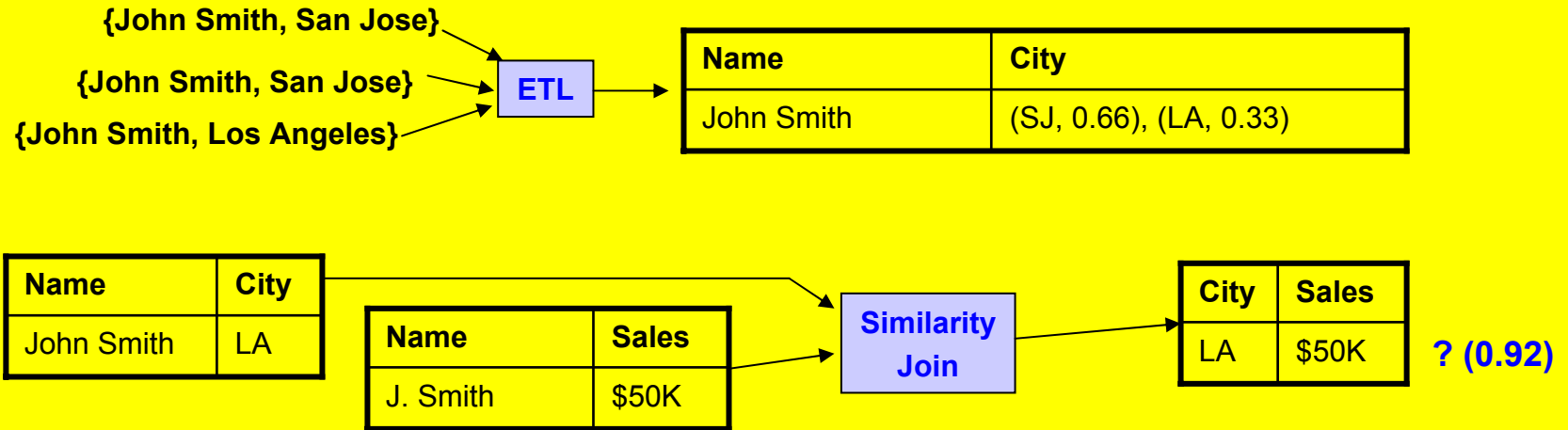
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Outline

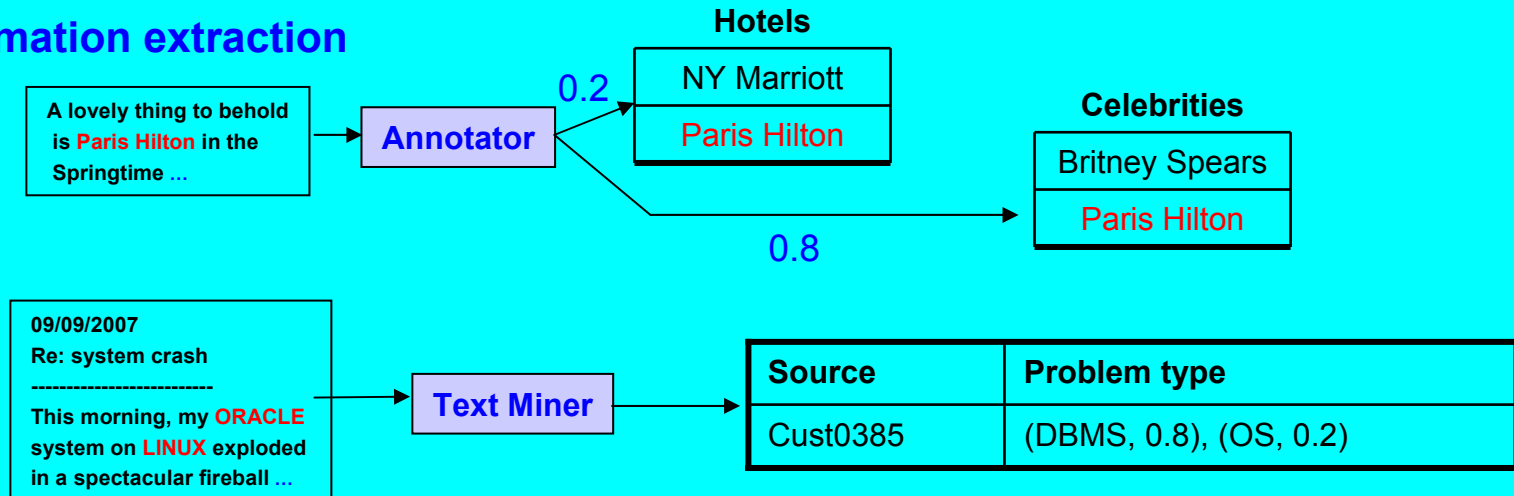
- Motivation via examples
- MCDB: Monte Carlo Database System
- MC³: MCDB + map-reduce
- Related projects
- Future directions

Sources of Data Uncertainty

Data Integration

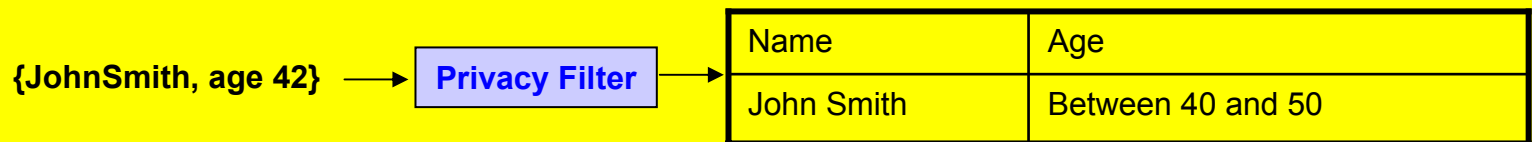


Information extraction

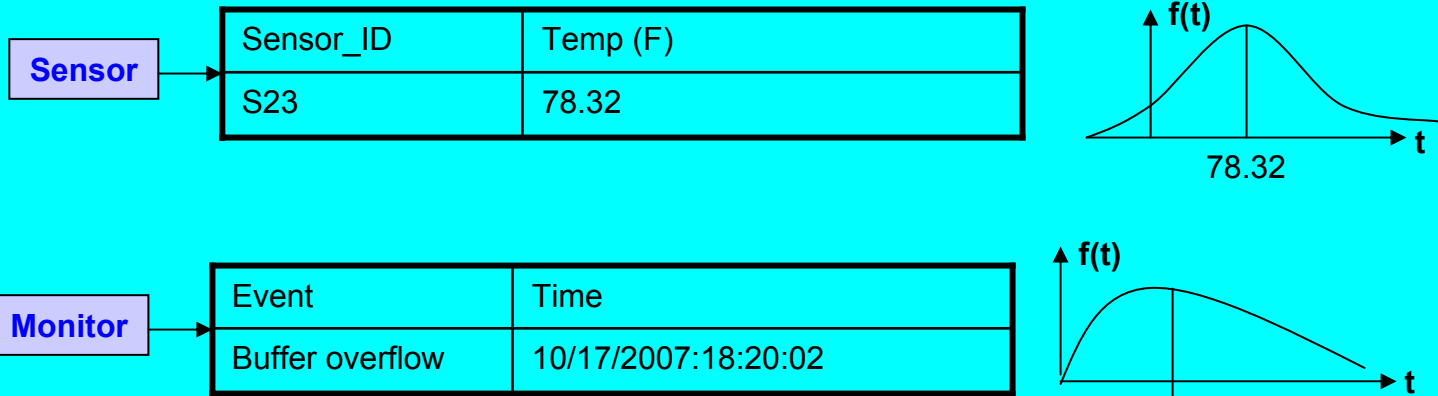


Data Uncertainty - Continued

Anonymization



Measurement Uncertainty



Extrapolation Uncertainty: Portfolio Values

Customer

CustID	OptionID	NumShares
John Smith	23	50
...		...

EuroCallOptions

OptionID	InitVal	r	a	dt	StrikeP	OVal
23	\$2.35	0.8	1.01	0.0001	\$4.00	?
...						...

```
SELECT SUM (c.NumShares * o.Val)
FROM Customer c, EuroCallOptions o
WHERE c.OptionID = o.OptionID
      AND c.CustID = 'John Smith'
```

Option value
one month from now
(exercise date)




Modified Black-Scholes model for European call option:

$$dV = rVdt + (a\sqrt{V})VdW \quad OVal = \max(V(t_{\text{final}}) - S, 0)$$

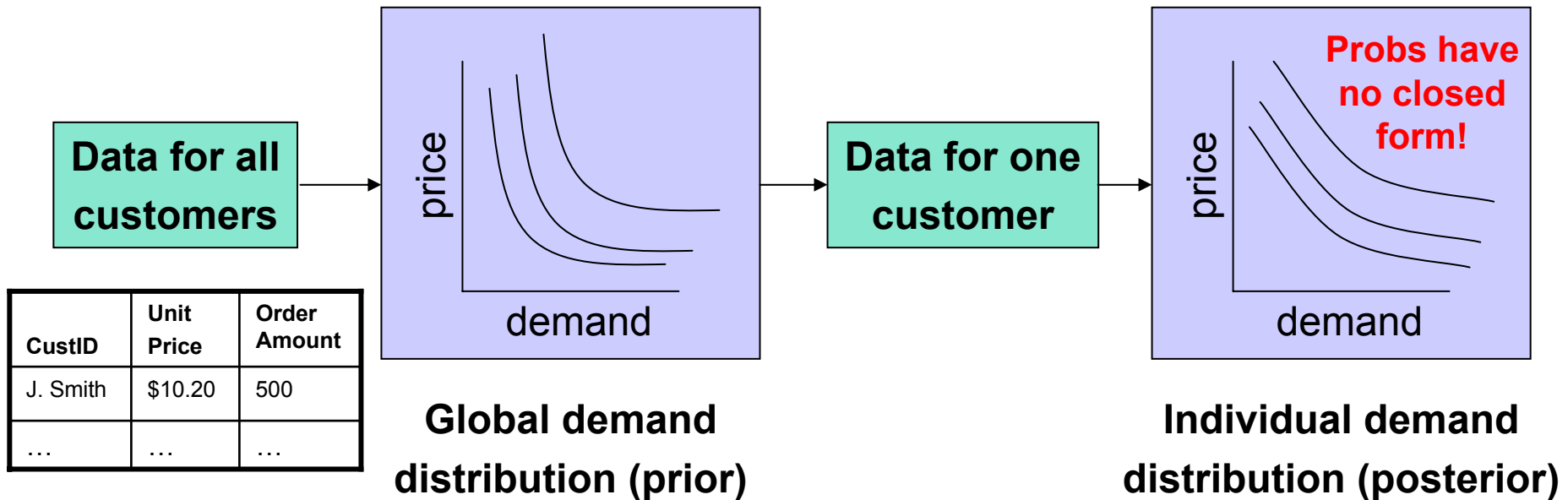
Simulation approximation (Euler formula):

$$V(t + \Delta t) = V(t) + rV(t)\Delta t + (a\sqrt{V(t)})V(t)\sqrt{\Delta t}Z_j$$

Sample from Normal dist'n



Pricing Decisions: Individual Demand Curves

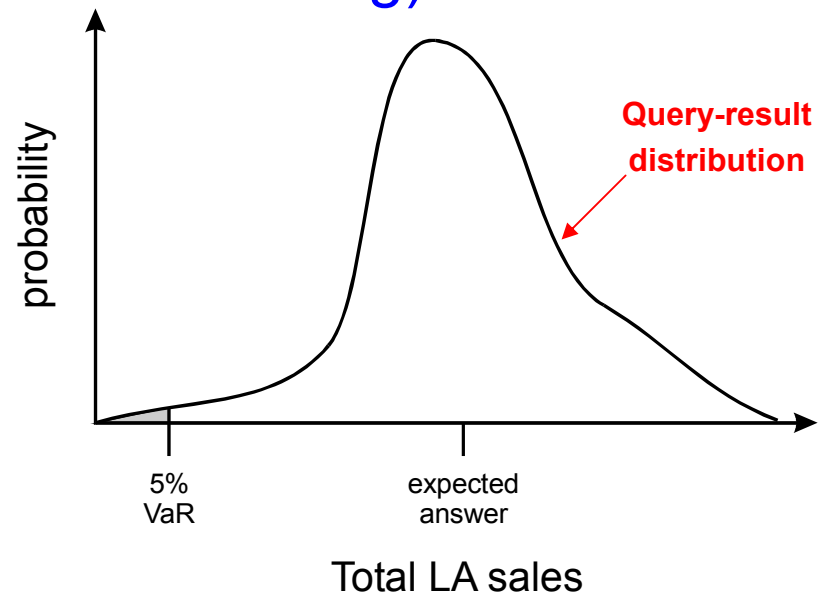


- Can analyze arbitrary dynamic customer segments when determining effect of price increase
- Similar approach for web-click behavior (EBay)
- Issues
 - Complex model, huge number of dynamic parameters
 - Can we integrate into database?

Risk Due to Data Uncertainty

- Ex: Value of assets (for financial reporting, compliance, business-process monitoring)

```
SELECT SUM (s.amount)
FROM SALES s, CUST c
WHERE s.ID = c.ID
      AND c.city = 'Los Angeles'
```



- Ex: ERP
 - # OS experts needed for help desk
 - Based on (uncertain) extracted text data from last year
 - Provide principled **safety factor**

Motivation: Summary

- Customer needs: translate data uncertainty into query uncertainty
 - Risk assessment
 - Decision-making under uncertainty
- Uncertainty models
 - Both **warehouse** and **extrapolation** uncertainty
 - Highly **heterogeneous** and complex
 - Often depend **dynamically** on **huge #** of parameters
 - Correlation matrices for multivariate distributions
 - Customer purchase histories
 - Probabilities perpetually changing
- BI Queries
 - Complicated SQL aggregation queries
 - Subqueries, DISTINCT clauses, ...
- What-if and sensitivity analysis are **crucial**
 - Input probabilities are **not** precise (so check sensitivity)
 - Want to try many different policies

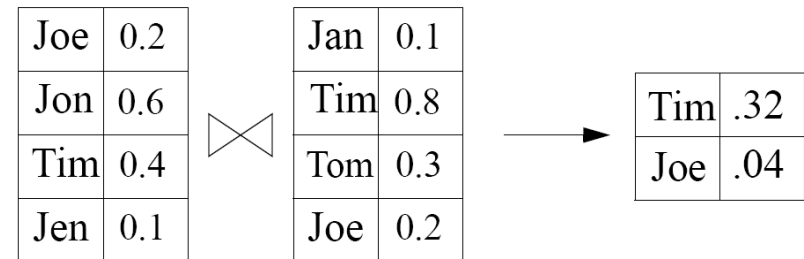
Prior Work: Extended Relational Models (ERM)

- ERM:

- Basis of “probabilistic databases”
- Relational model augmented with probabilities, correlations, etc.
- Relational operations modified accordingly
- Trio, MayBMS, ORION, MystiQ, K-relations, et al.
- Emphasis on “top-k” queries

- Drawbacks

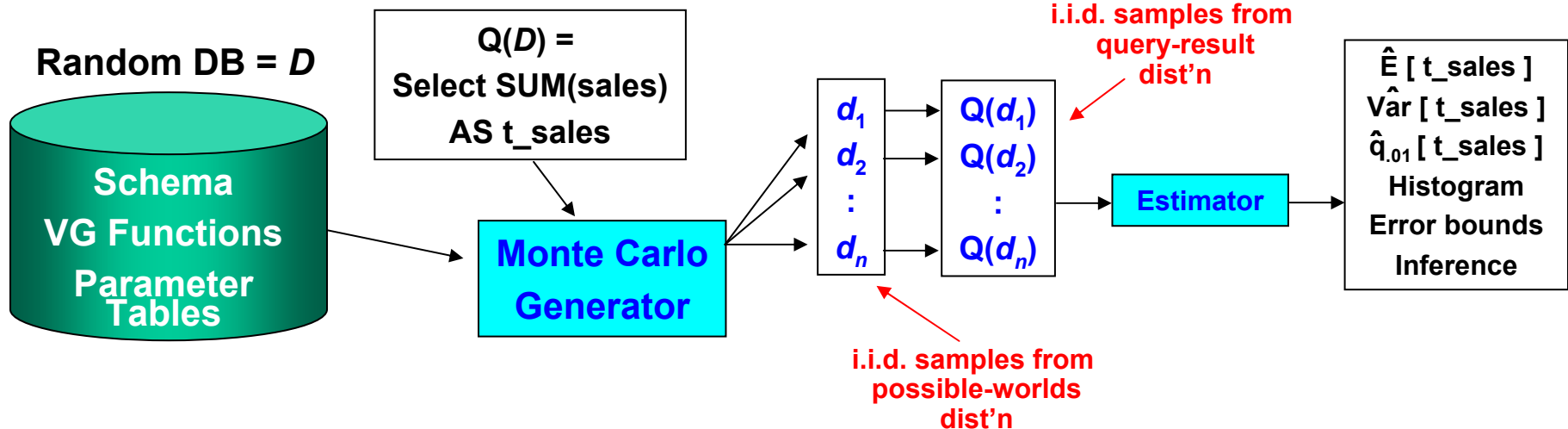
- Hard-wired uncertainty model
- Hard to fit data into tuples
- Hard to change probabilities
- What-if analysis is hard
- Exact analysis (PTIME) only for very simple queries, data, output stats
- Exact methods have trouble with aggregation queries



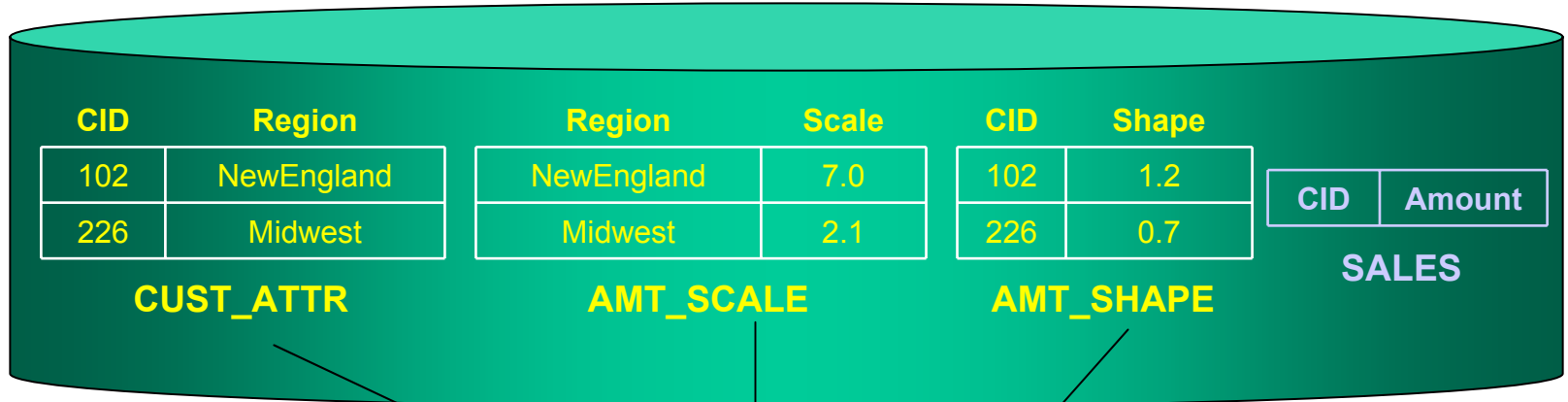
Outline

- Motivation
- MCDB: Monte Carlo Database System
- MC³
- Related projects
- Future directions

The MCDB System



MCDB Example



Q: SELECT SUM(Amount)
FROM SALES
AS t_sales

CID	Shape	Scale
102	1.2	7.0
226	0.7	2.1

Gamma(shape, scale)

VG function

d_1

CID	Amount
102	\$120.00
226	\$60.00

$Q(d_1) = \$180$

d_2

CID	Amount
102	\$80.00
226	\$90.00

$Q(d_2) = \$170$

d_3

CID	Amount
102	\$80.00
226	\$130.00

$Q(d_3) = \$210$

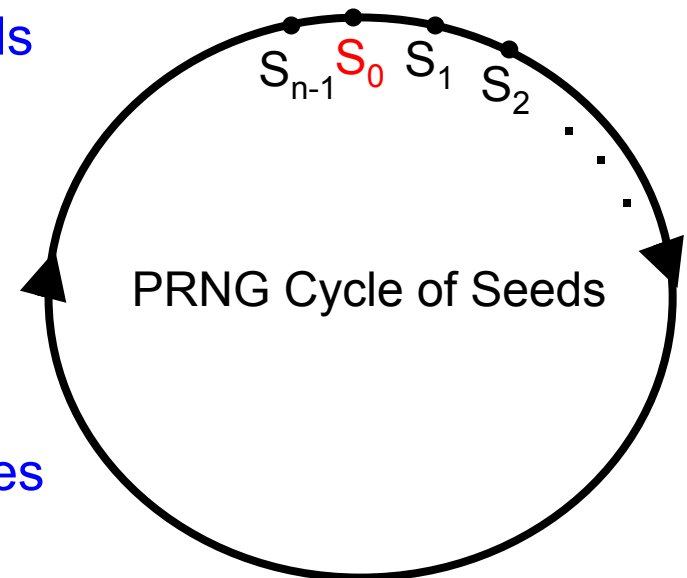
$\hat{E}[t_sales] = \$186.67$ $S\hat{T}D[t_sales] = \$20.82$

Advantages of MCDB

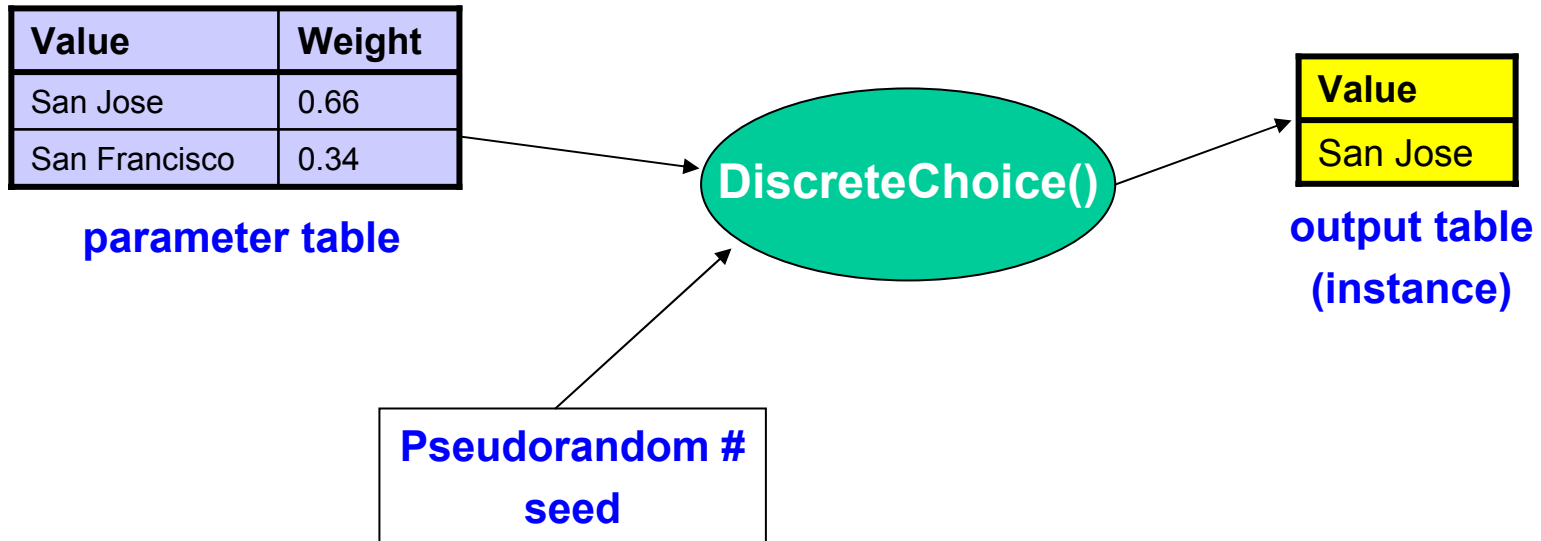
- Flexible and **extensible** uncertainty model
 - Can capture extended relational models (Trio, MayBMS, Mystiq,...)
 - Can capture arbitrarily complex correlations, continuous data
 - Can capture dynamic, highly parameterized distributions
 - Can bring complex stochastic models to data (no extraction needed)
- Encapsulates complexity
 - Once expert has written VG function, naïve user can run queries
- Can handle arbitrary SQL queries
- What-if analysis, sensitivity analysis, data updates are easy

Pseudorandom Number Generators (PRNG)

- Needed by VG function
 - E.g., to generate “random” sales values
- Produces a **deterministic** sequence of seeds
 - Appears random
 - Cycles around
- Typical PRNG recurrence:
 - $S_{i+1} = M * S_i \text{ mod } m$
 - Seed S = vector of k unsigned integers
 - M is a matrix
- Transform seeds to desired random samples
- Cycle usually “split” into disjoint segments
 - Skip factor
- Keeping only initial seed, S_0 , is sufficient to regenerate sequence

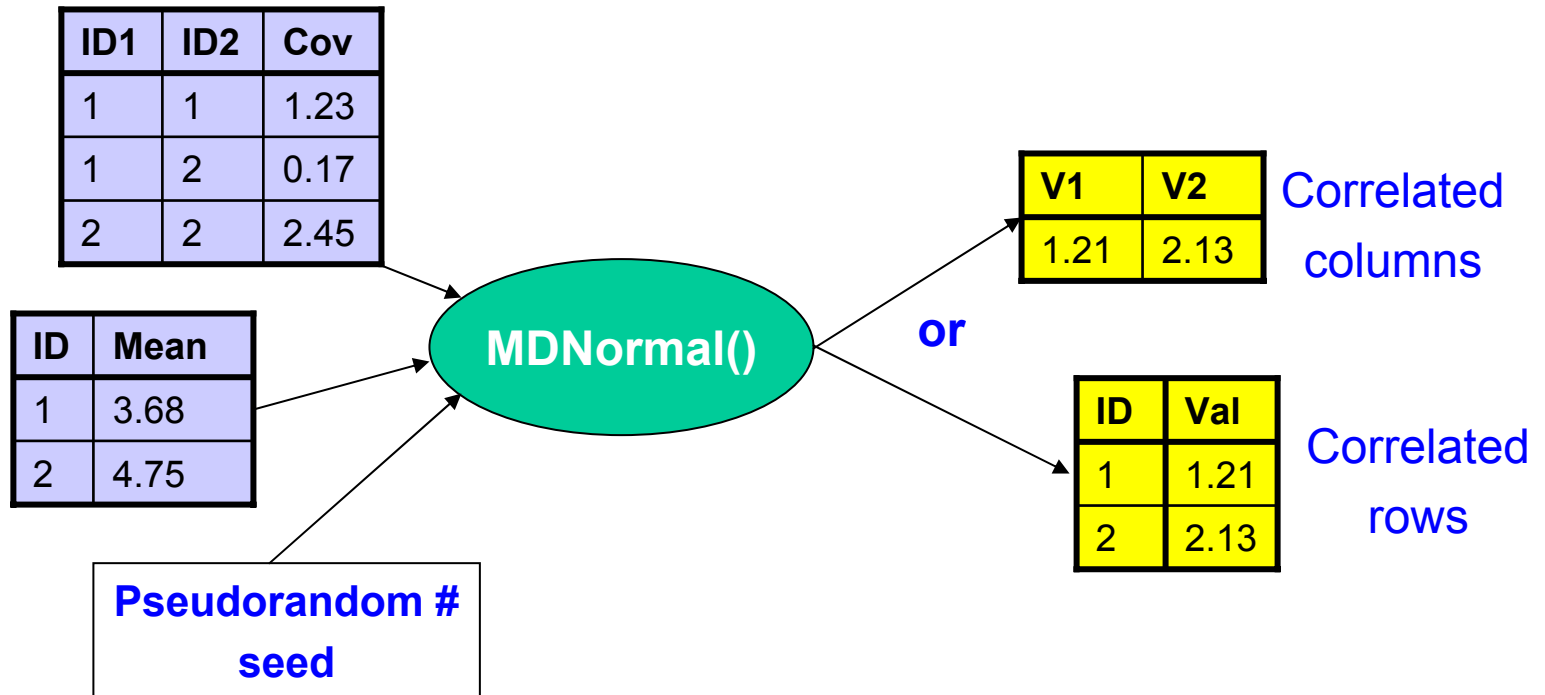


VG Functions



- **Used to generate instances of values in random tables**
 - Parameter tables are standard relational tables (can index, etc.)
 - Library of standard functions: DiscreteChoice, Normal, Poisson, ...
 - Can define custom functions (similar to UDFs)

VG Functions and Correlation



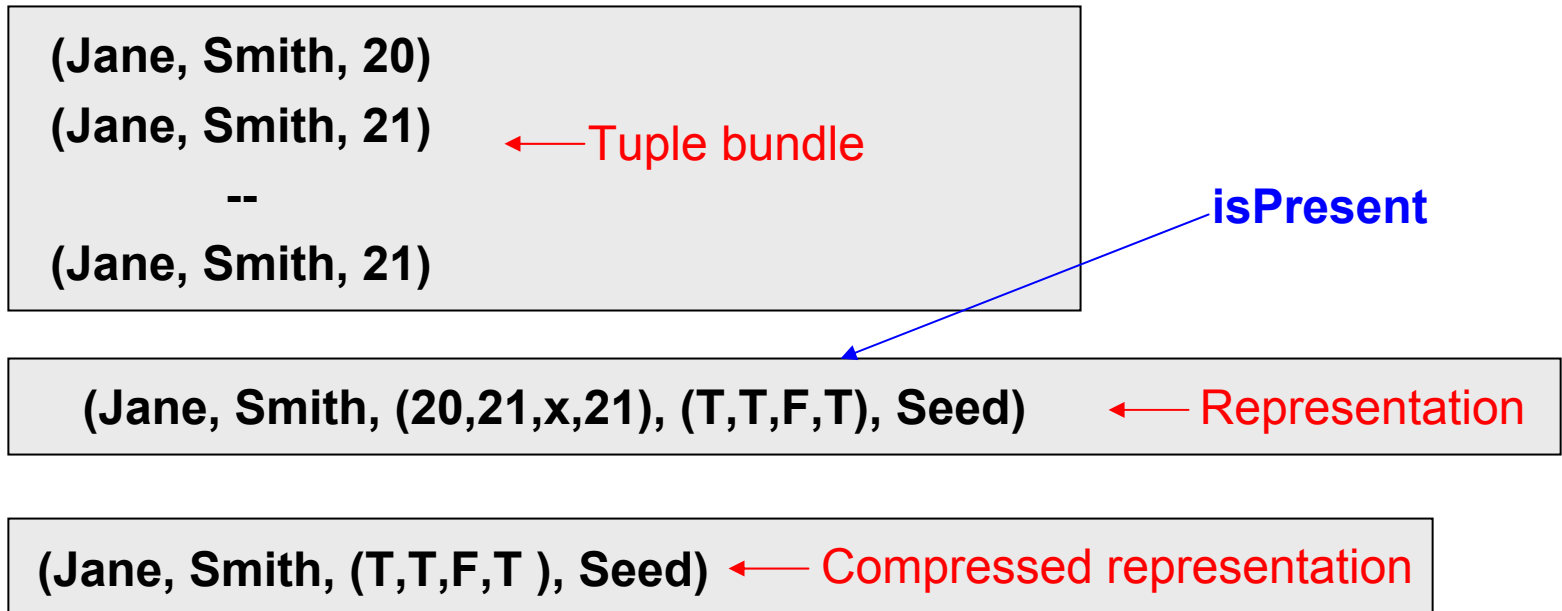
Schema Syntax: Example

```
CREATE TABLE RAND_CUST (CID, GENDER, MONEY, LIVES_IN) AS
FOR EACH d in CUST
WITH MONEY AS Gamma(
  (SELECT n.SHAPE FROM MONEY_SHAPE n WHERE n.CID = d.CID),
  (SELECT sc.SCALE FROM MONEY_SCALE sc WHERE sc.REGION =
    d.REGION),
  (SELECT SHIFT FROM MONEY_SHIFT)
)
WITH LIVES_IN AS DiscreteChoice (
  (SELECT c.NAME, c.PROB
   FROM CITIES c
   WHERE c.REGION = d.REGION)
)
SELECT d.CID, d.GENDER, m.VALUE, I.VALUE
FROM MONEY m, LIVES_IN I
```

Query Processing

- Naïve approach
 - Repeatedly instantiate DB and run query
 - Has **horrible** performance
- MCDB approach
 - Execute query plan **once**
 - Process **tuple bundles** instead of tuples
 - Represents tuple in all simulated possible worlds (MC reps)
 - Keep bundles in **compressed** form whenever possible
 - Use pseudorandom **seeds** for compression
 - Apply selections early to compressed bundles

Tuple Bundles (4 MC Repetitions)



Operations on Tuple Bundles

- **Seed:**

(Jane, Smith, --, --) \Rightarrow
(Jane, Smith, --, --, Seed)

- **Split:**

(Jane, Smith, (20,21,20,21), (T,T,T,T), Seed) \Rightarrow
(Jane, Smith, 20, (T,F,T,F), Seed),
(Jane, Smith, 21, (F,T,F,T), Seed)

- **Inference:**

(Jane, Smith, (20,21,20,21), (T,T,T,T), Seed) \Rightarrow
(Jane, Smith, 20, 0.5),
(Jane, Smith, 21, 0.5)

Also: Aggregate

Standard Operations

- **Select** (FNAME = 'Jane' AND AGE = 20)

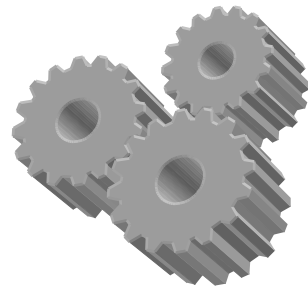
(Jane, Smith, (20,21,20,21), (F,T,T,T), Seed)
(John, Jones, (32,31,20,30), (T,T,F,T), Seed)
(Jane, Jones, (21,23,22,22), (T,T,T,T), Seed) ⇒
(Jane, Smith, (20,21,20,21), (F,F,T,F), Seed)

- **Join** (equijoin on Department #)

(Smith, (D1,D2,D2,D1), (F,T,T,T), Seed1)
(Jones, (D1,D2,D2,D2), (T,T,F,T), Seed2) ⇒
(Smith, D2, Jones, D2, (F,T,F,F), Seed1, Seed2)

Uses SPLIT
+
sort-merge

Estimation and Inference



MCDB inference operator

Distinct tuple values

TotSales	Frac
20K	0.324
...	...

Frac. replications where value appears (vs bit vector)

OutputTable

```
WITH Stats(Mu, Var) AS (  
  SELECT SUM(Val1*Frac),  
         SUM(Val*Val1*Frac)  
         - SUM(Val1*Frac)*SUM(Val1*Frac)  
  FROM OutputTable)  
SELECT Mu AS Mean, SQRT(Var) AS Stdev,  
       1.96*SQRT(Var)/SQRT(1000) AS CIHW  
FROM Stats
```

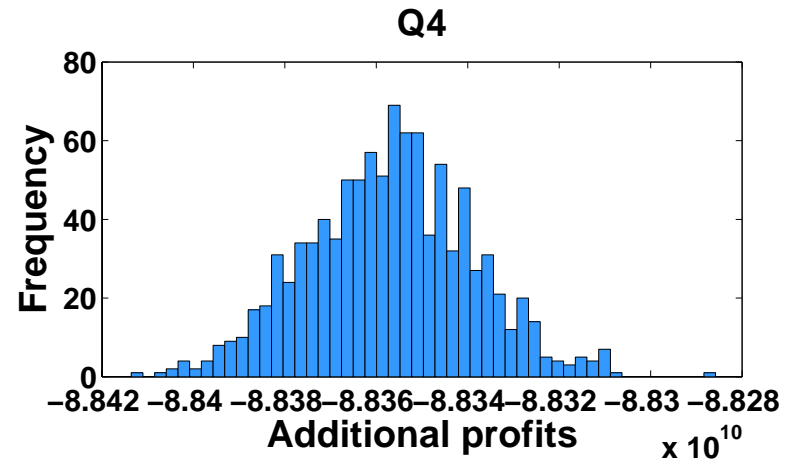
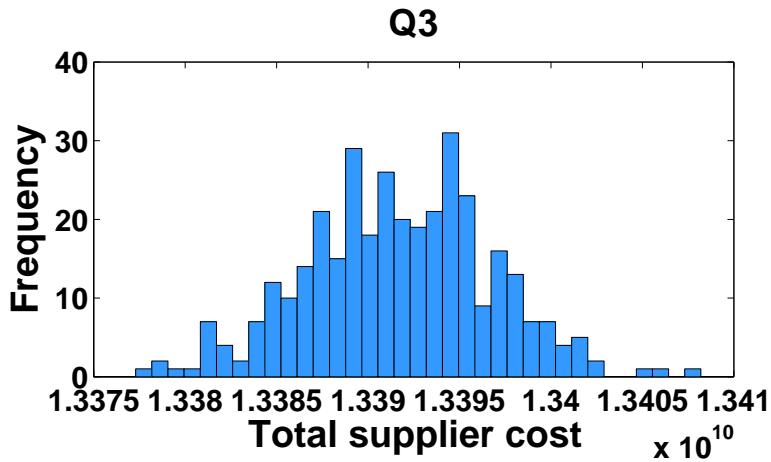
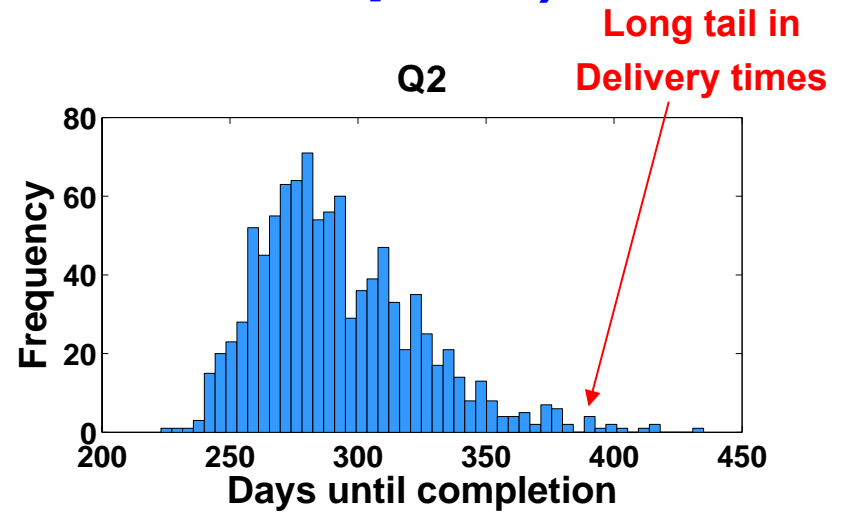
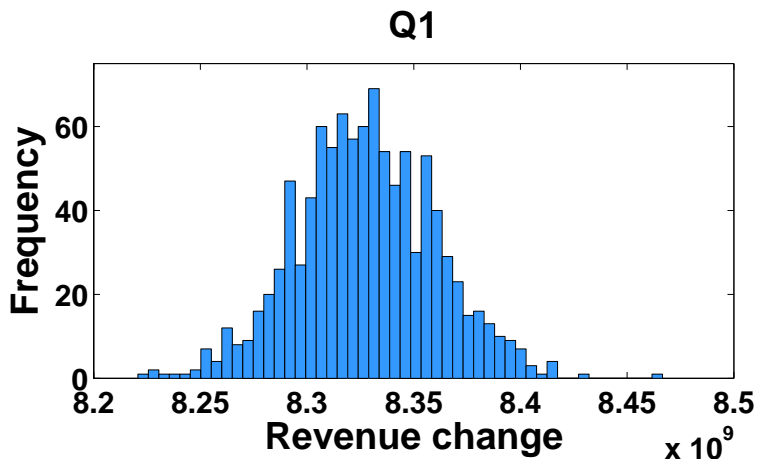
SQL queries

```
WITH CumDistFn(TotSales, Cum, PrevCum) AS (  
  SELECT TotSales,  
         SUM(Frac) OVER (ORDER BY TotSales  
                        ROWS BETWEEN UNBOUNDED PRECEDING  
                        AND CURRENT ROW),  
         SUM(Frac) OVER (ORDER BY TotSales  
                        ROWS BETWEEN UNBOUNDED PRECEDING  
                        AND 1 PRECEDING)  
  FROM OutputTable)  
SELECT Val FROM CumDistFn  
WHERE Cum >= 0.5 AND PrevCum < 0.5
```

Experimental Queries

- Q1: Next year's revenue gain from Japanese products
 - Assuming current trends hold
 - Each order duplicated Poisson # of times
 - Poisson mean = (this year)/(last year) for customer
- Q2: Order Delays
 - From placement to delivery
 - Fitted Gamma distribution for each delay type (for each part)
- Q3: What if we had used cheapest supplier?
 - TPC-H only has **current** prices
 - Prior prices generated by backwards random walk with drift
- Q4: Change in profits with 5% price increase
 - Bayesian model of customer demand
 - Based on **all** customers orders at current price

Results 1 (1000 Reps*)



*Q3 histogram based on 350 reps

Results 2: Execution Times (Min)

Query	1 rep	10 reps	100 reps	1000 reps
Q1	25	25	25	28
Q2	36	35	36	36
Q3	37	42	87	222*
Q4	42	45	60	214

vs 25000,
36000

*Based on 350 reps

- Much faster than naïve method in all cases

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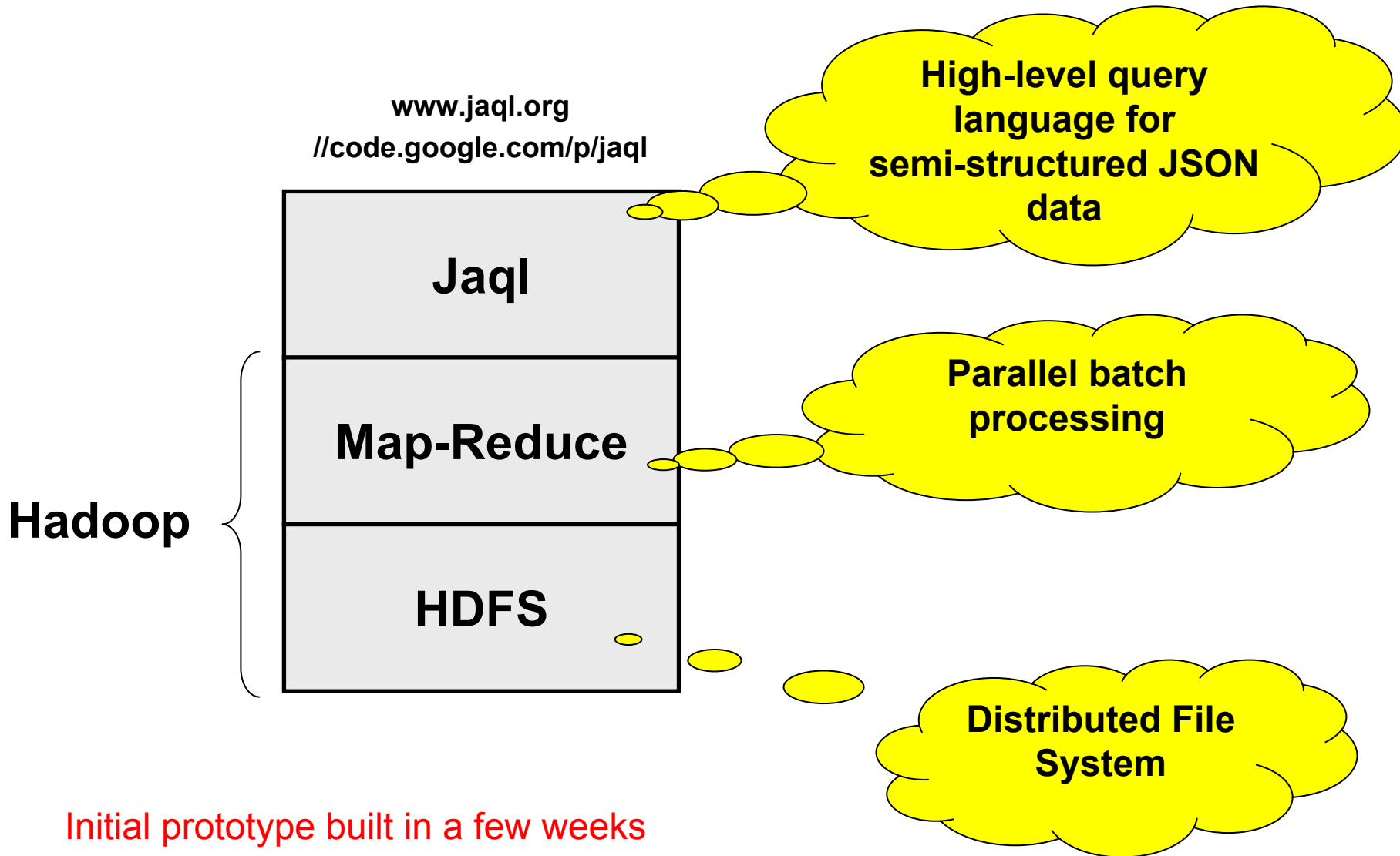
Motivation

- **Exploit massive parallelism of MCDB computations**
 - Extend domain of applicability
- **Faster path to market?**
 - Forward-looking architecture
- **Handle semi-structured, nested data**
 - E.g., web-click example: Petabytes of log file data
- **Local expertise/interest in map-reduce**
 - Learning experience for interesting analytical problem
 - MCDB computations often CPU-intensive
 - Ease of prototyping

Technical Issues

- How to represent bundles?
- How to specify map-reduce jobs?
- How to parallelize?
- How to seed tuple bundles?

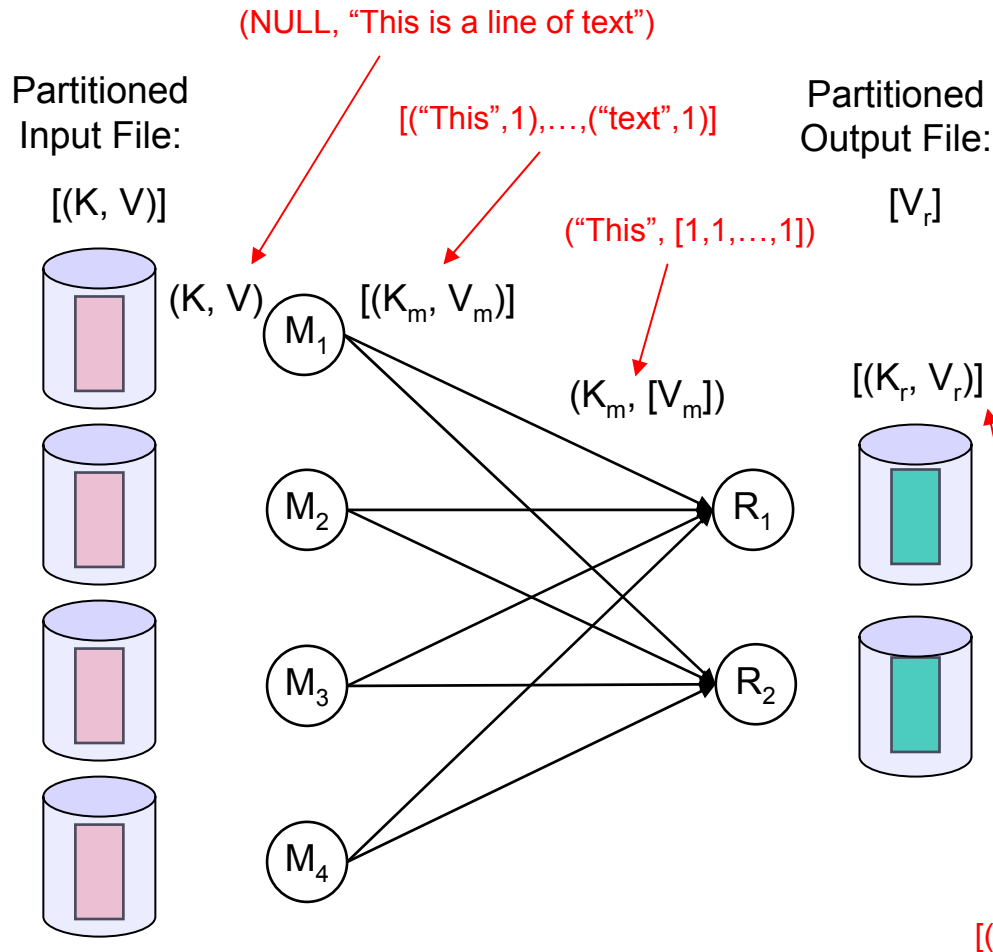
A Cluster-Computing Infrastructure



Initial prototype built in a few weeks

Map-Reduce Overview

Ex: parallel word counting

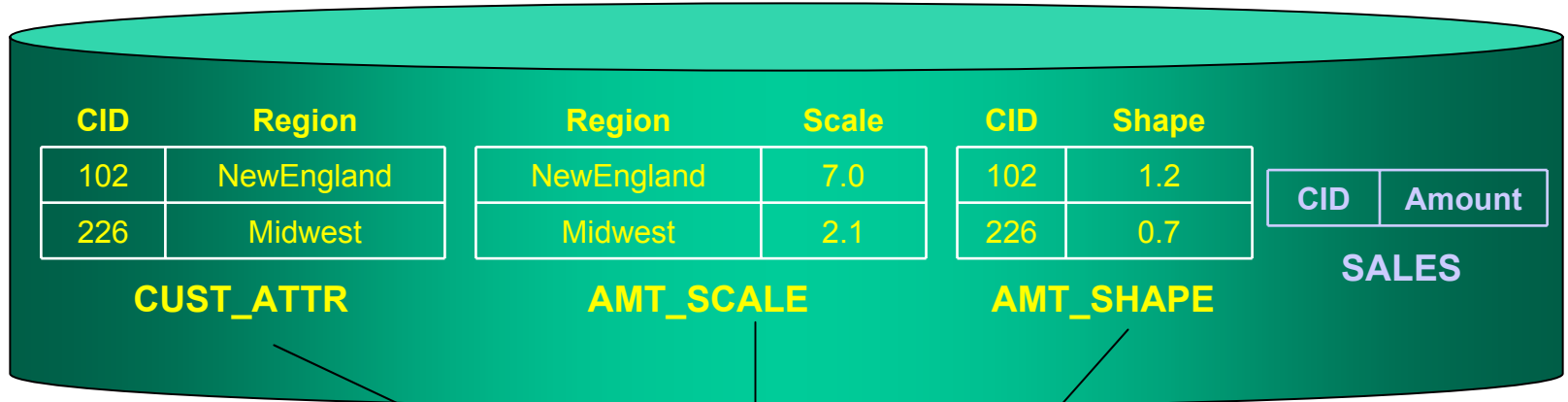


- Programmer focus:
 - Map: $(K, V) \rightarrow [(K_m, V_m)]$
 - Reduce: $(K_m, [V_m]) \rightarrow [(K_r, V_r)]$

- System provides:
 - Parallelism
 - Sorting
 - Synchronization
 - Fault tolerance
 - Resource allocation

On commodity hardware

MCDB Example



Q: SELECT SUM(Amount)
FROM SALES
AS t_sales

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102	1.2	7.0
226	0.7	2.1

Gamma(shape, scale)

VG function

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$Q(d_1) = \$180$

d_2

CID	Amount
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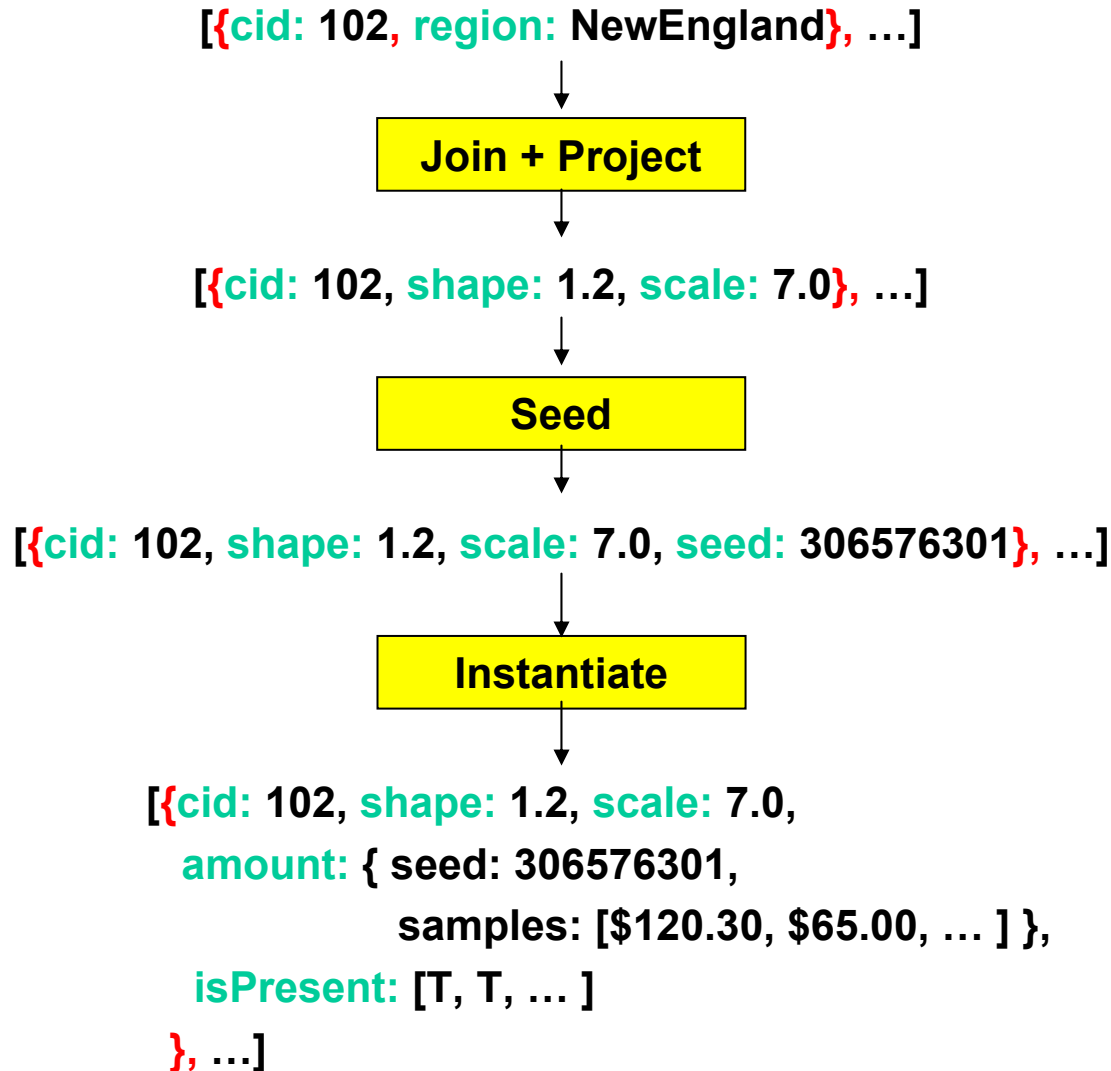
d_3

CID	Amount
102	\$80.00
226	\$130.00

$Q(d_3) = \$210$

$\hat{E}[t_sales] = \$186.67$ $S\hat{T}D[t_sales] = \$20.82$

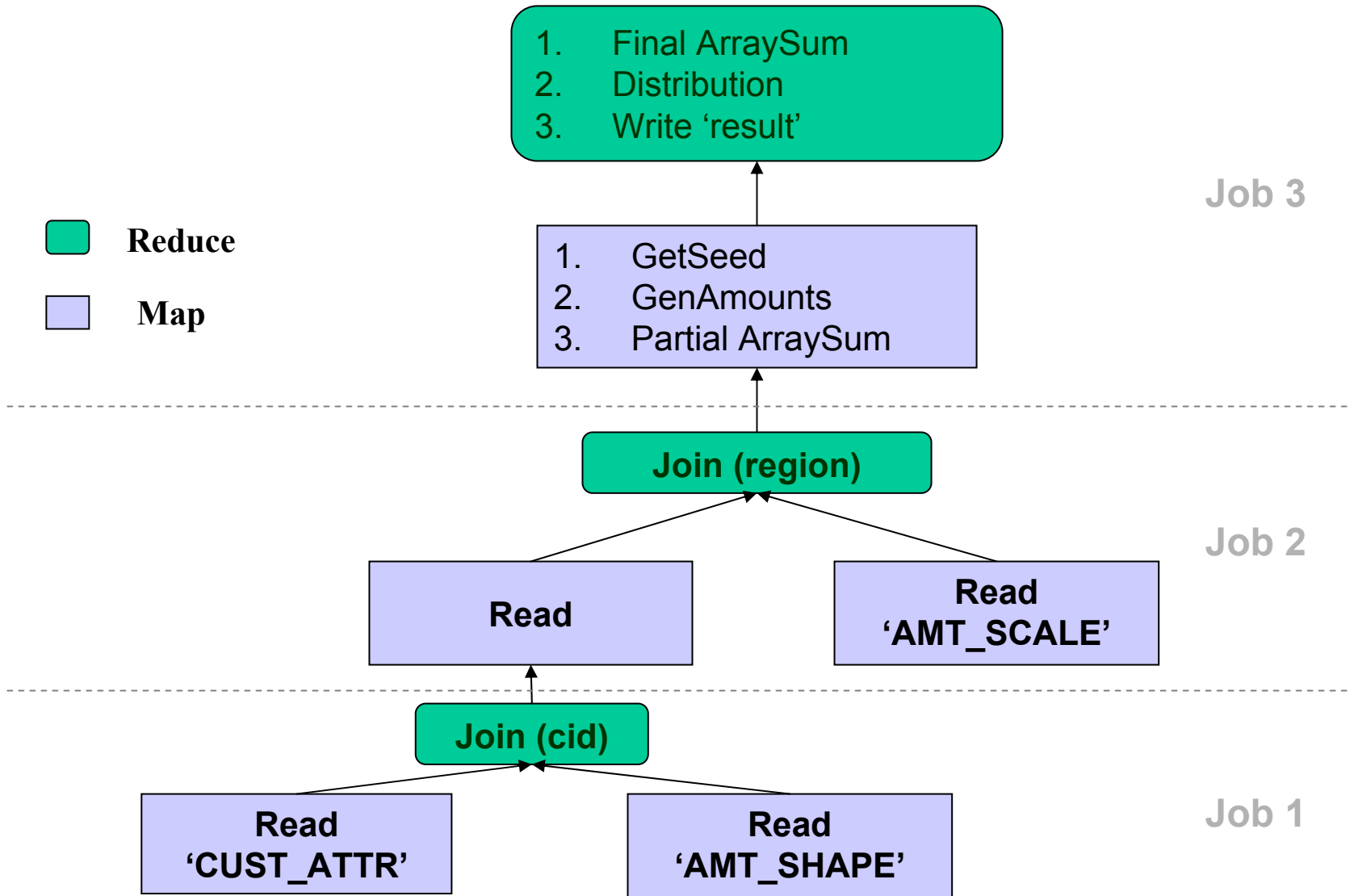
JSON and MC³



JAQL and MC³: Example

```
1 $cust = READ(hdfs('cust_attr'));
   $shape = READ(hdfs('amt_shape'));
   $scale = READ(hdfs('amt_scale'));
2 JOIN $shape, $cust, $scale
   WHERE $shape.cid == $cust.cid
       AND $cust.region == $scale.region
   INTO {$shape, $scale}
   //Seed
3 → TRANSFORM { $.*, seed: GetSeed() }
   //Instantiate: generate array of 1000 samples
4 → TRANSFORM GenAmounts($.seed, $.shape, $.scale, 1000)
   // Sum all sales tuple bundles
6 → GROUP INTO ArraySum($)
   // Compute the distribution
7 → TRANSFORM Distribution($)
8 → WRITE(hdfs('result'));
```

Example of a Query Plan



Parallelism Schemes

- **Inter-tuple parallelism**

- Partition tuple bundles among nodes
- Natural fit with Map-Reduce
- Good when many bundles or cheap VG functions

Tuple 1: (r1,...,r1000)

Tuple 2: (r1,...,r1000)

⋮

- **Intra-tuple parallelism**

- Split up tuple bundles
 - Break Monte Carlo replications into chunks
- Apply inter-tuple parallelism methods to chunks
- Good when few tuples with
 - Expensive VG functions and/or
 - Many MC replications

Tuple 1: (r1,...,r500)

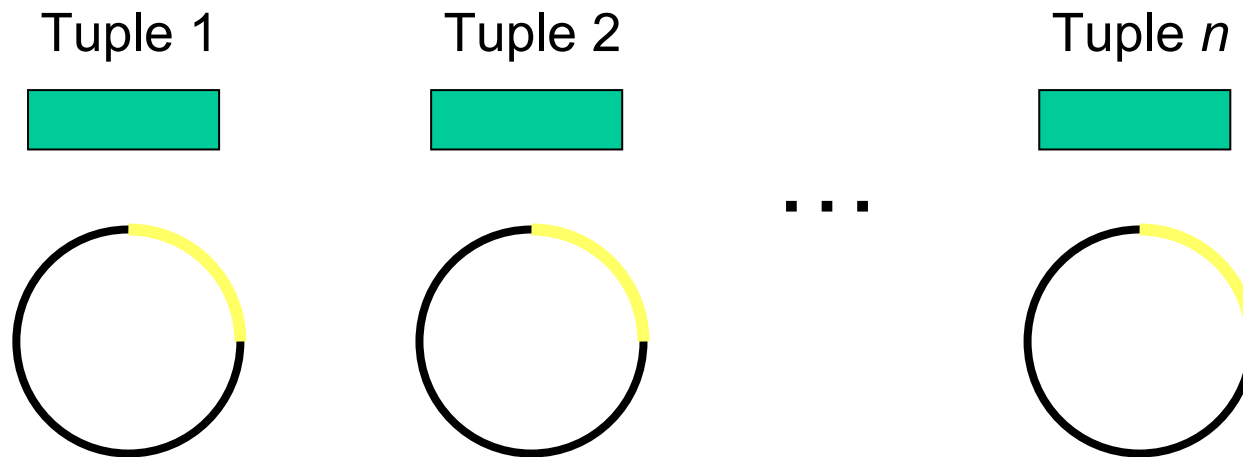
Tuple 1: (r501,...,r1000)

Tuple 2: (r1,...,r500)

Tuple 2: (r501,...,r1000)

⋮

Distributed Seeding



- Must avoid overlapping seed sequences
- Maximize parallelization (tuples on different processors)
- Minimize seed size stored in each tuple

Skip-Ahead Method

- Well512a generator: period = 2^{512}
- Assume inter-tuple parallelism (for simplicity)
- Assume that we know (or have good upper bound for)
 - # of bundles seeded per node (= b)
 - # of seeds per VG function call (= c)
 - # MC reps (= n)

Seeding

Tuple j at node i :

{cid: 102, shape: 1.2, scale: 7.0}



{cid: 102, shape: 1.2, scale: 7.0, seed: [i, j]}

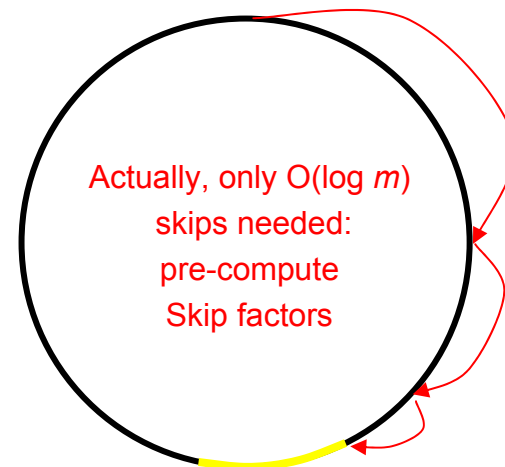
Instantiation

Tuple j at node i : Make

$$m = b \times i + j$$

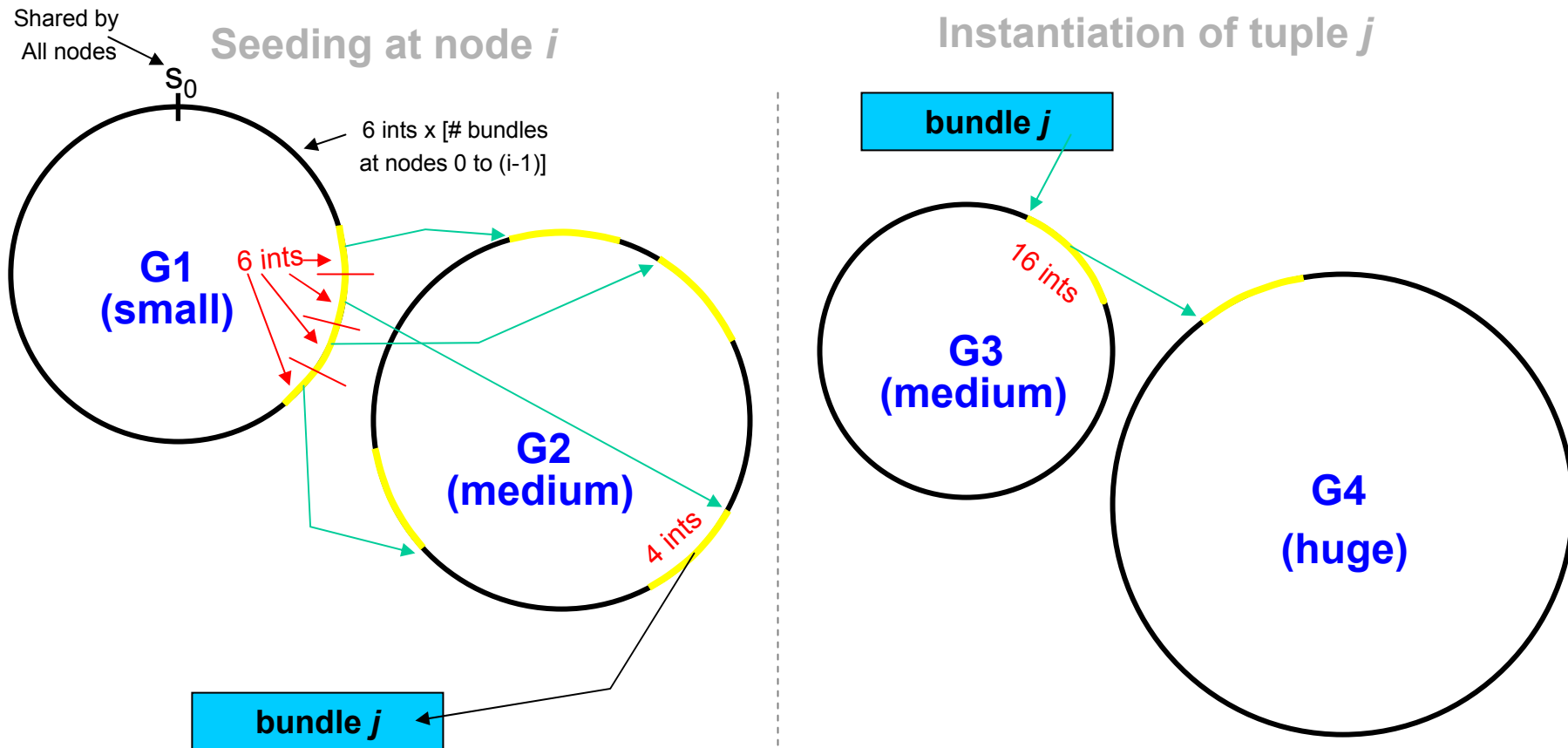
skips of length $c \times n$

to get to starting point



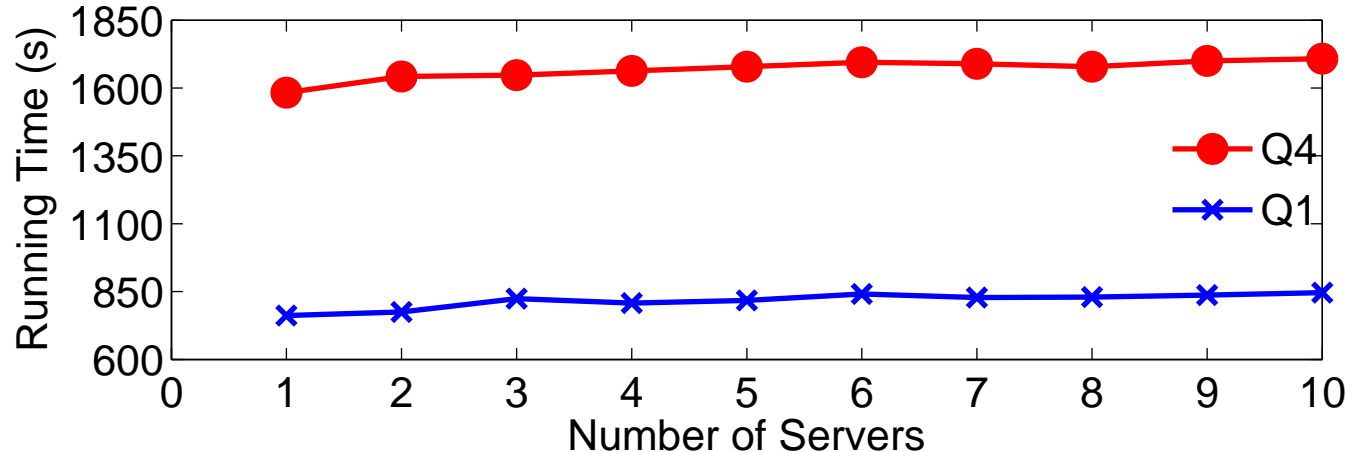
Multi-PRNG Method

- When # of seeds per VG function call is unknown
- When skip-ahead for huge PRNG is hard to implement
- Collisions possible, but probability $< 10^{-17}$



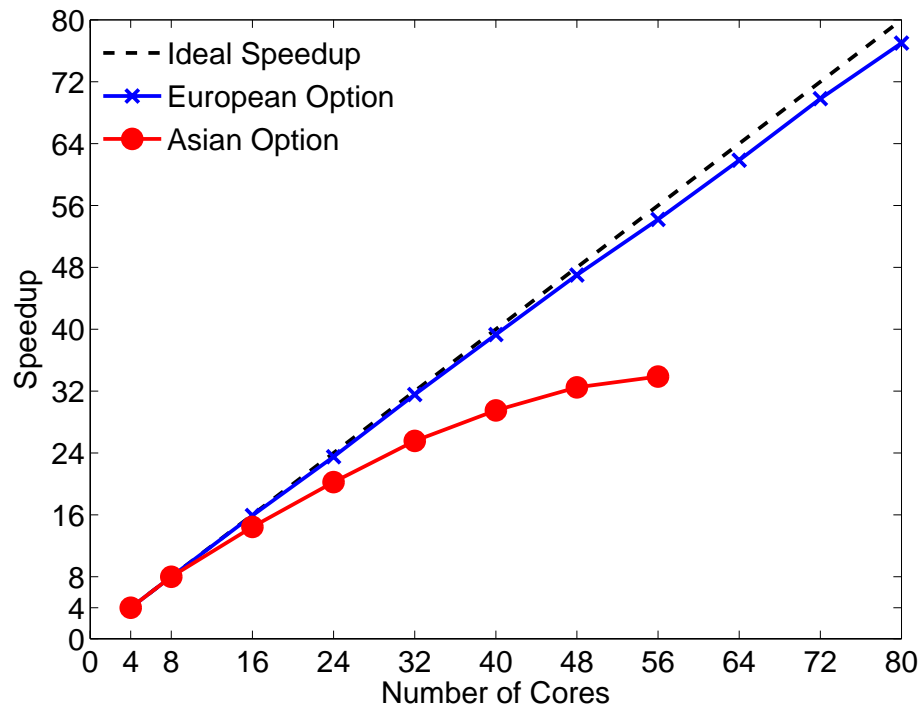
Scale-up Results: Inter-Tuple Parallelism

- Implemented two nontrivial queries from MCDB paper
 - Jaql: Map-Reduce plan = original MCDB plan
 - Good scalability with inter-tuple parallelism



Speed-up Results: Intra-Tuple Parallelism

- Implemented two call-option queries (Euro and Asian)
 - Euro option: expensive VG function, good speed-up
 - Asian option: cheap VG function, speed-up curve flattens
 - Sequential merging of chunks starts to dominate
 - Moral: choose appropriate parallelization scheme



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Related Projects

- **RAQA: Resolution-aware query answering for Business Intelligence** [Sismanis et al., ICDE09]

- Uncertainty due to entity resolution
- OLAP querying (roll-up, drill-down)
- **Bounds** on query answers
- Implemented via SQL queries
- Conservative approach

City	State	Strict range	Status
San Francisco	CA	[\$30,\$230]	guaranteed
San Jose	CA	[\$70,\$200]	non-guaranteed

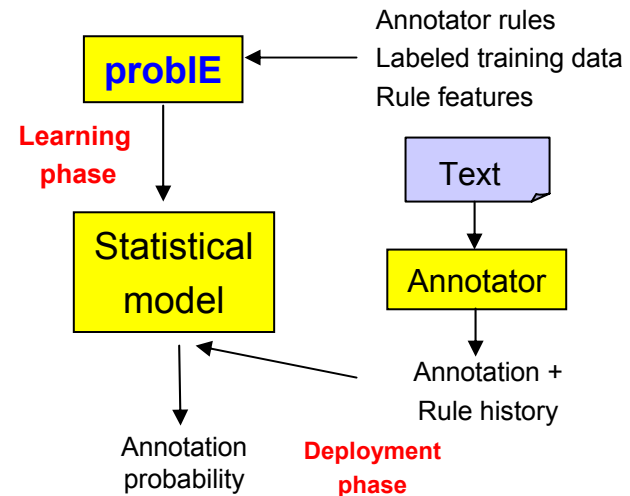
Sum(Sales) group by City,State

State	Strict range	Status
CA	[\$230,\$230]	guaranteed

Sum(Sales) group by State

- **ProBE: Probabilistic info extraction** [Michelakis et al., SIGMOD09]

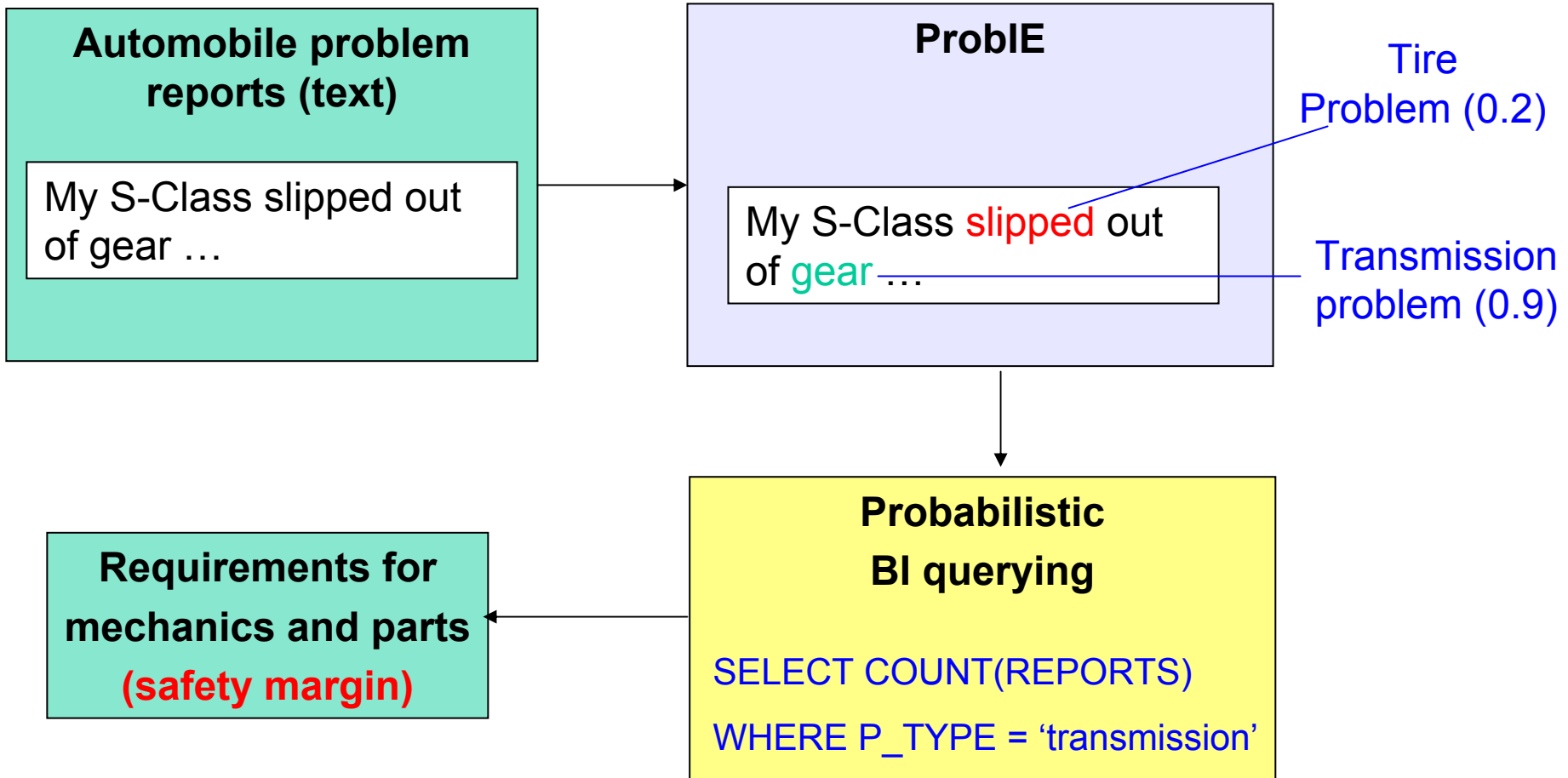
- For rule-based IE system (e.g., SystemT)
- Provides confidence #'s for base/derived annotations
- Based on “rule history”, lower-level results
- MaxEnt-based learning approach



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An End-to-End ERP Scenario



Future Directions

- Performance
 - Query optimizer
 - E.g., push down inference & instantiation, choose parallelization scheme
 - Improve JAQL rewriter (MC³ aware)?
 - Sequential and/or adaptive simulation? (MC³)
 - Combine with exact methods? Sampling?
 - Other architectures?
- Functionality
 - Correlated tables
 - Specification and provision of desired precision
 - General uncertainty model for semi- and unstructured data
- Extreme-quantile estimation (value-at-risk)
 - Black-box methods

Further Details:

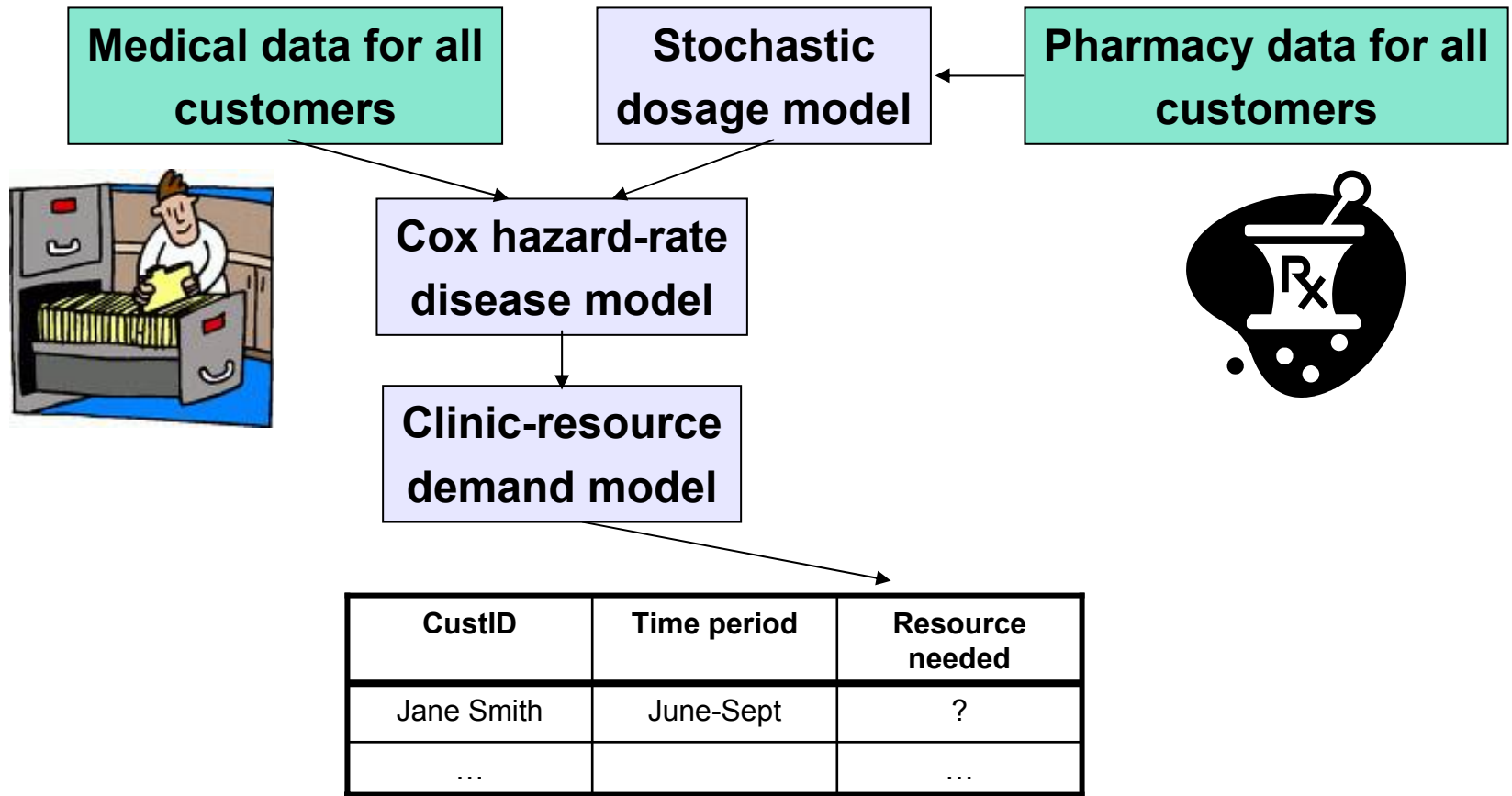
- MCDB: SIGMOD 2008
- RAQA: ICDE 2009
- MC³: SIGMOD 2009
- ProIE: SIGMOD 2009

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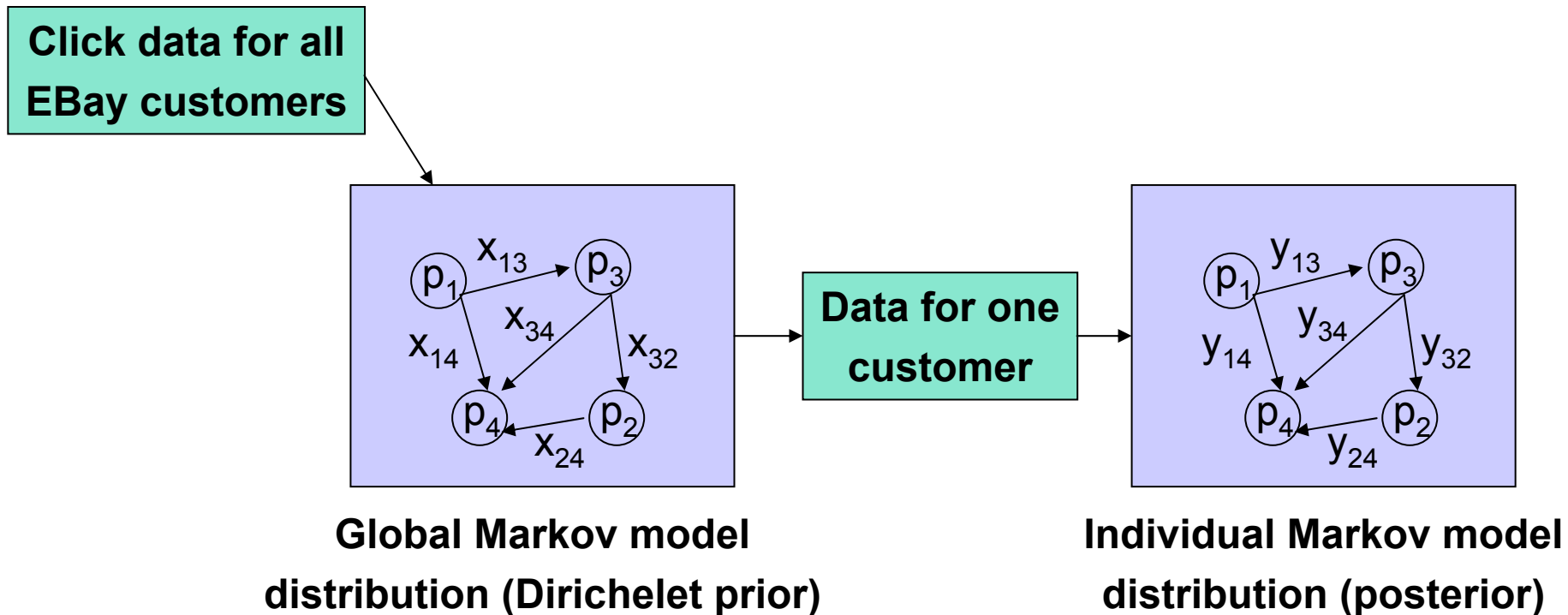
Thank You!

Backup Slides

Clinic-Capacity Risk



Individual Click Behavior (EBay)



- Can analyze arbitrary dynamic customer segments when determining effect of changing EBay pages

Logistics Under Uncertainty

- Retailer: ship from warehouses to outlets today or tomorrow?
- Deterministic tables

ITEM_ID	QUANTITY
curtains	50
...	...

ITEM_ID	QUANTITY
curtains	20
...	...

ITEM_ID	Price
curtains	\$120
...	...

- Random tables

CUST_ID	ITEM_ID	QUANTITY
Smith	curtains	?
...

CUST_ID	ITEM_ID	QUANTITY
Smith	curtains	?
...

- Queries:

```
SELECT SUM (c.price * s.quantity)
FROM SALES_W_SHIP s,
CUR_PRICE c
WHERE c.ITEM_ID = s.ITEM_ID
```

```
SELECT SUM (c.price * s.quantity)
FROM SALES_WO_SHIP s,
CUR_PRICE c
WHERE c.ITEM_ID = s.ITEM_ID
```

- Issues:
 - Complicated statistical models for purchase quantity (how to integrate in DB?)
 - Uncertainty (random tables) depend **dynamically** on **huge** number of parameters

VG Function Implementation

- C++ class with four public methods
 - **Initialize**: set up data structures, seed RNG
 - **TakeParams**: read in “parameter vector”
 - **OutputVals**: return random value(s) for possible world
 - Return NULL when done
 - **Finalize**: clean up

```
If newRep:  
    newRep = false  
    uniform = myRandGen()  
    probSum = i = 0  
    while (uniform >= probSum)  
        i++  
        probSum += L[i].wt / totWeight  
    return L[i].val  
Else  
    newRep = true  
    return NULL
```

**OutputVals method
For DiscreteChoice()**

Schema Syntax: Example 1

- Goal: generate random customer table
 - MONEY, LIVES_IN are uncertain attributes
 - MONEY has Gamma dist'n
 - shift, shape, scale parameters
 - Use DiscreteChoice for LIVES_IN value
 - Customers are mutually independent, given region
- Parameter table schemas
 - CUST (CID, GENDER, REGION)
 - CITIES (NAME, REGION, PROB)
 - Probabilities sum to 1 in each region
 - MONEY_SHIFT (SHIFT) ← 1 row, 1 column
 - MONEY_SCALE (REGION, SCALE)
 - MONEY_SHAPE (CID, SHAPE)

Normalized
storage

Schema Syntax: Example 2

- Suppose MONEY and LIVES_IN are correlated

```
CREATE TABLE RAND_CUST (CID, GENDER, MONEY, LIVES_IN) AS
FOR EACH d in CUST
WITH MLI AS MyJointDistribution(...)
SELECT d.CID, d.GENDER, MLI.V1, MLI.V2
FROM MLI
```

MLI has 1 row, 2 columns

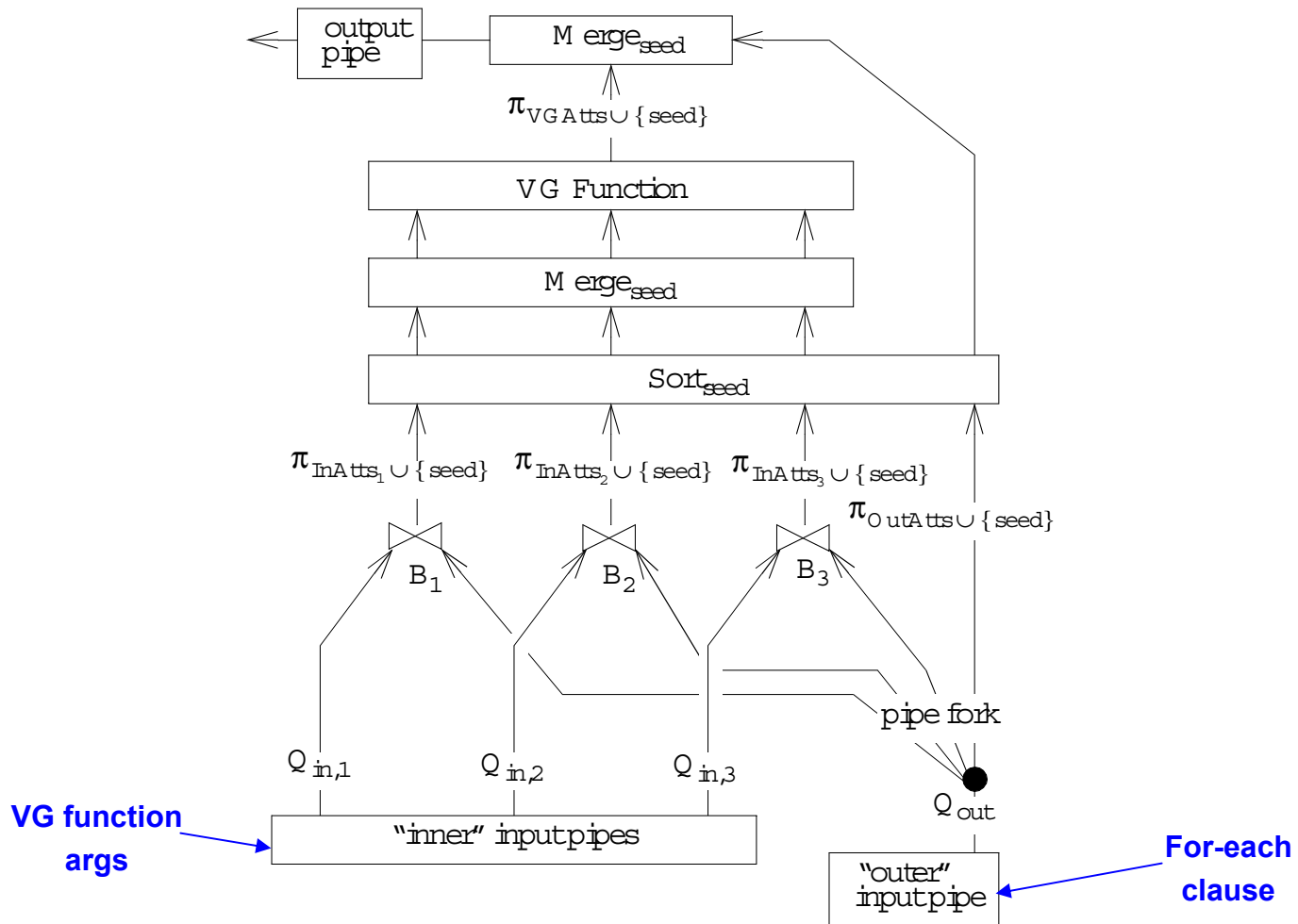


Schema Syntax: Example 3

- Correlated sensors
 - Sensors in same “sensor group” are correlated (multivariate normal)
- Parameter table schemas
 - S_PARAMS (ID, LAT, LONG, GID)
 - MEANS (ID, MEAN)
 - COVARS (ID1, ID2, COV)

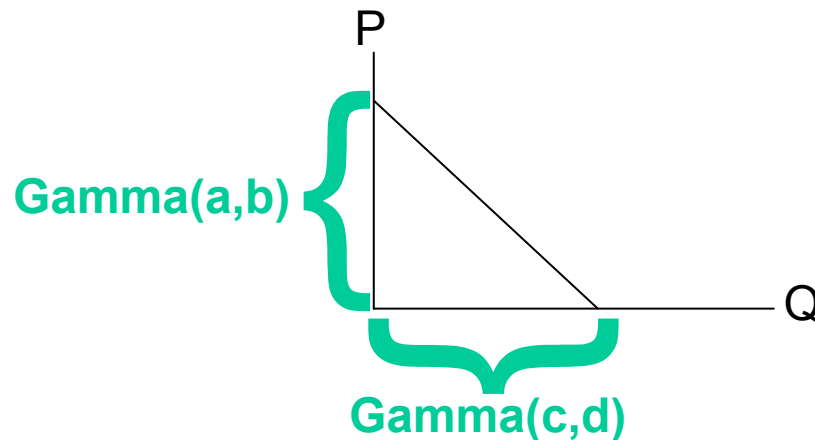
```
CREATE TABLE SENSORS (ID, LAT, LONG, TEMP) AS
FOR EACH g in (SELECT DISTINCT GID FROM S_PARAMS)
WITH TEMP AS MDNormal (
  (SELECT m.ID, m.MEAN FROM MEANS m S_PARAMS ss
   WHERE m.ID = ss.ID AND ss.GID = g.GID),
  (SELECT c.ID1, c.ID2, c.COV FROM COVARS c, S_PARAMS ss
   WHERE c.ID1 = ss.ID AND ss.GID = g.GID)
)
SELECT s.ID, s.LAT, s.LONG, t.VALUE
FROM S_PARAMS s, TEMP t
WHERE s.ID = t.ID
```

Instantiate Operation



Q4 Details

- Effect on profits of 5% price increase
 - Want more accuracy than usual aggregated demand functions
 - E.g, exploit detailed point-of-sale data
 - For each part
 - Fit “prior” demand-function distribution to all customers (MLE)
 - Determine “posterior” distribution for each cust. (Bayes Thm)
 - Generate random demand for each customer at new price
 - Use rejection algorithm to sample from posterior



Nested-Data Experiments

- TPC-H schema is used
- Two different ways to nest data
 - Nest *lineitem* table under *orders* table
 - Nest *lineitem* table under *partsupp* table
- Modified version of Q4 from MCDB paper
 - Compare MC³ execution time to flat scheme
 - First nesting scheme: running time is slower
 - Second nesting scheme: running time is faster
- Only uncertain “leaf attributes” are supported

Probabilistic Information Extraction in a Rule-Based System

Motivation: System T

Hand-crafted rules for specific domain:

Annotator	Candidate-Generation Rules	Rule Precision
Person Base annotator	P1: <Salutation><CapitalizedWord><CapitalizedWord> P2: <First Name Dictionary><Last Name Dictionary> P3: <CapitalizedWord><CapitalizedWord>	High High Low
PhoneNumber Base annotator	Ph1: <PhoneClue><\d{3}-\d{3}-\d{4}> Ph2: <\d{3}-\d{3}-\d{4}> Ph3: <\d{5}>	High Medium Low
PersonPhone Derived annotator	PP1: <Person><“can be reached at”><PhoneNumber> PP2: <“call”><Person><0-2 tokens><PhoneNumber> PP3: [<Person><PhoneNumber>] _{sentence}	High High Medium

+ Consolidation rule

Consolidate(“Joe Smith”, “Mr. Joe Smith”) = “Mr. Joe Smith”

Annotations

Document d_1

...Greg Mann can be reached
at 403-663-2817 in my absence ...

Annotator	Annotation	Rules
Person	Greg Mann	P2, P3
PhoneNumber	408-663-2817	Ph2
PersonPhone	(Greg Mann, 408-663-2817)	PP1

Document d_2

... please call Heather
Choate at x33278 ...

Annotator	Annotation	Rules
Person	Heather Choate	P2, P3
PhoneNumber	33278	Ph3
PersonPhone	(Heather Choate, 33278)	PP2

**Goal: Attach probabilities to annotations
in a principled, scalable manner**

Quantifying this uncertainty is critical as

- Extracted facts can then be queried using probabilistic databases
- Confidence numbers can be used by information integration and search applications
- It helps in improving the recall of annotators!!

Our approach

- Propose a probabilistic framework for handling uncertainty in rule-based IE
 - Each annotation is associated with a confidence
 - the probability that the annotation is correct
 - Probability is obtained by augmenting each annotator with a statistical model
- Design considerations
 - Applicable to grammar and declarative rule-based IE systems
 - Scale to annotators with a large number of (correlated) rules
 - Support incremental improvements in accuracy of probability estimates
 - as rules, data, or constraints are added

Rule Histories and Features

- Rule history

P1: <Salutation><CapitalizedWord><CapitalizedWord>
P2: <First Name Dictionary><Last Name Dictionary>
P3: <CapitalizedWord><CapitalizedWord>

Please call Heather Choate at



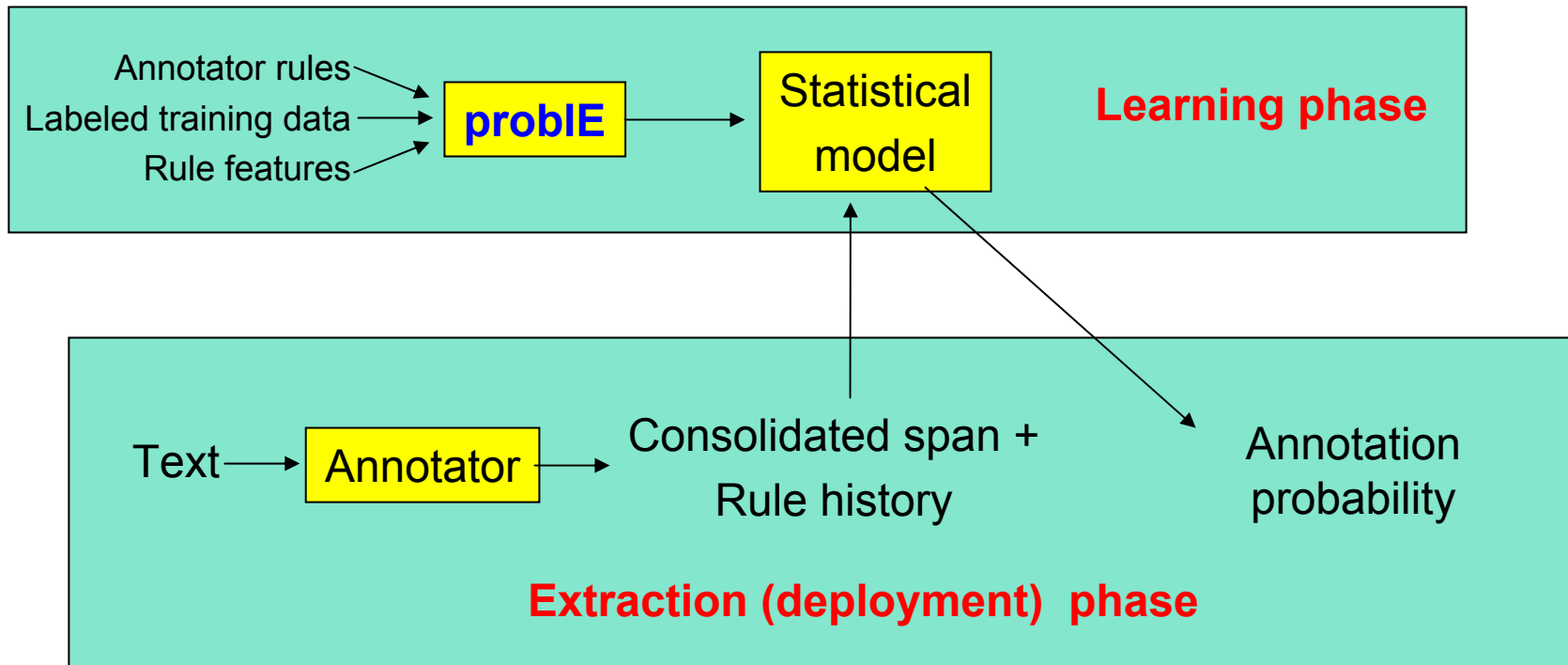
P1	P2	P3
0	1	1

Rule history

- Rule features

- Qualitative correlations and anti-correlations
- Ex: “Rules P1 and P2 tend to occur together”

Proble Framework (Base Annotator)



Probability Model of Uncertainty

- Binary random variables associated with text and annotator
 - $A(s) = 1$ iff span s is actually a Person
 - $K(s) = 1$ iff span s is annotated as a Person by consolidator
 - $R(s) = (R_1(s), R_2(s), \dots, R_k(s))$ is stochastic rule history on span s
 - $R_i(s) = 1$ iff i th rule holds at least once on span s

- Annotation probability:

$$q(r) = P(A(s) = 1 \mid R(s) = r, K(s) = 1)$$

- Indirect approach (estimate a prob dist'n rather than many small probs)
 - Estimate

$$p_0(r) = P(R(s) = r \mid A(s) = 0, K(s) = 1)$$

$$p_1(r) = P(R(s) = r \mid A(s) = 1, K(s) = 1)$$

\Rightarrow

$$q(r) = \frac{\pi p_1(r)}{\pi p_1(r) + (1 - \pi) p_0(r)}$$

$$\pi = P(A(s) = 1 \mid K(s) = 1)$$

- π is easy to estimate empirically
- Serious data-sparsity problem for p_0 and p_1 : 2^k possible histories, little training data
- Solution: Fit a parametric model

A Parametric Model

- Parametric exponential model for p_1 (model for p_0 is similar):
 - Recall: $p_1(r) = P(R(s) = r \mid A(s) = 1, K(s) = 1)$ with $R(s) = (R_1(s), \dots, R_k(s))$
 - From features to constraints

$$P(R_3(s) = 1 \mid A(s) = 1, K(s) = 1) = a_3 \quad (\text{one marginal constraint per rule})$$

$$P(R_2(s) = 1 \text{ and } R_7(s) = 1 \mid A(s) = 1, K(s) = 1) = a_{2,7} \quad (\text{important correlations})$$

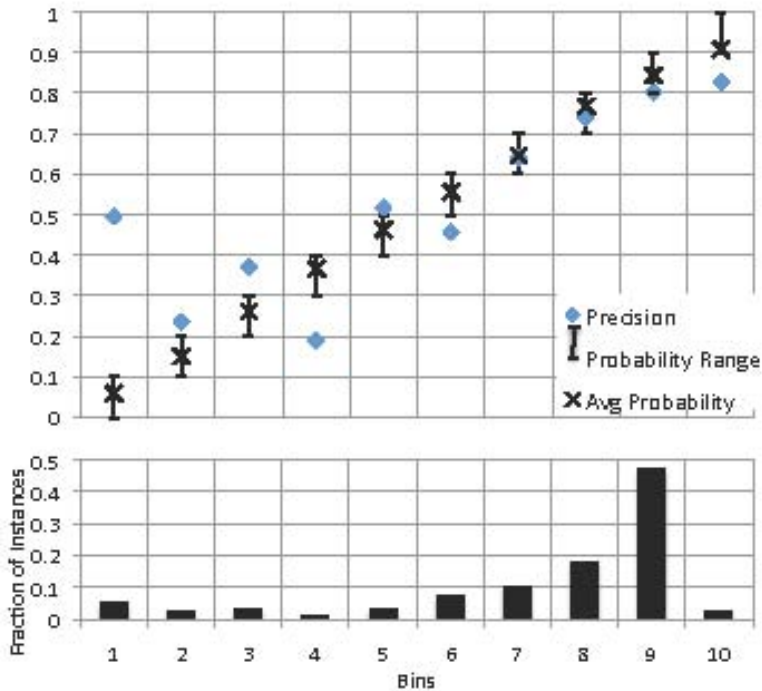
where constants a_3 , $a_{2,7}$, etc. computed from training data

- Approximate p_1 by “simplest” (**maximum entropy**) distribution satisfying constraints
- Equivalent to maximum-likelihood fit of parameter vector θ for exponential distribution

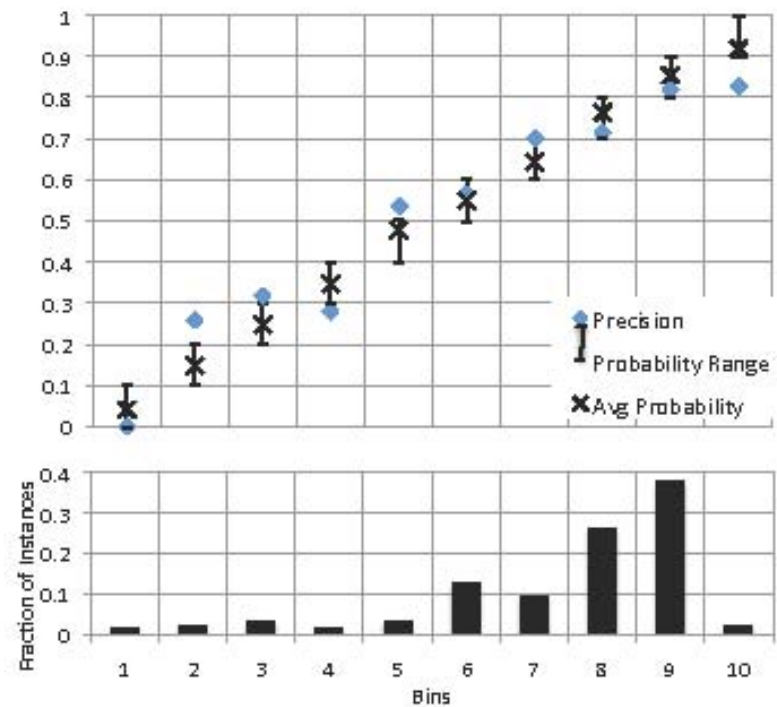
$$p_1(r; \theta) = \frac{1}{Z(\theta)} \exp \left\{ \sum_{c \in C} \theta_c f_c(r) \right\} \quad f_c = \text{Indicator function for constraint } c$$

- Use improved iterative scaling (IIS) to fit θ from training data
- Model-decomposition methods for IIS scalability to many rules and constraints
- Augment training data to handle constraints with 0 right-hand side
- Methodology extends to derived annotators such as PersonPhone

Some Experimental Results (Pay-As-You-Go)



**Person annotator
(No inter-rule constraints)**



**Person annotator
(4 inter-rule constraints)**