Abstract of "Building Query Optimizers with Combinators" by Mitch Cherniack, Ph.D., Brown University, May 1999.

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The goal of query rewriting is to transform queries into equivalent queries that are more amenable to plan generation. This process has proven to be error-prone. Rewrites over *nested queries* and queries returning duplicates have been especially problematic, as evidenced by the well-known COUNT bug of the unnesting rewrites of Kim. The advent of object-oriented and object-relational databases only exacerbates this issue by introducing more complex data and by implication, more complex queries and query rewrites.

This thesis addresses the correctness issue for query rewriting. We introduce a novel framework (COKO-KOLA) for expressing query rewrites that can be verified with an automated theorem prover. At its foundation lies KOLA: our *combinator-based* query algebra that permits expression of simple query rewrites (*rewrite rules*) without imperative code. While rewrite rules are easily verified, they lack the expressivity to capture many query rewrites used in practice. We address this issue in two ways:

- We introduce a language (COKO) to express complex query transformations using KOLA rule sets and an algorithm to control rule firing. COKO supports expression of query rewrites that are too *general* to be expressed with rewrite rules alone.
- We extend KOLA to permit expression of rewrite rules whose firing requires inferring *semantic conditions*. This extension permits expression of query rewrites that are too *specific* to be expressed with rewrite rules alone.

The recurring theme of this work is that all of the proposed techniques are made possible by a combinator-based representation of queries. Abstract of "Building Query Optimizers with Combinators" by Mitch Cherniack, Ph.D., Brown University, May 1999.

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The recurring theme of this work is that all of the proposed techniques are made possible by a combinator-based representation of queries.

#### Building Query Optimizers with Combinators

by Mitch Cherniack

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A dissertation submitted in partial fulfillment of the requirements for the Degree of Doctor of Philosophy in the Department of Computer Science at Brown University

> Providence, Rhode Island May 1999

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This dissertation by Mitch Cherniack is accepted in its present form by the Department of Computer Science as satisfying the dissertation requirement for the degree of Doctor of Philosophy.

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### Vita

Mitch Cherniack was born on August  $18^{th}$ , 1963 in Winnipeg, Canada. He completed secondary school in Denver, Colorado, and then attended McGill University in Montreal, Canada, where he received his Bachelor of Education degree (Elementary) in 1984, and a Diploma of Education degree (Secondary) in 1985. He taught in the far north of Canada for a time in 1984, and then taught high school Computer Science and Mathematics in Montreal from 1985–1989. He returned to school at Concordia University in Montreal in 1989, and subsequently earned a Diploma in Computer Science in 1990, and a Masters degree in Computer Science in 1992. He then joined the doctoral program at Brown University in the fall of 1992.

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### Credits

Some of these chapters are adapted from our papers. Chapter 3 is based on our 1996 SIGMOD paper [22] and our 1995 DBPL paper [23]. Chapter 4 is based on our 1998 SIGMOD paper [20]. Chapter 5 is based on our 1998 VLDB paper [21]. Chapter 6 is based on a recent conference submission [19]. Chapter 7 forms the basis of a paper currently in preparation. All of these papers were written jointly with Stan Zdonik. As well, [23] was written jointly with Marian H. Nodine and [19] was written jointly with Ashok Malhotra.

Joon Suk Lee and Kee-Eung Kim were primarily responsible for the implementation of the compiler described in Chapter 4. Joon Suk Lee implemented the semantic extensions described in Chapter 5. Blossom Sumulong is building the prototype implementation described in Chapter 7.

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### Chapter 1

# Introduction

Query optimizers produce plans to retrieve data specified by queries. Optimizers are inherently difficult to build because for any given query, there can be a prohibitively large space of candidate evaluation plans to consider. Further, the difficulty of formulating estimates of plan costs makes the comparisons of plans within this space difficult. As a result, optimizers invariably forego searches for "best plans" and instead are considered effective if they usually produce good plans and rarely produce poor ones.

Query optimizers are perhaps the most complex and error-prone components of databases. In describing software testing methodology developed at Microsoft, Bill Gates reported that hundreds of randomly generated queries were processed incorrectly by Microsoft's SQL Server [41]. The problem is not unique to Microsoft. Even research *literature* for query optimization has been susceptible to bugs, as in the notorious "COUNT bug" revealed of the optimization strategies proposed by Kim [63].

Software engineering has introduced formal methods for the development of correct software. This thesis applies software engineering methodology to the development of one error-prone component of query optimizers: the *query rewriter* [79].

#### **1.1** Preliminaries

We begin by defining terms that appear throughout this thesis: query optimization, query rewriting and rule-based query optimization and query rewriting.



Figure 1.1: A Traditional Architecture for Query Processors

#### 1.1.1 Query Optimization

Query optimizers typically follow an "assembly line" approach to processing queries, as illustrated in Figure 1.1:

- Translation first maps a query posed in a standard query language such as SQL (for relational databases) or OQL [14] (for object-oriented databases), into an *internal representation* (or *algebra*) manipulated by the optimizer. Example internal representations include the Query Graph Model (or QGM) which is used in Starburst [79] and DB2, and Excess which is used in Exodus [13].
- 2. Query Rewriting uses heuristics to rewrite queries (more accurately, query representations) into equivalent queries that are more amenable to plan generation.<sup>1</sup>
- 3. *Plan Generation* generates alternative execution plans that retrieve the data specified by the represented query, estimates the execution costs of each and then chooses the one it considers "best".
- 4. *Plan Evaluation* can immediately follow plan generation (in the case of *ad hoc* queries) or can occur later if queries are compiled (as with *embedded* queries).

This architecture is by no means fixed. For example, Cascades [42] generates multiple queries during query rewriting, and generates plans for each before choosing one that is best.

#### 1.1.2 Query Rewriting

Query rewriting has its roots in early relational databases such as System R [85] and Ingres [92] which supported *view merging*: the rewriting of a query over a view into a query over the data underlying the view. Kim [63] proposed *query unnesting* strategies that rewrite *nested queries* (queries containing other queries) into join queries, thereby giving plan generators more alternatives to consider. (Kim's ideas were later refined by many, including Ganski and Wong [39], Dayal [29] and Muralikrishnan [75, 76].) What is common to these early proposals is that they were intended as ad hoc extensions of query optimizers.

Starburst [79] elevates these ad hoc extensions to a distinct phase of query optimization known as *query rewriting*. Rewrites applied during this phase include view merging and query unnesting, as well as other rewrites that accomplish one of the following objectives:

<sup>&</sup>lt;sup>1</sup>Some (e.g., [95]) call the heuristic preprocessing optimization stage *algebraic optimization*, because this stage involves manipulation of expressions of a query algebra. The term *query rewriting* was introduced by Starburst [79].

- Normalization: Queries sometimes get posed in ways that force optimizers to choose poor evaluation plans. For example, because query optimizers build plans incrementally (i.e., by composing plans for subqueries to build full execution plans), nested queries tend to get evaluated using nested loop algorithms. By rewriting nested queries to join queries, optimizers are able to consider alternative algorithms such as *sort-merge joins*, *hash joins* etc. Therefore, one goal of query rewriting is to normalize a query into a form that allows a query optimizer to consider a greater number of alternative plans.
- Improvement: Query rewriting might also apply heuristics that are likely to lead to better plans, regardless of the contents or physical representation of the collections being queried. An example of this is a rewrite of a query that performs duplicate elimination into a query that does not. This rewrite is valid when duplicate elimination is performed on a collection that is already free of duplicates (for example, a collection resulting from projecting on a key attribute of a relation). Duplicate elimination is costly, requiring an initial sort or grouping of the elements of a collection. Therefore, rewriting a query to avoid duplicate elimination is always worthwhile.

#### 1.1.3 Rule-Based Query Optimizers and Query Rewriters

With the emergence of alternative data models in the 1980's (e.g., object-oriented) came the need for *extensible* query optimizers that could adjust to variations in data. Optimizers are extensible if they can be easily modified to account for new data models or data retrieval techniques. *Rule-based optimizers* (proposed concurrently by Freytag [38] and Graefe and DeWitt [13]) were the first optimizers introduced for this purpose.

Rule-based optimizers express the mapping of queries to plans (or queries to queries in the case of rule-based query rewriters) incrementally in terms of rules. Rules might be executed (*fired*) directly (as in Starburst, where rules are programmed in C), or used to generate an optimizer, as with Exodus/Volcano [13, 43] which express rules as rewrite rules supplemented with code. Rules make optimizers extensible because the behavior of the optimizer can be modified simply by modifying its rule set. Example rule-based systems aside from Starburst and Exodus/Volcano include Gral [6], Cascades [42] and Croque [50].

For query rewriters, rules offer a second potential benefit as formal specifications of query rewriting behavior, making it possible for query rewriters to be formally verified. This thesis shows how query rewrite rules can be expressed to enable their formal verification.

#### **1.2** Issues in Query Rewriting

#### 1.2.1 The Correctness Issue

As with other aspects of query optimization, query rewriting is complex and error-prone.

**Definition 1.2.1 (Correctness)** A query rewriter is correct if rewriting always produces an semantically equivalent query (i.e., a query that is guaranteed to produce the same result over all database states as the original query).

Many of Kim's nested query rewrites were revealed to be incorrect by Kiessling [62]. Among the errors revealed was the "COUNT bug" which adversely affected unnesting rewrites of queries with aggregates (such as COUNT).<sup>2</sup> Developers of Starburst have pointed out that aside from nested queries, queries involving duplicates and NULL's are also problematic for ensuring correctness [49]. The correctness problem is only getting worse with the emergence of *object databases* (i.e., *object-relational* and *object-oriented* databases). Object databases relax the flatness restrictions imposed by relational databases, and therefore allow queries to be nested to a far greater degree than was possible with relations. (For example, an OQL query can be nested in its SELECT clause and not just in its FROM and WHERE clauses.)

This thesis addresses the correctness issue for query rewriters. It is not enough to supplement rewrite strategies that appear in the literature with handwritten proofs. (Kim's rewrites were accompanied by formal correctness proofs that had bugs like the rewrites they were intended to verify.) Our goal is to instead make query rewriters verifiable with an *automated theorem prover*. Theorem provers were developed within the artificial intelligence community to assist with the development and error-checking of logic proofs [51]. They have since been adopted by the software engineering community as a means of verifying software relative to their formal specifications [90]. Theorem provers have proven to be especially valuable in verifying complex software (such as concurrent systems [54]) and safety-critical systems [77]. Verification of query rewriting is another natural application of this technology.

Automated theorem provers vary greatly in their complexity. Many higher-order provers (such as Isabelle [78]) are powerful but hard to use. As such, they are tools for logicians rather than software engineers. As our goal is to influence the work of systems builders, we have chosen a simple first-order theorem prover (LP [46]) that is straightforward to learn and use. Automated theorem provers are also software, and as such are fallible. For this

<sup>&</sup>lt;sup>2</sup>To this day, the "COUNT bug" has inspired numerous remedies. The most recent work we found to address the "COUNT bug" is Steenhagen's 1994 work [91]. More comprehensive studies of query unnesting have since appeared, such as Fegaras' 1998 work [32].

reason, absolute guarantees of software correctness are unrealistic. But correctness can be viewed as a relative measure of confidence rather than an absolute truth. Our inclination is to have more confidence in systems that have been verified with an established theorem prover than those that have not.

#### 1.2.2 The Expressivity Issue

Query rewrites can be quite complex. Rewrites that unnest nested queries must be able to do so for any degree of nesting. Rewrites that eliminate the need for duplicate elimination must have *semantic* knowledge of the data being queried (e.g., knowledge about keys). The inherent complexity of many query rewrites is another reason that in practice, query rewrites get expressed with code.

As with correctness, object databases exacerbate the expressivity issue. Unnesting rewrites for object queries must account for more kinds of nesting (e.g., nesting in SELECT clauses, nesting resulting from methods or attributes returning collections) than do rewrites for relational queries. Object queries can also invoke user-defined methods that dominate the cost of query processing, and about which the optimizer knows nothing. Such methods make semantic reasoning more difficult and more crucial. In short, correctness gains in query rewriting cannot come at the expense of expressivity. This thesis attempts to balance these two concerns.

#### **1.3** Contributions

#### **1.3.1** Conceptual Contributions

This thesis addresses the correctness and expressivity issues for query rewriting. To address the former, it proposes a framework for the expression, verification and implementation of rule-based query rewriters. The foundation of this work is our query algebra, KOLA. KOLA is a *combinator-based* algebra (i.e., an algebra that does not use variables). Combinators make simple rewrites of KOLA queries expressible with rewrite rules whose correctness can be verified with the theorem prover, LP [46].

Not all query rewrites are simple. The other conceptual contributions of this work address the expressivity issue for query rewriters. First, we address the expression of *complex* query rewrites that are too **general** to be expressed as rewrite rules. To express rewrites such as these, we developed a language (COKO) that permits the association of multiple KOLA rewrite rules with a *firing algorithm* that controls their firing. Expressivity is addressed without compromising correctness. As with KOLA rewrite rules, rewrites expressed in COKO are verifiable with LP.

Whereas COKO rewrites are too general to be expressed as rewrite rules, other rewrites are too **specific** to be expressed as rewrite rules. (That is, these rewrites depend on semantic, and not just syntactic properties of the queries they rewrite.) We have extended COKO and KOLA to permit the expression of such rewrites and the procedures that decide if semantic conditions hold. Again, this gain in expressivity does not compromise correctness; both semantic rewrites and condition checking are verifiable with LP.

#### 1.3.2 Implementations

The conceptual contributions described above are complemented by the following more tangible contributions that serve as proofs of concept:

- a *formal specification* of KOLA using the Larch specification tool, LSL [46],
- *scripts* for the Larch theorem prover, LP [46] that verify several hundred query rewrites,
- a *translator* to translate set and bag queries from the object query language OQL [14] into KOLA,
- a *compiler* to translate COKO specifications (including those with semantic rewrites) into executable query rewriting components, and
- a *query rewriter* generated using the software and methodology presented in this thesis, for an object-oriented database presently under development at IBM.

#### 1.3.3 High-Level Contributions

The high-level contribution of this work is the recognition of the impact of query representation on query optimizer design. The key to making query rewrites verifiable with a theorem prover is to express them *declaratively* (i.e., without supplemental code) as in the rewrite rules of term rewriting systems. In practice, query rewrites are not expressed declaratively and instead get expressed with code that performs the rewriting. This code is difficult to verify.

Query representations affect whether or not rewrites need to be expressed with code, and hence whether or not rewrites can be verified with a theorem prover. A query rewrite will typically (1) identify one or more subexpressions in a given query (*subexpression identification*) and (2) formulate a new query expression by recomposing these subexpressions (*query formulation*). Both subexpression identification and query formulation are difficult to express declaratively over *variable-based* query representations (i.e., query representations that use variables to denote arbitrary elements of queried collections) such as QGM. The problem is that query subexpressions can include *free* variables, making their meaning dependent on context. Subexpression identification then requires code to examine the context of subexpressions to ensure that the correct ones are identified. Query formulation requires code to ensure that subexpressions that are used in new contexts have their meanings preserved. Combinator-based algebras, by eliminating variables, eliminate the need for this kind of code.

In short, the combinator-based representation of KOLA queries makes it possible to express simple, complex and semantic query rewrites in a manner facilitating their verification with a theorem prover. Further, combinator-based query algebras also make it possible to consider alternative query processing architectures that vary *when* query rewriting occurs. We are presently studying the potential benefits of *dynamic* query rewriting: query rewriting that occurs during a query's evaluation. Dynamic query rewriting could potentially affect the processing of queries over collections whose contents and characteristics are not known until run-time, such as object queries (which might query embedded collections) or heterogeneous database queries (which might query collections known only to the local databases they oversee). Dynamic query rewriting also uses subexpression identification and query formulation, and therefore it too benefits from the combinator-based approach.

#### 1.4 Outline

The thesis is structured as follows. In Chapter 2, we motivate the work presented in this thesis by describing an example object database schema, some example queries over this database and some query rewrites that would be useful to express. Chapter 3 describes KOLA; our combinator-based query algebra that makes it possible to use a theorem prover to verify rewrites. Chapter 4 describes COKO; our language for expressing complex query rewrites in terms of sets of KOLA rewrite rules. Chapter 5 describes extensions to COKO and KOLA that permit the expression of semantic rewrites. Chapter 6 assesses the practicality of the COKO-KOLA approach in light of experiences building a query rewriting component for an object-oriented database being developed at IBM. Chapter 7 describes ongoing work in dynamic query rewriting. Chapter 8 describes related work conclusions

and future work follow in Chapter 9.

### Chapter 2

# Motivation

In this chapter, a potential application of the thesis work is described. We have chosen an object database example to motivate this work, as the potential complexity of object queries illustrates the need for expressive query rewriting for which correctness can be assured.

The application is based on the Thomas web site [97], which describes the activities of the United States Congress. After describing how Thomas could be modeled with an object database, two example sets of queries are presented to illustrate correctness and expressivity challenges for query rewriting. The first set of queries (the "Conflict of Interests" queries) demonstrates the potential complexity of object query rewrites and why correctness is a concern. The second set of queries (the "NSF" queries) demonstrates the need for semantic rewrites, and motivates our ongoing work in dynamic query rewriting.

#### 2.1 The Thomas Website

The United States Congress maintains the web site *Thomas* [97] to describe its daily activities. Thomas maintains information about each Congressional bill (both Senate resolutions and House resolutions) such as its name, topic and set of sponsors. Additionally, Thomas maintains information about every legislator (Senator and House Representative) such as his or her name, the region (state or Congressional district) he or she represents, his or her party affiliation, the city in which he or she was born, and the number of terms he or she has served. Every Congressional committee is represented with such information as its topic, chair and members. Thomas also includes links to related sites such as the United States Census Bureau [96], which maintains information about represented regions (states and Congressional districts) and cities. Regional information includes the name of the region, the set of major cities contained in the region, the largest city in the region and the population of the region. Information about cities includes the name of the city, its mayor and its population. Information about mayors include their name, the city they represent, their party affiliation, the city in which they were born and the number of terms they have served.

Thomas is not a database but a file system with hyperlinks. As a result, querying of Thomas (as with most web sites) is restricted to navigational queries (i.e., following links) and keyword searches. There is no support for associative access to data, as in a query that identifies committees whose chairs have potential conflict of interests due to their membership in other subcommittees (Figure 2.1), or a query that identifies the cities that potentally had influence in the formulation of policies regarding research funding (Figure 2.4). To support queries such as this, Thomas would have to be provided with a database backbone.

#### 2.2 An Object Database Schema for Thomas

An object database would be ideal for maintaining the data accessible from Thomas. Entities such as legislators, committees and bills are naturally modeled as objects. And because both object-oriented and object-relational databases support *complex data* (object attributes that name other objects or collections), a committee can have an attribute denoting its set of members, a bill can have an attribute denoting its set of sponsors, and a region can have an attribute denoting its set of major cities.

A schema for Thomas is shown in Table 2.1 and includes types: *Bill* (with subtypes *Senate\_Resolution* and *House\_Resolution*), *Legislator* (with subtypes *Senator* and *Representative*), *Mayor*, *Committee*, *Region* (with subtypes *State* and *District*) and *City*. The interface for these types is summarized below:

- Type *Bill* includes a name<sup>1</sup> attribute denoting the name of the bill, a topic attribute denoting the topic of the bill, and a spons attribute denoting the set of legislators who are the bill's sponsors. Subtypes *Senate\_Resolution* and *House\_Resolution* specialize their sets of sponsors to sets of Senators and House Representatives respectively.
- Type *Legislator* includes a name attribute denoting the name of the legislator, a reps attribute denoting the region of the country that the legislator represents, a

<sup>&</sup>lt;sup>1</sup>This proposal adopts the notational convention that all names of attributes are written in typewriter font (e.g., name).

Type	Supertype	А	ttributes	Collections
		name	String	
Bill		topic	String	$Bills^*$
		spons	$\{Legislator\}$	
$Senate\_Resolution$	Bill	spons	{Senator}	SenRes*
$House\_Resolution$	Bill	spons	$\{Representative\}$	$HouseRes^*$
		name	String	
		reps	Region	
Legislator		pty	String	
		bornin	City	
		terms	Int	
Senator	Legislator	reps	State	$\mathtt{Sens}^*$
Representative	Legislator	reps	District	$ ext{HReps}^*$
		topic	String	
Committee		chair	Legislator	Coms, SComs
		mems	$\{Legislator\}$	
		name	String	
Region		cities	$\{City\}$	
		lgst_cit	City	
		popn	Integer	
State	Region	_		${\tt Sts}^*$
District	Region	_		$\mathtt{Dists}^*$
		name	String	
City		mayor	Mayor	$\mathtt{Cits}^*$
		popn	Integer	
		name	String	
		city	City	
Mayor		pty	String	$\mathtt{Mays}^*$
		bornin	City	
		terms	Integer	

Table 2.1: A Database Schema for Thomas

pty attribute denoting the name of the political party that the legislator is affiliated with, a **bornin** attribute denoting the city where the legislator was born, and a **terms** attribute denoting the number of terms that the legislator has served. Subtypes *Senator* and *Representative* specialize the type of object denoted by attribute **reps** to *State* and *District* respectively.

- Type *Committee* includes a topic attribute naming the topic being investigated by the committee, a chair attribute denoting the legislator who is chair of the committee, and a mems attribute denoting a set of legislators who are members of the committee.
- Type *Region* includes a name attribute denoting the name of the region, a cities attribute denoting the set of major cities located in the region, a lgst\_cit attribute denoting the largest city contained in the region, and a popn attribute denoting the region's population. Subtypes *State* and *District* do not specialize these attributes in any way.
- Like *Region*, *City* also has name and popn attributes. But unlike *Region*, *City* also has a mayor attribute denoting the mayor of the city.
- Type *Mayor* has the same attributes as *Legislator*, but with a city attribute (denoting the city represented by the mayor) instead of a **reps** attrubute..

Collections of objects of each type are listed in the right most column of Table 2.1. Those with an asterisk denote the *extents* of the type (i.e., the collection of all objects of that type). For example, **Sens** is the extent of type *Senator*. The only collections that are not extents listed are **Coms** and **SComs**, that are collections of Congressional committees and subcommittees respectively. The union of these disjoint collections is the extent of type *Committee*.

#### 2.3 The "Conflict of Interests" Queries (COI)

Figure 2.1 shows an OQL [14] query over the Thomas database (hereafter, this query will be referred to as  $COI_1$  (COI is short for "Conflict of Interests") that finds committees that are chaired by a member of a subcommittee chaired by someone from the same party. This query might be posed to identify those committees whose integrity could be called into question.<sup>2</sup>

<sup>&</sup>lt;sup>2</sup>We deviate from OQL syntax in using "==" to denote an equality operator. We reserve "=" for reasoning about the meaning of query expressions throughout this thesis.

```
\begin{array}{l} \text{SELECT DISTINCT } x \\ \text{FROM } x \text{ IN Coms} \\ \text{WHERE EXISTS } y \text{ IN } \left( \begin{array}{c} \text{SELECT } c \\ \text{FROM } c \text{ IN SComs} \\ \text{WHERE } x. \text{chair.pty} == c. \text{chair.pty} \end{array} \right) : (x. \text{chair IN } y. \text{mems}) \end{array}
```

Figure 2.1:  $COI_1$ : Find all committees whose chairs belong to a subcommittee chaired by someone from the same party.

As in SQL, OQL queries have SELECT, FROM and WHERE clauses. The FROM clause of this query indicates that objects are drawn from the set of committees, Coms. The WHERE clause filters committees (x) by a complex predicate that determines whether a collection of committees returned by a subquery contains one (y) whose members (y.mems) include x's chair (x.chair). The subquery is another SELECT-FROM-WHERE query that returns the subset of SComs whose chair belongs to the same party as x's chair. The subset of committees in Coms that satisfy this predicate are returned free of duplicates (as directed by the "DISTINCT" qualifier in the SELECT clause).

#### 2.3.1 Naive Evaluation of COI<sub>1</sub>

A naive plan to evaluate  $COI_1$  might perform the following steps:

- 1. For each x in Coms:
  - (a) Extract the values x.chair and x.chair.pty
  - (b) Scan collection SComs. For each object c in SComs, extract the value c.chair.pty and compare this value to x.chair.pty. If the values are the same, then add c to a temporary collection.
  - (c) For each object y in the collection generated in (b), extract the collection y.mems.Scan y.mems comparing each object to x.chair.
  - (d) If x.chair is found in y.mems for some object y then add x to a temporary collection.
- 2. Remove duplicates from the temporary collection of legislators generated in 1d.

The naive evaluation plan is wasteful. First, it requires duplicates to be removed from a collection of committees that is guaranteed to be free of duplicates already. (A selection

```
SELECT DISTINCT x

FROM x IN Coms

WHERE EXISTS y IN \begin{pmatrix} SELECT c \\ FROM c IN SComs \\ WHERE x.chair.pty == c.chair.pty \end{pmatrix}: (x.chair IN y.mems)

\rightarrow

Temp = SELECT p, S: partition

FROM c IN SComs

GROUP BY p: c.chair.pty

SELECT DISTINCT x

FROM x IN Coms, t IN Temp

WHERE (x.chair.pty == t.p) AND (EXISTS y IN t.S: (x.chair IN y.mems))
```

Figure 2.2: Rewriting  $COI_1 \rightarrow \overline{COI_1}$ 

of a set is a set.) Duplicate elimination is costly, requiring sorting or grouping of the collection. A more subtle problem with this plan is that it requires processing the collection SComs (Step 1b) more times than necessary. In particular, the collection of all subcommittees chaired by a Democrat (Republican) will be regenerated as the inner query result for each Democratic (Republican) chair of a committee in Coms. Below, a query rewrite to address this inefficiency is considered.

#### 2.3.2 A Complex Query Rewrite for COI<sub>1</sub>

Figure 2.2 shows how query  $COI_1$  could be rewritten during query rewriting to an equivalent query for which plan generation is likely to be more effective. This figure shows the two queries,  $COI_1$  and  $\overline{COI_1}$  separated by the "rewrites to" symbol, " $\rightarrow$ ". Straightforward evaluation of  $\overline{COI_1}$  would require first preprocessing the collection SComs, and producing a new collection, Temp. OQL's "GROUP BY" operator partitions SComs on the equivalence of party affiliations of subcommittee chairs. The result of this partition (Temp) is a collection of pairs that associate a political party (p) with the set of subcommittees chaired by someone in that party (S), for each party affiliated with some subcommittee's chair. (For each party p, the OQL keyword partition names the collection of subcommittees chaired by someone whose party is p.) Temp is then used as an input to a join with Coms to find those committees whose chair is a member of some subcommittee chaired by someone from the same party.

```
SELECT DISTINCT x

FROM x IN Coms

WHERE FOR ALL y IN \begin{pmatrix} \text{SELECT } c \\ \text{FROM } c \text{ IN SComs} \\ \text{WHERE } x.\text{chair.pty} == c.\text{chair.pty} \end{pmatrix}: (x.\text{chair IN } y.\text{mems})

\not\rightarrow

Temp = SELECT p, S: partition

FROM c IN SComs

GROUP BY p: c.\text{chair.pty}

SELECT DISTINCT x

FROM x IN Coms, t IN Temp

WHERE (x.\text{chair.pty} == t.p) AND (FOR ALL y IN t.S: (x.\text{chair IN } y.\text{mems}))
```

Figure 2.3: An Incorrect Query Rewrite

A better plan is likely to be generated for  $\overline{COI_1}$  than for  $COI_1$  for two reasons:

- 1. Plans for  $\overline{COI_1}$  will generate the collection of subcommittees whose chairs are from the same party just once per party, rather than once per committee in Coms chaired by someone from that party.
- 2. Plans for  $\overline{COI_1}$  will perform a join of Coms and Temp rather than scanning all of SComs for each object in Coms. The conversion to a join query is advantageous for two reasons. First, join queries offer more algorithmic choice (e.g., sort-merge join, hash join, nested-loop join etc.) than do nested queries, which tend to get evaluated using nested loops. Secondly, even if a nested loop algorithm is chosen for the join, Temp will likely have fewer objects than SComs, having one entry per political party rather than one entry per subcommittee.

#### 2.3.3 Correctness

The unnesting query rewrite demonstrated in Figure 2.2 is useful, but under what circumstances is it correct? Clearly, it is correct if it is applied to queries that differ from  $COI_1$ only in trivial ways such as the choice of attributes. But what about queries that differ in more substantial ways? For example, what about a query for which the existential quantifier exists is replaced by the universal quantifier, for all as shown in Figure 2.3?



Figure 2.4:  $NSF_1$ : Find all House resolutions relating to the NSF and associate them with the set of cities that are largest in districts that the bills' sponsors represent

Such a subtle change results in an incorrect query rewrite. To see why, suppose there exists a committee in Coms chaired by Representative Bernie Sanders of Vermont, the sole independent in Congress, and suppose that Sanders is not the chair of any subcommittee in SComs. In this case, the initial query of Figure 2.3 will include the committee chaired by Sanders in the query result, but the rewritten (second) query of this figure will not. This is because no subcommittees are chaired by Sanders, and therefore independents are not represented in the preprocessed collection, Temp. Thus, Sanders will fail to satisfy the join predicate with all entries in Temp and will be excluded from the second query's result.

This discrepancy in query results is very similar to that which was symptomatic of the "COUNT bug" of Kim [63]. In fact, the query rewrite demonstrated in Figure 2.3 generalizes the *Type JA* rewrite that contains the bug. The subtlety of this bug illustrates the difficulty of determining correctness conditions for query rewrites. This particular rewrite is correct if it is applied only to queries with predicates that are not true of empty collections.  $COI_1$  is such a query because an existentially quantified predicate cannot be true of an empty collection. On the other hand, a universally quantified predicate is always true of an empty collection and therefore the effect of rewriting the initial query of Figure 2.3 is to produce a query with a different semantics.

#### 2.4 The "NSF" Queries (NSF)

Figure 2.4 shows an OQL query (hereafter referred to as  $NSF_1$ ) that associates every House resolution concerning the National Science Foundation (NSF) with the set of cities that are largest in the districts represented by the bill's sponsors. This query finds the cities that potentially have the most influence on research funding policies. Unlike  $COI_1$ , this query is nested in its SELECT clause and not its WHERE clause. Additionally, this query includes a
chain of attribute selections (a *path expression*),

```
x.reps.lgst_cit
```

that returns the largest city located in the district represented by legislator x. Path expressions can only be posed over object databases, as they require that all but the last attribute return a complex object.

## 2.4.1 Naive Evaluation of NSF<sub>1</sub>

A naive plan for  $NSF_1$  might perform the following steps: For each r in HouseRes:

- 1. Extract the value r.topic. If this value is "NSF", proceed to step 2.
- 2. Extract the collection attribute, r.spons. For each x in r.spons, extract the value

```
x.reps.lgst_cit.
```

- 3. Collect the extracted names of all cities identified in 2, and store in a new collection. Eliminate duplicates from this new collection.
- 4. Extract the value *r*.name. Add the tuple consisting of *r*.name and the set resulting from the previous step to the result collection.

## 2.4.2 A Semantic Query Rewrite for NSF<sub>1</sub>

The naive evaluation plan for the  $NSF_1$  includes costly duplicate elimination (in Step 3) from collections of cities. Duplicate elimination from these collections is unnecessary because:

- a House resolution has a *set* of House Representatives as its sponsors,
- each House Representative represents a unique district (i.e., the **reps** attribute of type *Representative* is an *injective* function), and
- each district's largest city is uniquely situated in that district (i.e., the lgst\_cit attribute of type *Region* is an injective function.)<sup>3</sup>

 $<sup>^{3}</sup>$ We make the simplifying assumption that every city is located in exactly one district. We can enforce this assumption by assigning a city to the district where the largest number of its residents reside.

Figure 2.5: Rewriting  $NSF_1 \rightarrow \overline{NSF_1}$ 

Because each attribute in its chain is injective,

## x.reps.lgst\_cit

is also injective over type *Representative*. An injective function that is applied to all elements of a set generates another set. Therefore, the collection of largest cities situated in the represented districts is guaranteed to be free of duplicates, and duplicate elimination is unnecessary. Figure 2.5 shows the NSF query before and after the application of the *semantic rewrite* that exploits semantic knowledge about keys and duplicates to produce a query that avoids duplicate elimination.

This example motivates the need to express semantic rewrites. But note that injective path expressions can be of any length, as in

## $x.reps.lgst\_cit.mayor$

which finds the mayor of the largest city of the district represented by x, or even

### x.reps.lgst\_cit.mayor.city.lgst\_cit

which returns the same result but in a more roundabout way. It is unrealistic to expect that any metadata file could list all injective path expressions, for there may be too many to list.<sup>4</sup> Therefore, a query rewriting facility must provide some way for an optimizer to *infer* the semantic properties (such as injectivity) on which semantic rewrites are conditioned.

<sup>&</sup>lt;sup>4</sup>Because the Thomas schema has mutually recursive references (e.g., a city has a mayor (mayor) and a mayor is born in a city (bornin)), the number of injective path expressions over this schema is infinite.

```
SELECT STRUCT \begin{pmatrix} bill: b.name, \\ cities: \begin{pmatrix} SELECT DISTINCT x.reps.lgst_cit \\ FROM x IN b.spons \end{pmatrix}
```

Figure 2.6:  $NSF_2$ : Find all Bills (Senate and House resolutions) relating to the NSF and associate them with the set of cities that are largest in regions that the bills' sponsors represent

## 2.4.3 Dynamic Query Rewriting

Consider the second NSF query  $(NSF_2)$  shown in Figure 2.6. This query is similar to  $NSF_1$ , but queries a collection (Bills) of House and Senate resolutions, and not just a collection of House resolutions.

As was stated previously, the application of the path expression,

over any set of House Representatives is guaranteed to return a set because **reps** is a key for type *House Representative* and **lgst\_cit** is a key over type *Region*. However,

#### x.reps.lgst\_cit

is **not** an injective function over type *Senator* because **reps** is not a key over type *Senator*. Rather, there are *two* Senators for every state represented by a Senator. Because Bills can include a Senate resolution *b*, *b*.**spons** can be a set of Senators. Therefore, the query rewrite described in the previous section cannot be applied to this query.

On the other hand, query  $NSF_2$  could be evaluated in the following way:

- For bills that are Senate resolutions, perform duplicate elimination on the collection of cities associated with the bill's sponsors.
- For bills that are House resolutions, do *not* perform duplicate elimination on the collection of cities associated with the bill's sponsors.

In other words, the semantic rewrite described in the previous section could be applied *dynamically* to rewrite subqueries applied to House resolutions and to leave alone subqueries applied to Senate resolutions. Because of its potential for avoiding duplicate elimination at least for some bills, this evaluation strategy offers potentially large savings in evaluation

cost. But this strategy requires the query rewriting to take place dynamically during a query's evaluation and not just during its optimization. Examples such as this motivate our ongoing work on dynamic query rewriting.

## 2.5 Chapter Summary

The schema presented in this Chapter will serve as the schema underlying all example queries in this thesis. The two sets of queries presented in this Chapter motivate the work described in the thesis. The "Conflict of Interests" queries presented in Section 2.3 demonstrate the potential complexity of query rewrites and the subtlety of ensuring correctness. Query  $COI_1$  is a nested query that can be transformed into a join query in the spirit of Kim's unnesting rewrites [63]. Query  $COI_2$  is syntactically very similar to  $COI_1$  but for the choice of quantifier appearing in the WHERE clause. This subtle difference is enough to distinguish a query that can be rewritten into a join query  $(COI_1)$  from one that cannot  $(COI_2)$ . Being able to pinpoint with confidence the exact conditions that make unnesting rewrites correct is one of the benefits that arises from the work presented in this thesis.

The "NSF" queries presented in Section 2.4 motivate our work on semantic rewrites, and our ongoing work studying dynamic query rewriting. Query  $NSF_1$  shows an object query for which an appropriate query rewrite (that makes duplicate elimination unnecessary) depends upon the semantics of the underlying data (i.e., key information and knowledge about the lack of duplicates in collections). This example also motivates the need for query rewriters to infer the conditions that guard semantic rewrites. Query  $NSF_2$  differs from  $NSF_1$  in that the collection it queries can contain both Senate and House resolutions. For this query, the semantic rewrite that makes duplicate elimination unnecessary can only be applied when House resolutions are processed. Selective application of semantic query rewrites motivated our ongoing work on dynamic query rewriting which allows query rewrites to be performed in the midst of a query's evaluation (e.g., as each bill is retrieved).

## Chapter 3

# **KOLA: Correct Query Rewrites**

This chapter motivates and describes KOLA, a novel *combinator-based* (variable-free) representation and query algebra. KOLA is intended to be a query representation for rule-based query rewriters, and thus is an alternative to query representations such as QGM [79], and query algebras such as Excess [13]. We chose to define a representation for a rulebased query rewriter because query rewrites expressed as rules offer the best opportunity for verification with a theorem prover. We chose to define a *new* representation because representations used in existing query optimizers, being variable-based, impede verification with a theorem prover.<sup>1</sup>

## 3.1 The Need for a Combinator-Based Query Algebra

The firing of a query rewrite consists of two steps:

• Step 1: Subexpression Identification

During this initial step, the query rewrite identifies relevant subexpressions of the query on which it is fired. If some specified subexpression cannot be identified, the query is not rewritten. (This case is a *failed firing*.) The second step of the rewrite is performed only if all specified subexpressions are identified.

• Step 2: Query Formulation

During this step, a new query expression is formulated using the subexpressions identified in the previous step. This new query is returned as the result of the rewrite.

<sup>&</sup>lt;sup>1</sup>KOLA was developed in response to difficulties faced attempting to formulate declarative rules over the variable-based algebra, AQUA [70].

Different rule-based systems express subexpression identification and query formulation in different ways. Starburst [79] expresses both steps *algorithmically* with C code. Exodus and Volcano [13, 43] also use code, but as supplements to *rewrite rules*.

Rewrite rules consist of pairs of patterns and are *fired* using standard *pattern matching*. Firing first matches the pattern of the left-hand side of a rule (the *head* pattern) with the query on which the rule is fired. Patterns can include *pattern variables* that match arbitrary subexpressions. Therefore, successful matching creates a set of bindings (an *environment*) of subexpressions to pattern variables. Firing then proceeds to use this environment to substitute for pattern variables appearing in the pattern of the right-hand side of the rule (the *body* pattern). The resulting expression is returned as the result of firing.

The two steps of rule firing correspond to subexpression identification and query formulation. But unlike query rewrites that are expressed with code, query rewrites that are expressed with rewrite rules describe the effects of the rewrite without saying how the rewrite takes place. (The latter is instead described by the pattern matching algorithm.) Therefore, rewrite rules are *declarative* specifications of query rewrites. Declarative query rewrites are much easier to verify than query rewrites expressed with code because verification of the former simply requires proving the equivalence of the two expressions characterized by the head and body patterns of the rule. On the other hand, verification of query rewrites expressed with code requires reasoning about the state of the rewrite computation after each statement in the code is executed. Verification with a theorem prover is similarly far simpler when query rewrites are expressed with rewrite rules. This is because theorem provers are special-purpose term rewriting systems [51] that have natural application to proofs establishing that two expressions are equivalent.

## 3.1.1 Variables Considered Harmful

Exodus/Volcano and Starburst must express query rewrites with code because both systems use variable-based query representations. Variables make it difficult to express subexpression identification and query formulation with rewrite rules, as we show below.

#### Variables Complicate Subexpression Identification

Two queries represented in a variable-based representation can have syntactically identical parse trees and yet be semantically distinct and subject to different query rewrites. This is due to the nature of variables which typically are represented uniformly in a parse tree

SELECT DISTINCT 
$$x$$
  
FROM  $x$  IN Coms  
WHERE EXISTS  $y$  IN  $\begin{pmatrix} \text{SELECT } c \\ \text{FROM } c \text{ IN SComs} \\ \text{WHERE } x.chair.pty == c.chair.pty \end{pmatrix}$ :  $y.chair \text{ IN } y.mems$ 

Figure 3.1: COI<sub>2</sub>: Find all committees whose chairs belong to a party that includes someone that both chairs and is a member of the same subcommittee.

representation regardless of the variable name. Pattern matching relies on syntactic distinctions recognized during subexpression identification to determine when rewrite rules can fire. Therefore, query rewrites over variable-based query representations must be at least partially expressed with code to make the distinctions that pattern matching cannot.

We illustrate this point with an example. Figure 3.1 shows an OQL query  $(COI_2)$  that is syntactically identical to query  $COI_1$  of Figure 2.1. The only difference between these two queries is the variable that appears in the existentially quantified expression in the WHERE clause: for query  $COI_1$  this variable is x (x.chair IN y.mems) and for query  $COI_2$ this variable is y (y.chair IN y.mems).

Queries  $COI_1$  and  $COI_2$  differ only by this variable and therefore are syntactically identical. But these queries have very different semantics. Whereas  $COI_1$  finds committees whose chairs belong to subcommittees chaired by someone from the same party,  $COI_2$  finds committees whose chairs belong to parties that include members who are both chairs and members of the same subcommittees.  $COI_1$  and  $COI_2$  are also subject to different query rewrites. We showed in Section 2 that query  $COI_1$  can be rewritten into the equivalent join query,  $\overline{COI_1}$  (Figure 2.2).  $COI_2$  can similarly be rewritten to  $\overline{COI_2}$  as demonstrated by the first rewrite of Figure 3.2. But this query can be further rewritten into  $\overline{\overline{COI_2}}$  as shown in the second query rewrite of Figure 3.2.<sup>2</sup> A rewrite rule for this query rewrite is shown in Figure 3.3. The rule separates two OQL patterns with the "rewrites to" symbol,  $\equiv$ .<sup>3</sup> These patterns include pattern variables:

$$A_1,\ldots,A_6,V_1,\ldots V_4,C_1,\ldots,C_3, \text{ and } \mathsf{Op}_1.$$

<sup>&</sup>lt;sup>2</sup>The second rewrite returns a query that uses OQL's HAVING clause to filter Temp. This clause excludes entries for parties with which some subcommittee chair is affiliated, but with which no subcommittee chair who is also a member of his subcommittee is affiliated. This rewrite is useful because the mems collection for a given subcommittee will be scanned once, rather than once for every committee in Coms whose chair is from the same party.

 $<sup>\</sup>stackrel{3}{=}$  should not be confused with  $\rightarrow$ , which separates two queries rather than two patterns.

 $\overline{COI_2}$  matches the head pattern of this rule by making the following bindings of subexpressions to pattern variables:

$\mathtt{A}_1$	=	р	$\mathtt{V}_1$	=	С	$C_1$	=	Coms
$\mathtt{A}_2$	=	S	$\mathtt{V}_2$	=	x	$C_2$	=	SComs
$\mathtt{A}_3$	=	chair.pty	$\mathtt{V}_3$	=	t	$C_3$	=	${\tt Temp}$
$\mathtt{A}_4$	=	chair.pty	$\mathtt{V}_4$	=	y	$\mathtt{Op}_1$	=	IN
$\mathtt{A}_5$	=	chair						
$\mathtt{A}_6$	=	mems						

Substituting for the pattern variables appearing in the body pattern of the rule leaves  $\overline{COI_2}$ .

The rule of Figure 3.3 appropriately expresses the transformation in such a way that  $\overline{COI_2}$  will be rewritten and  $\overline{COI_1}$  will not be. This discrimination is guaranteed by the use of the same pattern variable (V<sub>4</sub>) in both operands of the operator (Op<sub>1</sub>) that appears in the WHERE clause. But this discrimination comes at a cost of making this predicate pattern overly specific. This rule should transform queries whose quantified predicate includes no variables other than y (i.e., the variable bound by the quantifier). For example, queries that substitute any of the following expressions for

## y.chair IN y.mems

should be rewritten according to this rule, but will not be given its expression in Figure 3.3:

- y.chair == "Newt Gingrich",
- "Newt Gingrich" IN y.mems
- y.chair.pty == "GOP".

The condition that an expression contain only one particular free variable cannot be expressed with a head pattern alone. Instead a head pattern would have to match all expressions, and supplemental code would have to analyze matched expressions to see if variables other than y occur free. Code supplements to rules could be defined perhaps by the writers of rules, or could be provided by way of a library available to rule designers. Regardless, the actions of code supplements (such as checking for the existence of free variables) are meta-level actions and as such complicate verification, making it necessary to use complicated (higher-order) theorem prover tools for which performance and ease-of-use become issues. This example illustrates the need for code to perform subexpression identification for rules expressed over variable-based query representations.

```
SELECT DISTINCT x
FROM x IN Coms
WHERE EXISTS y IN \begin{pmatrix} \text{SELECT } c \\ \text{FROM } c \text{ IN SComs} \\ \text{WHERE } x.\text{chair.pty} == c.\text{chair.pty} \end{pmatrix}: y.\text{chair IN } y.\text{mems}
                                              (COI_2)
                                                \rightarrow
 Temp = SELECT p, S: partition
             FROM c IN SComs
             GROUP BY p: c.chair.pty
SELECT DISTINCT x
FROM x IN Coms, t IN Temp
WHERE (x.chair.pty == t.p) AND (EXISTS y IN t.S : (y.chair IN y.mems))
                                             (\overline{COI_2})
 Temp = SELECT p, S: partition
             {\tt FROM} \ c \ {\tt IN} \ {\tt SComs}
             GROUP BY p: c.chair.pty
             HAVING EXISTS y IN partition: (y.chair IN y.mems)
SELECT DISTINCT x
FROM x IN Coms, t IN Temp
WHERE x.chair.pty == t.p
                                             (\overline{COI_2})
```

Figure 3.2: Transforming  $COI_2 \rightarrow \overline{COI_2} \rightarrow \overline{\overline{COI_2}}$ 

Figure 3.3: A Rewrite Rule Justifying  $\overline{COI_2} \rightarrow \overline{\overline{COI_2}}$ 

To summarize, queries  $COI_1$  and  $COI_2$  are syntactically similar but semantically distinct. Further, these two queries are subject to different query rewrites. Query rewrites perform subexpression identification in part to determine if rewriting can occur. As pattern matching can only make syntactic distinctions between expressions, code must be used by any nontrivial query rewrite that rewrites  $\overline{COI_2}$  to  $\overline{\overline{COI_2}}$  to ensure that  $\overline{COI_1}$  is not affected.

### Variables Complicate Query Formulation

In formulating new queries, query rewrites can reuse subexpressions identified in the original query. But if these subexpressions include free variables, the meanings of these subexpressions may change as a result of their use in a different context. Code is required under these circumstances to massage subexpressions to ensure that their semantics are preserved.

We illustrate this again with an example. Figure 3.4a shows an equivalent query to  $COI_1$  ( $COI_{1*}$ ) and its rewrite into  $COI_1$ . This rewrite uses a quantified predicate expression,

x.chair.pty == y.chair.pty

SELECT DISTINCT xFROM x IN Coms WHERE EXISTS y IN SComs : ((x.chair IN y.mems) AND (x.chair.pty == y.chair.pty))

 $(COI_{1*})$ 

SELECT DISTINCT x

FROM x IN Coms

WHERE EXISTS y IN  $\begin{pmatrix} \text{SELECT } c \\ \text{FROM } c \text{ IN SComs} \\ \text{WHERE } x.\text{chair.pty} == c.\text{chair.pty} \end{pmatrix}$ : x.chair IN y.mems

 $(COI_1)$ 

(a)

SELECT DISTINCT  $V_1$  FROM  $V_1$  IN  $C_1$  WHERE EXISTS  $V_2$  IN  $C_2:(E_1 \text{ AND } (V_3.A_1 \text{ Op}_1 \text{ } V_2.A_2))$ 

 $\stackrel{\rightarrow}{=}$ 

SELECT DISTINCT  $V_1$ FROM  $V_1$  IN  $C_1$ WHERE EXISTS  $V_2$  IN  $\begin{pmatrix} \text{SELECT } V_4 \\ \text{FROM } V_4 \text{ IN } C_2 \\ \text{WHERE } V_3.A_1 \text{ Op}_1 \text{ } V_4.A_2 \end{pmatrix} : E_1$  (b)

Figure 3.4:  $COI_{1*} \rightarrow COI_1$  (a) and a Rule to Justify It (b)

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as a filter condition for a new (inner) subquery:

This rewrite is useful as it enables  $COI_{1*}$  to be subsequently rewritten into  $\overline{COI_1}$ .

Figure 3.4b shows a rewrite rule expressing this rewrite. Again, this rewrite rule is overly specific. Any predicate expression can be moved out of a quantifier and into an inner query; predicate expressions need not be of the form,

$$V_3.A_1 \text{ Op}_1 V_2.A_2$$

as stipulated by the rule of Figure 3.4b. But if any predicate that is moved includes occurences of the quantified variable  $V_2(y)$ , then all occurences of this variables must be renamed. In this case, y is renamed to c, changing the expression

 $\operatorname{to}$ 

Thus, code is necessary to rename variables appearing in subexpressions used to formulate new queries, and more generally, to substitute any expressions (not just variables) for variables appearing in other expressions.

## 3.1.2 The Need for a Combinator-Based Query Algebra: Summary

Query rewrites perform two steps in rewriting a query: (1) subexpression identification, and (2) query formulation. For query rewrites to be expressed as rewrite rules, a query representation must ensure that subexpressions of the query:

- 1. can be identified on the basis of their structure (syntax), and
- 2. have context-independent semantics so that they can be reused without modification when new queries are formulated.

Variable-based query representations fail to satisfy both criteria. Therefore, query rewrites expressed over variable-based representations must be fully or partially expressed with code that analyzes or manipulates the variables appearing in subexpressions. Combinator-based representations eliminate variables, and in so doing, eliminate the need for this supplementary code. In the next section, we illustrate this by revisiting the examples presented in this section in the context of our combinator-based query algebra, KOLA.

## 3.2 KOLA

Variable-based query representations impede the formulation of query rewrites with rewrite rules. Therefore, we designed the query algebra, KOLA, which is variable-free (*combinator-based*).<sup>4</sup> More accurately, KOLA is an algebra of functions and predicates, of which query operators are simply those that apply to or return collections.

KOLA functions and predicates are expressed using combinator *primitives* whose semantics are predefined, and combinator *formers* (second-order functions) that produce complex functions and predicates from simpler ones. Because combinators have no variables, KOLA avoids the problems that variables introduce. The semantics of a KOLA expression is tied to its structure and **not** to the context in which it appears. Therefore KOLA rewrite rules need no code to assist with subexpression identification or query formulation.

It should be noted that KOLA is a language for optimizers and not users, and KOLA queries are far more difficult to read than OQL queries. As best as possible, we will assist the reader in decomposing KOLA queries referring to the definitions that appear in the coming sections. The reader is advised to trace reductions of KOLA queries as we do in the next section, until becoming comfortable with the notation and combinator style.

## 3.2.1 An OQL Query Expressed in KOLA

KOLA is a language for expressing functions and predicates invokable on objects. Invocation is explicit, with "f ! x" denoting the invocation of function f on object x (returning an object of any type) and "p ? x" denoting the invocation of predicate p on object x (returning a *Bool*). The KOLA style of querying is illustrated with a simple query shown in Figure 3.5. Figure 3.5a shows an OQL query that finds all subcommittees in **SComs** chaired by Republicans. Figure 3.5b shows its KOLA equivalent.

The KOLA query of Figure 3.5b includes:

- the primitive identity function, id, which maps every object to itself,
- the complex predicate,

 $C_p (eq, "GOP") \oplus (pty \circ chair)$ 

which is true of a committee if its chair is Republican, and

<sup>&</sup>lt;sup>4</sup>KOLA resembles AQUA but for its combinator foundation and some other language differences described in our 1995 DBPL paper [23]. Thus, the name KOLA was coined from the acronym, [K]ind [O]f [L]ike [A]QUA.

SELECT c FROM c IN SComs WHERE c.chair.pty == "GOP"

 $\textbf{iterate} \ (\texttt{C}_p \ (\textbf{eq}, \ \texttt{``GOP''}) \ \oplus \ (\texttt{pty} \ \circ \ \texttt{chair}), \ \textbf{id}) \ ! \ \texttt{SComs}$ 

(a)

(*b*)

Figure 3.5: A Simple OQL Query (a) and its KOLA Equivalent (b): *Name All Subcommittees Chaired by Republicans* 

• the complex query function,

**iterate**  $(C_p (eq, "GOP") \oplus (pty \circ chair), id)$ 

which filters a bags of committees for those whose chair is Republican.

We can break these query components down even further as follows.

• pty and chair are primitive functions named for attributes of the Thomas schema (Table 2.1). For any legislator *l*,

pty ! 
$$l = l.pty$$

and for any committee c,

chair ! c = c.chair.

Therefore, the semantics of attribute-based primitives such as these depend on the values of the corresponding attributes for objects populating the database.

- eq is a primitive equality predicate invoked on *pairs* (denoted by [\_\_, \_\_]) of objects of the same type. The definition of eq is depends on each type's definition of equality (==).
- \_\_  $\circ$  \_\_ is a function composition *former* that builds a new function that invokes two other functions in succession. That is, given functions f and g the function  $f \circ g$  has an operational semantics defined in terms of invocation on an object x:

$$(f \circ g) ! x = f ! (g ! x)$$

For example, given a committee x, the semantics of  $(pty \circ chair) ! x$  is revealed by the reduction below:

$$(pty \circ chair) ! x = pty ! (chair ! x)$$
  
= pty ! (x.chair)  
= x.chair.pty

•  $C_p$  (\_\_, \_\_) is a currying predicate *former* that builds a unary predicate from a binary predicate by binding the first argument. The semantics of this predicate can be expressed in terms of any binary predicate p and objects x and y by the equation,

$$C_p(p, x) ? y = p ? [x, y].$$

For example, given some string, x,  $(C_p (eq, "GOP") ? x)$  has semantics revealed by the reduction below:

$$C_p$$
 (eq, "GOP") ?  $x = eq$  ? ["GOP",  $x$ ]  
= "GOP" ==  $x$   
=  $x ==$  "GOP"

•  $\_\_\oplus$  \_\_ is a combination predicate former that builds a predicate from another predicate and function. Much like function composition,  $\_\_\oplus$  \_\_ first applies the function to its argument and then tests the predicate on the result. That is, given predicate pand function f, the predicate  $(p \oplus f)$  has semantics expressible in terms of invocation on an object x:

$$(p \oplus f)$$
 ?  $x = p$  ?  $(f ! x)$ .

For example, when invoked on a committee, x,

$$extsf{C}_p \ ( extsf{eq}, \ extsf{``GOP"}) \oplus ( extsf{pty} \circ extsf{chair})$$

has semantics revealed by the reduction below:

$$\begin{array}{rcl} (\mathbf{C}_p \ (\mathbf{eq}, \ \ ^{\boldsymbol{\mathsf{"GOP"}}}) \oplus \ (\mathtt{pty} \circ \mathtt{chair})) \ ? \ x \\ &= & \mathbf{C}_p \ (\mathbf{eq}, \ \ ^{\boldsymbol{\mathsf{"GOP"}}}) \ ? \ ((\mathtt{pty} \circ \mathtt{chair}) \ ! \ x) \\ &= & \mathbf{C}_p \ (\mathbf{eq}, \ \ ^{\boldsymbol{\mathsf{"GOP"}}}) \ ? \ (x.\mathtt{chair.pty}) \\ &= & x.\mathtt{chair.pty} == \ \ ^{\boldsymbol{\mathsf{"GOP"}}} \end{array}$$

• iterate (\_, \_) is a querying function former that builds a function on bags given a predicate and a function as inputs. Given any predicate p, function f and bag A, we have

iterate 
$$(p, f) ! A = \{(f ! x)^i | x^i \in A, p ? x\},\$$

such that the expression on the right hand side describes a bag (delimited by "{" and "}") that contains the result of invoking f on all objects in A that satisfy p. The expression,  $x^i \in A$  indicates that there are i copies of x in A and that i > 0.5. Therefore, the number of elements, x that are in A determines the number of elements, f ! x that are inserted into the result.

Given these definitions, we can reduce the query expression,

iterate (
$$C_p$$
 (eq, "GOP")  $\oplus$  (pty  $\circ$  chair), id) ! SComs

as follows:

$$extsf{iterate} \ ( extsf{C}_p \ ( extsf{eq}, \ extsf{``GOP"}) \oplus ( extsf{pty} \circ extsf{chair}), \ extsf{id}) \ ! \ extsf{SComs}$$

$$= \{ (\mathbf{id} ! x)^i \mid x^i \in \mathtt{SComs}, (\mathtt{C}_p (\mathbf{eq}, \texttt{``GOP"}) \oplus (\mathtt{pty} \circ \mathtt{chair})) ? x \}$$
(By the definition of **iterate**)

 $= \{x^i \mid x^i \in \texttt{SComs}, (\texttt{C}_p \ (\texttt{eq}, \texttt{"GOP"}) \oplus (\texttt{pty} \circ \texttt{chair})) ? x\}$ (By the definition of **id**)

= 
$$\{x^i \mid x^i \in \text{SComs}, x.\text{chair.pty} == \text{``GOP''}\}$$
  
(By the definitions of  $C_p$ ,  $eq$ ,  $\oplus$ ,  $\circ$ ,  $pty$  and  $chair.$ )

Thus, this query returns those committees in SComs whose chair is Republican.

## 3.2.2 The KOLA Data Model

The KOLA data model assumes a universe of objects, each associated with a type that defines its interface. A type's interface can include operators that *construct* the object, or *observe* or *mutate* its state. A type which includes operators that can mutate an object's

<sup>&</sup>lt;sup>5</sup>To keep our notation similar to set comprehension notation, we write  $x \notin A$  when there are no copies of x in A rather than  $x^0 \in A$ .

state is called a *mutable type* and its objects are *mutable objects*. Conversely, a type or object upon which no mutating operations are defined is *immutable*.

Immutable objects have immutable state, and hence their state reveals their identity. That is, the integer object 3 has an identity that is inseparable from its value (i.e., all instances of objects representing the value 3 are equal). On the other hand, mutable objects should not be compared on the basis of their mutable states as this makes their identities ephemeral and provokes unintuitive behaviors in any collections that contain them [23]. Rather, mutable objects are assumed to be implemented with immutable, unique *object identifiers* (*OID*'s) that are used by the run-time system to decide if two objects are equal. In short, KOLA supports both mutable and immutable objects, but mutable objects are assumed to be compared for equality on the basis of their immutable object identifiers while immutable objects are compared on the basis of their immutable objects.

An informal description of the object types supported by the KOLA data model follows. Appendix A includes a formal specification of the data model expressed in Larch [46].

## • Base Types

The base types supported in KOLA are the immutable types *Bool* (booleans), *Int* (integers), *Char* (characters), *Float* (floats) and *String* (strings). A standard interface for these types is assumed. Constants of these types have the usual form. As well, NULL is assumed to be a constant belonging to all types.

• Class Types

KOLA permits queries over collections of objects that are instances of class types. It is assumed that a class definition defines an interface to which queries have access. In particular, we assume that queries can invoke the observer operators of objects but not their mutators or constructors, as queries are assumed to be free of side-effects.<sup>6</sup> Finally, it is assumed that observers are unary (*attributes*).

• Pair Types

A pair type is any type of the form

 $<sup>(</sup>t_1 \times t_2)$ 

<sup>&</sup>lt;sup>6</sup>This is one way that KOLA is less expressive than OQL, as OQL queries can return collections of new mutable objects. This confuses the issue of optimizer correctness which must then be based on similarity rather than equality of results. We discuss this issue at length elsewhere [18], but have yet to modify KOLA in light of our analysis.

such that  $t_1$  and  $t_2$  are types. Given object x of type  $t_1$   $(x : t_1)$  and y of type  $t_2$   $(y : t_2)$ , [x, y] is a pair object of type  $(t_1 \times t_2)$   $([x, y] : (t_1 \times t_2))$ . (For example, the type of [3, *Joe*] is  $(Int \times Person)$  assuming that 3 is of type *Int* and *Joe* is of type *Person*.) Pairs are used to express relationships between objects of potentially differing types.

• Collection (Bag and Set) Types

For any type t,  $\{t\}$  denotes the type of *bags* whose elements are all of type t. Formally, a bag  $A : \{t\}$  is a function,  $t \to \mathbb{Z}$  such that for any object x : t, A(x) is the number of occurences of x in A. It is easier to formalize bags and bag operators when bags are defined in terms of their characteristic functions rather than as collections containing elements. But sometimes it is more intuitive to use comprehension notation (as used, for example, in Fegaras and Maier's work [33]) to reason about the "contents" of a bag. Therefore, this proposal uses the following shorthand notation:

- for any bag  $A : \{t\}$  and expression e : t,

$$e \in A$$

is shorthand for A(e) > 0 and

$$e^i \in A$$

(for i > 0) is shorthand for A(e) = i.

- for any  $x_1, \ldots, x_n : t$ , and positive integers  $i_1, \ldots, i_n$ ,

$$\{(x_1)^{i_1},\ldots,(x_n)^{i_n}\}$$

denotes a bag  $B : \{t\}$  containing elements  $x_1, \ldots, x_n$  whose count of any element, y(B(y)) is

$$\sum_{\leq j \leq n, \, y = = x_j} i_j.$$

For example,  $\{(3)^1, (-3)^2, (2)^2, (-3)^1\}$  denotes the bag B such that:

$$B(-3) = 3,$$
  
 $B(2) = 2,$   
 $B(3) = 1,$ 

and for any i not equal to -3, 2 or 3, B(i) = 0. As a further shorthand, we write

$$\{x_1,\ldots,x_n\}$$

$$\{x_1, \ldots, x_n\} = \{(x_1)^1, \ldots, (x_n)^1\}$$

- for any bag,  $A : \{\!\!\{t\}\!\!\}$ , variable x : t, and expressions, f(x) : u, g(x) : Int and p(x) : Bool,

$$\{\!\!\{f(x)^{g(i)} \,|\, x^i \in A, \, p(x)\}\!\!\}$$

denotes a bag  $B : \{\!\!\{u\}\!\!\}$  containing elements f(x) (for each  $x \in A$ ) whose count of any element y : u (B(y)) is:

$$\sum_{x^i \in A, \, y \, = = \, f(x), \, p(x)} g(i)$$

For example, if  $A = \{3, -3, 2, -3\}$ . Then

$$\{\!\!\{(x\ast x)^i\,|\,x^i\in A\}\!\!\}$$

denotes the bag, B such that

$$B(4) = 1,$$
  
 $B(9) = 3,$ 

and for any e not equal to 4 or 9, B(e) = 0.

More generally, for bags  $A_1 : \{\!\!\{t_1\}\!\} \dots A_n : \{\!\!\{t_n\}\!\}$ , variables  $x_1 : t_1, \dots, x_n : t_n$ , positive integers  $i_1, \dots, i_n$  and  $g(i_1, \dots, i_n)$ , and expressions  $f(x_1, \dots, x_n) : u$ ,  $p(x_1, \dots, x_n) : Bool$ , and y : u:

$$\{ \{ f(x_1, \dots, x_n)^{g(i_1, \dots, i_n)} \mid (x_1)^{i_1} \in A_1, \dots, (x_n)^{i_n} \in A_n, \ p(x_1, \dots, x_n) \} \}$$

denotes  $B : \{\!\!\{u\}\!\!\}$  such that for all y : u:

$$B(y) = \sum_{(x_1)^{i_1} \in A_1, \dots, (x_n)^{i_n} \in A_n, y == f(x_1, \dots, x_n), p(x_1, \dots, x_n)} g(i_1, \dots, i_n)$$

As an example, suppose that A is defined as above and  $A' = \{5, 11, 5, 6\}$ , then

$$\{\!\!\{(x+y)^{ij} \,|\, x^i \in A, \, y^j \in A'\}\!\!\}$$

denotes the bag, B such that

$$B(2) = 4,$$
  

$$B(3) = 2,$$
  

$$B(7) = 2,$$
  

$$B(8) = 5,$$
  

$$B(9) = 1,$$
  

$$B(13) = 1,$$
  

$$B(14) = 1,$$

and for any *i* not equal to 2, 3, 7, 8, 9, 13 or 14, B(i) = 0.

A set is a special kind of bag whose element counts are either 0 or 1. That is, A is a set of elements of t if it is a bag of t's and for all x of type t, A(x) = 1 or A(x) = 0. We use set comprehension notation in discussing sets. That is, for any x : t, p(x) : Booland f(x) : u

$$\{f(x) \mid x \in A, p(x)\}$$

is equivalent to

$$\{\!\!\{(f(x))^1 \mid x \in A, \ p(x)\}\!\!\}$$

For simplicity, we assume a namespace of identifiers that refer exclusively to stored collections. All named bags and sets (e.g., **Coms**, **SComs**, **Lgs** etc.) are assumed to be mutable. However, all bags and sets constructed by KOLA operators are assumed to be immutable (as in OQL). For queries, the mutable vs. immutable distinction only makes a difference when deciding if two bags (sets) are equal. Two mutable bags (sets) are equal if they are the same object (i.e., they have the same object identifier). Two immutable bags (sets) are equal if they have the same members (modulo equality definitions for the type of objects they contain). An immutable bag (set) is never equal to a mutable bag (set). Thus, a query rewrite that rewrites the OQL query,

#### SELECT x

#### ${\tt FROM} \; x \; {\tt IN} \; {\tt Coms}$

to "Coms" is incorrect, as this rewrites a query returning an immutable collection into one that returns a mutable collection.

## 3.2.3 KOLA Primitives and Formers

The operators of KOLA are listed in Tables 3.1 (primitives), 3.2 (formers) and 3.3 (query formers). Each primitive or former is named in the left columns of these tables, and given

an operational semantics in the right columns of these tables. These tables are intended to provide a brief summary of KOLA, and therefore express KOLA's semantics somewhat informally. A formal semantics of KOLA expressed in Larch [46] is presented in Appendix A.

## Table 3.1: KOLA's Primitives

KOLA's primitives functions and predicates are listed in Table 3.1. The operational semantics of these primitives are defined by showing the result of invoking these primitives on arbitrary objects (x, y and z), integers or floats (i and j), bags (A and B) and bags containing bags (X).

Primitive functions include the *identity function* (id) defined over all types, and *projection functions* ( $\pi_1$  and  $\pi_2$ ) and *shifting functions* (shl and shr) defined over pairs. Integer and float primitives include an absolute value function (abs) and basic arithmetic operations (add, sub, mul, and div). The remainder function, mod is also a primitive defined on pairs of integers only. String functions include an *indexing* function on (*string* × *integer*) pairs to isolate a character in the string (at) and a string *concatenation* function on pairs of strings (concat). Bag primitives include a *singleton* constructor (single), an *element extraction* function (elt), a *duplicate removal* function (set), a nested bag *flattening* function (flat), bag *union* (uni), *intersection* (int) and *difference* (dif) operators over pairs of bags, an insertion function (ins), and aggregate operators max, min, cnt, sum and avg. KOLA's aggregates as defined in [28]. Therefore, some of these aggregates (e.g., MAX) return NULL when invoked on empty collections.

Basic predicate primitives include *equality* (**eq**) and *inequality* (**neq**) predicates on pairs of objects of the same type. String, float and integer predicate primitives include the *ordering relations* (**lt**, **leq**, **gt** and **geq**) on pairs of integers and pairs of strings. Not listed but assumed are schema-dependent functions and predicates based on unary methods or attributes of objects such as **pty** and **chair**. The semantics of such primitives are determined by the population of the underlying database.

#### Table 3.2: KOLA's Basic Formers

KOLA's basic function and predicate formers are listed in Table 3.2. The operational semantics of functions and predicates formed with these formers are given in terms of arbitrary functions (f and g), predicates (p and q), objects (x and y) and bools (b).

Description	Semantics					
Basic Function Primitives						
identity	id ! $x = x$					
projection $(1)$	$\pi_1$ ! $[x, y]$ = $x$					
projection (2)	$\pi_2$ ! $[x, y] = y$					
shift left	shl ! [x, [y, z]] = [[x, y], z]					
shift right	shr ! [[x, y], z] = [x, [y, z]]					
Int and	<i>L</i> Float Function Primitives (i, j integers or floats)					
absolute value	$\mathbf{abs} \ ! \ i \ = \  i $					
addition	$\mathbf{add} \hspace{.1cm} ! \hspace{.1cm} [i, \hspace{.1cm} j] \hspace{.1cm} = \hspace{.1cm} i + j$					
subtraction	$\mathbf{sub}$ ! $[i, j] = i - j$					
multiplication	$\mathbf{mul}  !  [i, j]  =  i * j$					
division	$\operatorname{\mathbf{div}}$ ! $[i, j]$ = $i/j$					
modulus	<b>mod</b> ! $[i, j] = i \mod j$ (for integers $i$ and $j$ only	)				
String I	Function Primitives (s, t strings (arrays of chars))					
string indexing	$\mathbf{at}$ ! $[s, i]$ = $s[i]$					
string concatenation	$\mathbf{concat}  !  [s, t] = s \parallel t$					
Bag H	Function Primitives (A, B bags, X a bag of bags)					
singleton	single ! $x = \{x\}$					
element extraction	elt ! $\{\!\!\{x\}\!\!\}$ = $x$					
$duplicate \ removal$	$\mathbf{set} \ ! \ A  =  \{x     x \in A\}$					
bag flattening	flat ! $X = \{x^{ij}   x^i \in A, A^j \in X\}$					
bag union	<b>uni</b> ! $[A, B] = \{x^{(i+j)}   x^i \in A, x^j \in B\}$					
bag intersection	int ! [A, B] = { $x^{min(i,j)}   x^i \in A, x^j \in B$ }					
bag difference	dif ! [A, B] = { $x^{(i-j)}   x^i \in A, x^j \in B, i > j$ }					
insertion	ins ! $[x, A] =$ uni ! $[\{x\}, A]$					
Aggregate Prim	itives (A a bag of integers or floats, u, v integers or floats)					
maximum	$\max \ ! \ A = v \ s.t. \ (v^i \in A \ \land \ \forall u(u^j \in A \Rightarrow v \geq v)) $	(u))				
minimum	$\min ! A = v \ s.t. \ (v^i \in A \land \forall u(u^j \in A \Rightarrow v \leq a))$	$(\underline{s} u))$				
count	$\mathbf{cnt} \hspace{.1cm} ! \hspace{.1cm} A \hspace{.1cm} = \hspace{.1cm} \sum_{v^i \hspace{.1cm} \in \hspace{.1cm} A} (i)$					
sum	sum ! $A = \sum_{v^i \in A} (vi)$					
average	$\mathbf{avg} ! A = (\mathbf{sum} ! A) / (\mathbf{cnt} ! A)$					
Basic Predicate Primitives $(x \text{ and } y \text{ of type } T)$						
equality	eq ? $[x, y] = x = y$					
inequality	$\mathbf{neq}$ ? $[x, y] = x \neq y$					
String, Float and Int Predicate Primitives (x and y strings or integers)						
less than	lt ? $[x, y] = x < y$					
less than or equal	leq ? $[x, y] = x \le y$					
greater than	$\mathbf{gt}$ ? $[x, y] = x > y$					
greater than or equal	$\mathbf{geq}$ ? $[x, y] = x \ge y$					

Table 3.1: KOLA Primitives

Description	Semantics				
Basic Function Formers					
composition	$(f \circ g) \mathrel{!} x$	=	f ! (g ! x)		
pairing	$\langle f, \ g  angle$ ! $x$	=	[f ! x, g ! x]		
products	$(f \times g) ! [x, y]$	=	[f ! x, g ! y]		
$constant\ function$	${f K}_f$ $(x)$ ! $y$	=	x		
curried function	$\mathtt{C}_f~(f,~x)$ ! $y$	=	$f \hspace{0.1cm} ! \hspace{0.1cm} [x, \hspace{0.1cm} y]$		
conditional function	$\mathbf{con} \ (p, \ f, \ g) \ ! \ x$	=	$\begin{cases} f ! x, & \text{if } p ? x \\ g ! x, & \text{else} \end{cases}$		
Basic Predicate Formers					
combination	$(p \oplus f)$ ? $x$	=	p ? (f ! x)		
conjunction	(p & q) ? $x$	=	$(p ? x) \land (q ? x)$		
disjunction	$(p \mid q)$ ? $x$	=	$(p ? x) \lor (q ? x)$		
negation	$\sim$ $(p)$ ? $x$	=	$\neg (p ? x)$		
inverse	$p^{-1}$ ? [ $x, y$ ]	=	p ? [ $y, x$ ]		
products	$(p \times q)$ ? $[x, y]$	=	$(p ? x) \land (q ? y)$		
$constant\ predicate$	$\mathtt{K}_p$ $(b)$ ? $x$	=	b		
curried predicate	${ t C}_p \ (p, \ x)$ ? $y$	=	p ? $[x, y]$		

Table 3.2: Basic KOLA Formers

Function formers include the function *composition* former ( $\circ$ ), the function *pairing* former ( $\langle \rangle$ ) that produces functions that construct pairs, the *pairwise product* function former ( $\times$ ) that applies separate functions to separate members of a pair to produce another pair, the *constant function* former ( $K_f$ ) that builds a function that always returns the same result, the *currying* function former ( $C_f$ ) that fixes one argument of a binary (pair) function to produce a unary function and a *conditional* function former (**con**) that applies one of two functions to its arguments depending on whether a given predicate holds.

KOLA's predicate formers include the predicate/function combination former  $(\oplus)$  that acts much like function composition but producing a predicate, the logic-inspired conjunction, disjunction and negation predicate formers  $(\&, | \text{ and } \sim)$ , the predicate inverse former  $(^{-1})$  that flips its pair argument before applying a given predicate, a pairwise predicate former  $(\times)$  that applies distinct predicates to each element of a pair, a constant predicate former  $(K_p)$  that always returns true or always returns false, and a currying predicate former  $(C_p)$  that fixes one of the arguments of a binary predicate to produce a unary predicate.

Description	Semantics				
Query Function Formers					
iteration	iterate $(p, f) ! A = \{ (f ! x)^i   x^i \in A, p ? x \}$				
$iteration_2$	iter $(p, f) ! [x, B] = \{ (f ! [x, y])^j   y^j \in B, p ? [x, y] \}$				
unnest	<b>unnest</b> $(f, g) ! A = \{ (f ! [x, y])^{ij}   x^i \in A, y^j \in (g ! x) \}$				
join	$\mathbf{join}~(p,~f)$ ! [A, B] =				
	$\{(f \ ! \ [x, y])^{ij} \mid x^i \in A,  y^j \in B,  p \ ? \ [x, y]\}\}$				
left semijoin	<b>lsjoin</b> $(p, f)$ ! $[A, B] = \{ (f ! x)^i   x^i \in A, p ? [x, B] \}$				
right semijoin	<b>rsjoin</b> $(p, f)$ ! $[A, B] = \{ (f ! y)^j   y^j \in B, p ? [y, A] \}$				
nested join	$\mathbf{njoin} \ (p, \ f, \ g) \ ! \ [A, \ B] =$				
	$\{  \llbracket x, \ g \ ! \ \{ (f \ ! \ y)^j     y^j \in B, \ p \ ? \ \llbracket x, \ y \rrbracket \} \}     x \in A \}$				
Query Predicate Formers					
Ξ	exists (p) ? $A = \exists x \ (x \in A \land p ? x)$				
$\forall$	forall $(p)$ ? $A = \forall x (x \in A \Rightarrow p ? x)$				
$\exists _2$	<b>ex</b> $(p)$ ? $[x, B] = \exists y (y \in B \land p ? [x, y])$				
$\forall _{2}$	$\mathbf{fa} \ (p) \ ? \ [x, B] \ = \forall y \ (y \in B \ \Rightarrow \ p \ ? \ [x, y])$				

Table 3.3: KOLA Query Formers

## Table 3.3: KOLA's Query Formers

A query former is simply a former that constructs a function or predicate on bags. KOLA's query formers are listed in Table 3.3. As with tables 3.2, p and q denote predicates, f, g and h denote functions, and x and y denote function and predicate arguments. As well, A and B denote bags, X denotes a bag of bags and i and j are integers denoting element counts.

KOLA's Function Formers: KOLA's function query formers include the following:

- iterate (p, f) forms a function on bags, A that behaves much like SQL/OQL's SELECT-FROM-WHERE in that it invokes a function (f) on every element of A that satisfies a predicate (p).
- iter (p, f) forms a function on object, bag pairs, [x, B] that behaves much like iterate but absorbs the constant x into binary predicate p and binary function f.
- unnest (f, g) forms a function on bags A that returns a bag of elements, f ! [x, y] for each x drawn from A and each y drawn from (g ! x).

- join (p, f) forms a function on pairs of bags, [A, B] that applies f to every pair of elements, [x, y] such that x is in A, y is in B and the pair [x, y] satisfies p.
- Isjoin (p, f) (short for *left semijoin*) forms a function on pairs of bags, [A, B] that applies f to every element of A, x for which [x, B] satisfies p.
- rsjoin (p, f) (short for *right semijoin*) forms a function on pairs of bags, [A, B] that applies f to every element of B, y for which [y, A] satisfies p.
- njoin (p, f, g) (short for nested join) forms a function on pairs of bags, [A, B] that returns a set of pairs, [x, S<sub>x</sub>] for each x ∈ A. For a given x, S<sub>x</sub> is the result of invoking g on the collection of (f ! y)'s such that y ∈ B and [x, y] satisfies p. For example, the SQL query,

SELECT 
$$T.c_1$$
, agg  $(T.c_2)$   
FROM  $T$   
GROUP BY  $T.c_1$ 

would be translated into the KOLA query,

 $\mathbf{njoin} \ (\mathbf{eq} \oplus (\mathbf{id} \times \mathtt{c_1}), \, \mathtt{c_2}, \, \overline{\mathtt{agg}}) \ ! \ [\mathbf{iterate} \ (\mathtt{K}_p \ (\mathtt{true}), \, \mathtt{c_1}) \ ! \ T, \, T]$ 

such that  $\overline{\text{agg}}$  is the KOLA equivalent of SQL aggregate, agg (e.g.,  $\overline{\text{COUNT}} = \text{cnt}$ ,  $\overline{\text{SUM}} = \text{sum}$ ).

Nested joins formed by **njoin** can also express groupings resulting from joins and outerjoins. For example, the SQL join query,

```
SELECT T_1.c_1, agg (T_2.c_2)
FROM T_1, T_2
WHERE T_1.c_3 == T_2.c_3
GROUP BY T_1.c_1
```

is equivalent to the KOLA query,

njoin (eq  $\oplus$  ( $\pi_1 \times$  ( $c_1 \circ \pi_1$ )),  $\pi_2$ ,  $\overline{agg}$ ) ! [iterate ( $K_p$  (true),  $c_1 \circ \pi_1$ ) ! A, A] such that

$$A = \mathbf{join} \ (\mathbf{eq} \oplus (\mathbf{c_3} \times \mathbf{c_3}), \ \mathbf{id} \times \mathbf{c_2}) \ ! \ [T_1, T_2].$$

The SQL outerjoin query,

SELECT 
$$T_1.c_1$$
, agg  $(T.c_2)$   
FROM  $T_1$  LEFT JOIN  $T_2$  ON  $T_1.c_1 == T_2.c_1$   
GROUP BY  $T_1.c_1$ 

is expressed in similar fashion to GROUP BY queries:

$$\mathbf{njoin} \ (\mathbf{eq} \oplus (\mathbf{id} \times \mathtt{c_1}), \, \mathtt{c_2}, \, \overline{\mathbf{agg}}) \, ! \, [\mathbf{iterate} \ (\mathtt{K}_p \ (\mathtt{true}), \, \mathtt{c_1}) \, ! \, T_1, \, T_2].$$

Note that if for some element of  $t_1 \in T_1$  there are no elements  $t_2 \in T_2$  such that

```
t_1.c_1 == t_2.c_2,
```

then  $t_1.c_1$  will be paired with  $(\overline{agg} ! \oslash)$  in the result. If agg is an aggregate that returns NULL when applied to an empty collection (such as MAX), then  $(\overline{agg} ! \oslash)$  is also NULL and  $t_1.c_1$  is paired with NULL in the result.

The OQL query below partitions a bag on the basis of predicates  $p_1, \ldots, p_n$ .

```
SELECT * FROM t IN T GROUP BY label_1 : p_1, ..., label_n : p_n.
```

The result of this query is a set of tuples consisting of n + 1 fields. The first n fields contain the truth values for the n predicates for a given partition of elements of Tthat agree on these values. The  $(n + 1)^{th}$  field contains the associated partition of T. The KOLA version of this query uses functions of the form,

$$f_i = \operatorname{con} (\overline{p_i}, K_f (1), K_f (0)),$$

that when invoked on some object, x, return a 1 or 0 depending on whether predicate  $\overline{p_i}$  (the KOLA translation of  $p_i$ ) is satisfied by x. The partition of T is then based on equivalence of the bitstring formed by applying functions  $f_i$  for each  $1 \le i \le n$ . That is, given

$$f = \langle f_1, \langle f_2, \ldots \langle f_{n-1}, f_n \rangle \ldots \rangle \rangle,$$

the KOLA equivalent to the OQL query above is:

njoin (eq  $\oplus$  (id  $\times$  f), id, id) ! [iterate (K<sub>p</sub> (true), f) ! T, T].

KOLA's Predicate Formers: KOLA's query predicate formers include the following.

- Formers exists (p) and forall (p) form existential and universal quantifier predicates on bags A that return *true* if some (all) elements of A satisfy p.
- Formers **ex** and **fa** are to **exists** and **forall** as **iter** is to **iterate**. Like functions formed with **iter**, **ex** (p) and **fa** (p) are invoked on pairs of the form [x, B], such that x is absorbed into the predicate, p. The result of invocation depends on whether any (**ex**) or all (**fa**) elements y in B are such that (p ? [x, y]) holds.

## 3.3 Using a Theorem Prover to Verify KOLA Rewrites

## 3.3.1 A Formal Specification of KOLA Using LSL

Appendix A contains a formal specification of the KOLA data model and algebra. The specification is expressed in the Larch algebraic specification language, LSL. LSL permits the definition of *traits*, which roughly correspond to *abstract data types* [72]. LSL includes a library of basic traits such as Int, Bool, FloatingPoint and String, which are assumed by the KOLA specification.

KOLA bags (bag [T]) are defined by two traits: BagBasics (which defines bag constructors, {} and insert and unary operators on bags) and Bag which defines binary bag operators (such as union and intersection) These traits introduce the bag *constructors*,

as well as operators,

membership:	$- \in -:$	T, bag [T]	$\rightarrow$	Bool,
element difference:	:	bag [T], T	$\rightarrow$	bag [T],
bag union:	∪:	bag [T], bag [T]	$\rightarrow$	bag [T],
bag intersection:	∩:	bag [T], bag [T]	$\rightarrow$	bag [T], and
bag difference:	:	bag [T], bag [T]	$\rightarrow$	bag [T].

The axioms for these operators assume universally quantified variables A and B of type bag [T] and x and y of type T. Membership is defined by the axioms:

$$\begin{split} & x \in \{\} &= \text{ false, and} \\ & x \in \text{insert } (y, \text{ A}) &= (x == y) \ \lor \ (x \in \text{A}).^7 \end{split}$$

Element difference is defined by axioms:

$$\{\} - x = \{\}, \text{ and} \\ \neg (x == y) \Rightarrow (\text{insert} (x, A) - y == \text{insert} (x, A - y)).$$

Bag union, intersection and difference are defined by axioms:

(1) {}  $\cup$  B = B, (2) insert (x, A)  $\cup$  B = insert (x, A  $\cup$  B), (3) {}  $\cap$  B = {}, (4) x  $\in$  B  $\Rightarrow$  (insert (x, A)  $\cap$  B == insert (x, A  $\cap$  (B - x))), (5)  $\neg$  (x  $\in$  B)  $\Rightarrow$  (insert (x, A)  $\cap$  B == A  $\cap$  B) (6) {} - B = {}.

(0) 
$$\{\} - B = \{\},$$
  
(7)  $\mathbf{x} \in \mathbf{B} \Rightarrow (\text{insert}(\mathbf{x}, \mathbf{A}) - \mathbf{B} == \mathbf{A} - (\mathbf{B} - \mathbf{x})), \text{ and}$   
(8)  $\neg (\mathbf{x} \in \mathbf{B}) \Rightarrow (\text{insert}(\mathbf{x}, \mathbf{A}) - \mathbf{B} == \text{insert}(\mathbf{x}, \mathbf{A} - \mathbf{B})).$ 

These axioms are typical of algebraic specifications, in that they define each operator over each constructor. Note that the use of the element difference operator "-" in axioms (4) and (7) distinguishes the definition of bags from sets. The corresponding axioms for sets would be:

(4b) 
$$\mathbf{x} \in \mathbf{B} \Rightarrow (\text{insert} (\mathbf{x}, \mathbf{A}) \cap \mathbf{B} == \text{insert} (\mathbf{x}, \mathbf{A} \cap \mathbf{B}))$$
, and  
(7b)  $\mathbf{x} \in \mathbf{B} \Rightarrow (\text{insert} (\mathbf{x}, \mathbf{A}) - \mathbf{B} == \mathbf{A} - \mathbf{B})$ .

Note also that the axiom defining the singleton bag,  $\{x\}$ , establishes it as shorthand for insert  $(x, \{\})$ . Therefore, this constructor does not need to be accounted for in these axioms.

All function primitives and formers "inherit" the generic Function specification, which introduces invocation (\_ ! \_\_: fun [T, U], T  $\rightarrow$  U) (for domain type T and range type U), and function equality (\_\_ == \_: fun [T, U], fun [T, U]  $\rightarrow$  Bool), which is defined universally for functions f and g (fun [T, U]) by the axiom,

$$f == g = \forall x:T (f ! x == g ! x).$$

Similarly, predicate primitives and formers "inherit" the generic Predicate specification, which introduces invocation (\_? \_: pred [T],  $T \rightarrow Bool$ ) (for domain type T), and predicate equality (\_ == \_: pred [T], pred [T] \rightarrow Bool) which is defined universally for predicates p and q (pred [T]) by the axiom,

$$\mathbf{p} == \mathbf{q} = \forall \mathbf{x} : \mathbf{T} (\mathbf{p} ? \mathbf{x} == \mathbf{q} ? \mathbf{x}).$$

The axioms defining all KOLA predicate and function primitives and formers are given in Appendix A. Axioms defining basic primitives and formers (i.e., defining functions and predicates on arguments that are not collections) resemble the equations shown in Tables 3.1 and 3.2. Query primitives and formers are defined inductively over bag constructors {} and insert, as in the axioms for

iterate: pred [T], fun [T,U]  $\rightarrow$  fun [bag [T], bag [U]]

shown below:

 $\neg (p ? x) \Rightarrow (iterate (p, f) ! insert (x, A) == iterate (p, f) ! A).$ 

## 3.3.2 Proving KOLA Rewrite Rules Using LP

Theorem provers are term rewriters that apply rewrite rules to simplify terms. The LP theorem prover interprets notation that resembles the notation of logic proofs as operations to the term rewriting system. LP then gives the following operational interpretations to these elements of logical proofs:

- the operational interpretation of a conjecture, goal or subgoal is a term,
- the operational interpretation of an axiom is a rewrite rule, and
- the operational interpretation of a proof is a rewrite of a term (conjecture) to the built-in term true.<sup>8</sup>

To illustrate the operation of LP, we demonstrate a proof of the KOLA rewrite rule that pushes projections and selections past unions::

iterate  $(p, f) ! (A \cup B) \stackrel{\rightarrow}{=} (\text{iterate } (p, f) ! A) \cup (\text{iterate } (p, f) ! B).$ 

e == e

 $<sup>^{8}</sup>$ Larch uses a number of built-in rewrite rules to supplement those that are generated from formal specifications. For example, Larch has a rewrite rule that rewrites any term of the form

for some expression e into the term true. Therefore, rewrites of conjectures into the term true are possible even when true does not appear as a term in a formal specification, as in the specification of KOLA.

```
prove
iterate (p, f) ! (A \setminus U B) =
 (iterate (p, f) ! A) \U (iterate (p, f) ! B)
. .
 resume by induction on A
                                         % Step 1
   % Base Case: Trivial
   % Trivial Case
                                         % Step 2
     resume by induction on B
      % Base Case: Trivial
      % Trivial Case
        resume by cases p ? u1
                                         % Step 3
        % Case 1
          resume by cases pc ? u
                                         % Step 4a
        % Case 2
                                         % Step 4b
          resume by cases pc ? u
```

## qed

Figure 3.6: An Example LP Proof Script

As with OQL rules, KOLA rules are expressed with patterns (KOLA queries supplemented with pattern variables) separated by " $\stackrel{\longrightarrow}{=}$ ". Verification of this rule requires proving the LP conjecture

```
iterate (p, f) ! (A U B) = (iterate (p, f) ! A) U (iterate (p, f) ! B)
```

Verification of this conjecture proceeds according to the the *proof script* shown in Figure 3.6<sup>9</sup>. To facilitate the tracing of this script, we have numbered the steps that appear in the script in comments (delimited by %) to the right of each executable statement. Below we trace the logic behind the proof, and the mechanics of the theorem prover as it processes each step's instruction.

<sup>&</sup>lt;sup>9</sup>We use ASCII notation in presenting inputs to LP (e.g.,  $\forall U$  is used instead of  $\cup$ , **p** is used instead of p etc.) to emphasize their executable flavor.

```
1. {} \U B --> B
2. insert (x, A) \U B --> insert (x, A \U B)
3. iterate (p, f) ! {} --> {}
4. (p ? x) ::
    iterate (p, f) ! insert (x, A) --> insert (f ! x, iterate (p, f) ! A)
5. ~(p ? x) ::
    iterate (p, f) ! insert (x, A) --> iterate (p, f) ! A
```

Figure 3.7: Some LP Rewrite Rules Generated from Specification Axioms

The proof begins with the generation of a bank of rewrite rules from the axioms defining the operators appearing in the proof. For this proof, these axioms generate a bank of rewrite rules that include those shown in Figure 3.7. As with KOLA's rewrite rules, LP's rewrite rules consist of pairs of patterns (separated by "-->" rather than  $\stackrel{=}{=}$  to distinguish them from KOLA rules). As well, LP's rules can be *conditional* — an idea inspiring extensions to KOLA presented in Chapter 5. Rules 4 and 5 can fire only if the conditions, (p ? x) and ~ (p ? x) are respectively satisfied.

**Step 1:** The proof begins by induction on the collection **A**. The theorem prover interprets this instruction by first creating the basis subgoal,

iterate (p, f) ! ({} \U B) ==
 (iterate (p, f) ! {}) \U (iterate (p, f) ! B).

This subgoal trivially reduces to **true** (i.e., is proven) by LP rewrite rules 1 and 3 of Figure 3.7.

Successful proof of the basis subgoal initiates the addition of a new rewrite rule (corresponding to the induction hypothesis) and the attempted proof of a second subgoal (corresponding to the induction subgoal). For this proof, the induction hypothesis is the rewrite rule,

```
iterate (p, f) ! (Ac \U B) -->
  (iterate (p, f) ! Ac) \U (iterate (p, f) ! B)
```

and the induction subgoal is,

```
iterate (p, f) ! (insert (u, Ac) \U B) ==
  (iterate (p, f) ! insert (u, Ac)) \U (iterate (p, f) ! B)
```

**Step 2:** Induction is again initiated, this time on the collection B in order to prove the induction subgoal remaining after step 1. The basis subgoal,

```
iterate (p, f) ! (insert (u, Ac) \U {}) ==
  (iterate (p, f) ! insert (u, Ac)) \U (iterate (p, f) ! {})
```

again reduces to true by rewrite rules 1 and 3 of Figure 3.7. Again, a rewrite rule corresponding to a induction hypothesis is added:

```
iterate (p, f) ! insert (u, Ac \U Bc) ==
  (iterate (p, f) ! insert (u, Ac)) \U (iterate (p, f) ! Bc)
```

and a new induction subgoal is generated:

```
iterate (p, f) ! insert (u, Ac \U insert (u1, Bc)) ==
(iterate (p, f) ! insert (u, Ac)) \U (iterate (p, f) ! insert (u1, Bc))
```

**Step 3:** The rest of the proof proceeds by cases. A proof by cases requires proving the current subgoal assuming each case in turn. The assumption of a case is captured operationally by adding the rewrite rule,  $p \rightarrow true$  (such that p is the term corresponding to the case) to the bank of rewrite rules available to the rest of the proof. Step 3 first adds the rewrite rule,

p ? u1 --> true

to the bank of rewrite rules.

**Step 4a:** A second case is assumed, adding

p ? u --> true

to the bank of rewrite rules. This rule, taken with the rule generated in step 3 and rule 4 of Figure 3.7 is sufficient to prove the induction subgoal. Then the converse case is considered, with

p ? u --> false

added to the bank of rewrite rules in place of the previously added rule. Again, the induction subgoal is proved using this rule, the rule added in step 3 and rule 5 of Figure 3.7.

**Step 4b:** Having proven the conjecture assuming the case, p ? u1 (Step 3), the converse case is assumed and

p ? u1 --> false

is added to the bank of rewrite rules replacing the rule added in Step 3. As in Step 4a, a second case adds

and

p ? u --> false

successively to the bank of rewrite rules. The induction subgoal is proven in both cases with the rewrite rules generated from the case assumptions, and rules 4 and 5 of Figure 3.7.  $\Box$ 

Proofs such as that for the rewrite rule shown above have been completed for well over 300 KOLA rules. LP proof scripts that execute the operational versions of some of these proofs are available electronically from the addresses listed in Appendix B.

## 3.4 Revisiting the "Conflict of Interests" Queries

In this section, we revisit the "Conflict of Interests" queries presented earlier in this chapter and in Chapter 2. In Section 3.4.1, we show how each OQL query,  $COI_1$  (Figure 2.1),  $COI_{1*}$  (Figure 3.4),  $\overline{COI_1}$  (Figure 2.2), and  $COI_2$ ,  $\overline{COI_2}$  and  $\overline{COI_2}$  (Figure 3.2), would get expressed in KOLA. Then in Section 3.4.2, we show how the same set of rules and sequence of rule applications rewrites KOLA translations of  $COI_1$ ,  $COI_2$ , and  $COI_{1*}$  into their final forms. The point of this section is to show that these rewrites, when expressed over KOLA query representations, can be expressed without code.

## 3.4.1 KOLA Translations of the COI Queries

Figure 3.8 shows KOLA translations of the Conflicts of Interests queries of Chapter 2 and Section 3.1.1. Queries 1–3 in this figure are translations of  $COI_1$ ,  $COI_{1*}$  and  $\overline{COI_1}$  from Figures 2.1, 3.4a and 2.2 respectively. Queries 4–6 are translations of queries  $COI_2$ ,  $\overline{COI_2}$ , and  $\overline{COI_2}$  from Figure 3.2. As before, we begin this section begins by tracing the reductions of these queries to show that they are valid translations of their OQL equivalents.

Queries 1, 2 and 3 of Figure 3.8 are the KOLA translations of OQL queries  $COI_1$ ,  $COI_{1*}$  and  $\overline{COI_1}$  (from Figures 2.1, 3.4a and 2.2) respectively. Therefore, each of these

1. set ! (iterate (ex 
$$(\overline{p}) \oplus \langle id, \overline{f} \rangle, id)$$
 ! Coms)  
 $COI_1^K$ : A KOLA Translation of COI<sub>1</sub> (Figure 2.1)

2. set ! (iterate (ex (
$$\overline{\mathbf{p}} \& \overline{\mathbf{q}}$$
)  $\oplus \langle \mathbf{id}, \mathsf{K}_f (\mathsf{SComs}) \rangle$ , id) ! Coms)  
 $COI_{1*}^K$ : A KOLA Translation of COI<sub>1\*</sub> (Figure 3.4a)

3. set ! (join (
$$\overline{\mathbf{r}} \& (\mathbf{ex} (\overline{\mathbf{p}}) \oplus (\mathbf{id} \times \pi_2)), \pi_1$$
) ! [Coms, Temp<sub>K</sub>])  
 $\overline{COI_1^K}$ : A KOLA Translation of  $\overline{COI_1}$  (Figure 2.2)

4. set ! (iterate (ex 
$$(\overline{p_2}) \oplus \langle id, \overline{f} \rangle, id)$$
 ! Coms)  
 $COI_2^K$ : A KOLA Translation of  $COI_2$  (Figure 3.2)

5. set ! (join (
$$\overline{\mathbf{r}} \& (\mathbf{ex} (\overline{\mathbf{p}_2}) \oplus (\mathbf{id} \times \pi_2)), \pi_1$$
) ! [Coms, Temp<sub>K</sub>])  
 $\overline{COI_2^K}$ : A KOLA Translation of  $\overline{COI_2}$  (Figure 3.2)

6. set ! (join (
$$\overline{\mathbf{r}}, \pi_1$$
) ! [Coms, iterate ( $\overline{\mathbf{p}_3}, \mathbf{id}$ ) ! Temp<sub>K</sub>])  
 $\overline{\overline{COI_2^K}}$ : A KOLA Translation of  $\overline{\overline{COI_2}}$  (Figure 3.2)

such that

 $\begin{array}{rcl} \overline{\mathbf{p}} &\equiv& \mathbf{ex} \ (\mathbf{eq}) \oplus \langle \mathtt{chair} \circ \pi_1, \, \mathtt{mems} \circ \pi_2 \rangle \\ \overline{\mathbf{p}_2} &\equiv& \mathbf{ex} \ (\mathbf{eq}) \oplus \langle \mathtt{chair} \circ \pi_2, \, \mathtt{mems} \circ \pi_2 \rangle \\ \overline{\mathbf{p}_3} &\equiv& \mathtt{exists} \ (\mathbf{ex} \ (\mathbf{eq}) \oplus \langle \mathtt{chair}, \, \mathtt{mems} \rangle) \oplus \pi_2 \\ \end{array}$   $\begin{array}{rcl} \overline{\mathbf{q}} &\equiv& \mathbf{eq} \oplus ((\mathtt{pty} \circ \mathtt{chair}) \times (\mathtt{pty} \circ \mathtt{chair})) \\ \overline{\mathbf{r}} &\equiv& \mathtt{eq} \oplus ((\mathtt{pty} \circ \mathtt{chair}) \times \pi_1) \\ \overline{\mathbf{f}} &\equiv& \mathtt{iter} \ (\overline{\mathbf{q}}, \, \pi_2) \circ \langle \mathtt{id}, \, \mathtt{K}_f \ (\mathtt{SComs}) \rangle \end{array}$   $\begin{array}{rcl} \mathtt{Temp}_K &\equiv& \mathtt{njoin} \ (\mathtt{eq} \oplus (\mathtt{id} \times (\mathtt{pty} \circ \mathtt{chair})), \, \mathtt{id}, \, \mathtt{id}) \ ! \\ & [\mathtt{iterate} \ (\mathtt{K}_f \ (\mathtt{true}), \, \mathtt{pty} \circ \mathtt{chair}) \ ! \ \mathtt{SComs}, \, \mathtt{SComs} \end{bmatrix} \end{array}$ 

Figure 3.8: KOLA Translations of the Conflict of Interests Queries

queries returns a set consisting of committees whose chairs are members of a subcommittee whose chair is from the same party. Queries 4, 5 and 6 of Figure 3.8 translate OQL queries  $COI_2$ ,  $\overline{COI_2}$  and  $\overline{COI_2}$  from Figure 3.2. Therefore, each of these queries returns a set of committees whose chairs who belong to a party that includes someone who both chairs and is a member of the same subcommittee. All of these queries remove duplicates from intermediate subquery results generated with **iterate** or **join**.

These queries are fairly complex, and are easiest to understand when decomposed. Therefore, we begin by examining some of the common subexpressions that appear in these queries.

1. The predicate  $\overline{p}$ ,

 $\mathbf{ex} \ (\mathbf{eq}) \oplus \langle \texttt{chair} \circ \pi_1, \, \texttt{mems} \circ \pi_2 \rangle$ 

appears in queries 1, 2 and 3, and is a predicate on committee, subcommittee pairs, [x, y]. The expression,  $\overline{p}$ ? [x, y] reduces as follows:

$$(\mathbf{ex} \ (\mathbf{eq}) \oplus \langle \mathbf{chair} \circ \pi_1, \, \mathbf{mems} \circ \pi_2 \rangle) ? [x, y] \\ = \mathbf{ex} \ (\mathbf{eq}) ? (\langle \mathbf{chair} \circ \pi_1, \, \mathbf{mems} \circ \pi_2 \rangle ! [x, y]) \\ = \mathbf{ex} \ (\mathbf{eq}) ? [(\mathbf{chair} \circ \pi_1) ! [x, y], \, (\mathbf{mems} \circ \pi_2) ! [x, y]] \\ = \mathbf{ex} \ (\mathbf{eq}) ? [(\mathbf{chair} \circ \pi_1) ! [x, y], \, \mathbf{mems} ! (\pi_2 ! [x, y])] \\ = \mathbf{ex} \ (\mathbf{eq}) ? [(\mathbf{chair} ! x, \, \mathbf{mems} ! y] \\ = \mathbf{ex} \ (\mathbf{eq}) ? [\mathbf{chair} ! x, \, \mathbf{mems}] \\ = \exists z : Legislator(z \in y. \mathbf{mems} \land \mathbf{eq} ? [x. \mathbf{chair}, z]) \\ = \exists z : Legislator(z \in y. \mathbf{mems} \land x. \mathbf{chair} == z) \\ = x. \mathbf{chair} \in y. \mathbf{mems}$$

Therefore,  $\overline{p}$ ? [x, y] is equivalent to the OQL boolean expression,

$$x.\texttt{chair IN } y.\texttt{mems}$$

2. The predicate  $\overline{p_2}$ ,

$$\mathbf{ex} \ (\mathbf{eq}) \oplus \langle \mathtt{chair} \circ \pi_2, \, \mathtt{mems} \circ \pi_2 \rangle$$

appears in queries 4 and 5, and is similar to  $\overline{p}$  in that it too is a predicate on committee, subcommittee pairs, [x, y]. However,  $\overline{p_2}$  ignores x as shown in the reduction below.

```
(\mathbf{ex} \ (\mathbf{eq}) \oplus \langle \mathtt{chair} \circ \pi_2, \, \mathtt{mems} \circ \pi_2 \rangle) ? [x, y]
```

 $= \mathbf{ex} (\mathbf{eq}) ? (\langle \operatorname{chair} \circ \pi_2, \operatorname{mems} \circ \pi_2 \rangle ! [x, y])$   $= \mathbf{ex} (\mathbf{eq}) ? [(\operatorname{chair} \circ \pi_2) ! [x, y], (\operatorname{mems} \circ \pi_2) ! [x, y]]$   $= \mathbf{ex} (\mathbf{eq}) ? [(\operatorname{chair} \circ \pi_2) ! [x, y], \operatorname{mems} ! (\pi_2 ! [x, y])]$   $= \mathbf{ex} (\mathbf{eq}) ? [\operatorname{chair} ! y, \operatorname{mems} ! y]$   $= \mathbf{ex} (\mathbf{eq}) ? [y.\operatorname{chair}, y.\operatorname{mems}]$   $= \exists z : Legislator(z \in y.\operatorname{mems} \land \mathbf{eq} ? [y.\operatorname{chair}, z])$   $= \exists z : Legislator(z \in y.\operatorname{mems} \land y.\operatorname{chair} == z)$   $= y.\operatorname{chair} \in y.\operatorname{mems}$ 

Therefore,  $\overline{\mathbf{p}_2}$  ? [x, y] is equivalent to the OQL boolean expression,

$$y.\texttt{chair IN} y.\texttt{mems}$$

3. The predicate  $\overline{p_3}$ ,

 $\mathbf{exists} \ (\mathbf{ex} \ (\mathbf{eq}) \oplus \langle \texttt{chair}, \, \texttt{mems} \rangle) \oplus \pi_2$ 

appears in query 6, and is a predicate on pairs, [p, S], such that p is the name of a party and S is a set of subcommittees. Reducing  $\overline{p_3}$ ? [p, S], we get:

$$\begin{array}{rcl} (\text{exists } (\text{ex} \ (\text{eq}) \oplus \langle \text{chair, mems} \rangle) \oplus \pi_2) ? [p, S] \\ = & \text{exists } (\text{ex} \ (\text{eq}) \oplus \langle \text{chair, mems} \rangle) ? (\pi_2 ! [p, S]) \\ = & \text{exists } (\text{ex} \ (\text{eq}) \oplus \langle \text{chair, mems} \rangle) ? S \\ = & \exists y \ (y \in S \land (\text{ex} \ (\text{eq}) \oplus \langle \text{chair, mems} \rangle) ? y) \\ = & \exists y \ (y \in S \land \text{ex} \ (\text{eq}) ? (\langle \text{chair, mems} \rangle ! y)) \\ = & \exists y \ (y \in S \land \text{ex} \ (\text{eq}) ? [y.\text{chair, y.mems}]) \\ = & \exists y \ (y \in S \land \exists z \ (z \in y.\text{mems} \land \text{eq} ? [y.\text{chair, z}])) \\ = & \exists y \ (y \in S \land \exists z \ (z \in y.\text{mems} \land y.\text{chair == }z)) \\ = & \exists y \ (y \in S \land (y.\text{chair} \in y.\text{mems})). \end{array}$$

Thus,  $\overline{p_3}$ ? [p, S], is equivalent to the OQL boolean expression,

EXISTS 
$$y$$
 IN  $S : (y.chair IN y.mems)$ .

4. The predicate  $\overline{q}$ ,

$$\mathbf{eq} \, \oplus \, ((\mathtt{pty} \circ \mathtt{chair}) \, imes \, (\mathtt{pty} \circ \mathtt{chair}))$$
appears in every query in Figure 3.8, and is a predicate on committee, subcommittee pairs, [x, y]. Reducing  $\overline{q}$ ? [x, y], we get:

Thus,  $\overline{q}$ ? [x, y], is equivalent to the OQL boolean expression,

x.chair.pty == y.chair.pty.

5. The predicate  $\overline{\mathbf{r}}$ ,

$$\mathbf{eq} \oplus ((\mathtt{pty} \circ \mathtt{chair}) imes \pi_1)$$

of queries 3, 5 and 6 is similar to  $\overline{q}$ , but is a predicate on *nested* pairs, [x, [p, S]] such that x is a committee in Coms, p is the name of a political party and S is a bag of subcommittees. Reducing  $\overline{r}$ ? [x, [p, S]], we get:

$$(eq \oplus ((pty \circ chair) \times \pi_1)) ? [x, [p, S]]$$
  
=  $eq ? (((pty \circ chair) \times \pi_1) ! [x, [p, S]])$   
=  $eq ? [(pty \circ chair) ! x, \pi_1 ! [p, S]]$   
=  $eq ? [pty ! (x.chair), p]$   
=  $eq ? [x.chair.pty, p]$   
=  $x.chair.pty == p$ 

Thus,  $\overline{\mathbf{r}}$ ? [x, [p, S]], is equivalent to the OQL boolean expression,

$$x.\texttt{chair.pty} == p.$$

6. The function  $\overline{\mathbf{f}}$ ,

iter 
$$(\overline{\mathbf{q}}, \pi_2) \circ \langle \mathbf{id}, \mathbf{K}_f (\mathbf{SComs}) \rangle$$

appears in queries 1 and 4, and is a function on committees, x. Reducing  $\overline{f} ! x$ , we get:

$$(\mathbf{iter} \ (\overline{\mathbf{q}}, \ \pi_2) \circ \langle \mathbf{id}, \ \mathsf{K}_f \ (\mathtt{SComs}) \rangle)$$
!  $x$ 

 $= \operatorname{iter} (\overline{q}, \pi_2) ! (\langle \operatorname{id}, K_f (\operatorname{SComs}) \rangle ! x)$   $= \operatorname{iter} (\overline{q}, \pi_2) ! [\operatorname{id} ! x, K_f (\operatorname{SComs}) ! x]$   $= \operatorname{iter} (\overline{q}, \pi_2) ! [x, \operatorname{SComs}]$   $= \{(\pi_2 ! [x, c])^j | c^j \in \operatorname{SComs}, \overline{q} ? [x, c]\}$   $= \{c^j | c^j \in \operatorname{SComs}, \overline{q} ? [x, c]\}$   $= \{c^j | c^j \in \operatorname{SComs}, x.\operatorname{chair.pty} == c.\operatorname{chair.pty}\}$ 

Thus,  $\overline{f}$  ! x is equivalent to the OQL query expression,

```
SELECT c
FROM c IN SComs
WHERE x.chair.pty == c.chair.pty.
```

7. Temp<sub>K</sub> is a subquery of queries 3, 5 and 6. Temp<sub>K</sub> uses iterate and njoin to generate the KOLA equivalent of subquery Temp of Figure 2.2. This is illustrated by the derivation below:

njoin (eq  $\oplus$  (id  $\times$  (pty  $\circ$  chair)), id, id) ! [iterate (K<sub>p</sub> (true), pty  $\circ$  chair) ! SComs, SComs]

- = njoin (eq  $\oplus$  (id × (pty  $\circ$  chair)), id, id) ! [{((pty  $\circ$  chair) ! c)<sup>i</sup> |  $c^i \in$  SComs, K<sub>p</sub> (true) ? c}, SComs]
- $= njoin (eq \oplus (id \times (pty \circ chair)), id, id) !$  $[\{(pty ! (chair ! c))^i | c^i \in SComs, K_p (true) ? c\}, SComs]$
- = njoin (eq  $\oplus$  (id × (pty  $\circ$  chair)), id, id) ! [{(pty ! (c.chair))<sup>i</sup> |  $c^i \in \text{SComs}$ }, SComs]
- = njoin (eq  $\oplus$  (id × (pty  $\circ$  chair)), id, id) ! [{(c.chair.pty)<sup>i</sup> |  $c^i \in \text{SComs}$ }, SComs]
- $= \{ [c.\texttt{chair.pty}, S_c] \mid c.\texttt{chair.pty} \in \{ (c.\texttt{chair.pty})^i \mid c^i \in \texttt{SComs} \} \} \ s.t.$  $S_c = \mathbf{id} ! \{ (\mathbf{id} ! s)^j \mid s^j \in \texttt{SComs}, (\mathbf{eq} \oplus (\mathbf{id} \times \texttt{pty} \circ \texttt{chair})) ? [p, s] \}$

$$= \{ s^{j} \mid s^{j} \in \text{SComs}, (\text{eq} \oplus (\text{id} \times (\text{pty} \circ \text{chair}))) ? [p, s] \}$$

$$= \{ s^{j} \mid s^{j} \in \text{SComs}, \text{eq} ? ((\text{id} \times (\text{pty} \circ \text{chair})) ! [p, s]) \}$$

$$= \{ s^{j} \mid s^{j} \in \text{SComs}, \text{eq} ? [\text{id} ! p, (\text{pty} \circ \text{chair}) ! s] \}$$

$$= \{ s^{j} \mid s^{j} \in \text{SComs}, \text{eq} ? [\text{id} ! p, \text{pty} ! (\text{chair} ! s)] \}$$

$$= \{ s^{j} \mid s^{j} \in \text{SComs}, \text{eq} ? [p, s.\text{chair.pty}] \}$$

$$= \{ s^{j} \mid s^{j} \in \text{SComs}, p == s.\text{chair.pty} \}$$

$$= \{ [c.chair.pty, S_c] \mid c^i \in \texttt{SComs} \}$$
  
s.t.  $S_c = \{ s^j \mid s^j \in \texttt{SComs}, c.chair.pty == s.chair.pty \}$ 

Therefore, this subquery returns a set of pairs, [p, S], such that p is the name of a party affiliated with some subcommittee's chair and S is the bag of all subcommittees chaired by someone from that party. In other words,  $\text{Temp}_K$  is equivalent to the OQL query,

SELECT 
$$p, S$$
: partition  
FROM  $c$  IN SComs  
GROUP BY  $p:c.chair.pty$ 

Using the subexpressions above, a description of each of the queries of Figure 3.8 follows.

 $COI_{1}^{K}$  (1):

Predicates  $\overline{\mathbf{p}}$ ,  $\overline{\mathbf{q}}$  and  $\overline{\mathbf{f}}$  are all subexpressions of  $COI_1^K$ 's subpredicate,  $(\mathbf{ex} \ (\overline{\mathbf{p}}) \oplus \langle \mathbf{id}, \overline{\mathbf{f}} \rangle)$ , which when invoked on a committee  $x \in \texttt{Coms}$  is equivalent to the OQL expression,

 $\begin{array}{l} {\tt EXISTS} \; y \; {\tt IN} \; \left( \begin{array}{c} {\tt SELECT} \; c \\ {\tt FROM} \; c \; {\tt IN} \; {\tt SComs} \\ {\tt WHERE} \; x. {\tt chair.pty} \; == \; c. {\tt chair.pty} \end{array} \right) : (x. {\tt chair} \; {\tt IN} \; y. {\tt mems}). \end{array}$ 

as is demonstrated by the derivation below:

$$\begin{array}{rcl} (\mathbf{ex} \ (\overline{\mathbf{p}}) \oplus \langle \mathbf{id}, \overline{\mathbf{f}} \rangle) ? x &=& \mathbf{ex} \ (\overline{\mathbf{p}}) ? (\langle \mathbf{id}, \overline{\mathbf{f}} \rangle \ ! \ x) \\ &=& \mathbf{ex} \ (\overline{\mathbf{p}}) ? \ [x, \overline{\mathbf{f}} \ ! \ x] \\ &=& \mathbf{ex} \ (\overline{\mathbf{p}}) ? \ [x, S_x] \\ && s.t. \ S_x \ = \ \{ c^j \ | \ c^j \in \mathsf{SComs}, \ x.\mathsf{chair.pty} == c.\mathsf{chair.pty} \} \\ &=& \exists y \ (y \in S_x \ \land \ \overline{\mathbf{p}} \ ? \ [x, y]) \\ &=& \exists y \ (y \in S_x \ \land \ x.\mathsf{chair} \in y.\mathsf{mems}) \end{array}$$

Therefore, the **iterate** subquery generates the collection derived below,

Removing duplicates from this result leaves,

$$\{x \mid x \in \texttt{Coms}, \exists y \ (y \in S_x \land x.\texttt{chair} \in y.\texttt{mems})\}$$

which is the same result returned by the OQL query,  $COI_1$ .

# $COI_{1*}^{K}$ (2):

 $COI_{1*}^{K}$  is similar to  $COI_{1}^{K}$  in that it performs duplicate elimination on the result of an **iterate** subquery, and contains the same subpredicates,  $\overline{\mathbf{p}}$  and  $\overline{\mathbf{q}}$ . But this query differs from  $COI_{1}^{K}$  in that it does not generate an intermediate collection  $(S_{x})$  for each  $x \in \text{Coms}$ . Instead, the existential predicate ( $\mathbf{ex}$  ( $\overline{\mathbf{p}} \& \overline{\mathbf{q}}$ )) searches SComs for some subcommittee y that with x satisfies both  $\overline{\mathbf{p}}$  and  $\overline{\mathbf{q}}$ . Therefore, when invoked on a committee  $x \in \text{Coms}$ , this predicate is equivalent to the OQL expression,

EXISTS y IN SComs : ((x.chair IN y.mems) AND (x.chair.pty == y.chair.pty)),

as shown by the derivation below:

$$(\mathbf{ex} \ (\overline{\mathbf{p}} \& \overline{\mathbf{q}}) \oplus \langle \mathbf{id}, \mathsf{K}_f \ (\mathsf{SComs}) \rangle) ? x$$

$$= \mathbf{ex} \ (\overline{\mathbf{p}} \& \overline{\mathbf{q}}) ? (\langle \mathbf{id}, \mathsf{K}_f \ (\mathsf{SComs}) \rangle ! x)$$

$$= \mathbf{ex} \ (\overline{\mathbf{p}} \& \overline{\mathbf{q}}) ? [\mathbf{id} ! x, \mathsf{K}_f \ (\mathsf{SComs}) ! x]$$

$$= \mathbf{ex} \ (\overline{\mathbf{p}} \& \overline{\mathbf{q}}) ? [x, \mathsf{SComs}]$$

$$= \exists y \ (y \in \mathsf{SComs} \land (\overline{\mathbf{p}} \& \overline{\mathbf{q}}) ? [x, y])$$

$$= \exists y \ (y \in \mathsf{SComs} \land \overline{\mathbf{p}} ? [x, y] \land \overline{\mathbf{q}} ? [x, y])$$

$$= \exists y \ (y \in \mathsf{SComs} \land x.\mathsf{chair} \in y.\mathsf{mems} \land x.\mathsf{chair.pty} == y.\mathsf{chair.pty})$$

Thus, the **iterate** subquery of  $COI_{1*}^K$  returns:

iterate (ex  $(\overline{p} \& \overline{q}) \oplus \langle id, K_f (SComs) \rangle$ , id) ! Coms

$$= \{ (\mathbf{id} \mid x)^i \mid x^i \in \operatorname{Coms}, (\mathbf{ex} \mid \overline{\mathbf{p}} \And \overline{\mathbf{q}}) \oplus \langle \mathbf{id}, \operatorname{K}_f (\operatorname{SComs}) \rangle ) ? x \}$$

$$= \{ x^i \mid x^i \in \operatorname{Coms}, (\mathbf{ex} \mid \overline{\mathbf{p}} \And \overline{\mathbf{q}}) \oplus \langle \mathbf{id}, \operatorname{K}_f (\operatorname{SComs}) \rangle ) ? x \}$$

$$= \{ x^i \mid x^i \in \operatorname{Coms} \\ \exists y \mid (y \in \operatorname{SComs} \land x.\operatorname{chair} \in y.\operatorname{mems} \land x.\operatorname{chair.pty} == y.\operatorname{chair.pty}) \}.$$

Removing duplicates from this result leaves,

$$\{x \mid x \in \text{Coms}, \exists y \ (y \in \text{SComs} \land x.\text{chair} \in y.\text{mems} \land x.\text{chair.pty} == y.\text{chair.pty})\}$$

which is also the result of the OQL query,  $COI_{1*}$ .

# $\overline{\mathbf{COI}_{1}^{K}}$ (3):

 $\overline{COI_1^K}$  computes the same result as  $COI_1^K$  and  $COI_{1*}^K$ , but using join in its subquery rather than iterate. The join is of Coms and Temp<sub>K</sub>, and uses predicates  $\overline{\mathbf{r}}$  and  $(\mathbf{ex} \ (\overline{\mathbf{p}}) \oplus (\mathbf{id} \times \pi_2))$ . The latter complex predicate is a predicate on nested pairs

[x, [p, S]]

(such that  $x \in \text{Coms}$  and  $[p, S] \in \text{Temp}_K$ ) that is equivalent to the OQL boolean expression,

EXISTS y IN S: (x.chair IN y.mems)

as illustrated by the derivation below:

$$(\mathbf{ex} \ (\overline{\mathbf{p}}) \oplus (\mathbf{id} \times \pi_2)) ? [x, [p, S]] = \mathbf{ex} \ (\overline{\mathbf{p}}) ? ((\mathbf{id} \times \pi_2) ! [x, [p, S]])$$
$$= \mathbf{ex} \ (\overline{\mathbf{p}}) ? [\mathbf{id} ! x, \pi_2 ! [p, S]]$$
$$= \mathbf{ex} \ (\overline{\mathbf{p}}) ? [x, S]$$
$$= \exists y \ (y \in S \ \land \ \overline{\mathbf{p}} ? [x, y])$$
$$= \exists y \ (y \in S \ \land \ x.chair \in y.mems)$$

Therefore, the result of the join is a collection of committees whose chairs are members of a subcommittee chaired by someone from the same party, as illustrated by the derivation:

$$\begin{aligned} \mathbf{join} \ (\overline{\mathbf{r}} \ \& \ (\mathbf{ex} \ (\overline{\mathbf{p}}) \ \oplus \ (\mathbf{id} \ \times \ \pi_2)), \ \pi_1) \ ! \ [\texttt{Coms, Temp}_K] \\ &= \begin{array}{c} \left\{ (\pi_1 \ ! \ [x, \ [p, \ S]])^{ij} \ | \\ & x^i \in \texttt{Coms, } \ [p, \ S]^j \in \texttt{Temp}_K, \ (\overline{\mathbf{r}} \ \& \ (\mathbf{ex} \ (\overline{\mathbf{p}}) \ \oplus \ (\mathbf{id} \ \times \ \pi_2))) \ ? \ [x, \ [p, \ S]] \right\} \\ &= \begin{array}{c} \left\{ x^{ij} \ | \ x^i \in \texttt{Coms, } \ [p, \ S]^j \in \texttt{Temp}_K, \ (\overline{\mathbf{r}} \ \& \ (\mathbf{ex} \ (\overline{\mathbf{p}}) \ \oplus \ (\mathbf{id} \ \times \ \pi_2))) \ ? \ [x, \ [p, \ S]] \right\} \end{aligned}$$

$$= \{x^i \mid x^i \in \text{Coms}, [p, S] \in \text{Temp}_K, (\overline{r} \& (\mathbf{ex} (\overline{p}) \oplus (\mathbf{id} \times \pi_2))) ? [x, [p, S]]\}$$

$$= \begin{array}{c} \{x^i \mid x^i \in \texttt{Coms}, \ [p, \ S] \in \texttt{Temp}_K, \\ \hline \mathbf{r} ? \ [x, \ [p, \ S]], \ (\mathbf{ex} \ (\overline{p}) \oplus (\mathbf{id} \times \pi_2)) ? \ [x, \ [p, \ S]] \} \end{array}$$

After duplicate elimination, this becomes,

$$\{x \mid x \in \texttt{Coms}, [p, S] \in \texttt{Temp}_K, \overline{r} ? [x, [p, S]], (\mathbf{ex} \ (\overline{p}) \oplus (\mathbf{id} \times \pi_2)) ? [x, [p, S]]\}.$$

Because  $\overline{\mathbf{r}}$ ? [x, [p, S]] is true if

$$x.\texttt{chair.pty} == p$$

and  $(\mathbf{ex} \ (\overline{\mathbf{p}}) \oplus (\mathbf{id} \times \pi_2))$ ? [x, [p, S]] is true if

$$\exists y \ (y \in S \land x.\texttt{chair} \in y.\texttt{mems}),$$

this expression reduces to

 $\{x \, | \, x \in \texttt{Coms}, \ [p, S] \in \texttt{Temp}_K, \, x.\texttt{chair.pty} \texttt{ == } p, \, \exists y \ (y \in S \ \land \ x.\texttt{chair} \in y.\texttt{mems}) \}$ 

which is also what is returned by the OQL query,  $\overline{COI_1}$ .

 $COI_{2}^{K}$  (4):

Query  $COI_2^K$  (4) is almost identical to query  $COI_1^K$  (1) but using the predicate  $\overline{p_2}$  rather than  $\overline{p}$ . Given a committee  $x \in \text{Coms}$ ,  $((\mathbf{ex} \ (\overline{p_2}) \oplus \langle \mathbf{id}, \overline{\mathbf{f}} \rangle) ? x)$  is equivalent to the OQL expression,

 $\begin{array}{l} \texttt{EXISTS} \ y \ \texttt{IN} \ \left( \begin{array}{c} \texttt{SELECT} \ c \\ \texttt{FROM} \ c \ \texttt{IN} \ \texttt{SComs} \\ \texttt{WHERE} \ x.\texttt{chair.pty} == c.\texttt{chair.pty} \end{array} \right) : y.\texttt{chair} \ \texttt{IN} \ y.\texttt{mems} \end{array}$ 

as is revealed by the derivation below:

$$\begin{aligned} (\mathbf{ex} \ (\overline{\mathbf{p}_2}) \oplus \langle \mathbf{id}, \overline{\mathbf{f}} \rangle) ? x \\ &= \mathbf{ex} \ (\overline{\mathbf{p}_2}) ? \ [\mathbf{id} \ ! \ x, \overline{\mathbf{f}} \ ! \ x] \\ &= \mathbf{ex} \ (\overline{\mathbf{p}_2}) ? \ [x, \ S_x] \\ &\quad \text{such that} \ S_x = \{c^i \ | \ c^i \in \mathsf{SComs}, \ x.\mathsf{chair.pty} == c.\mathsf{chair.pty}\} \\ &= \ \exists y \ (y \in S_x \ \land \ \overline{\mathbf{p}_2} \ ? \ [x, \ y]) \\ &= \ \exists y \ (y \in S_x \ \land \ y.\mathsf{chair} \in y.\mathsf{mems}) \end{aligned}$$

Therefore, the **iterate** subquery of this query generates the collection,

$$\{x^i \mid x^i \in \text{Coms}, \exists y \ (y \in S_x \land y.\text{chair} \in y.\text{mems})\}$$

Removing duplicates from this result leaves,

$$\{x \mid x \in \texttt{Coms}, \exists y \ (y \in S_x \land y.\texttt{chair} \in y.\texttt{mems})\},\$$

which is the same result returned by the OQL query,  $COI_2$ .

# $\overline{\mathbf{COI}_{2}^{K}}$ (5):

Query  $\overline{COI_2^K}$  (5) is almost identical to query  $\overline{COI_1^K}$  (3) but for its use of  $\overline{p_2}$  rather than  $\overline{p}$ . The join predicate for this query consists of  $\overline{r}$  and (ex ( $\overline{p_2}$ )  $\oplus$  (id  $\times \pi_2$ )). The latter predicate on nested pairs [x, [p, S]] (such that x is in Coms and [p, S] is in Temp<sub>K</sub>) is equivalent to the OQL expression

#### EXISTS y IN S : (y.chair IN y.mems),

as is revealed by the derivation below:

$$(\mathbf{ex} \ (\overline{\mathbf{p}_2}) \oplus (\mathbf{id} \times \pi_2)) ? [x, [p, S]] = \mathbf{ex} \ (\overline{\mathbf{p}_2}) ? ((\mathbf{id} \times \pi_2) ! [x, [p, S]])$$
$$= \mathbf{ex} \ (\overline{\mathbf{p}_2}) ? [\mathbf{id} ! x, \pi_2 ! [p, S]]$$
$$= \mathbf{ex} \ (\overline{\mathbf{p}_2}) ? [x, S]$$
$$= \exists y \ (y \in S \ \land \ \overline{\mathbf{p}_2} ? [x, y])$$
$$= \exists y \ (y \in S \ \land \ y.\mathsf{chair} \in y.\mathsf{mems}).$$

Therefore, the result of the join is a collection of committees whose chairs belong to a party which also includes someone who both chairs and is a member of some subcommitee:

$$\begin{array}{l} \mathbf{join} \ (\overline{\mathbf{r}} \ \& \ (\mathbf{ex} \ (\overline{\mathbf{p}_2}) \ \oplus \ (\mathbf{id} \ \times \ \pi_2)), \ \pi_1) \ ! \ [\mathsf{Coms}, \ \mathsf{Temp}_K] \\ = & \{x^{ij} \ | \ x^i \in \mathsf{Coms}, \ [p, \ S]^j \in \mathsf{Temp}_K, \ (\overline{\mathbf{r}} \ \& \ (\mathbf{ex} \ (\overline{\mathbf{p}_2}) \ \oplus \ (\mathbf{id} \ \times \ \pi_2))) \ ? \ [x, \ [p, \ S]] \} \\ = & \{x^i \ | \ x^i \in \mathsf{Coms}, \ [p, \ S] \in \mathsf{Temp}_K, \ (\overline{\mathbf{r}} \ \& \ (\mathbf{ex} \ (\overline{\mathbf{p}_2}) \ \oplus \ (\mathbf{id} \ \times \ \pi_2))) \ ? \ [x, \ [p, \ S]] \} \\ = & \frac{\{x^i \ | \ x^i \in \mathsf{Coms}, \ [p, \ S] \in \mathsf{Temp}_K, \ (\overline{\mathbf{r}} \ \& \ (\mathbf{ex} \ (\overline{\mathbf{p}_2}) \ \oplus \ (\mathbf{id} \ \times \ \pi_2))) \ ? \ [x, \ [p, \ S]] \} \\ = & \frac{\{x^i \ | \ x^i \in \mathsf{Coms}, \ [p, \ S] \in \mathsf{Temp}_K, \ (\overline{\mathbf{r}} \ \& \ (\mathbf{ex} \ (\overline{\mathbf{p}_2}) \ \oplus \ (\mathbf{id} \ \times \ \pi_2))) \ ? \ [x, \ [p, \ S]] \} \\ \end{array}$$

After duplicate elimination, this becomes,

 $\{x \mid x \in \text{Coms}, [p, S] \in \text{Temp}_K, \overline{r} ? [x, [p, S]], (ex (\overline{p_2}) \oplus (id \times \pi_2)) ? [x, [p, S]]\}.$ 

Because  $\overline{\mathbf{r}}$ ? [x, [p, S]] is true if

$$x.\texttt{chair.pty} == p$$

and  $(\mathbf{ex} \ (\overline{\mathbf{p}_2}) \oplus (\mathbf{id} \times \pi_2))$ ? [x, [p, S]] is true if

$$\exists y \ (y \in S \land y.\texttt{chair} \in y.\texttt{mems}),$$

this expression reduces to

 $\{x \mid x \in \texttt{Coms}, \ [p, \ S] \in \texttt{Temp}_K, \ x.\texttt{chair.pty} \texttt{==} \ p, \ \exists y \ (y \in S \ \land \ y.\texttt{chair} \in y.\texttt{mems})\},$ 

which is what is also returned by the OQL query,  $COI_2$ .

# $\overline{\mathbf{COI}_{2}^{K}}$ (6):

Query  $\overline{COI_2^K}$  (6) generates  $\operatorname{Temp}_K$  as a subquery result as in  $\overline{COI_2^K}$ , but then filters this result before proceeding with the join. The filtering subquery uses the predicate  $\overline{p_3}$  which is a predicate on pairs from  $\operatorname{Temp}_K$  [p, S] that is equivalent to the OQL boolean expression,

EXISTS y IN S: (y.chair IN y.mems)

as illustrated by the derivation below:

$$\begin{array}{rcl} (\text{exists } (\text{ex} \ (\text{eq}) \oplus \langle \text{chair, mems} \rangle) \oplus \pi_2) ? [p, S] \\ = & \text{exists } (\text{ex} \ (\text{eq}) \oplus \langle \text{chair, mems} \rangle) ? (\pi_2 ! [p, S]) \\ = & \text{exists } (\text{ex} \ (\text{eq}) \oplus \langle \text{chair, mems} \rangle) ? S \\ = & \exists y \ (y \in S \ \land \ (\text{ex} \ (\text{eq}) \oplus \langle \text{chair, mems} \rangle) ? y) \\ = & \exists y \ (y \in S \ \land \ \text{ex} \ (\text{eq}) ? (\langle \text{chair, mems} \rangle ! y)) \\ = & \exists y \ (y \in S \ \land \ \text{ex} \ (\text{eq}) ? [y.\text{chair, y.mems}]) \\ = & \exists y \ (y \in S \ \land \ \exists z \ (z \in y.\text{mems} \ \land \ q ? [y.\text{chair, z]})) \\ = & \exists y \ (y \in S \ \land \ \exists z \ (z \in y.\text{mems} \ \land \ y.\text{chair == }z)) \\ = & \exists y \ (y \in S \ \land \ (y.\text{chair} \in y.\text{mems})). \end{array}$$

Therefore, the result of filtering  $\text{Temp}_K$  is the set of party, subcommittee collection pairs ([p, S]) such that for some subcommittee in  $c \in S$ , c's chair is also a member of c. The intermediate result returned as a result of **join** is therefore:

join  $(\overline{\mathbf{r}}, \pi_1)$  ! [Coms, iterate  $(\overline{\mathbf{p}_3}, \mathbf{id})$  ! Temp<sub>K</sub>]

- = join  $(\overline{\mathbf{r}}, \pi_1)$  ! [Coms,  $\{(\operatorname{id} ! [p, S])^j | [p, S]^j \in \operatorname{Temp}_K, \overline{p_3} ? [p, S]\}\}$ ]
- $= \text{ join } (\overline{\mathbf{r}}, \pi_1) ! [Coms, \{[p, S] \mid [p, S] \in \text{Temp}_K, \overline{p_3} ? [p, S]\}]$
- $= \{ \{(\pi_1 ! [x, [p, S]])^i \mid x^i \in \text{Coms}, [p, S] \in \text{Temp}_K, \overline{p_3} ? [p, S], \overline{r} ? [x, [p, S]] \} \}$

$$= \{x^i \mid x^i \in \text{Coms}, [p, S] \in \text{Temp}_K, \overline{p_3} ? [p, S], \overline{r} ? [x, [p, S]]\}.$$

Because  $\overline{\mathbf{r}}$ ? [x, [p, S]] is true if

$$x.\texttt{chair.pty} == p$$

and  $\overline{p_3}$ ? [p, S] is true if

$$\exists y \ (y \in S \land (y.\texttt{chair} \in y.\texttt{mems})),$$

this expression reduces to,

$$\{x^i \mid x^i \in \text{Coms}, [p, S] \in \text{Temp}_K, \exists y \ (y \in S \land (y.\text{chair} \in y.\text{mems})), x.\text{chair.pty} == p\},$$

which is also what is returned by the OQL query,  $\overline{COI_2}$ .

#### 3.4.2 A Rule Set for Rewriting the COI Queries

Figure 3.9 shows a set of KOLA rewrite rules that can be fired in the same sequence to rewrite:

- $COI_1^K \to COI_{1*}^K \to \overline{COI_1^K}$ , and
- $COI_2^K \to \overline{COI_2^K} \to \overline{\overline{COI_2^K}}.$

(The KOLA transformation chain is slightly different than that presented for the OQL versions of these queries in that  $COI_1^K$  is transformed into  $COI_{1*}^K$  rather than vice-versa.) The sequence used for these rules is:

 $1, \ 2, \ 3, \ 4, \ 5, \ 6, \ 5^{-1}, \ 7, \ 5, \ 8, \ 9$ 

such that  $5^{-1}$  indicates that rule 5 is fired in right-to-left fashion. For the purposes of discussion, this sequence can be broken down into four subsequences.<sup>10</sup> To show the effects of firing these rules, we illustrate by tracing the rewrite of query  $COI_2^K$  (Query 4 of Figure 3.8) first into query  $\overline{COI_2^K}$  (5) and then into  $\overline{COI_2^K}$  (6). The steps of this query rewrite are shown in Figure 3.10 and summarized below.

<sup>&</sup>lt;sup>10</sup>These rewrites could instead be expressed with four rules (one for each subsequence), but these four rules would be very complex and would make the specification of the rewrite harder to understand and verify. Such complex rules also hide the fact that the simpler rules have general applicability (rules 4, 5 and 7 being the most obvious in this example). Thus, it was decided to keep rules as simple as possible and to group rules into complex rewrites using COKO, as will be discussed in Section 4.

(1) 
$$\mathbf{ex} (p) \oplus \langle \mathbf{id}, \mathbf{iter} (q, \pi_2) \circ \langle \mathbf{id}, \mathsf{K}_f (B) \rangle \stackrel{\simeq}{=} \mathbf{ex} (q \& p) \oplus \langle \mathbf{id}, \mathsf{K}_f (B) \rangle$$

(2) set ! (iterate (ex 
$$(p) \oplus \langle id, K_f (B) \rangle, f)$$
 ! A) = set ! (join  $(p, f \circ \pi_1)$  ! [A, B])

(3) set ! (join 
$$(q \& p, h \circ \pi_1)$$
 !  $[A, B]) \stackrel{\rightarrow}{=}$   
set ! (join  $(r \& (ex (p) \oplus (id \times \pi_2)), h \circ \pi_1)$  !  $[A, T]$ )

such that

 $\begin{array}{rcl} q &=& \mathbf{eq} \oplus (f \times g) \\ r &=& \mathbf{eq} \oplus (f \times \pi_1) \\ T &=& \mathbf{njoin} \ (\mathbf{eq} \oplus (\mathbf{id} \times g), \ \mathbf{id}, \ \mathbf{id}) \ ! \ [\mathbf{iterate} \ (\mathtt{K}_p \ (\mathtt{true}), \ g) \ ! \ B, \ B] \end{array}$ 

(4)  $\langle f \circ h, g \circ h \rangle \stackrel{\rightarrow}{=} \langle f, g \rangle \circ h$ (5)  $p \oplus (f \circ g) \stackrel{\rightarrow}{=} (p \oplus f) \oplus g$ 

(6) 
$$p \oplus (j \oplus g) = (p \oplus f) \oplus g$$
  
 $ex (p \oplus \pi_2) \stackrel{=}{=} exists (p) \oplus \pi_2$ 

 $(7) \qquad \qquad \pi_2 \circ (f \times g) \stackrel{\rightarrow}{=} g \circ \pi_2$ 

(8) **join** 
$$(p \& (q \oplus \pi_2), f) ! [A, B] \stackrel{\rightarrow}{=} \mathbf{join} (p, f) ! [A, \mathbf{iterate} (q, \mathbf{id}) ! B]$$

(9)  $\mathbf{id} \circ f \stackrel{\Rightarrow}{=} f$ 

Figure 3.9: Rewrite Rules For the Query Rewrites of the "Conflict of Interests" Queries

**Firing Rule 1:** Rule 1 pulls a predicate (q) out of an inner query (**iter**  $(q, \pi_2)$ ) and into the existential quantifier, **ex**. Matching rule 1 with  $COI_2^K$  binds pattern variables p and qto KOLA predicates  $\overline{\mathbf{p}_2}$  and  $\overline{\mathbf{q}}$ . Rewriting then absorbs the predicate  $\overline{\mathbf{q}}$  in **iter**  $(\overline{\mathbf{q}}, \pi_2)$  into the existentially quantified predicate, resulting in **ex**  $(\overline{\mathbf{q}} \And \overline{\mathbf{p}_2})$ . In short, the result of firing this rule on  $COI_2^K$  is a KOLA query equivalent to the OQL query,

SELECT DISTINCT x.chair FROM x IN Coms WHERE EXISTS y IN SComs : ((y.chair  $\in$  y.mems) AND (x.chair.pty == y.chair.pty)).

Firing Rules 2 and 3: Rules 2 and 3 together transform the query resulting from the previous step into  $\overline{COI_2^K}$ . Rule 2 fires on queries matching the head pattern

set ! (iterate (ex  $(p) \oplus \langle id, K_f (B) \rangle, f) ! A$ ).

This pattern characterizes nested OQL and SQL queries whose WHERE clause contains a correlated membership or existence predicate (p). Once fired, Rule 2 transforms such queries into the form,

set ! (join  $(p, f \circ \pi_1)$  ! [A, B]),

set ! (iterate (ex  $(\overline{p_2}) \oplus \langle id, \overline{f} \rangle, id)$  ! Coms)  $\overline{\mathbf{p}_2} \equiv \mathbf{ex} \ (\mathbf{eq}) \oplus \langle \mathtt{chair} \circ \pi_2, \, \mathtt{mems} \circ \pi_2 \rangle$  $\begin{array}{rcl} \overline{\mathbf{q}} & \equiv & \mathbf{eq} \oplus ((\mathtt{pty} \circ \mathtt{cnall}) \land \mathtt{vr}) \\ \overline{\mathbf{f}} & \equiv & \mathbf{iter} \ (\overline{\mathbf{q}}, \ \pi_2) \circ \langle \mathbf{id}, \ \mathtt{K}_f \ (\mathtt{SComs}) \rangle \end{array}$  $\equiv$  eq  $\oplus$  ((pty  $\circ$  chair)  $\times$  (pty  $\circ$  chair))  $\xrightarrow{1}$ set ! (iterate (ex ( $\overline{q} \& \overline{p_2}$ )  $\oplus \langle id, K_f(SComs) \rangle, id)$  ! Coms)  $\xrightarrow{2}$ set ! (join ( $\overline{\mathbf{q}} \& \overline{\mathbf{p}_2}$ , id  $\circ \pi_1$ ) ! [Coms, SComs])  $\xrightarrow{3}$ set ! (join ( $\overline{\mathbf{q}} \& \overline{\mathbf{p}_2}$ , id  $\circ \pi_1$ ) ! [Coms, Temp<sub>K</sub>])  $\texttt{Temp}_K \equiv \texttt{njoin} \ (\texttt{eq} \oplus (\texttt{id} \times (\texttt{pty} \circ \texttt{chair})), \ \texttt{id}, \ \texttt{id}) \ !$ [iterate (K<sub>p</sub> (true), pty  $\circ$  chair) ! SComs, SComs]  $\overline{\mathbf{p}_2} \equiv \mathbf{ex} \ (\mathbf{ex} \ (\mathbf{eq}) \oplus \langle \mathtt{chair} \circ \pi_2, \, \mathtt{mems} \circ \pi_2 \rangle) \oplus (\mathbf{id} \times \pi_2)$  $\overline{\mathbf{q}} \equiv \mathbf{eq} \oplus ((\mathtt{pty} \circ \mathtt{chair}) \times \pi_1)$ (a) The first transformation of  $COI_2^K$  to  $\overline{COI_2^K}$  $\xrightarrow{4}$ set ! (join ( $\overline{\mathbf{q}} \& \overline{\mathbf{p}_2}$ , id  $\circ \pi_1$ ) ! [Coms, Temp<sub>K</sub>])  $\overline{\mathbf{p}_2} \equiv \mathbf{ex} \ (\mathbf{ex} \ (\mathbf{eq}) \oplus (\langle \mathtt{chair}, \, \mathtt{mems} \rangle \circ \pi_2)) \oplus (\mathbf{id} \times \pi_2)$  $\xrightarrow{5}$ set ! (join ( $\overline{\mathbf{q}} \& \overline{\mathbf{p}_2}$ , id  $\circ \pi_1$ ) ! [Coms, Temp<sub>K</sub>])  $\overline{\mathbf{p}_2} \equiv \mathbf{ex} \ (\mathbf{ex} \ (\mathbf{eq}) \oplus \langle \mathtt{chair}, \, \mathtt{mems} \rangle \oplus \pi_2) \oplus (\mathbf{id} \times \pi_2)$  $6,5^{-1}$ set ! (join ( $\overline{q} \& \overline{p_2}, id \circ \pi_1$ ) ! [Coms, Temp<sub>K</sub>])  $\overline{\mathbf{p}_2} \equiv \mathbf{exists} (\mathbf{ex} (\mathbf{eq}) \oplus \langle \mathtt{chair}, \mathtt{mems} \rangle) \oplus (\pi_2 \circ (\mathbf{id} \times \pi_2))$  $\xrightarrow{7,5}$ set ! (join ( $\overline{\mathbf{q}} \& \overline{\mathbf{p}_2}$ , id  $\circ \pi_1$ ) ! [Coms, Temp<sub>K</sub>])  $\overline{p_2} \equiv \text{exists} (\text{ex} (\text{eq}) \oplus \langle \text{chair}, \text{mems} \rangle) \oplus \pi_2 \oplus \pi_2$  $\xrightarrow{8}$ set ! (join ( $\overline{q}$ , id  $\circ \pi_1$ ) ! [Coms, iterate ( $\overline{p_3}$ , id) ! Temp<sub>K</sub>])  $\text{Temp}_K \equiv \text{njoin} (\text{eq} \oplus (\text{id} \times (\text{pty} \circ \text{chair})), \text{id}, \text{id}) !$ [iterate (K<sub>p</sub> (true), pty  $\circ$  chair) ! SComs, SComs]  $\overline{\mathbf{p}_3} \equiv \mathbf{exists} \ (\mathbf{ex} \ (\mathbf{eq}) \oplus \langle \mathtt{chair}, \, \mathtt{mems} \rangle) \oplus \pi_2$  $\overline{\mathbf{q}} \equiv \mathbf{eq} \oplus ((\mathtt{pty} \circ \mathtt{chair}) \times \pi_1)$  $\xrightarrow{9}$ set ! (join ( $\overline{q}$ ,  $\pi_1$ ) ! [Coms, iterate ( $\overline{p_3}$ , id) ! Temp<sub>K</sub>]) (b) The second transformation of  $\overline{COI_2^K}$  to  $\overline{\overline{COI_2^K}}$ 

Figure 3.10: Transforming  $COI_2^K \to \overline{COI_2^K} \to \overline{\overline{COI_2^K}}$ 

thus eliminating the nesting by eliminating the existential predicate former,  $\mathbf{ex}$ , and replacing it with a join. Thus, this rule generalizes the Type N and Type J query transformations of Kim [63].

Rule 3 is the most complex rule in this rule set. It fires on queries matching the head pattern,

set ! (join 
$$(q \& p, h \circ \pi_1)$$
 ! [A, B])

such that  $q = \mathbf{eq} \oplus (f \times g)$ . Queries matching this pattern return

$$\{h \mid a \mid a \in A, b \in B, f \mid a == g \mid b, p ? [a, b]\}$$

as their result. What is noteworthy is that an element,  $(h \mid a)$  only figures into the result if there exists some  $b \in B$  such that  $f \mid a == g \mid b$  and p ? [a, b]. The idea behind rule 3 is to group elements of B by their values for  $(g \mid b)$  so that the comparison,

$$f ! a == g ! b$$

need not be made for each  $b \in B$  but instead for each unique value of (g ! b). This grouping is expressed with the body pattern subexpression,

$$T = njoin (eq \oplus (id \times g), id, id) ! [iterate (K_p (true), g) ! B, B]$$

that returns the grouped result,

$$\{ [g ! b, S_b] \mid b \in B \}$$

such that

$$S_b = \{ (b_2)^i \mid (b_2)^i \in B, g ! b == g ! b_2 \}$$

That is, this subquery produces a set of pairs,  $[g ! b, S_b]$  such that  $S_b$  is the subcollection of B whose elements have the same value for g as b.

The entire body pattern of rule 3 is:

set ! (join 
$$(r \& (\mathbf{ex} (p) \oplus (\mathbf{id} \times \pi_2)), h \circ \pi_1) ! [A, T])$$

such that  $r = \mathbf{eq} \oplus (f \times \pi_1)$ . Queries rewritten to this form perform a join of A and T, and for each pair  $[a, [g ! b, S_b]]$  such that  $a \in A$  and  $[g ! b, S_b] \in T$ : determines if:

- f ! a == g ! b, and
- $\exists b_2 \in S_b (p ? [a, b_2]).$

Finally, duplicates are removed from the result of this join. The result of firing these two rules on  $COI_2^K$  is  $\overline{COI_2^K}$ .

**Firing Rules 4, 5, 6, 5**<sup>-1</sup>, **7 and 5:** These rules are fired on the predicate  $\overline{\mathbf{p}_2}$  of  $\overline{COI_2^K}$ . The effect is to normalize the predicate to make it of the form,  $p \oplus \pi_2$  for some predicate p. This sequence prepares it for the *predicate pushdown* rule, 8b.

When applied to  $\overline{COI_2^K}$ , rule 4 factors the function  $\pi_2$  from the pair function,

$$\langle \texttt{chair} \circ \pi_2, \, \texttt{mems} \circ \pi_2 \rangle,$$

leaving

 $\langle \text{chair, mems} \rangle \circ \pi_2.$ 

Rules 5, 6, 5<sup>-1</sup>, 7 and 5 again continue to factor  $\pi_2$  from  $\mathbf{p}_2$ , leaving a predicate,  $p_2 \oplus \pi_2$  such that

 $p_2 = \mathbf{exists} \ (\mathbf{ex} \ (\mathbf{eq}) \oplus \langle \mathtt{chair}, \, \mathtt{mems} \rangle) \oplus \pi_2.$ 

On the other hand, rule 4 fails to fire on  $\overline{COI_1^K}$ 's corresponding subfunction,

$$\langle \texttt{chair} \circ \pi_1, \texttt{mems} \circ \pi_2 \rangle.$$

The other rules that continue to factor  $\pi_2$  out of  $\overline{p}$  (6 and 7) fail to fire also.

Firing Rule 8: This rule identifies the join predicate  $(\overline{p})$  that is a predicate on the second argument to the join, and pushes this predicate onto a selection over this second argument. Thus, the firing of this rule after the normalizing steps of the previous subsequence of rules transforms  $\overline{COI_2^K}$  into  $\overline{\overline{COI_2^K}}$ . This rule has no effect on  $\overline{COI_1^K}$  because this query was not normalized by the previous set of rule firings,

**Firing Rule 9:** Finally, rule 9 simplifies the data function of the **join**, rewriting **id**  $\circ \pi_1$  to  $\pi_1$ .

## 3.5 Discussion

#### 3.5.1 The Expressive Power of KOLA

There are downsides to using KOLA as a query representation, but a lack of expressive power for denoting queries is not one of them. Combinators can appear to lack expressivity to those who first use them, but the right set of combinators can have rich expressive power. For example, Schönfinkel [82] established that three combinators ( $\mathbf{S}$ ,  $\mathbf{K}$  and  $\mathbf{I}$ ) were all that were required as an alphabet for a free algebra over which one could translate all of the lambda calculus. (It even was shown later that  $\mathbf{I}$  was unnecessary.) Within the context of querying, the rich expressivity of KOLA has been established via the design, correctness proof and implementation of a translator from a set and bag based subset of OQL to KOLA. This translator is described in Chapter 6.

#### 3.5.2 Addressing the Downsides of KOLA

#### **KOLA** Query Representations Are Large

KOLA query representations tend to be larger than their variable-based counterparts (as measured in parse tree nodes). The size increase is up to a factor of m where m is a measure of how nested the query is.<sup>11</sup> Intuitively, combinator representations are bigger because functions can require expression with several parse tree nodes, whereas variable references (which they replace) always require just one node. Deeply nested queries can be especially problematic because variables that are used long after they are declared will be replaced by functions that are long compositions of projection functions ( $\pi_1$  and  $\pi_2$ ) that probe the nested pair data structures that replace the variable's implicitly constructed environment.

The representation size issue has been a major concern to the functional programming community's effort to use combinators internally to represent functional programs within a compiler. One solution applied to this problem is to add combinators to the representation language at the expense of redundancy. Also, a solution has been proposed that has specialpurpose combinators (*supercombinators*) generated on-the-fly [52].

The supercombinator approach has little practical benefit for querying given that query rewriting relies on the existence of a *fixed* set of query operators. But queries tend to be smaller than programs, and thus such drastic solutions may not be required. We could get around the problem of having large representations for deeply nested queries by adding special purpose environment accessing combinators (e.g.,  $\pi_3, \pi_4, \ldots$ ) to make the increase in representation size effectively linear in the size of the original query. But as yet, we haven't come across queries that have produced representations that were too large for our system.

The potential modification of KOLA brings up another philosophical issue, which is that this thesis does not argue for KOLA as the ideal query algebra, but rather for the benefits of (any) well-designed combinator-based query algebra. KOLA has been and continues to be plastic – operators are added, removed and modified regularly as new insights are gleaned into the optimization process. Thus, the potential addition of combinators (such as  $\pi_3$ ) will

<sup>&</sup>lt;sup>11</sup>More precisely, m is the maximum number of variables that ever appear in an environment at one time while evaluating the variable-based query.

not compromise our position. We fully expect KOLA to live and grow.

#### KOLA Requires More Rules than Variable-Based Representations

The other downside to KOLA specifically, and combinator-based query algebras in general, is the apparent need for multiple rules to express desired transformations. In some ways, this problem is self-induced. KOLA rules are purposely kept as small as possible to make them more likely to be reused and understood. But optimizers that are left on their own to choose a sequence in which to apply multiple rules to perform a single complex transformation are greatly handicapped when there is an explosion in the number of rules to consider.

As we saw in Section 3.4.2, a fixed sequence of rule applications (perhaps with some rules applied conditionally) can express a complex transformation for a large class of queries. This makes a specific sequence of rule firings resemble a theorem prover script that guides normalization of one expression into another to establish that the two expressions are equivalent. This similarity reveals a serendipitous detail of this thesis work. Theorem prover verifiability inspired KOLA, but actually working with a theorem prover and seeing how it operated motivated COKO, our language for "programming" KOLA rule firing scripts. COKO is discussed in the next section.

# 3.6 Chapter Summary

In order to use a theorem prover to verify query rewrites, rewrites must be expressed *declaratively*, as in rewrite rules of term rewriting systems. In practice however, query rewrites get expressed with code, or with rewrite rules supplemented with code.

Query rewrites perform two tasks: (1) subexpression identification identifies relevant subexpressions of a query, and (2) query formulation constructs new query expressions from the identified subexpressions. These two steps are captured within standard pattern matching by actions that use head and body patterns of a rule respectively. But pattern matching is insufficient for expressing query rewrites when the underlying query representation is *variable-based*. The problem is that an expression can contain free variables, which make its semantics dependent on the context in which it appears. Context-dependent semantics makes subexpression identification require context analysis, and query formulation require massaging of subexpressions to ensure that their semantics are preserved when used in a new query. Neither of these actions can be expressed with rule patterns, and therefore in practice, they get expressed with code. As variables are the problem, our solution was to remove the variables. We have introduced the combinator-based query algebra, KOLA, which expresses functions and predicates as primitives or as the result of instantiating formers with other functions and predicates. This approach made it possible to express query rewrites that had been problematic to express over variable-based representations, in a purely declarative fashion.

# Chapter 4

# **COKO:** Complex Query Rewrites

Our KOLA work only partially explains the reason why, in practice, query rewrites get expressed with code. Rewrite rules are inherently "small" in their operation. They are well-suited for expressing simple rewrites, such as ones that change the order of arguments to a join or push selections past joins. But some query rewrites are too complex to be expressed with rewrite rules, regardless of the underlying query representation. For example, a rewrite to convert Boolean expressions to *conjunctive normal form* (CNF) cannot be expressed with a rewrite rule because patterns are too constraining to capture its generality. (All boolean expressions can be transformed into CNF.) Instead, this rewrite is more appropriately described algorithmically. In this chapter, we introduce a language, COKO,<sup>1</sup>) for specifying complex query rewrites such as CNF, in a manner that permits verification with a theorem prover.

A COKO specification of a query rewrite (a *transformation*) consists of two parts:

- 1. a set of KOLA rewrite rules, and
- 2. a *firing algorithm* that specifies how the KOLA rewrite rules are to be fired.

Code is confined to firing algorithms that specify the order in which KOLA rewrite rules are fired, the query subexpressions on which rules are fired and the conditions that must be satisfied for firing to occur. Code is **not** used to rewrite queries. Instead, rewriting occurs only by firing KOLA rewrite rules. Therefore, a COKO transformation is correct if each of the KOLA rewrite rules it fires is correct. We showed in Chapter 3 that a theorem prover can verify KOLA rewrite rules. By implication, a theorem prover can verify COKO transformations also.

<sup>&</sup>lt;sup>1</sup>COKO is an acronym for [C]ontrol [O]f [K]OLA [O]ptimizations.

This work generalizes and extends KOLA. COKO transformations behave like rewrite rules in that they can be *fired* and can succeed or fail as a result. Therefore, the set of "rules" maintained by a rule-based optimizer could include KOLA rules to express simple query rewrites, and COKO transformations to express complex query rewrites. COKO transformations are also built from KOLA rules. By grouping sets of KOLA rewrite rules into COKO transformations, one can control the number of derivations produced by a rulebased optimizer. Further, the modular approach of expressing complex transformations in terms of simpler rewrite rules simplifies reasoning about the meanings of rewrites, just as expressing complex KOLA queries in terms of simpler functions simplified reasoning about the meanings of queries.

We begin this chapter in Section 4.1 by describing why COKO is necessary, and why general purpose programming languages such as C do not satisfy our goal of expressing complex query rewrites in a manner permitting verification with a theorem prover. We then introduce COKO in Section 4.2 with three example transformations that convert KOLA predicates into CNF. These examples also show how firing algorithms can determine the performance of query rewriting.<sup>2</sup> We discuss COKO's language of firing algorithms fully in Section 4.3. Then in Sections 4.4, 4.5, and 4.6 we demonstrate the expressive power of COKO by showing how we were able to specify a number of complex, yet useful query rewrites. These rewrites include a normalization (SNF) to identify subpredicates of a binary predicate that are effectively unary (Section 4.4), and some common rewrites such as *predicate-pushdown* (Section 4.5.1), *join-reordering* (Section 4.5.2) and the *magic-sets* rewrites of Mumick et al. [74] (Section 4.6).

# 4.1 Why COKO?

A complex query rewrite such as CNF cannot be expressed with a rewrite rule. Such rewrites are best described algorithmically. But why invent a new language for expressing these query rewrites? Why not use a general purpose programming language (such as C) to express rewrites as in Starburst?

What COKO provides that general purpose programming languages do not is *disciplined* query rewriting. COKO transformations are expressed algorithmically, but modifications of queries can only occur as a result of firing rewrite rules. This restriction ensures that COKO transformations are correct if the KOLA rewrite rules they fire are correct. Given

 $<sup>^{2}</sup>$ Note that the performance of query rewriting differs from the performance of queries *produced* as the result of rewriting.

the results of Chapter 3, COKO transformations can therefore be verified with a theorem prover.

On the other hand, languages like C do not impose this discipline. Query rewrites expressed in C might use assignment statements both to modify a query and to change the position of a cursor within the query representation (e.g., as the representation is traversed). This dual use of assignment statements makes it difficult to identify which parts of the rewrite code make changes to a query representation, and therefore which parts require verification. Also, assignment statements are much finer-grained modification primitives than are rule firings. The changes made to a query by one rule may have to be expressed with several assignment statements, each but the last leaving the query in an inconsistent state. Thus, verification is also complicated by the need to consider the flow of control of the rewrite code to determine if consistent states are revisited once left.

All of this is not to say that correct query rewrites cannot be written in C. Of course they can, but incorrect query rewrites can be written in C also and discerning between them is difficult. Writers of COKO transformations have a far easier task as they are using a language that permits easy identification of proof obligations (i.e., rules), and can use a theorem prover to help with the task of proving the rules correct.

## 4.2 Example 1: CNF

In this section, we introduce COKO by presenting COKO transformations that rewrite KOLA predicates into CNF. These transformations demonstrate the potential performance benefits possible from customizing firing algorithms.

We first describe what CNF means for KOLA predicates, and show three COKO transformations that rewrite predicates to CNF. The first two transformations are *exhaustive* in that they simply fire some set of KOLA rules on a query until rule firing no longer has any effect. The last transformation uses a more efficient rewrite algorithm than the exhaustive algorithms, thereby demonstrating that COKO firing algorithms can do more than just group rules.

## 4.2.1 CNF for KOLA Predicates

A boolean subexpression of an OQL or SQL query is in CNF if it is a conjunct (AND) of disjuncts (OR) of (possibly negated (NOT)) *literals* (i.e., expressions lacking conjuncts, disjuncts and negations). A query rewrite to convert predicates into CNF is a typical

preprocessing step in the course of rewriting. For example, this rewrite might be fired before selection predicates are reordered.

A KOLA predicate p is in CNF if for any argument x, p? x reduces by the definitions of Tables 3.1, 3.2, and 3.3 to a boolean expression that is in CNF. Put another way, p is in CNF if it is a conjunction (&) of disjunctions (|) of (possibly negated ( $\sim$ )) literals (i.e., predicates lacking subpredicates of forms, (q & r), (q | r) or  $(\sim (q))$ ).

Figures 4.1a and 4.1b shows example KOLA predicates over the Thomas schema of Table 2.1. Both queries contain subpredicates (literals) over pairs of committees ([x, y])

•  $P_k$ : which when invoked on a pair, [x, y] is equivalent to the OQL expression,

x.chair.pty == y.chair.pty,

•  $Q_k$ : which when invoked on a pair, [x, y] is equivalent to the OQL expression,

```
x.chair.terms > y.chair.terms,
```

•  $R_k$ : which when invoked on a pair, [x, y] is equivalent to the OQL expression,

$$x.topic == "NSF"$$
, and

•  $S_k$ : which when invoked on a pair, [x, y] is equivalent to the OQL expression,

 $(x.\texttt{chair.terms} + \texttt{SUM} \left( egin{array}{c} \texttt{SELECT} y.\texttt{terms} \\ \texttt{FROM} y \texttt{IN} x.\texttt{mems} \end{array} 
ight) > 100$ 

The query of Figure 4.1b is equivalent to that of Figure 4.1a, but is in CNF.

#### 4.2.2 An Exhaustive Firing Algorithm

Figure 4.2 shows two COKO transformations that convert KOLA predicates lacking negations (i.e., subpredicates of the form,  $\sim (p)$ ) into CNF. A COKO transformation begins with the keyword, TRANSFORMATION, followed by the name of the transformation. The rest of the transformation consists of two parts:

- a rule section (introduced by the keyword, USES) that lists the KOLA rewrite rules and other COKO transformations fired by the transformation, and
- a firing algorithm (delimited by keywords BEGIN and END).

$$(\mathsf{P}_{\mathsf{k}} \And \mathsf{Q}_{\mathsf{k}} \And \mathsf{R}_{\mathsf{k}}) | \mathsf{S}_{\mathsf{k}} \qquad (\mathsf{P}_{\mathsf{k}} | \mathsf{S}_{\mathsf{k}}) \And (\mathsf{Q}_{\mathsf{k}} | \mathsf{S}_{\mathsf{k}}) \And (\mathsf{R}_{\mathsf{k}} | \mathsf{S}_{\mathsf{k}})$$
(a)
(b)
*such that*

$$\mathsf{P}_{\mathsf{k}} = \mathbf{e} \mathbf{q} \oplus \langle f \circ \pi_{1}, f \circ \pi_{2} \rangle,$$

Figure 4.1: A KOLA Predicate Before (a) and After (b) its Transformable into CNF

TRANSFORMATION CNF-BU TRANSFORMATION CNF-TD USES USES d1:  $(p \& q) | r \stackrel{\rightarrow}{=} (p | r) \& (q | r)$ d1:  $(p \& q) | r \stackrel{\rightarrow}{=} (p | r) \& (q | r)$ d2:  $\mathbf{r} \mid (\mathbf{p} \& \mathbf{q}) \stackrel{\rightarrow}{=} (\mathbf{p} \mid \mathbf{r}) \& (\mathbf{q} \mid \mathbf{r})$ d2:  $\mathbf{r} \mid (\mathbf{p} \& \mathbf{q}) \stackrel{\rightarrow}{=} (\mathbf{p} \mid \mathbf{r}) \& (\mathbf{q} \mid \mathbf{r})$ BEGIN BEGIN BU {d1 || d2}  $\rightarrow$  CNF-BU TD {d1 || d2}  $\rightarrow$  CNF-TD END END (a)(b)

Figure 4.2: Exhaustive CNF Transformations Expressed in COKO

A COKO transformation can be fired on any KOLA parse tree (example KOLA parse trees are shown in Figure 4.3), and may transform this tree as a result. In describing the transformations of Figure 4.4, we will assume that they have been fired on the parse tree for some KOLA predicate p. Hereafter, we will use p to name the KOLA predicate and its parse tree and rely on context to differentiate between the two.

#### **CNF-BU**

CNF-BU uses two KOLA rewrite rules that distribute disjunctions over conjunctions:

 $\begin{array}{rrrr} \texttt{d1:} & (\texttt{p \& q}) \mid \texttt{r} & \stackrel{\rightarrow}{=} & (\texttt{p} \mid \texttt{r}) \And (\texttt{q} \mid \texttt{r}) \\ \texttt{d2:} & \texttt{r} \mid (\texttt{p \& q}) & \stackrel{\rightarrow}{=} & (\texttt{p} \mid \texttt{r}) \And (\texttt{q} \mid \texttt{r}) \end{array}$ 



Figure 4.3: Illustrating CNF-BU on the KOLA Predicate of Figure 4.1a

In relation to a KOLA parse tree, the effect of either rule is to "push down" a disjunction (|) past a conjunction (&). Fired exhaustively on an unnegated predicate, these rules "push down" all disjuncts past all conjuncts, thereby leaving the predicate in CNF.

The firing algorithm for CNF-BU consists of the single complex COKO statement,

 $\texttt{BU} \; \{\texttt{d1} \; || \; \texttt{d2} \} \; \rightarrow \; \texttt{CNF-BU}.$ 

This statement can be broken down as follows:

- d1 and d2 are rule firing statements. That is, by referencing these rules in the firing algorithm (and provided each was defined in the rule section), these rules get fired. Each rule succeeds in firing if, as a result of pattern matching, its head pattern matches with the KOLA predicate on which it is fired.
- BU {d1 || d2} instructs the transformation to perform a *bottom-up* (or more accurately, a preorder) traversal of predicate *p*, executing the statement,

$$\{d1 || d2\}$$

on each visited subtree, s. The effect of executing this statement on s is to first fire d1 on s. If d1 succeeds in firing, then the statement is finished executing. If d1 fails to fire, then d2 is fired on s. This statement succeeds if either d1 or d2 successfully fires, and fails if both rules fail. The full statement

succeeds if the statement,

 $\{d1 || d2\}$ 

succeeds when executed on any subtree. Therefore, the effect of this statement as a whole is to perform a bottom-up pass of p, firing d1 and d2 on each visited subtree and succeeding if one of these rules successfully fires once.

• BU {d1 || d2}  $\rightarrow$  CNF-BU executes the statement,

BU 
$$\{d1 || d2\},\$$

and if it succeeds, fires CNF-BU recursively. Therefore, the effect of this statement (and the transformation as a whole) is to perform successive bottom-up passes of p, firing rules d1 and d2, and continuing with new passes until a pass of p is completed where no rules have successfully fired. Put another way, this transformation fires rules d1 and d2 exhaustively in bottom-up fashion.

Figure 4.3 illustrates the effect of firing CNF-BU on the KOLA predicate of Figure 4.1a. Figure 4.3a shows the parse tree representation of this predicate before it is transformed. The bottom-up pass visits the subtrees rooted at shaded nodes of the initial tree in the order indicated beneath each. Attempts to fire d1 and d2 on each proper subtree fail. But d1 successfully fires on the root, resulting in the predicate tree of Figure 4.3b. Because d1 successfully fired, another bottom-up pass is initiated on the tree resulting from firing (Figure 4.3b). Rule d1 fires successfully on the 8th subtree visited during this pass, resulting in the parse tree of Figure 4.3c. A final pass is performed over this parse tree where no rules successfully fire. Therefore, the tree of Figure 4.3c is returned as the final result of the transformation.

#### CNF-TD

Transformation CNF-TD (Figure 4.2b) is also an exhaustive algorithm for CNF. Unlike CNF-BU, CNF-TD fires rules in *top-down* (i.e., inorder) fashion during each pass, as indicated by the COKO operator TD. For CNF, the order in which subtrees are visited makes no difference to the final result. Rules d1 and d2 form a *confluent set* — the same result is returned no matter what order these rules are fired and no matter in what order parse trees are visited, provided that these rules are fired exhaustively.

Though the order in which subtrees are visited during rule firing has no effect on the predicate that results, order *does* affect the performance of the query rewrite itself. Table 4.1 shows a performance comparison of CNF-TD and CNF-BU. The transformations were compiled with our COKO compiler (described in Section 4.3.3) into C++ code which in turn was compiled on Sparcestation 10's using the Sun C++ compiler. For each height class, both

Height	Elapsed		CPU	
	CNF-TD	CNF-BU	CNF-TD	CNF-BU
4	0.17	0.17	0.07	0.07
5	0.42	0.48	0.23	0.26
6	1.19	2.05	1.07	1.68
7	3.24	4.18	3.05	3.98
8	7.71	12.95	6.69	11.63

Table 4.1: Average Times (in seconds) for CNF-TD and CNF-BU

transformations were run on the same 25 randomly generated queries. Both the elapsed time (the total time taken by the system to perform the rewrite) and the CPU time (the time for which the CPU is busy) were measured, and the times for all 25 queries were averaged.

For CNF, top-down exhaustive firing has better performance overall than bottom-up exhaustive firing. The performance discrepancy is due to the rules involved in these transformations. Consider that the result of firing either rule successfully is a conjunction of the form, (p | r) & (q | r). If additional rule firings are required, it would be because p (Case 1), q (Case 2) or r (Case 3) are of the form  $p_1 \& p_2$ , or because (Case 4) the entire predicate is a subpredicate,  $p_1$  of some disjunctive predicate,  $p_1 \mid p_2$ . Each of the four cases is equally likely given that our randomized query generating algorithm decides that a node is a conjunct or disjunct with equal probability. But top-down passes of the query tree will "catch" cases 1, 2 or 3 on the same pass that resulted in the initial firing because p, q and r will be subtrees of the newly formed predicate. On the other hand, a bottom-up pass will only "catch" case 4 on the same pass as the initial firing, and will require an additional pass to "catch" cases 1, 2 and 3. Therefore, a bottom-up transformation is more likely to require an additional pass to deal with the repercussions of a successful rule firing. This example illustrates how even subtle differences in firing algorithms such as traversal order can result in differences in performance. As we show below, the performance differences become marked when exhaustive firing algorithms can be avoided altogether.

#### 4.2.3 A Non-Exhaustive Firing Algorithm for CNF

Figure 4.4 shows an alternative COKO transformation (CNF) that rewrites KOLA predicates into CNF using a firing algorithm that is more efficient than the exhaustive algorithms of CNF-BU and CNF-TD. When CNF is fired on a predicate p, the statement

```
TRANSFORMATION CNFAuxTRANSFORMATION CNFUSESUSESd1: (p \& q) | r \rightleftharpoons (p | r) \& (q | r)CNFAuxd2: r | (p \& q) \rightleftharpoons (p | r) \& (q | r)BEGINBEGINBU CNFAux{d1 || d2} \rightarrowEND{GIVEN p' & q' DO {CNFAux (p'); CNFAux (q')}}(a)(b)
```

Figure 4.4: An Efficient CNF Transformation

performs a bottom-up pass of p, firing the auxiliary transformation, CNFAux on every subtree of p. The effect of firing CNFAux on a subtree s is described below:

- 1. As in CNF-BU and CNF-TD,  $\{d1 \mid | d2\}$  fires d1 on s, and then fires d2 on s if d1 fails.
- 2. Successful firing of either d1 or d2 results in the execution of the statement,

{GIVEN  $p' \& q' DO {CNFAux(p'); CNFAux(q')}$ 

on the predicate resulting from firing. This predicate will have the form,

 $(p \mid r) \& (q \mid r).$ 

The pattern, (p' & q') that follows the keyword GIVEN is matched with this predicate (i.e., p' gets bound to (p | r) and q' gets bound to (q | r)) and CNFAux is fired recursively on the subtrees bound to p' and q' respectively.

In short, CNF performs a bottom-up (BU) pass of p, firing the auxiliary transformation, CNFAux, on each visited subtree. CNFAux fires rewrite rules d1 and d2 and if either succeeds, initiates top-down passes on the conjunct subtrees that result from rule firing (by recursively firing CNFAux). Each top-down pass proceeds until a subtree is visited on which both d1 and d2 fail to fire.

The effect of this transformation on the KOLA predicate of Figure 4.1a are illustrated in Figure 4.5. Figure 4.5a shows the parse tree representation of this predicate before it is transformed. The bottom-up pass visits the shaded nodes of the initial tree in the order indicated beneath each. The firing of CNFAux fires d1 and d2. CNFAux fails to fire both rules (and therefore fails to fire) on every visited subtree except the root which is visited



Figure 4.5: Illustrating the CNF Firing Algorithm on the KOLA Predicate of Figure 4.1a

Height	Elapsed		CPU	
	CNF-TD	CNF	CNF-TD	CNF
4	0.17	0.15	0.07	0.05
5	0.42	0.20	0.23	0.10
6	1.19	0.35	1.07	0.24
7	3.24	0.59	3.05	0.48
8	7.71	1.35	6.69	1.17

Table 4.2: Average Times (in seconds) for CNF-TD and CNF

last (node 7). Firing d1 on the root results in the predicate tree of Figure 4.5b. Because d1 successfully fired, CNFAux is fired recursively on the two disjuncts produced from firing (the subtrees rooted by the shaded nodes of Figure 4.5b). Firing d1 and d2 on the first of these subtrees fails, and therefore terminates the top-down pass of this subtree. But d1 fires successfully on the second subtree, producing the predicate tree of Figure 4.5c. Again, successful firing initiates recursive firings of CNFAux on the subtrees rooted by the shaded nodes of Figure 4.5c. d1 and d2 fail to fire on both subtrees, and the tree of Figure 4.5c is returned.

Table 4.2 shows a performance comparison of the more efficient of the two exhaustive CNF transformations (CNF-TD) and CNF. CNF was run on the same 25 randomly generated queries as was used for the comparisons of Table 4.1. As before, both the elapsed time (the total time taken by the system to perform the transformation) and the CPU time (the time for which the CPU is busy) were measured, and the times for all 25 queries were averaged.

CNF exhibits far better performance than either of the exhaustive transformations. (For predicates of height 8, performance was improved by a factor of 6.) Intuitively, this is

because CNF is discriminating in how it fires rules:

- Successful firing of either d1 and d2 requires both exhaustive transformations to perform additional passes over the entire query tree. On the other hand, successful firing of either rule requires CNF to perform passes over only selected parts of the query tree.
- The exhaustive transformations require a complete pass of failed rule firings in order to terminate. This pass is not required by transformation CNF.

The savings in rule firings is illustrated by considering how all three transformations transform the KOLA predicate,

$$(\mathtt{P}_k \And \mathtt{Q}_k \And \mathtt{R}_k) \ | \ \mathtt{S}_k$$

CNF performs one complete and two partial passes over this predicate's representation, firing rules 20 times with two firings succeeding. On the other hand, CNF-TD performs two complete passes over this predicate's representation, firing rules 42 times with two succeeding. CNF-TD performs three complete passes over this predicate's representation, firing rules 52 times with two succeeding.<sup>3</sup>

#### Exhibited Features of COKO Firing Algorithms

CNF exhibits the fine-grained control of rule and transformation firing supported by COKO firing algorithms. It is this control that makes it possible to express efficient query rewrites. COKO supports four forms of rule-firing control:

- *Explicit Firing:* Rewrite rules used within a transformation are named (e.g., d1 and d2) and explicitly fired by the firing algorithm.
- *Traversal Control:* Both bottom-up (in CNF) and top-down (in CNFAux) passes can be performed in the course of rewriting predicates into CNF.
- Selective firing: CNFAux is fired recursively on the two disjuncts that result from successful firings of either d1 or d2. CNFAux is not fired on the conjunct resulting from these firings because both d1 and d2 can only succeed on trees rooted by "|".

<sup>&</sup>lt;sup>3</sup>For simplicity, we count each rule's firing on a literal (such as  $P_k$ ) as one firing. In fact, each literal is a subtree with multiple nodes. Therefore, visiting a literal results in more than one firing. These uncounted firings are the same for each algorithm. However, CNF will visit literals less frequently than the exhaustive transformations, and therefore will exhibit even better performance in comparison.

• Conditional firing: Some firings are conditioned on the success or failure of previous firings. E.g., CNFAux fires d2 only if d1 fails; CNFAux is only fired recursively if one of the rules d1 or d2 succeeds.

#### Correctness of CNF

Theorem 4.2.1 (Correctness) CNF is correct.

*Proof:* All query modification performed by CNF occurs as result of firing CNFAux, which in turn occurs as result of firing rules d1 and d2. Therefore, CNF is correct if both rewrite rules are correct. Rules d1 and d2 are proved correct by execution of the theorem prover scripts of Appendix B.1 using LP [46].  $\Box$ 

Proof that CNF transforms all KOLA predicates into CNF follows below.

**Lemma 4.2.1** Let p be a KOLA predicate tree lacking negations, and whose child subtrees are in CNF. Then CNFAux (p) is in CNF.

**Proof:** (By induction on the height, h(p) of the highest &-node in p.) For the base case (h(p) = 0) p must contain no &-nodes and therefore is in CNF and is returned untouched by CNFAux. For the inductive case, either p is already in CNF and is returned untouched, or p is not in CNF and is a disjunction,  $Q \mid R$  such that Q and R are in CNF and at least one of Q or R is a conjunction  $(x_0 \& x_1)$ . For the case where exactly one of Q and R is a conjunction, assume without loss of generality that Q is a conjunction. Then, h(Q) is larger than both  $h(x_0)$  and  $h(x_1)$  because both  $x_0$  and  $x_1$  are children of a &-node. Further, because R is in CNF it has no &-nodes and therefore h(p) = h(Q). Firing d1 on  $(Q \mid R)$  returns (S & T) such that  $S = (x_0 \mid R)$  and  $T = (x_1 \mid R)$ , and CNFAux is subsequently fired on S and T. But  $h(S) = h(x_0)$  and  $h(T) = h(x_1)$  and therefore by induction, these firings result in trees that are in CNF. Therefore, the tree returned by CNFAux (p) is in CNF.

For the case where both Q  $(x_0 \& x_1)$  and R  $(y_0 \& y_1)$  are conjunctions, h(p) is larger than  $h(x_0)$ ,  $h(x_1)$ ,  $h(y_0)$  and  $h(y_0)$  as all of the latter subtrees are children of &-nodes. Firing CNFAux on p fires d1 once, and d2 on each of the resulting disjuncts, leaving

$$(S_1 \& S_2) \& (T_1 \& T_2)$$

such that  $S_1 = (x_0 | y_0)$ ,  $S_2 = (x_1 | y_0)$ ,  $T_1 = (x_0 | y_1)$  and  $T_2 = (x_0 | y_1)$ . CNFAux is fired on each of  $S_1$ ,  $S_2$ ,  $T_1$  and  $T_2$  and by induction, each of these firings return a predicate in CNF. Therefore, CNFAux (p) is in CNF.  $\Box$ 

```
TRANSFORMATION CNF-NEG

USES

CNF,

involution: \sim (\sim (p)) \stackrel{\rightarrow}{=} p,

deMorgan1: \sim (p \& q) \stackrel{\rightarrow}{=} \sim (p) | \sim (q),

deMorgan2: \sim (p | q) \stackrel{\rightarrow}{=} \sim (p) \& \sim (q)

BEGIN

TD {involution || deMorgan1 || deMorgan2};

BU {involution};

CNF

END
```

Figure 4.6: The Full CNF Transformation Expressed in COKO

**Theorem 4.2.2** Let p be any KOLA predicate lacking negations. Then CNF (p) is in CNF.

*Proof:* Note that CNF (p) fires CNFAux on every subtree visited during a bottom-up traversal of p. By Lemma 4.2.1, each firing leaves a subtree in CNF, and therefore p is left in CNF.  $\Box$ 

#### Accounting for Negations

Figure 4.6 contains a COKO transformation that transforms all KOLA predicates into CNF, including those with negations. Besides using CNF, this transformation includes three other rules:

- involution eliminates double negations,
- deMorgan1 pushes down a negation past a conjunction, and
- deMorgan2 pushes down a negation past a disjunction.

The firing algorithm for the full CNF transformation executes two statements on the argument tree, p before firing CNF. These statements effectively push negations to the bottom of p's query tree while ensuring that consecutive negations are eliminated. The first statement performs a top-down pass of p firing the involution and deMorgan rules on each subtree visited during the traversal. Involution is then performed in a bottom-up pass of the resulting tree. This second pass is necessary because the first pass may construct doubly negated predicates. For example, a predicate of the form,

$$\sim~(\sim~(p)$$
 &  $q)$ 

will be transformed after the first pass to

$$\sim$$
 ( $\sim$  (p)) |  $\sim$  (q)

which must be transformed by a second pass firing the involution rule to

$$p \mid \sim (q).$$

Once all negations have been pushed to the bottom of the query (i.e., below all conjuncts and disjuncts), the resulting predicate can then be transformed into CNF using transformation CNF.

We have introduced COKO with a simple yet practical example. The normalization of predicates into CNF is a typical preprocessing rewrite for useful rewrites such as one that reorders selection predicates. We showed a COKO transformation (CNF) that performs this rewrite for predicates lacking negations and a complete COKO transformation (CNF-NEG) that removes this restriction and fires CNF as if it were a subroutine. Because its rules are confluent, CNF can also be implemented with exhaustive firing algorithms as in CNF-BU and CNF-TD. But exhaustive firing is an inefficient means of performing this transformation. Therefore, this example demonstrates the potential performance benefits from using customized firing algorithms to express complex query rewrites.

# 4.3 The Language of COKO Firing Algorithms

The semantics of statements that appear in COKO transformation firing algorithms have two parts:

- their operation (what they do when executed), and
- their success value (what they return as a result of execution).

Success values are truth values that indicate if a statement succeeds when executed. For example, fired rules return success values of *true* if their head patterns match the expressions on which they are fired. In general, success values are intended to indicate whether or not a statement accomplishes what it is intended to do. Note that a success value of false does **not**, in general, mean that a statement has failed to modify the expression on which it was executed.

#### 4.3.1 The COKO Language

Below we present COKO's statements, categorizing them by the kinds of firing control they provide. Each is presented with its *operation* and *success value* semantics. For the purposes of discussion, we assume that statements are contained in some transformation that has been fired on some KOLA query tree, p.

#### **Explicit Firing**

Rules and transformations declared in the USES section of a transformation can be fired as if they were procedures invoked in a programming language such as C. Rules and transformations can be fired on subtrees of p named by pattern variables (see Section 4.3.1) or can be fired on p directly, in which case no argument needs to be named. As well, rules that use the same pattern variables in their heads and their bodies can be fired *inversely*. For example, d1 of Figure 4.4 could be fired inversely (d1 INV) to factor a common subexpression ( $\mathbf{r}$ ) from a conjunction of disjuncts. Rule (and inverse rule) firings return *true* as their success values if they successfully fire. Transformation firings succeed if the complex statements that are their main bodies succeed (see Section 4.3.1).

#### **Traversal Control**

Query trees can be traversed in bottom-up (postorder) or top-down (preorder) fashion. For any statement S,

#### ${\rm BU}\;S$

performs a bottom-up pass of p executing S on every subtree. Analogously, TD S executes S on every subtree during a top-down pass of p. Both traversal statements return a success value of *true* if S succeeds when fired on some subtree visited during the traversal. Also,

#### ${\tt REPEAT} \ S$

fires S repeatedly on p until S no longer succeeds, and returns a success value of *true* if S succeeds at least once. Thus far, we have found BU, TD and REPEAT to be sufficient for expressing the kinds of traversal control we have needed to express for our firing algorithms. Our COKO compiler could be easily extended however, should we determine the need for another form of traversal control at a later point.

#### Selective Firing

Rules and transformations need not be fired on all of p and can instead be fired on selected subtrees of p. These subtrees are identified by matching patterns to query trees using COKO's GIVEN statement.

GIVEN patterns are like rule patterns, but can also include "don't care" variables ("\_"),<sup>4</sup> which act like pattern variables, but whose bindings are ignored. The COKO matching statement, GIVEN, identifies these patterns with variables, producing environments for use in subsequent statements. A GIVEN statement has the form,

GIVEN 
$$eqn_1, \ldots, eqn_n$$
 DO S.

such that S is any COKO statement, and each "equation",  $eqn_i$  is of the form,

$$< variable_i > = < pattern_i >$$

(or just  $pattern_i$ , if this pattern is to be matched with all of p). The processing of  $eqn_i$  results in an attempted match of  $pattern_i$  with the tree previously bound to  $variable_i$ . Successful matching adds the variables appearing in  $pattern_i$  (and the subtrees that they matched) to an environment that is then visible to equations appearing after  $eqn_i$  and S. The success value for the entire GIVEN statement is *true* if all n equations successfully match.

Unlike most programming languages, the environment visible inside statement S can shrink dynamically. Dynamically varying environments are necessary because environment entries label parts of a tree that can become obsolete as a result of a rule or transformation firing. To illustrate, suppose that the GIVEN statement,

GIVEN f ! \_\_, f = g  $\circ$  \_\_, g =  $\langle h, \pi_2 \rangle$  DO {transform-1 (g); transform-2 (h)}

were executed on the query,

$$(\langle \pi_1, \pi_2 \rangle \circ \pi_1) ! [[x, y], z].$$

The result of matching the three equations is to create an environment consisting of the labels f, g and h matched with the subtrees shown in Figure 4.7a.

Suppose that transform-1 is a transformation or rule that replaces g with a completely new tree. For example, transform-1 could be the rule,

$$\langle \pi_1, \pi_2 \rangle \stackrel{\rightarrow}{=} \mathbf{id}.$$

<sup>&</sup>lt;sup>4</sup>The COKO compiler recognizes four different "don't care" variables denoting predicates ( $\_P$ ), functions ( $\_F$ ), objects ( $\_O$ ) and Bools ( $\_B$ ) respectively. To simplify the presentation, we will use only a single "don't care" variable ( $\_\_$ ) for the examples presented in this thesis.



Figure 4.7: The Effects of a GIVEN Statement on Environments

Then the result of this firing would invalidate all variable bindings to trees that were proper subtrees of g (i.e., h), as these would no longer point to valid subtrees. Thus, the result of this firing would be to change the environment seen by the statement that follows to remove invalidated variable bindings, to the transformed environment of Figure 4.7b that no longer includes an entry for h.

The COKO compiler performs a dependency analysis of variables declared in matching equations, and indicates at compile time if a variable is used after it is invalidated. Thus, it would flag the firing of transform-2 (h) in this example as an error. In general, the invalidation of a variable, v occurs following execution of some statement S provided that S is a statement that modifies a query (i.e., a firing of a rule or another transformation), and S is executed on some variable w such that v names a subtree of the tree named by w.

#### **Conditional Firing**

One can condition the execution of a COKO statement, S' on the result of a previous statement, S in three ways:

- $S \to S'$  executes S and then executes S' if S succeeds. This statement succeeds if S succeeds.
- $S \parallel S'$  executes S and then executes S' if S fails. This statement succeeds if S or S' succeed.
- S; S' executes S and then executes S'. This statement succeeds if either S or S' succeed.

The complex statement connector, " $\rightarrow$ " is right-associative, and "|" and ";" are left-associative. One can override default associativities using braces ({}).

#### 4.3.2 TRUE, FALSE and SKIP

TRUE, FALSE and SKIP allow one to circumvent the default success values associated with COKO statements. For any statement, S,

#### TRUE S

executes S and returns a success value of *true*, regardless of the success value of S. (Similarly, FALSE S returns a success value of *false*.)

The statement SKIP performs no action at all and returns a success value of *true*. This statement is useful if one wants to define a transformation that returns a success value of *true* only if it rewrites expressions to a particular form. For example, consider a transformation whose purpose is to rewrite KOLA functions into constant functions (i.e., of the form,  $K_f(x)$  for some x). It might be desirable to return a success value of *true* only if functions that result from the transformation are of this form. However, the firing algorithm for this transformation may be a complex statement, S that does not always return the proper success value. In this case, one can achieve the desired effect by replacing the firing algorithm with

FALSE S;

GIVEN  $K_f(x)$  DO SKIP

The effect of this firing algorithm is to first execute S. Then, if a constant function is produced by S, the subsequent GIVEN statement succeeds and a success value of *true* is returned (because the ";"-separated statement succeeds if either of the separated statements succeeds, and because the GIVEN statement succeeds if the pattern,  $K_f(x)$  successfully matches the expression resulting from executing S). If a constant function is not generated by S, the GIVEN statement fails and so too does the transformation as a whole.

#### 4.3.3 The COKO Compiler

We have implemented a compiler for COKO ([68]) that generates C++ classes from COKO transformations. Objects of these generated classes manipulate KOLA trees according to the firing algorithm of the compiled COKO transformation. The compiler has an object-oriented design. Every COKO statement is implemented with its own C++ class. Each of these classes is a subclass of the virtual class, **Statement**, and is obligated to define a

method exec that takes an environment of variable-to-KOLA tree bindings as input and produces a transformed version of this environment as output. These environments include entries for the trees on which each statement is executed.

The compilation of a COKO transformation generates a new subclass of Statement, complete with an implementation of an exec method. The exec method definition for a compiled transformation simply constructs a tree of COKO Statement objects corresponding to the parse structure of the COKO code, and then invokes exec on the root. By compiling COKO transformations into Statements, COKO's language of firing algorithms is made extensible even at the level of its implementation.

# 4.4 Example 2: "Separated Normal Form" (SNF)

In this section we describe a novel normalization and show its expression in COKO. The normalization is of binary predicates, (in KOLA, predicates on pairs) and involves isolating those subpredicates that act as unary predicates on just one argument. This normalization is a useful preprocessing step when unary predicates need to be moved to other parts of the query as in predicate-pushdown, join-reordering and magic-sets rewrites. Because this normalization "separates" unary and binary subpredicates, we characterize the predicates that result as being in "Separated Normal Form" or SNF.

The point of this example is to show that COKO transformations are expressive enough to to be used in place of rules in existing rule-based systems. We make this point in several ways:

- The SNF normalization is more complex than CNF, even firing CNF as part of its firing algorithm. Therefore, COKO is expressive enough to capture complex normalizations.
- SNF is itself fired in the firing algorithms of many transformations that are not normalizations. These include predicate-pushdown (Section 4.5.1), join-reordering (Section 4.5.2) and Magic-Sets rewrites (Section 4.6). These examples show that COKO can express a wide variety of complex rewrites in modular fashion.
- SNF is not usually thought of as a normalization, and as far as we know has not been expressed before with declarative rewrite rules. Thus, COKO can express rewrites that are usually expressed only with code.

#### 4.4.1 Definitions

Intuitively, a KOLA binary predicate, op on pairs [x, y] is in SNF if it is of the form,

p & q & r

such that p is a unary predicate on x, q is a unary predicate on y and r is the minimal subpredicate of op that is a predicate on both x and y. In this section, we present a COKO transformation (SNF) that converts unnested SQL predicates into SNF. More formal definitions follow.

#### Qualifications

A qualification predicate is defined by Ramakrishnan [80] as:

... a Boolean combination (i.e., an expression using the logical connectives AND, OR and NOT) of <u>conditions</u> of the form expression cmp expression, where cmp is one of the comparison operators  $\{<, <=, =, <>, >=, >\}$ , [and an] <u>expression</u> is a *column* name, a *constant* or an arithmetic or string expression.

Essentially, qualifications are the predicates of unnested SQL queries.

KOLA qualification predicates are translations of SQL qualification predicates. They are defined formally in terms of *basic functions* (the KOLA equivalents of *expressions*) and *basic predicates* (the KOLA equivalents of *conditions*).

**Definition 4.4.1 (Basic Functions)** A basic function is a KOLA function of one of the forms below:

- att  $\circ \pi_1$  such that att is a primitive attribute (e.g., a column name),
- att  $\circ \pi_2$  such that att is a primitive attribute,
- $K_f(c)$  such that c is a constant, or
- op ⟨f, g⟩ such that f and g are basic functions and op is a binary primitive function (e.g., add).

**Definition 4.4.2 (Basic Predicate)** A basic predicate is a predicate of the form,

 $p\,\oplus\,\langle f,\,g
angle$ 

such that p is a binary primitive (eq, lt, gt, leq, geq or neq), and f and g are basic functions.
**Definition 4.4.3 (Qualifications)** A KOLA qualification predicate is a predicate consisting of conjunctions  $(\mathfrak{A})$ , disjunctions () and negations (~) of basic predicates.

#### SNF

We begin by defining functions and predicates that are *inherently binary*. Intuitively, inherently binary functions and predicates cannot be simplified in any way that makes them unary.

**Definition 4.4.4 (Inherently Binary Functions)** A KOLA function  $\overline{f}$  is inherently binary if it is of either of the forms:

- $op \circ \langle f \circ \pi_1, g \circ \pi_2 \rangle$ ,
- $op \circ \langle f \circ \pi_2, g \circ \pi_1 \rangle$ , or
- $op \circ \langle f, g \rangle$  such that f or g is inherently binary.

**Definition 4.4.5 (Inherently Binary Predicates)** A KOLA predicate  $\overline{p}$  is inherently binary if it is of the form,

 $p \, \oplus \, f$ 

such that f is an inherently binary function, or of the form.

 $p \mid q$ 

such that

- p or q is inherently binary, or
- one of p or q is of the form  $(r_1 \oplus \pi_1)$  and the other is of the form  $(r_2 \oplus \pi_2)$ .

**Definition 4.4.6 (SNF)** A KOLA predicate p is in SNF if it is of the form,

$$(
ho \oplus \pi_1)$$
 &  $(\sigma \oplus \pi_2)$  &  $au$ 

such that  $\tau$  is a conjunction,

 $au_1$  & ... &  $au_m$ 

of inherently binary and constant  $(K_p(b))$  predicates.

 $(\rho \oplus \pi_1)$  &  $(\sigma \oplus \pi_2)$  &  $\tau$  such that

Figure 4.8: The SQL/KOLA Predicates of Figure 4.1 in SNF

Given any pair argument  $[x, y], (\rho_k \oplus \pi_1)$ ?  $[x, y] = \rho_k$ ? x and therefore  $\rho_k$  denotes a predicate that requires only the first of its arguments. Similarly,  $\sigma_k$  denotes a predicate requiring the second argument. The restriction that  $\tau$  consist of inherently binary predicates ensures that a predicate in SNF has "moved" as many non-constant subpredicates into  $\rho$ and  $\sigma$  as possible. Figure 4.8 shows the SNF equivalent of the KOLA predicates of Figure 4.1. Note that for this predicate,  $\tau$  is a conjunction of inherently binary predicates,

 $P_k \mid (S2_k \oplus \pi_1)$ 

(which is inherently binary because  $P_k$  is inherently binary), and

 $Q_k \mid (S2_k \oplus \pi_1)$ 

(which is inherently binary because  $Q_k$  is inherently binary).

#### 4.4.2 A COKO Transformation for SNF

A COKO transformation that rewrites qualification predicates into SNF is shown in Figure 4.9 and its auxiliary transformations are shown in Figure 4.10. The latter figure contains three COKO transformations: SimpLits, LBConj and OrderConjs.

#### Tracing the Execution

The firing algorithm for transformation SNF of Figure 4.9 consists of the seven steps described below. We demonstrate these steps by showing how this transformation rewrites TRANSFORMATION SNF USES SimpLits, CNF, LBConj, OrderConjs,  $p \stackrel{\sim}{=} (K_p (true) \oplus \pi_1) \& (K_p (true) \oplus \pi_2) \& K_p (true) \& p,$ init: pull1:  $(p \oplus f) \mid (q \oplus f) \stackrel{\rightarrow}{=} (p \mid q) \oplus f$ , pull2:  $(\mathbf{p} \oplus \mathbf{f}) \mid \mathbf{K}_p$  (b)  $\stackrel{\rightarrow}{=} (\mathbf{p} \mid \mathbf{K}_p$  (b))  $\oplus$   $\mathbf{f}$ , pull3:  $K_p$  (b) | (q  $\oplus$  f)  $\stackrel{\rightarrow}{=}$  ( $K_p$  (b) | q)  $\oplus$  f, pull4:  $K_p$  (b1) |  $K_p$  (b2)  $\stackrel{\rightarrow}{=} K_p$  (b1 OR b2),  $\stackrel{}{=} p$  $K_p$  (true) & p simp: BEGIN -- (1) SimpLits; -- (2) CNF; -- (3) init; BU {pull1 || pull2 || pull3 || pull4}; -- (4) -- (5) LBConj; OrderConjs; -- (6) GIVEN  $(p \oplus \pi_1) \& (q \oplus \pi_2) \& r DO \{ simp (p); simp (q); simp (r) \}$  -- (7) END

Figure 4.9: The SNF Normalization Expressed in COKO

qualification predicate p of Figure 4.1a:

into the predicate of Figure 4.8. Figures 4.11 and 4.12 show the parse tree for this predicate at various stages during the execution of the transformation. The original predicate tree is shown in Figure 4.11a.

**Step 1:** The first step of SNF fires the transformation SimpLits (Simplify Literals) shown in Figure 4.10. The effect of firing SimpLits is to reduce subpredicates of the form  $(p \oplus f)$ to the forms  $(p \oplus \pi_1)$  or  $(p \oplus \pi_2)$  if such a reduction is possible. More precisely, SimpLits

```
TRANSFORMATION SimpLits
 USES
   sft: f \circ (g \circ h) \qquad \stackrel{\rightarrow}{\equiv} (f \circ g) \circ h
   sl1: \langle K_f(\mathbf{x}), K_f(\mathbf{y}) \rangle \stackrel{\rightarrow}{=} K_f([\mathbf{x}, \mathbf{y}]),
                                                  \stackrel{\rightarrow}{=} K<sub>f</sub> (f ! x),
   sl2: f \circ K_f(x)
                                                   \stackrel{\rightarrow}{=} \langle \mathbf{id}, \mathbf{K}_f (\mathbf{x}) \rangle \circ \mathbf{f},
   sl3: \langle f, K_f(x) \rangle
                                              \stackrel{\rightarrow}{\equiv} \langle \mathbf{K}_{f} (\mathbf{x}), \mathbf{id} \rangle \circ \mathbf{f},
   sl4: \langle K_f(x), f \rangle
   sl5: \langle f \circ h, g \circ h \rangle \stackrel{\rightarrow}{=} \langle f, g \rangle \circ h,
                                                 \stackrel{\rightarrow}{=} \mathbf{p} \oplus \mathbf{f} \oplus \mathbf{g},
   sl6: p \oplus (f \circ g)
                                        \stackrel{\rightarrow}{=} K<sub>p</sub> (p ? x)
   sl7: p \oplus K_f(x)
 BEGIN
   BU {s11 || s12 || {{s13 || s14} \rightarrow REPEAT sft} || s15 || s16 || s17 || REPEAT sft}
 END
TRANSFORMATION LBConj
 USES
  sftp: p \& (q \& r) \longrightarrow (p \& q) \& r
 BEGIN
  BU {sftp \rightarrow {GIVEN p & _ DO LBConj (p)}}
 END
TRANSFORMATION OrderConjs
 USES
   oc1: (\mathbf{p} \oplus \pi_1) \& (\mathbf{q} \oplus \pi_2) \& r \& (\mathbf{s} \oplus \pi_1) \stackrel{\rightarrow}{=} ((\mathbf{p} \& \mathbf{s}) \oplus \pi_1) \& (\mathbf{q} \oplus \pi_2) \& \mathbf{r},
  oc2: (\mathbf{p} \oplus \pi_1) \& (\mathbf{q} \oplus \pi_2) \& r \& (\mathbf{s} \oplus \pi_2) \stackrel{\rightarrow}{=} (\mathbf{p} \oplus \pi_1) \& ((\mathbf{q} \& \mathbf{s}) \oplus \pi_2) \& \mathbf{r},
                                                                          \stackrel{\scriptstyle \sim}{=} (\mathbf{p} \oplus \pi_1) \& (\mathbf{q} \oplus \pi_2) \& (\mathbf{r} \& \mathbf{s})
   oc3: (p \oplus \pi_1) & (q \oplus \pi_2) & r & s
 BEGIN
  BU {oc1 || oc2 || oc3}
 END
```

Figure 4.10: Auxiliary Transformations Used by SNF

transforms any basic predicate lacking subfunctions of the form  $(f \circ \pi_1)$  to either of the forms  $(p \oplus \pi_2)$  or  $K_p(x)$  (and similarly for predicates lacking  $(f \circ \pi_2)$  as a subfunction).

SimpLits performs a single bottom-up pass of the input predicate, firing rules

on each visited subtree. Rules sl1, ..., sl5 only fire successfully on function subtrees while sl6 and sl7 only fire successfully on predicate subtrees. Because the pass is bottom-up, a basic predicate is visited only after its subfunctions are visited.

SimpLits rewrites  $R_k$  (to  $R2_k$ ) and  $S_k$  (to  $S2_k$ ) but has no effect on  $P_k$  or  $Q_k$ . In rewriting  $R_k$ , SimpLits first fires rule s13 on its subfunction,

$$\langle \texttt{topic} \circ \pi_1, \texttt{K}_f (\texttt{"NSF"}) \rangle$$

generating

$$\langle \mathbf{id}, \mathsf{K}_f ("\mathsf{NSF"}) \rangle \circ (\mathsf{topic} \circ \pi_1)$$

The successful firing of s13 triggers the firing of sft leaving

$$(\langle \mathbf{id}, \mathsf{K}_f ("\mathsf{NSF"}) \rangle \circ \mathtt{topic}) \circ \pi_1.$$

Finally, rule s16 fires on the entire predicate leaving  $(R2_k \oplus \pi_1)$ .

When fired on  $S_k,\,\tt SimpLits$  first fires  $\tt sl5$  on its subfunction

$$\langle g \circ \pi_1, \mathbf{sum} \circ h \circ \mathbf{mems} \circ \pi_1 \rangle$$

leaving

$$\langle g, \mathbf{sum} \circ h \circ \mathsf{mems} \rangle \circ \pi_1.$$

Then, sl3, sft and sl6 fire, resulting in  $(S2_k \oplus \pi_1)$ . Therefore, the result of firing SimpLits on p is

$$p_1 = (\mathsf{P}_{\mathsf{k}} \And \mathsf{Q}_{\mathsf{k}} \And (\mathsf{R2}_{\mathsf{k}} \oplus \pi_1)) \mid (\mathsf{S2}_{\mathsf{k}} \oplus \pi_1)$$

as illustrated in Figure 4.11b.

**Step 2:** Next, transformation CNF of Figure 4.4 is fired. Applied to  $p_1$ , this firing results in

$$p_2 = (\mathsf{P}_{\mathsf{k}} \mid (\mathsf{S2}_{\mathsf{k}} \oplus \pi_1)) \And (\mathsf{Q}_{\mathsf{k}} \mid (\mathsf{S2}_{\mathsf{k}} \oplus \pi_1)) \And ((\mathsf{R2}_{\mathsf{k}} \oplus \pi_1) \mid (\mathsf{S2}_{\mathsf{k}} \oplus \pi_1))$$

as illustrated in Figure 4.11c.

**Step 3:** Rule **init** is fired, appending trivial conjuncts to the current predicate. The purpose of this step is to ensure the satisfaction of an invariant for **Step 4** which performs a bottom-up pass on the resulting predicate. This invariant establishes that every subtree visited during this bottom-up pass is of the form,

$$(
ho \oplus \pi_1)$$
 &  $(\sigma \oplus \pi_2)$  &  $au$ 

such that  $\tau$  is a conjunction of subpredicates to be "appended" to either  $\rho$ ,  $\sigma$  or neither. Fired on  $p_2$ , this step results in

$$p_3 = (\mathtt{K}_p \ (\mathtt{true}) \, \oplus \, \pi_1)$$
 &  $(\mathtt{K}_p \ (\mathtt{true}) \, \oplus \, \pi_2)$  &  $\mathtt{K}_p \ (\mathtt{true})$  &  $p_2$ 

as illustrated in Figure 4.11d.

**Step 4:** This step executes the COKO statement,

The effect of firing these rules in bottom-up fashion is to "pull" common functions out of disjuncts. For example, the result of executing pull1 on  $p_3$ 's subpredicate,

$$(\mathtt{R2}_{\mathtt{k}} \oplus \pi_1) \mid (\mathtt{S2}_{\mathtt{k}} \oplus \pi_1)$$

is  $(\mathtt{R2}_{\mathtt{k}} | \mathtt{S2}_{\mathtt{k}}) \oplus \pi_1$ . Therefore, this step converts disjuncts to the forms  $(p \oplus \pi_1)$  or  $(p \oplus \pi_2)$  where possible. Applied to  $p_3$ , this statement results in

$$p_4 = \begin{array}{l} \left( (\texttt{K}_p \ (\texttt{true}) \oplus \pi_1) \And (\texttt{K}_p \ (\texttt{true}) \oplus \pi_2) \And \texttt{K}_p \ (\texttt{true}) ) \And \\ \left( (\texttt{P}_k \mid (\texttt{S2}_k \oplus \pi_1)) \And (\texttt{Q}_k \mid (\texttt{S2}_k \oplus \pi_1)) \And (\texttt{R2}_k \mid \texttt{S2}_k) \oplus \pi_1 \right) \end{array}$$

as illustrated in Figure 4.11e.

Step 5: This step executes the COKO transformation, LBComp. This transformation rewrites a predicate that is in CNF,

$$p_1 \And p_2 \And \ldots \And p_n$$

(with conjunctions associated in any way), into a predicate of the form,

$$(\ldots(p_1 \& p_2) \& \ldots \& p_n)$$



Figure 4.11: Tracing the effects of SNF on the Predicate p of Fig 4.1a (Part 1)



Figure 4.12: Tracing the effects of SNF on the Predicate p of Fig 4.1a (Part 2)

that is "left-bushy" with respect to its parse tree. (Left-bushy conjunctions are defined more formally in the next section.) This step prepares the predicate for the following step that orders conjuncts. When applied to  $p_4$ , LBConj returns the left-bushy conjunction,

$$p_5 = \begin{array}{l} ((((((\mathsf{K}_p \ (\texttt{true}) \oplus \pi_1) \And (\mathsf{K}_p \ (\texttt{true}) \oplus \pi_2)) \And \mathsf{K}_p \ (\texttt{true})) \And \\ (\mathsf{P}_k \mid (\mathsf{S2}_k \oplus \pi_1))) \And (\mathsf{Q}_k \mid (\mathsf{S2}_k \oplus \pi_1))) \And ((\mathsf{R2}_k \mid \mathsf{S2}_k) \oplus \pi_1)) \end{array}$$

as illustrated in Figure 4.12f.

Step 6: This step fires the transformation OrderConjs shown in Figure 4.10. This transformation performs a bottom-up pass, firing rules oc1, oc2 and oc3 on subtrees of the form,

$$(p\oplus\pi_1)$$
 &  $(q\oplus\pi_2)$  &  $r$  &  $S$ 

for predicates p, q, r and S. Because of step **3**, the first subtree visited with this form has p, q and r equal to  $K_p$  (true), and S equal to a conjunct from the original predicate. The structure of S determines which rule gets fired:

- if S is of the form  $(s \oplus \pi_1)$ , then s is merged with p by rule oc1 to form  $((p \& s) \oplus \pi_1)$ .
- if S is of the form,  $(s \oplus \pi_2)$ , then s is merged with q by rule oc2 to form  $((q \& s) \oplus \pi_2)$ .
- if S is of any other form, then it is combined with r by rule oc3 to form (r & s).

The effect of this step on  $p_5$  is to transform it to

$$p_6 = ((\mathtt{K}_p \ (\mathtt{true}) \And 
ho_k) \oplus \pi_1) \And (\sigma_k \oplus \pi_2) \And (\mathtt{K}_p \ (\mathtt{true}) \And au_k)$$

(as illustrated in Figure 4.12g) such that  $\rho_k$ ,  $\sigma_k$  and  $\tau_k$  are as defined in Figure 4.8.

**Step 7:** Finally, this step fires rule simp to get rid of the  $K_p$  (true) predicates that were added in **Step 3**. (Note that  $\sigma_k$  of  $p_6$  above is not affected by this step.) The effect of this step on  $p_6$  is to produce the final KOLA predicate of Figure 4.8 that is illustrated in Figure 4.12h.

#### Correctness of SNF

Theorem 4.4.1 (Correctness) SNF is correct.

*Proof:* All query modification performed by SNF occurs as result of firing rules init, pull1, ..., pull4, and simp of transformation SNF; sft, sl1, ... sl7, of transformation SimpLits;

sftp of transformation LBComp; d1, d2, involution, deMorgan1 and deMorgan2 of CNF; and oc1, oc2, and oc3 of OrderConjs. Therefore, SNF is correct if these rules are correct. CNF's rules are proven correct by execution of the LP [46] theorem prover scripts of Appendix B.1. All other rules are proven correct by execution of the LP [46] theorem prover scripts of Appendix B.2.  $\Box$ 

Proof that SNF succeeds in transforming KOLA qualification predicates into SNF is shown by the lemmas and theorem below.

Lemma 4.4.1 (The Effect of SimpLits on Basic Functions) Let f be any basic function. Then SimpLits (f) will be a function of any of the forms shown below:

- $\overline{f} \circ \pi_1$  (type 1),
- $\overline{f} \circ \pi_2$  (type 2),
- $K_f(x)$  (type 3), or
- $\overline{f}$  such that  $\overline{f}$  is an inherently binary function (type 4).

*Proof:* (by induction on the height of f). For the base case, assume that f has height,  $h \leq 2$ . Then f must be either:

- 1. att  $\circ \pi_1$ ,
- 2. att  $\circ \pi_2$ , or
- 3.  $K_f(x)$ .

In any of these cases, no rules in SimpLits are fired and the functions are returned as is. The returned functions are types 1, 2 and 3 respectively.

For the inductive case, f has height = k > 2, and therefore must be of the form,

$$op \circ \langle f_1, f_2 \rangle$$

for some function op and basic functions  $f_1$  and  $f_2$ . Because SimpLits works bottom-up, induction applies to  $f_1$  and  $f_2$  and therefore, by the time the root of f is visited,  $f_1$  and  $f_2$ will have been rewritten to one of types 1, 2, 3 or 4. We summarize all possible combinations for  $f_1$  and  $f_2$  below: **Case 1** —  $f_1$  and  $f_2$  are type 3: Assume that  $f_1 = K_f(x)$  and  $f_2 = K_f(y)$ . In this case, rule **sl1** fires on  $\langle f_1, f_2 \rangle$  leaving  $K_f([x, y])$ . Subsequently, rule **sl2** fires on  $(op \circ K_f([x, y]))$  leaving

$$K_f (op ! \langle x, y \rangle)$$

which is also type 3.

**Case 2** —  $f_1$  and  $f_2$  are both type 1 or type 2: Let n be the type of  $f_1$  and  $f_2$ . Assume that  $f_1 = f'_1 \circ h$  and  $f_2 = f'_2 \circ h$  such that  $h = \pi_1$  or  $h = \pi_2$ . In this case, rule **sl5** fires on  $\langle f'_1 \circ h, f'_2 \circ h \rangle$  leaving  $(\langle f'_1, f'_2 \rangle \circ h)$ . Subsequently, rule **sft** fires on  $(op \circ (\langle f'_1, f'_2 \rangle \circ h))$ , leaving,

$$(op \circ \langle f'_1, f'_2 \rangle) \circ h$$

which is type n.

**Case 3** — One of  $f_1$  and  $f_2$  is type 3, and the other is type n (for  $n \neq 3$ ): Suppose first that  $f_1$  is type 3 and  $f_2 = f'_2 \circ h$  is type n. Then, rule s14 fires on  $\langle f_1, f_2 \rangle$  leaving

$$\langle g_1, g_2 \rangle \circ (f'_2 \circ h)$$

for some functions  $g_1$  and  $g_2$ . Sft subsequently fires on this function leaving

$$(\langle g_1, g_2 \rangle \circ f'_2) \circ h).$$

Sft fires again on

$$op \circ (\langle g_1, g_2 \rangle \circ f'_2) \circ h)$$

leaving

$$(op \circ (\langle g_1, g_2 \rangle \circ f'_2)) \circ h$$

which is type n.

A symmetric argument (such that s13 is fired instead of s14) handles the case where  $f_2$  is type 3.

**Case 4** – One of  $f_1$  and  $f_2$  is type 4, or one is type 1 and the other is type 2: If one of  $f_1$  or  $f_2$  is type 4, then no rules fire and  $\langle f_1, f_2 \rangle$  is inherently binary. No rules fire on  $(op \circ \langle f_1, f_2 \rangle)$ , and SimpLits returns this type 4 function.

If one of  $f_1$  or  $f_2$  is type 1 and the other is type 2, then no rules fire and again  $\langle f_1, f_2 \rangle$  is inherently binary. No rules fire on  $(op \circ \langle f_1, f_2 \rangle)$ , and SimpLits returns this type 4 function.  $\Box$ 

Lemma 4.4.2 (The Effect of SimpLits on Pairs of Basic Functions) Let  $f_1$  and  $f_2$  be any basic functions. Then SimpLits  $(\langle f_1, f_2 \rangle)$  will be a function of one of the forms shown below:

- $\overline{f} \circ \pi_1$  (type 1),
- $\overline{f} \circ \pi_2$  (type 2),
- $K_f(x)$  (type 3), or
- $\overline{f}$  such that  $\overline{f}$  is an inherently binary function (type 4).

*Proof:* Because SimpLits works bottom-up,  $f_1$  and  $f_2$  will be visited before  $\langle f_1, f_2 \rangle$ . By Lemma 4.4.1, when  $\langle f_1, f_2 \rangle$  is visited, both  $f_1$  and  $f_2$  will be of one of the following forms:

- $\overline{f} \circ \pi_1$  (type 1),
- $\overline{f} \circ \pi_2$  (type 2),
- $K_f(x)$  (type 3), or
- $\overline{f}$  such that  $\overline{f}$  is an inherently binary function (type 4).

The proof then proceeds by cases as before.

**Case 1** —  $f_1$  and  $f_2$  are both type 3: Assume that  $f = K_f(x)$  and  $g = K_f(y)$ . In this case, rule sl1 fires on  $\langle f, g \rangle$  leaving

$$\mathsf{K}_f([x, y])$$

which is type 3.

**Case 2** —  $f_1$  and  $f_2$  are both type 1 or type 2: Let n be the type of  $f_1$  and  $f_2$ . Assume that  $f_1 = f'_1 \circ h$  and  $f_2 = f'_2 \circ h$  such that  $h = \pi_1$  or  $h = \pi_2$ . In this case, rule s15 fires on  $\langle f'_1 \circ h, f'_2 \circ h \rangle$  leaving

$$\langle f_1', f_2' \rangle \circ h,$$

which is type n.

**Case 3** — One of  $f_1$  and  $f_2$  is type 3, and the other is type n (for  $n \neq 3$ ): Suppose first that  $f_1$  is type 3 and  $f_2 = f'_2 \circ h$  is type n. Then, rule s14 fires on  $\langle f_1, f_2 \rangle$  leaving

$$\langle g_1, g_2 \rangle \circ (f'_2 \circ h)$$

for some functions  $g_1$  and  $g_2$ . Sft subsequently fires on this function leaving

$$(\langle g_1, g_2 \rangle \circ f'_2) \circ h)$$

which is type n. A symmetric argument (such that **sl3** is fired instead of **sl4**) handles the case where  $f_2$  is type 3.

**Case 4** – One of  $f_1$  and  $f_2$  is type 4, or one is type 1 and the other is type 2: If one of  $f_1$  or  $f_2$  is type 4, then no rules fire and  $\langle f_1, f_2 \rangle$  is inherently binary (type 4). If one of  $f_1$  or  $f_2$  is type 1 and the other is type 2, then no rules fire and again  $\langle f_1, f_2 \rangle$  is inherently binary (type 4).  $\Box$ 

Lemma 4.4.3 (The Effect of SimpLits on Basic Predicates) Let  $p = q \oplus f$  be any basic predicate. Then SimpLits (p) will be a predicate of one of the following forms:

- $\overline{p} \oplus \pi_1$  (type 1),
- $\overline{p} \oplus \pi_2$  (type 2),
- $K_p$  (b) (type 3), or
- $\overline{p}$  such that  $\overline{p}$  is an inherently binary predicate (type 4).

*Proof:* Observe that the bottom-up pass of SimpLits ensures that f is visited before p. Function f is of the form,  $\langle f_1, f_2 \rangle$  such that  $f_1$  and  $f_2$  are basic functions. By Lemma 4.4.2, once p is visited during the bottom-up pass of SimpLits, it is of one of the forms below:

- 1.  $\overline{p} \oplus (\overline{f} \circ \pi_1)$
- 2.  $\overline{p} \oplus (\overline{f} \circ \pi_2),$
- 3.  $\overline{p} \oplus K_f(x)$ , or
- 4.  $\overline{p} \oplus \overline{f}$  such that  $\overline{f}$  is inherently binary.

$$(\overline{p} \oplus \overline{f}) \oplus \pi_1$$
 (type 1), or  
 $(\overline{p} \oplus \overline{f}) \oplus \pi_2$  (type 2).

In the third case, rule **s17** fires leaving

$$K_p$$
 ( $\overline{p}$  ?  $x$ ) (type 3).

And in the fourth case, no rule fires leaving the inherently binary predicate,

$$\overline{p} \oplus \overline{f}$$
 (type 4)  $\Box$ .

Lemma 4.4.4 (The Effect of SimpLits on Qualification Predicates) Let p be a qualification predicate. Then SimpLits (p) will consist of conjunctions, disjunctions and negations of predicates of one of the forms listed below:

- $\overline{p} \oplus \pi_1$ ,
- $\overline{p} \oplus \pi_2$ ,
- $K_p(b)$ , or
- $\overline{p}$  such that  $\overline{p}$  is an inherently binary predicate.

*Proof:* Because SimpLits works bottom-up, all basic predicates are visited before those of the form (p & q), (p | q) or  $(\sim (p))$ . SimpLits has no effects on predicates of these latter forms. Therefore, by Lemma 4.4.3 SimpLits leaves a predicate consisting of conjuncts, disjuncts or negations of predicates of the forms above.  $\Box$ 

**Definition 4.4.7 (Left-Bushy Conjunctions)** A left-bushy conjunction is any KOLA predicate that can be constructed according to the following rules:

- literals and disjuncts containing no subpredicates of the form  $(r_1 \& r_2)$  are left-bushy conjunctions,
- p & q is a left-bushy conjunction if p is a left-bushy conjunction and q is a literal or disjunct containing no subpredicates of the form  $(r_1 \& r_2)$ .

Next, we show that LBComp rewrites predicates in CNF into left-bushy conjunctions.

Lemma 4.4.5 (The Effect of LBConj on Predicates in CNF (Part 1)) Let p and q be left-bushy conjunctions. Then, LBConj (p & q) is a left-bushy conjunction.

*Proof:* The proof is by induction on the number, n, of conjunctions in q. For the base case, n = 0, (p & q) is already left-bushy and LBConj does nothing. In the inductive case,  $q = q_1 \& q_2$ . By the definition of left-bushy conjunctions,  $q_1$  is a left-bushy conjunction and  $q_2$  is a literal or disjunct containing no subpredicates that are conjunctions. In this case, rule sftp fires leaving,

$$(p \& q_1) \& q_2.$$

LBConj is subsequently fired on  $(p \& q_1)$  leaving, by induction, a left-bushy conjunction,  $p_2$ . Therefore, the predicate

 $p_2$  &  $q_2$ 

is also a left-bushy conjunction.  $\Box$ 

Lemma 4.4.6 (The Effect of LBConj on Predicates in CNF (Part 2)) Let p be a predicate in CNF. Then, LBConj (p) is left-bushy conjunction.

*Proof:* Because LBConj works bottom up, it visits p and q before it visits (p & q). A simple inductive argument using Lemma 4.4.5 establishes LBConj to return a left-bushy conjunction when fired on p.  $\Box$ 

**Theorem 4.4.2 (SNF)** Given any KOLA qualification predicate p, SNF (p) is a predicate in SNF.

Proof: The proof consists of seven parts, proving invariants that hold after the execution of each step 1-7.

**Invariant** 1 : After firing SimpLits, p consists of conjunctions, disjunctions and negations of predicates of one of the forms listed below:

- $\overline{p} \oplus \pi_1$  (type 1),
- $\overline{p} \oplus \pi_2$  (type 2),
- $K_p$  (b) (type 3),
- $\overline{p}$  such that  $\overline{p}$  is an inherently binary predicate (type 4).

This invariant was shown to result from firing SimpLits by Lemma 4.4.4.

**Invariant 2:** After firing CNF, p is of the form,

$$p_0$$
 & ... &  $p_n$ 

with each  $p_i$  a disjunction of possibly negated literals of one of the four types listed in *Invariant 1*. This invariant was shown to result from firing CNF in Section 4.2.3.

*Invariant 3:* After firing init, p is of the form,

 $(\mathtt{K}_p (\mathtt{true}) \oplus \pi_1)$  &  $(\mathtt{K}_p (\mathtt{true}) \oplus \pi_2)$  &  $(\mathtt{K}_p (\mathtt{true}))$  &  $p_1$  &  $\dots$  &  $p_n$ 

with each  $p_i$  disjunction of possibly negated literals of one of the four types listed in *Invariant* 1.

*Invariant 4:* After executing BU {pull1 || pull2 || pull3 || pull4}, p is of the form,

 $(\texttt{K}_p (\texttt{true}) \oplus \pi_1)$  &  $(\texttt{K}_p (\texttt{true}) \oplus \pi_2)$  &  $(\texttt{K}_p (\texttt{true}))$  &  $q_1$  &  $\dots$  &  $q_n$ 

such that each  $q_i$  is of any of the forms shown below:

- $\overline{p} \oplus \pi_1$  (type 1),
- $\overline{p} \oplus \pi_2$  (type 2),
- $K_p$  (b) (type 3), or
- $\overline{p}$  such that  $\overline{p}$  is an inherently binary predicate (type 4).

Note that none of the rewrite rules,  $pull1, \ldots, pull4$ , affect the conjuncts at the top of the tree, or the negations at the bottom. Rather, only disjuncts are affected. The proof then is by induction on the height h of a disjunct (such that literals are viewed as having height 0). For the base case, h = 0 and no rules fire. In this case, we are left with a literal of types 1, 2, 3 or 4 (as listed in *Invariant 1*).

The induction proof considers the disjunct,  $p_1 \mid p_2$  such that  $p_1$  and  $p_2$  are (by induction) of types 1, 2, 3 or 4. The proof proceeds by cases:

- Case  $1 p_1$  and  $p_2$  are both type 1 or type 2: Let n be the type of  $p_1$  or  $p_2$ . In this case, rule pull1 fires and we are left with a type n predicate.
- Case  $2 p_1$  and  $p_2$  are both type 3: In this case, pull4 fires and we are left with a type 3 predicate.
- Case 3 One of  $p_1$  or  $p_2$  is type 4, or one is type 1 and the other is type 2: In this case, no rule fires and we are left with a type 4 predicate.

*Invariant 5:* After firing LBConj, *p* is a left-bushy conjunction (as proven by Lemma 4.4.6).

**Invariant 6:** After firing OrderConjs, p will be of the form

$$(
ho \oplus \pi_1)$$
 &  $(\sigma \oplus \pi_2)$  &  $au$ 

such that  $\tau$  is a conjunction of  $m \ (m \ge 0)$  inherently binary or constant predicates (i.e., p will be in SNF). Again, the proof of the invariant is by structural induction. exploiting the bottom-up nature of OrderConjs. In the base case, OrderConjs is fired on

$$(\mathtt{K}_p (\mathtt{true}) \oplus \pi_1)$$
 &  $(\mathtt{K}_p (\mathtt{true}) \oplus \pi_2)$  &  $\mathtt{K}_p (\mathtt{true}),$ 

doing nothing and leaving a predicate that is trivially in SNF.

Because p is a left-bushy conjunction, in the inductive case OrderConjs is fired on a predicate of the form,

$$((((
ho \oplus \pi_1) \And (\sigma \oplus \pi_2)) \And au) \And p_1$$

such that  $p_1$  is of one of the types listed in **Invariant 4**. If  $p_1$  is type 1, then it is merged with  $\rho$  by rule oc1 to form ( $\rho \& p_1$ )  $\oplus \pi_1$ , leaving,

$$((
ho \& p_1) \oplus \pi_1) \& (\sigma \oplus \pi_2) \& au$$

which is in SNF. If  $p_1$  is type 2, then it is merged with  $\sigma$  by rule oc2 to form ( $\sigma \& p_1$ )  $\oplus \pi_2$ , leaving,

$$(
ho \oplus \pi_1)$$
 &  $((\sigma$  &  $p_1) \oplus \pi_2)$  &  $au$ 

which is in SNF. Finally, if  $p_1$  is type 3 or 4, then it is merged with  $\tau$  by rule oc3 to form  $(\tau \& p_1)$ , leaving,

$$(
ho \oplus \pi_1)$$
 &  $(\sigma \oplus \pi_2)$  &  $(\tau$  &  $p_1)$ 

which is in SNF.

*Invariant 7:* After completion of the final step of the firing algorithm, we are left with a predicate in SNF,

$$(
ho \oplus \pi_1)$$
 &  $(\sigma \oplus \pi_2)$  &  $au$ 

such that neither  $\rho$ ,  $\sigma$  nor  $\tau$  is of the for,

$$K_p$$
 (true) &  $p$ .

Satisfaction of this invariant follows trivially by examination of the rewrite rule, simp.

# 4.5 Example Applications of SNF

#### 4.5.1 Example 3: Predicate-Pushdown

Figure 4.13 shows a COKO transformation that pushes predicates past joins. The key rule of this transformation is **push**, which identifies subpredicates (**p** and **q**) of join predicates that apply only to one argument, and pushes these subpredicates out of the join and onto the join inputs. This heuristic is useful as it will usually result in a join of smaller collections.

Rule **push** will not fire successfully on every join query, for the predicate used in the join may not be in a form that makes "pushable" subpredicates recognizable. For example, if this rule were fired on the query,

join  $(p, \pi_1)$  ! [Coms, SComs]

such that Coms and SComs are collections of committees and subcommittees respectively as presented in Table 2.1, and p is the predicate of Figure 4.1a, it fails because this predicate does not match the pattern,

$$(\mathsf{p}\oplus\pi_1)$$
 &  $(\mathsf{q}\oplus\pi_2)$  & r.

Therefore before this rule is fired, the predicate argument to **join** is normalized into SNF so that "pushable" subpredicates can be identified. In the case of the predicate of Figure 4.1a, normalization into SNF results in the query,

$$\mathbf{join}~((
ho\oplus\pi_1)$$
 &  $(\sigma\oplus\pi_2)$  &  $au,~\pi_1)$  ! [Coms, SComs]

such that  $\rho$ ,  $\sigma$  and  $\tau$  are as defined in Figure 4.8. Once in this form, firing **push** results in

join  $(\tau, \pi_1)$  ! [iterate  $(\rho, id)$  ! Coms, iterate  $(\sigma, id)$  ! SComs].

In this case,  $\sigma$  is  $K_p$  (true). Therefore, the subsequent firing of rule, simplify results in the query,

join  $(\tau, \pi_1)$  ! [iterate  $(\rho, id)$  ! Coms, SComs].

#### 4.5.2 Example 4: Join-Reordering

Figure 4.14 shows a COKO transformation that might be fired to change the order in which multiple joins are evaluated. Transfomation Join-Associate reassociates a composition of join queries. That is, a query of the form,

join (..., ...) ! [join (..., ...) ! [A, B], C]

```
TRANSFORMATION Pushdown

USES

SNF,

push: join ((p \oplus \pi_1) \& (q \oplus \pi_2) \& r, f) ! [A, B] \stackrel{\rightarrow}{=}

join (r, f) ! [iterate (p, id) ! A, iterate (q, id) ! B],

simplify: iterate (K_p (true), id) ! A \stackrel{\rightarrow}{=} A

BEGIN

GIVEN join (p, \_) ! \_ DO SNF (p);

push;

GIVEN __ ! [A, B] DO {simplify (A); simplify (B)}

END
```

Figure 4.13: Pushdown: A COKO Transformation to Push Predicates Past Joins

gets rewritten to

```
join (..., ...) ! [A, join (..., ...) ! [B, C]].
```

Join-Associate first normalizes join predicates into SNF. The innermost join predicate (q) gets normalized by SNF into,

 $(p_2 \oplus \pi_1) \& (q_2 \oplus \pi_2) \& r_2.$ 

The outermost join predicate (p) gets normalized by SNF into the form,

 $(\mathtt{p_1} \oplus \pi_1)$  &  $(\mathtt{q_1} \oplus \pi_2)$  &  $\mathtt{r_1}$ .

The innermost join predicate applies to pairs, [a, b] (for  $a \in A$  and  $b \in B$ ). Therefore,  $p_2$  applies to a,  $q_2$  applies to b, and  $r_2$  applies to [a, b]. The outermost join predicate applies to pairs,  $[f_2 ! [a, b], c]$  (for  $f_2 ! [a, b]$  in the result of the innermost join, and  $c \in C$ ). Therefore,  $p_1$  applies to  $f_2 ! [a, b]$ ,  $q_2$  applies to c, and  $r_3$  applies to  $f_2 ! [[a, b], c]$ .

Firing shift on this normalized query results in a new query for which the innermost join predicate and function are applied to pairs, [b, c] and and the outermost join predicate and function are applied to pairs, [a, [b, c]]. Therefore, the rewrite rule places:

- $(q_2 \oplus \pi_1)$  in the innermost predicate because  $(q_2 \oplus \pi_1)$ ?  $[b, c] = q_2$ ? b.
- $(q_1 \oplus \pi_2)$  in the innermost predicate because  $(q_1 \oplus \pi_2)$ ?  $[b, c] = q_1$ ? c.
- $(\mathbf{p}_2 \oplus \pi_1)$  in the outermost predicate because  $(\mathbf{p}_2 \oplus \pi_1)$ ?  $[a, [b, c]] = \mathbf{p}_2$ ? a.
- $(\mathbf{r}_2 \oplus (\mathbf{id} \times \pi_1))$  in the outermost predicate because

 $(r_2 \oplus (id \times \pi_1))$ ?  $[a, [b, c]] = r_2$ ? [a, b].

```
TRANSFORMATION Join-Associate

USES

shift: join ((p_1 \oplus \pi_1) \& (q_1 \oplus \pi_2) \& r_1, f_1) !

[join ((p_2 \oplus \pi_1) \& (q_2 \oplus \pi_2) \& r_2, f_2) ! [A, B], C] \stackrel{\rightarrow}{=}

join ((p_1 \oplus f_1) \& (r_1 \oplus h_1) \& (p_2 \oplus f_2) \& (r_2 \oplus h_2), f_1 \circ h_1) !

[A, join ((q_1 \oplus g_1) \& (q_2 \oplus g_2), id) ! [B, C]]

SNF

BEGIN

GIVEN join (p, \_) ! [join (q, \_) ! [\_, \_], \_] DO \{SNF (p); SNF (q); shift\}

END
```

such that

$$f_1 = \mathbf{f}_2 \circ (\mathbf{id} \times \pi_1)$$
  

$$g_1 = \pi_2$$
  

$$h_1 = \langle \mathbf{f}_2 \circ (\mathbf{id} \times \pi_1), \pi_2 \circ \pi_2 \rangle$$
  

$$f_2 = \pi_1$$
  

$$g_2 = \pi_1$$
  

$$h_2 = \mathbf{id} \times \pi_1$$

Figure 4.14: Join-Associate: A COKO Transformation to Reassociate a Join

•  $(p_1 \oplus (f_2 \oplus (id \times \pi_1)))$  in the outermost predicate because

 $(p_1 \oplus (f_2 \oplus (id \times \pi_1)))$ ?  $[a, [b, c]] = p_1$ ?  $(f_2 ! [a, b]),$ 

and

•  $(\mathbf{r_1} \oplus \langle \mathbf{f_2} \circ (\mathbf{id} \times \pi_1), \pi_2 \circ \pi_2 \rangle)$  in the outermost predicate because

 $(\mathbf{r}_1 \oplus \langle \mathbf{f}_2 \circ (\mathbf{id} \times \pi_1), \pi_2 \circ \pi_2 \rangle)$ ?  $[a, [b, c]] = \mathbf{r}_1$ ?  $[\mathbf{f}_2 ! [a, b], c]$ .

While the predicates that result from this rewrite are quite complex, in most cases they can be simplified afterwards. For example, any subpredicates for which  $p_1, q_1, \ldots, r_2$  is  $K_p$  (true) can be made to drop away as a result of simplification.

# 4.6 Example 5: Magic-Sets

The idea behind the Magic-Sets transformation for relational queries introduced by Mumick et al [74] is to restrict the inputs to a join by filtering those elements that cannot possibly satisfy the join predicate. Therefore, this transformation is very much in the spirit of predicate-pushdown, but passing filter predicates "sideways" from one join input to another,

```
SELECT c

FROM c IN Coms, t in Temp

WHERE P(c, t) AND Q(c, t) AND R(c)

Temp (chair, avgTerms) =

SELECT z.chair, AVG (SELECT m.terms FROM x IN partition, m IN x.mems)

FROM z IN Coms

GROUP BY z.chair

P(c, t) = c.chair == t.chair

Q(c, t) = c.chair.terms > t.avgTerms

R(c) = c.chair.terms > t.avgTerms

a. Before (OQL)
```

```
join (P_k \& Q_k \& R_k, \pi_1) ! [Coms, Temp<sub>K</sub>]
```

Figure 4.15: OQL (a) and KOLA (b) queries to find all committees whose chair is a Democrat and has served more than the average number of terms of the members of his/her chaired committees.

rather than down from the join predicate. As with predicate-pushdown and join-reordering, the magic-sets rewrite requires first normalizing the join predicate into SNF so that the predicate that can be passed sideways can be identified.

#### 4.6.1 An Example Magic-Sets Rewrite

#### Expressed in OQL

To illustrate, consider the OQL query of Figure 4.15a. This query returns the committees in Coms that are chaired by someone who is a Democrat and who has served more terms than

```
SELECT c
FROM c IN MComs, t IN MTemp
WHERE P(c, t) AND Q(c, t)
MComs =
    SELECT m3
    FROM m3 IN MComs
    WHERE R(m3)
CSet(chair) =
    SELECT DISTINCT m2.chair
    FROM m2 IN MComs
MTemp (chair, avgTerms) =
   SELECT z.chair, AVG (SELECT m.terms FROM x IN partition, m IN x.mems)
   FROM z IN Coms, y IN CSet
   WHERE z.chair == y.chair
   \texttt{GROUP} \ \texttt{BY} \ z.\texttt{chair}
 P(c,t) = c.chair == t.chair
 Q(c,t) = c.\texttt{chair.terms} > \texttt{t.avgTerms}
R(m3) = m3.chair.pty == "Dem"
                                                  c. After (OQL)
join (P_k' \& Q_k', \pi_1) ! [MComsk, MTempk]
MComs_k = iterate (R'_k, id) ! Coms
  CSet_k = set ! (iterate (K_p (true), chair) ! MComs_k)
\texttt{MTemp}_k = \texttt{njoin} (\texttt{eq} \oplus (\texttt{id} \times \texttt{chair}), \texttt{mems}, \texttt{avg} \circ \texttt{flat}) ! [\texttt{CSet}_k, \texttt{Coms}]
\begin{array}{lll} P'_k &=& \mathbf{eq} \oplus (\texttt{chair} \times \mathbf{id}) \oplus (\mathbf{id} \times \pi_1) \\ Q'_k &=& \mathbf{gt} \oplus ((\texttt{terms} \circ \texttt{chair}) \times \pi_2) \oplus (\mathbf{id} \times \pi_2) \\ R'_k &=& \mathbf{eq} \oplus (\langle \mathbf{id}, \texttt{K}_f \ (\texttt{``Dem"}) \rangle \circ \texttt{pty} \circ \texttt{chair}) \end{array}
                                                 d. After (KOLA)
```

Figure 4.16: The queries of Figure 4.15 after rewriting by Magic-Sets

is average for the members of the committees he or she chairs. The query result is generated from a join of Coms and the view, Temp. Temp groups each committee chair, c.chair with the result of the OQL expression,

AVG (SELECT m.terms FROM x IN partition, m IN x.mems)

that averages the number of terms served by members of committees chaired by c.chair (partition names the collection of all member sets for committees chaired by a given legislator). The join of Coms and Temp then uses join predicates P, Q and R on pairs from Coms (c) and Temp (t) such that

- P holds if c is chaired by the chair represented by t,
- Q holds if c's chair has served more terms than the number of terms associated with t, and
- *R* holds if **c** is chaired by a Democrat.

Each entry in Temp can be expensive to calculate, as each requires averaging values extracted from a collection of collections. The Magic-Sets query rewrite addresses this expense by observing that entries need not be computed for every committee chair. In particular, only committees whose chairs are Democrats can possibly contribute to the query result. Therefore, the Magic-Sets rewrite passes the predicate on Coms that requires committee chairs to be Democrats (R) sideways to Temp. Rewriting produces the query shown in Figure 4.16c, which includes three view definitions:

- MComs is the subcollection of Coms chaired by Democrats.
- CSet is the set of committee chairs who are Democrats.
- MTemp is the subcollection of Temp consisting of entries only for those committee chairs who are represented in CSet.

Unlike Temp of Figure 4.15a, MTemp does not compute average numbers of terms for every chair of a committee in Coms. Instead, only those chairs who are represented in CSet are represented in the result. CSet is the set of all committee chairs who are Democrats. Therefore, the equijoin of Coms and CSet prior to grouping ensures that aggregation is performed only for committee chairs that are Democrats.

The main query then is a join of MComs and MTemp using join predicates P and Q. Unlike the original form of the query, this form of the query requires additional projection and duplicate elimination to generate CSet and an additional join to compute MTemp. However, in many cases this additional cost is more than offset by the savings in not having to compute average terms for committee chairs who are not Democrats.

#### Expressed in KOLA

Figures 4.15b and 4.16d show the KOLA equivalents of the OQL queries of Figures 4.15a and 4.16c respectively. The main query of Figure 4.15b performs a join of Coms and Temp<sub>K</sub> (the KOLA equivalent of Temp). The join predicate is the conjunction,

$$P_k$$
 &  $Q_k$  &  $R_k$ 

such that  $P_k$  is the KOLA equivalent to P and so on. The join function returns the first element (the committee) of each pair, [c, t] ( $c \in \text{Coms}$  and  $t \in \text{Temp}_K$ ) satisfying the join predicate.

 $\operatorname{Temp}_K$  is the KOLA equivalent of  $\operatorname{Temp}$ , but for the naming of fields in the result. It uses **njoin** to associate chairs of committees in Coms,

(**iterate** (
$$K_p$$
 (true), chair) ! Coms)

with the sets of committees they chair. (For any committee chair l and committee c,

$$(\mathbf{eq} \oplus \langle \pi_1, \mathtt{chair} \circ \pi_2 \rangle)$$
 ? [*l*, *c*]

holds if c is chaired by l.) For each committee c chaired by l, the set of c's members (c.mems) are added to an intermediate collection of legislator collections associated with l. Then, the function,  $\mathbf{avg} \circ \mathbf{flat}$  is applied to the result, first flattening this collection into a single collection of legislators, and then averaging the number of terms they have served.

As with the OQL query of Figure 4.16c, the KOLA query of Figure 4.16d performs a join of two new collections,  $MComs_k$  and  $MTemp_k$ . The join predicate for this join is a conjunction of predicates  $P'_k$  and  $Q'_k$  that are equivalent but transformed versions of predicates  $P_k$  and  $Q_k$  of Figure 4.15b. Like MComs,  $MComs_k$  filters Coms for those committees that satisfy  $R'_k$ (which is equivalent to  $R_k$ , but rewritten into a unary predicate). Like MTemp,  $MTemp_k$ groups committees only if the committees are chaired by someone represented in  $CSet_k$ (CSet). And like CSet,  $CSet_k$  determines the set of committee chairs for committees in  $MComs_k$  (MComs).

```
TRANSFORMATION Magic
 USES
  SNF2, Pushdown, SimplifyJoins,
            join (q \oplus (id \times \pi_1) \& r, f) ! [A1, njoin (p, g, h) ! [A2, B]]
                                                                                   \stackrel{\rightarrow}{=}
  magic:
               join (q \oplus (id \times \pi_1) \& r, f)!
                 [A1, njoin (p, g, h) !
                        [set ! (join (q, \pi_2) ! [A1, A2]), B]],
            (p \& q) \& r \stackrel{\rightarrow}{=} p \& (q \& r)
  sftp:
 BEGIN
   Pushdown;
                                                                           -- Step 1
   GIVEN join (p, __) ! __ DO {SNF2 (p); sftp (p)}
                                                                           -- Step 2
                                                                           -- Step 3
   magic
   GIVEN _ ! [_, A], A = _ ! [B, _] DO {SimplifyJoin (B)}
                                                                           -- Step 4
 END
```

Figure 4.17: The Magic-Sets Rewrite Expressed in COKO

#### 4.6.2 Expressing Magic-Sets in COKO

A COKO Magic-Sets transformation that converts the KOLA query of Figure 4.15b to that of Figure 4.16d is shown in Figure 4.17. The key rewrite rule of this transformation is **magic**, which assumes that a predicate argument to a join query has first been normalized into the form

$$(\mathbf{q} \oplus (\mathbf{id} \times \pi_1))$$
 & r.

This normal form isolates the subpredicate,  $\mathbf{q}$ , which relates elements of A1 and A2, as is evident by tracing the evaluation of this predicate on any pair,  $[a_1, [a_2, S]]$  such that  $a_1 \in A1$ , and  $[a_2, S]$  belongs to the result of the **njoin** subquery:

$$(q \oplus (id \times \pi_1))$$
 ?  $[a_1, [a_2, S]] = q$  ?  $[id ! a_1, \pi_1 ! [a_2, S]]$   
= q ?  $[a_1, a_2]$ .

Rule magic then rewrites the query so that q is used to "filter" elements of A2 so that only those that relate to some element of A1 will be involved in the grouping and aggregate computation performed by **njoin**. This filtering is expressed in the body pattern of magic with the subexpression,

**join** 
$$(q, \pi_2)$$
 ! [A1, A2]

which performs a right semi-join of A1 and A2 with respect to q. The elements of B that are collected from this query are then freed of duplicates via a subsequent invocation of **set**.

Note that the semantics of **njoin** show that duplicate elimination on the result of the semi-join is strictly not necessary (**njoin** ignores duplicates in the first collection argument). The reason that rule **magic** introduces this unnecessary operator is to prepare this expression for simplification by transformation SimplifyJoin whose rewrite rules are listed in Figure 4.3. Rule (8) of Figure 4.3 rewrites this semijoin into an intersection. But semijoins can only be rewritten into intersections when the result of the semijoin is returned as a set. Therefore, the operator **set** is introduced into the semijoin expression as an "indicator" that duplicates in the result can be ignored.

Below we describe the steps performed by this transformation, demonstrating their effects on the KOLA query of Figure 4.15b, and showing how they result in a rewrite of this query to that shown in Figure 4.16d. In practice, translation into KOLA performs view merging, and therefore the query of Figure 4.15b would be presented to the COKO Magic transformation as  $Q_0$ :

 $\begin{array}{l} \textbf{join} \ (P_k \And Q_k \And R_k, \ \pi_1) \ ! \\ [\texttt{Coms, njoin} \ (\textbf{eq} \oplus (\textbf{id} \times \textbf{chair}), \ \texttt{mems, avg} \circ \textbf{flat}) \ ! \\ [\textbf{iterate} \ (\texttt{K}_p \ (\texttt{true}), \ \texttt{chair}) \ ! \ \texttt{Coms, Coms}] \end{array}$ 

such that

 $P_{k} = \mathbf{eq} \oplus \langle \operatorname{chair} \circ \pi_{1}, \pi_{1} \circ \pi_{2} \rangle$   $Q_{k} = \mathbf{gt} \oplus \langle \operatorname{terms} \circ \operatorname{chair} \circ \pi_{1}, \pi_{2} \circ \pi_{2} \rangle, \text{ and }$   $R_{k} = \mathbf{eq} \oplus \langle \operatorname{pty} \circ \operatorname{chair} \circ \pi_{1}, \operatorname{K}_{f} (\text{``Dem''}) \rangle$ 

#### Steps 1 and 2:

The purpose of the first two steps of the transformation is to isolate that part of the join predicate,

$$P_k \& Q_k \& R_k$$

that is of the form

$$(\mathsf{q} \oplus (\mathbf{id} \times \pi_1))$$
 & r

to prepare it for firing by magic.

1. In Step 1, transformation pushdown (Section 4.5.1) is fired. Pushdown fires SNF on the join predicate to convert it to the form,

$$(
ho\oplus\pi_1)$$
 &  $(\sigma\oplus\pi_2)$  &  $au$ .

Then,  $\rho$  and  $\sigma$  are pushed out of the join. Applied to  $Q_0$ , this step leaves  $Q_1$ :

$$\begin{array}{l} \textbf{join} \ (P_k \And Q_k, \ \pi_1) \texttt{!} \\ \\ [\texttt{MComs}_k, \ \textbf{njoin} \ (\textbf{eq} \oplus (\textbf{id} \times \texttt{chair}), \ \texttt{mems}, \ \textbf{avg} \circ \textbf{flat}) \texttt{!} \\ \\ \\ [\textbf{iterate} \ (\texttt{K}_p \ (\texttt{true}), \ \texttt{chair}) \texttt{!} \ \texttt{Coms}, \ \texttt{Coms}] \end{bmatrix} \end{array}$$

such that

$$\operatorname{MComs}_{\mathbf{k}} = \operatorname{iterate} (R'_k, \operatorname{id}) ! \operatorname{Coms}, \operatorname{and} R'_k = \operatorname{eq} \oplus (\langle \operatorname{id}, \operatorname{K}_f (\operatorname{"Dem"}) \rangle \circ \operatorname{pty} \circ \operatorname{chair}).$$

2. The second step normalizes  $\tau$  by an SNF-like normalization. Transformation SNF2 is similar to SNF, but rewrites  $\tau$  into the form,

$$(\alpha \oplus (\mathbf{id} \times \pi_1)) \& (\beta \oplus (\mathbf{id} \times \pi_2)) \& \gamma.$$

After these steps, the predicate is easily put into the desired form by setting  $\mathbf{q} = \alpha$  and  $\mathbf{r} = ((\beta \oplus (\mathbf{id} \times \pi_2)) \& \gamma)$ . This step prepares the predicate for a subsequent firing of rule magic.

SNF2 is identical to SNF (Figure 4.9) but for the following exceptions:

- 1. Rather than firing SimpLits in Step 1, SNF2 fires the transformation SimpLits2 of Figure 4.18.
- 2. Rather than firing rule init in Step 4, SNF2 fires the rule,

 $\mathtt{p} \;\stackrel{\rightarrow}{=}\; (\mathtt{K}_p \;(\mathtt{true}) \;\oplus\; (\mathbf{id} \,\times\, \pi_1)) \; \texttt{\&}\; (\mathtt{K}_p \;(\mathtt{true}) \;\oplus\; (\mathbf{id} \,\times\, \pi_2)) \; \texttt{\&}\; \mathtt{K}_p \;(\mathtt{true}) \; \texttt{\&}\; \mathtt{p}.$ 

3. Rather than firing OrderConjs in Step 6, SNF2 fires the transformation OrderConjs2 which fires the rules,

instead of rules oc1, oc2 and oc3 of Figure 4.10.

SimpLits2 adds transformation Pr2Times and rules sl8 - sl13 to the rules fired by SimpLits. Pr2Times converts functions to products  $(f \times g)$  where possible. Together with the rules of SimpLits, rules sl8 - sl13 ensure that predicates on pairs [a, [b, S]] of the form,

$$p = q \oplus \langle f, g \rangle$$

such that f and g are basic functions, are transformed into one of the forms shown below:

TRANSFORMATION SimpLits2 USES Pr2Times,  $\stackrel{\rightarrow}{=}$  (f  $\circ$  g)  $\circ$  h sft:  $f \circ (g \circ h)$  $\stackrel{\rightarrow}{=}$  K<sub>f</sub> ([x, y]), sl1:  $\langle K_f(\mathbf{x}), K_f(\mathbf{y}) \rangle$  $\stackrel{\rightarrow}{=}$  K<sub>f</sub> (f ! x),  $sl2: f \circ K_f(x)$  $\stackrel{\rightarrow}{=} \langle \mathbf{id}, \mathsf{K}_f (\mathbf{x}) \rangle \circ \mathbf{f},$ sl3:  $\langle f, K_f(x) \rangle$  $\stackrel{\rightarrow}{=} \langle \mathbf{K}_f (\mathbf{x}), \mathbf{id} \rangle \circ \mathbf{f},$  $sl4: \langle K_f(\mathbf{x}), \mathbf{f} \rangle$  $\stackrel{\rightarrow}{\equiv} \langle f, g \rangle \circ h,$  $sl5: \langle f \circ h, g \circ h \rangle$  $\stackrel{\rightarrow}{=}$  **p**  $\oplus$  **f**  $\oplus$  **g**,  $sl6: p \oplus (f \circ g)$  $\stackrel{\rightarrow}{=}$  K<sub>p</sub> (p ? x),  $sl7: p \oplus K_f(x)$  $\stackrel{\rightarrow}{=} \langle \mathbf{f} \circ \pi_1, \mathbf{g} \rangle \circ (\mathbf{id} \times \mathbf{h}),$  $\begin{array}{lll} {\tt sl8}: & \langle {\tt f} \circ \pi_1, \, {\tt g} \circ ({\tt id} \times {\tt h}) \rangle & \qquad \stackrel{\scriptstyle \rightarrow}{=} & \langle {\tt f} \circ \pi_1, \, {\tt g} \rangle \circ ({\tt id} \times {\tt h}), \\ {\tt sl9}: & \langle {\tt f} \circ ({\tt id} \times {\tt h}), \, {\tt g} \circ \pi_1 \rangle & \qquad \stackrel{\scriptstyle \rightarrow}{=} & \langle {\tt f}, \, {\tt g} \circ \pi_1 \rangle \circ ({\tt id} \times {\tt h}), \end{array}$ sl10:  $\langle \mathbf{f} \circ (\mathbf{h} \circ \pi_2), \mathbf{g} \circ (\mathbf{id} \times \mathbf{h}) \rangle \stackrel{\rightarrow}{=} \langle \mathbf{f} \circ \pi_2, \mathbf{g} \rangle \circ (\mathbf{id} \times \mathbf{h}),$ sl11:  $\langle \mathbf{f} \circ (\mathbf{id} \times \mathbf{h}), \mathbf{g} \circ (\mathbf{h} \circ \pi_2) \rangle \stackrel{\rightarrow}{=} \langle \mathbf{f}, \mathbf{g} \circ \pi_2 \rangle \circ (\mathbf{id} \times \mathbf{h}),$  $\stackrel{\rightarrow}{=} \langle \mathbf{f} \circ \mathbf{g}, \mathbf{h} \rangle \, \circ \, \pi_2,$ sl12:  $\langle \mathbf{f} \circ (\mathbf{g} \circ \pi_2), \mathbf{g} \circ \pi_2 \rangle$  $\stackrel{\rightarrow}{=} \langle \mathbf{f}, \mathbf{h} \circ \mathbf{g} \rangle \circ \pi_2,$ sl13:  $\langle \mathbf{f} \circ \pi_2, \mathbf{h} \circ (\mathbf{h} \circ \pi_2) \rangle$ BEGIN BU {Pr2Times || s11 || s12 || {{s13 || s14}  $\rightarrow$  REPEAT sft} || s15 || s16 || s17 || s18 || s19 || s110 || s111 || s112 || s113 || REPEAT sft}

END

```
TRANSFORMATION Pr2Times
```

USES  $\begin{array}{rcl} \mathsf{co1}: & \langle \mathtt{f} \circ \pi_1, \, \mathtt{g} \circ (\mathtt{h} \circ \pi_2) \rangle & & \stackrel{\rightarrow}{=} & (\mathtt{f} \times \mathtt{g}) \circ (\mathtt{id} \times \mathtt{h}), \\ \mathsf{co2}: & \langle \mathtt{f} \circ (\mathtt{h} \circ \pi_2), \, \mathtt{g} \circ \pi_1 \rangle & & \stackrel{\rightarrow}{=} & \langle \pi_2, \, \pi_1 \rangle \circ (\mathtt{f} \times \mathtt{g}) \end{array}$  $\stackrel{\rightarrow}{=} \langle \pi_2, \pi_1 \rangle \circ (\mathbf{f} \times \mathbf{g}) \circ (\mathbf{id} \times \mathbf{h}),$  $\mathbf{co3}: \quad \langle \mathbf{f} \circ (\pi_1 \circ \pi_2), \mathbf{g} \circ (\pi_2 \circ \pi_2) \rangle \stackrel{\rightarrow}{=} (\mathbf{f} \times \mathbf{g}) \circ \pi_2,$ co4:  $\langle \mathbf{f} \circ (\pi_2 \circ \pi_2), \mathbf{g} \circ (\pi_1 \circ \pi_2) \rangle \stackrel{\rightarrow}{=} \langle \pi_2, \pi_1 \rangle \circ (\mathbf{f} \times \mathbf{g}) \circ \pi_2,$  $\stackrel{\rightarrow}{=} (\mathbf{f} \times \mathbf{id}) \circ (\mathbf{id} \times \mathbf{g}),$ co5:  $\langle \mathbf{f} \circ \pi_1, \mathbf{g} \circ \pi_2 \rangle$  $\stackrel{\rightarrow}{=} \langle \pi_2, \pi_1 \rangle \circ (\mathbf{f} \times \mathbf{id}) \circ (\mathbf{id} \times \mathbf{g}),$  $co6: \langle f \circ \pi_2, g \circ \pi_1 \rangle$  $\stackrel{\rightarrow}{=}$  id, co7 :  $\langle \pi_1, \pi_2 \rangle$  $\stackrel{\rightarrow}{\equiv} f,$  $co8: f \circ id$  $\stackrel{\rightarrow}{=} f$  $co9: id \circ f$ BEGIN BU {co1 || co2 || co3 || co4 || co5 || co6 || co7 || co8 || co9} END

Figure 4.18: Transformation SimpLits2 and its Auxiliary Transformation Pr2Times

- $K_p$  (b) (if q ignores its inputs),
- $\overline{p} \oplus \pi_1$  (if q only requires a),
- $\overline{p} \oplus \pi_2$  (if q only requires b and S),
- $\overline{p} \oplus (\mathbf{id} \times \pi_1)$  (if q only requires a and b),
- $\overline{p} \oplus (\mathbf{id} \times \pi_2)$  (if q only requires a and S).

When fired on  $P_k$ , rule co5 transforms the function,

$$\langle \texttt{chair} \circ \pi_1, \, \pi_1 \circ \pi_2 \rangle$$

into

$$(\texttt{chair} \times \texttt{id}) \circ (\texttt{id} \times \pi_1).$$

Then, rule pr1 fires leaving the predicate

$$\mathbf{eq} \oplus (\mathtt{chair} \times \mathbf{id}) \oplus (\mathbf{id} \times \pi_1).$$

When fired on  $Q_k$ , rule co5 transforms the function,

$$\langle \texttt{terms} \circ \texttt{chair} \circ \pi_1, \, \pi_2 \circ \pi_2 \rangle$$

into

 $((\texttt{terms} \circ \texttt{chair}) \times \texttt{id}) \circ (\texttt{id} \times \pi_2).$ 

Then, rule pr1 fires leaving the predicate

$$\mathbf{gt} \oplus ((\mathtt{terms} \circ \mathtt{chair}) \times \mathbf{id}) \oplus (\mathbf{id} \times \pi_2).$$

All subsequent steps in SimpLits2 are as in SimpLits. Therefore, the the result of firing SimpLits2 on  $Q_1$  is the query,  $Q_2$ :

$$\begin{array}{l} \textbf{join} \ ((\alpha \oplus (\textbf{id} \times \pi_1)) \And ((\beta \oplus (\textbf{id} \times \pi_2)) \And \gamma), \ \pi_1) \ ! \\ \\ [\texttt{MComs}_k, \ \textbf{njoin} \ (\textbf{eq} \oplus (\textbf{id} \times \textbf{chair}), \ \texttt{mems}, \ \textbf{avg} \circ \textbf{flat}) \ ! \\ \\ [\textbf{iterate} \ (\texttt{K}_p \ (\texttt{true}), \ \textbf{chair}) \ ! \ \texttt{Coms}, \ \texttt{Coms}] \end{array}$$

such that

$$\begin{aligned} \alpha &= \mathbf{eq} \oplus (\mathtt{chair} \times \mathtt{id}), \text{ and} \\ \beta &= \mathtt{gt} \oplus ((\mathtt{terms} \circ \mathtt{chair}) \times \mathtt{id}), \text{ and} \\ \gamma &= \mathtt{K}_p \ (\mathtt{true}). \end{aligned}$$

After SNF2 is fired, rule sftp is fired to reassociate the three conjunct join subpredicates,

$$((\alpha \oplus (\mathbf{id} \times \pi_1)) \& (\beta \oplus (\mathbf{id} \times \pi_2))) \& \gamma$$

into

$$(\alpha \oplus (\mathbf{id} \times \pi_1)) \& ((\beta \oplus (\mathbf{id} \times \pi_2)) \& \gamma)$$

This firing prepares the predicate for the firing of rule magic in the next step. The result of firing sftp on  $Q_2$  is  $Q_3$ :

$$\begin{array}{l} \textbf{join} \ ((\textbf{q} \oplus (\textbf{id} \times \pi_1)) \And \textbf{r}, \pi_1) \texttt{!} \\ \\ [\texttt{MComs}_k, \ \textbf{njoin} \ (\textbf{eq} \oplus (\textbf{id} \times \texttt{chair}), \texttt{mems}, \textbf{avg} \circ \textbf{flat}) \texttt{!} \\ \\ \\ [\textbf{iterate} \ (\texttt{K}_p \ (\texttt{true}), \ \texttt{chair}) \texttt{!} \ \texttt{Coms}, \ \texttt{Coms}] \end{bmatrix} \end{array}$$

such that

#### Step 3:

Next, rewrite rule magic is fired. This rule introduces the left join argument (A1) into the right-hand side of the join. Firing magic makes it possible to restrict the input (A2) to njoin to elements that are related by q to A1. Fired on  $Q_3$ , magic leaves  $Q_4$ :

 $\begin{array}{l} \textbf{join} \ ((\textbf{q} \oplus (\textbf{id} \times \pi_1)) \ \texttt{\&r}, \ \pi_1) \ ! \\ \\ [\texttt{MComs}_k, \ \textbf{njoin} \ (\textbf{eq} \oplus (\textbf{id} \times \texttt{chair}), \ \texttt{mems}, \ \textbf{avg} \circ \textbf{flat}) \ ! \ [\texttt{CSet}'_k, \ \texttt{Coms}]] \end{array}$ 

or equivalently,

 $\begin{array}{l} \textbf{join} \ (P'_k \And Q'_k, \ \pi_1) \ ! \\ \\ [\texttt{MComs}_k, \ \textbf{njoin} \ (\textbf{eq} \oplus (\textbf{id} \times \texttt{chair}), \ \texttt{mems}, \ \textbf{avg} \circ \textbf{flat}) \ ! \ [\texttt{CSet}'_k, \ \texttt{Coms}] ] \end{array}$ 

such that

$$\texttt{CSet}'_{\texttt{k}} = \texttt{set} ! (\texttt{join} (\texttt{eq} \oplus (\texttt{chair} \times \texttt{id}), \pi_2) !$$
  
[MComs<sub>k</sub>, iterate (K<sub>p</sub> (true), chair) ! Coms]),

 $\vec{\stackrel{\rightarrow}{=}} id$  $\vec{\stackrel{\rightarrow}{=}} p$  $\vec{\stackrel{\rightarrow}{=}} K_p (true)$  $\vec{\stackrel{\rightarrow}{=}} p$  $\vec{\stackrel{\rightarrow}{=}} f$ 1.  $(\mathbf{id} \times \mathbf{id})$ 2.  $p \oplus id$ 3.  $K_p$  (true)  $\oplus$  f 4. p & K<sub>p</sub> (true) 5a. **f** ∘ **id**  $\stackrel{\rightarrow}{=}$ 5b. id • f f  $\vec{\stackrel{-}{\equiv}} (\mathbf{f} \circ \mathbf{h}) \times (\mathbf{g} \circ \mathbf{j})$  $\vec{\stackrel{-}{\equiv}} \mathbf{p} \oplus (\mathbf{f} \circ \mathbf{g})$ 6.  $(f \times g) \circ (h \times j)$  $p \oplus f \oplus g$ 7.  $\stackrel{\rightarrow}{\equiv}$  set ! (A  $\cap$  B) 8. set ! (join (eq,  $\pi_2$ ) ! [A, B]) 9. **join**  $(\mathbf{p} \oplus (\mathbf{f} \times \mathbf{g}), \pi_2)$  ! [A, B] **join**  $(p \oplus (id \times g), \pi_2)$  ! [iterate  $(K_p (true), f)$  ! A, B] 10. iterate (p, f) ! (iterate (q, g) ! A)  $\stackrel{=}{=}$  iterate (q & (p  $\oplus$  g), f  $\circ$  g) ! A 11. (iterate (p, f) ! A)  $\cap$  (iterate (K<sub>p</sub> (true), f) ! A)  $\stackrel{\rightarrow}{=}$  iterate (p, f) ! A  $\mathbf{njoin} \ (p, \ f, \ g) \ ! \ [\mathbf{set} \ ! \ A, \ B]$  $\stackrel{\rightarrow}{=}$  njoin (p, f, g) ! [A, B] 12.iterate (p, f) !  $A \stackrel{\rightarrow}{=}$  iterate (K<sub>p</sub> (true), f) ! (iterate (p, id) ! A) 13.

Table 4.3: Rewrite Rules Used In SimplifyJoin

### Step 4:

Step 4 fires transformation SimplifyJoin on the semijoin expression resulting from the previous step. SimplifyJoin uses the rules of Table 4.3 to rewrite  $CSet'_k$  into  $CSet_k$  (of Figure 4.16d) as we show below:

• The first rule fired is rule 9, which rewrites  $\mathtt{CSet}'_{\mathtt{k}}$ ,

set ! (join (eq  $\oplus$  (chair  $\times$  id),  $\pi_2$ ) ! [MComs<sub>k</sub>, iterate (K<sub>p</sub> (true), chair) ! Coms])

 $\operatorname{to}$ 

```
set !

(join (eq \oplus (id \times id), \pi_2) !

[iterate (K<sub>p</sub> (true), chair) ! MComs<sub>k</sub>, iterate (K<sub>p</sub> (true), chair) ! Coms]).
```

• Firing rules 1 and 2 simplifies the join predicate, leaving

```
set !

(join (eq, \pi_2) !

[iterate (K<sub>p</sub> (true), chair) ! MComs<sub>k</sub>, iterate (K<sub>p</sub> (true), chair) ! Coms]).
```

• Expanding for  $MComs_k$  and firing rules 10, 3, 4 and 5a, leaves

```
set !

(join (eq, \pi_2) !

[iterate (R'_k, chair) ! Coms, iterate (K_p (true), chair) ! Coms]).
```

• Next, rule 8 fires, converting the right semijoin to an intersection. Firing rule 8 leaves:

set ! ((iterate  $(R'_k, \text{chair}) ! \text{Coms}) \cap (iterate (K_p (true), \text{chair}) ! \text{Coms})).$ 

• This expression in turn reduces by firing rule 11 to:

set ! (iterate  $(R'_k, \text{ chair})$  ! Coms),

which then gets split up by firing rule 13 to:

set ! (iterate ( $K_p$  (true), chair) ! (iterate ( $R'_k$ , id) ! Coms)) = set ! (iterate ( $K_p$  (true), chair) ! MComs<sub>k</sub>) = CSet<sub>k</sub>.

Therefore, after SimplifyJoin has finished firing, we are left with the query of Figure 4.16d:

join  $(P'_k \& Q'_k, \pi_1)$  ! [MComs<sub>k</sub>, MTemp<sub>K</sub>]

such that  $MTemp_K$  is:

 $\mathbf{njoin} \ (\mathbf{eq} \oplus (\mathbf{id} \times \mathtt{chair}), \ \mathtt{mems}, \ \mathbf{avg} \circ \mathbf{flat}) \ ! \ [\mathtt{CSet}_{\mathtt{k}}, \ \mathtt{Coms}].$ 

## 4.7 Discussion

#### 4.7.1 The Expressivity of COKO

COKO is still evolving. Our goal is to reach a point with it where we are able to express all of the useful query rewrites that can be expressed with a programming language without compromising the separation of rewrite rules from firing algorithms. To this end, our design process alternates between modifying the language and using it to express complex query rewrites. In this chapter, we have presented some of the rewrites that we have generated with COKO, including CNF (exhaustive and non-exhaustive versions), SNF, Pushdown, Join-Associate and Magic. Though COKO is evolving, it is not immature. We believe that COKO already provides most of the useful idioms required to express query rewriting. By combining COKO statements in varying ways, we are able to express such common firing algorithms as

• BU  $\{\mathbf{r}_1 \parallel \ldots \parallel \mathbf{r}_n\}$ :

fire every rule  $r_1$ , ...,  $r_n$  successively on every subtree,

• BU r<sub>1</sub>; ... BU r<sub>n</sub>:

fire every rule  $r_1$ , ...,  $r_n$  on every succesive subtree,

• BU {{REPEAT  $r_1$ }; ...; {REPEAT  $r_n$ }:

fire every rule  $r_1$ , ...,  $r_n$  repeatedly on every successive subtree,

•  $S \rightarrow S' \parallel S''$ :

execute S and then S' if S succeeds and S'' if S fails, and

•  $S \rightarrow$  recursive fire:

 $execute \ S \ exhaustively.$ 

As before, attempts to express transformations drive the design of the language. Provided that we are able to maintain the separation of rewrite rules from firing algorithms, we are prepared to let COKO evolve into a steady and usable state.

#### 4.7.2 The Need for Normalization

The CNF and SNF query rewrites are normalizations: query rewrites that convert expressions into syntactically characterizable (i.e., normal) forms. Normalizations epitomize the kinds of complex query rewrites that cannot be expressed as rewrite rules and that typically get expressed with code.

Normalization gets little attention in the optimizer literature. And yet, normalization can be more complex, expensive and error-prone than the optimizations they preceed. (Consider that Kim's erroneous rewrites are normalizations whose normal forms are join queries.) In the context of object-oriented and object-relational databases, normalization assumes even greater importance. Firstly, nested object queries are far more prevalent and can be more deeply nested than relational queries making their normalization more difficult and more urgent. Secondly, because many object databases are built as extensions of existing systems (e.g., object-relational extensions of relational systems), normalization affords the opportunity to rewrite complex (e.g., object) queries into a series of simpler (e.g., relational) queries that can be posed of the original query engine. (We will see an example of this object  $\rightarrow$  relation translation in Chapter 6.)

We have shown with two examples (CNF and SNF) that COKO is capable of expressing complex normalizations that typically get expressed only with code. For both normalizations, we were able to show not only *correctness*, but also prove that the firing algorithms for these transformations did as they were intended. Neither of these results is straightforward when the normalizations are expressed with code, even when the normalizations themselves have more straightforward expression with code.<sup>5</sup> Therefore, the correctness results arising from the COKO-KOLA approach come at a complexity cost for expressing certain rewrites. In designing future versions of COKO, our goal will be to make firing algorithms simpler to formulate, in order to lower this cost.

# 4.8 Chapter Summary

In this chapter, we introduced a language (COKO) for defining *transformations*: complex query rewrites for rule-based optimizers. COKO transformations generalize rewrite rules. Like rules, they can be fired and can succeed or fail as a result. But because they are expressed algorithmically, they are able to express many rewrites (such as normalizations) that rewrite rules cannot.

A COKO transformation consists of a set of rewrite rules and a firing algorithm specifying how they are fired. The separation of rewriting (expressed with rewrite rules) and firing control (expressed with firing algorithms) makes it possible to express complex and efficient rewrites that can still (because rewrite rules are over KOLA queries) be verified with a theorem prover.

COKO transformations can be made efficient and expressive. The language for firing algorithms includes the kinds of operators that are most useful for describing rewrites. These include explicit rule firing, traversal control, selective firing and conditional firing. We demonstrated the efficiency benefits of firing algorithms with an example COKO transformation that converts predicates to CNF. We demonstrated the expressivity of COKO with numerous examples that typically do not get expressed with declarative rewrite rules. These examples included a complex normalization (SNF) and three complex rewrites that

<sup>&</sup>lt;sup>5</sup>SNF for example, is straightforward to express with code that 1) converts a binary predicate to CNF, and 2) traces the origins of all attributes appearing in each conjunct to see which conjuncts involve attributes only from the first input, second input or both.

depend on it (predicate-pushdown, join-reordering and Magic-Sets rewrites).

COKO extends and generalizes KOLA. Whereas KOLA used a modular approach to build queries from functions, COKO uses a modular approach to build complex query rewrites from rewrite rules. This modular approach facilitates the verification of query rewriters.

# Chapter 5

# Semantic Query Rewrites

Rewrite rules are inherently simple and as such, are not expressive enough to specify many query rewrites. In the previous chapter, we considered how to express complex query rewrites that are too *general* to express with rewrite rules. The CNF rewrite for example, cannot be expressed as a rewrite rule because no pair of patterns is both general enough to match all Boolean expressions and specific enough to express their CNF equivalents. To address this issue, we introduced the language COKO. COKO transformations express complex query rewrites using sets of KOLA rewrite rules accompanied by firing algorithms.

In this chapter, we consider the complementary issue of expressing query rewrites that are too *specific* for rewrite rules. To illustrate, consider a query rewrite that transforms a query that performs duplicate elimination into one that does not. The correctness of this rewrite depends on duplicate elimination being redundant, as it is when performed on the result of a subquery that projects on a key. A rewrite rule expressing this rewrite for SQL queries is shown below.

SELECT DISTINCT $x.f$		SELECT $x.f$
FROM $x$ IN $A$	$\stackrel{\rightarrow}{=}$	FROM $x$ IN $A$
WHERE $p$		WHERE $p$

This rule must be qualified by additional restrictions that ensure that attributes matching f are keys and collections matching A are sets. Any query that matches the head pattern of this rule but does not satisfy these additional conditions could have its semantics (specifically, its element counts) changed as a result of rewriting. Semantic conditions such as those identifying f as a key and A as a set cannot be expressed with patterns. Therefore, query rewrites whose correctness depends on semantic conditions such as these cannot be expressed solely with rewrite rules.
As with complex query rewrites, existing rule-based systems address this expressivity issue by replacing or supplementing rewrite rules with code. Whereas complex query rewrites use code to manipulate matched expressions in ways that cannot be expressed with patterns, semantic query rewrites use code to test semantic conditions of expressions that successfully unify. For example, the SQL transformation above that eliminates duplicate removal would be expressed in Starburst [79] with C code that examined annotations of the underlying query representation (QGM) to decide if a matched attribute was a key and if a matched collection was a set.

This chapter proposes an alternative approach for expressing semantic query rewrites that is consistent with our goal of making query rewriters verifiable with a theorem prover. As with COKO, this work builds upon the KOLA work introduced in Chapter 3. We add two new kinds of rules to the COKO-KOLA framework:

- Conditional rewrite rules, and
- Inference rules.

Conditional rewrite rules resemble (unconditional) rewrite rules, except that when they are fired, the match of the rule's head pattern to a query expression is followed by analysis to see if certain conditions hold of identified subexpressions. Inference rules tell the optimizer how to decide if these conditions hold.

The contributions of the work presented in this chapter are:

- 1. Verifiable Semantic Query Rewrites: In keeping with our goal outlined in Chapter 1, all query rewrites specifiable with inference and conditional rewrite rules are verifiable with a theorem prover.
- 2. Use of Inference Rules to Infer Query Semantics: This work is unique in its use of inference rules to specify semantic conditions. This technique separates the rules that depend on semantic conditions (conditional rewrite rules) from the decision-making process that decides if these semantic conditions hold. Our approach is distinct from that of existing rule-based systems that embed decision-making code within the rule that may or may not fire as a result.

The use of inference rules to specify semantic conditions makes optimizers extensible in ways that standard rule-based optimizers are not. By modifying a set of rewrite rules used by an optimizer, one can change *how* a query gets rewritten. On the other hand, by modifying a set of inference rules used by an optimizer, one can change *when* rewrite rules predicated on inferred conditions get fired.

The rest of this chapter proceeds as follows. In Section 5.1, we motivate this work by presenting queries over the Thomas database, and showing how the semantics of their data functions (in this case, their injectivity) can be inferred and exploited for rewriting. In this section, we also show how the conditional rewrite rules and inference rules that specify these semantic rewrites would be expressed within COKO-KOLA. Section 5.2 presents a second example of a semantic condition (*predicate strength*) that can be used as a condition for many useful semantic rewrites. Section 5.3 describes how our COKO compiler was modified to account for inference and conditional rewrite rules. Section 5.4 discusses issues that arose in the design and implementation of this compiler extension, and a chapter summary follows in Section 5.5.

The semantic query rewrites presented in this chapter are not new. The injectivity-based rewrites of Section 5.1 have been discussed in numerous texts (e.g., Ullman's introductory text on databases [95]). The predicate strength rewrites of Section 5.2 are similar to the predicate "move-around" rewrites introduced by Levy, et al. [71]. Our work is unique in its declarative expression of these rewrites that makes them verifiable with a theorem prover. Further, the use of inference rules to define these conditions makes rule-based query rewriters extensible in ways that have not been proposed before.

## 5.1 Example 1: Injectivity

Figures 5.1a and 5.1b show two simple OQL queries over the Thomas database. The "Major Cities" query (Figure 5.1a) queries a set of House Representatives (HReps) applying the *path* expression, x.reps.lgst\_cit, to each. The result of this query is the collection of cities that are the largest of those located in the districts represented by House Representatives in HReps, with duplicate cities removed.<sup>1</sup> The "Mayors" query (Figure 5.1b) also queries a set of House Representatives. For each Representative, this query returns the mayors of major cities located in the district that the Representative represents (this time, with duplicate mayor collections removed from the result).

The "Major Cities" query and the "Mayors" query can be evaluated in similar ways: by first retrieving House Representatives in HReps, applying a data function to each to generate

<sup>&</sup>lt;sup>1</sup>As we mentioned in Chapter 2, we make the simplifying assumption that cities are located in only one Congressional district. While this may not be the case in practice, we can enforce this assumption by assigning every city to that district where a majority of its inhabitants reside.

```
SELECT DISTINCT x.reps.lgst\_citSELECT DISTINCT (SELECT d.mayor<br/>FROM d IN x.reps.cities)(a)(b)(a)(b)(b)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)(c)</
```

Figure 5.1: The "Major Cities" (a) and "Mayors" (b) Queries Before and After Rewriting

an intermediate collection, and then eliminating duplicates. For the "Major Cities" query, duplicates are cities with the same OID. For the "Mayors" query, duplicates are collections with the same members.

Duplicate elimination is expensive, requiring an initial sort or hash of the contents of a collection. But for both the "Major Cities" query and the "Mayors" query, duplicate elimination is unnecessary. Because of the *semantics* of their data functions, both queries generate intermediate collections that already are free of duplicates. No Congressional district is represented by more than one House Representative, and no city is found in more than one district.<sup>2</sup> Therefore, the "Major Cities" query inserts a distinct city into its intermediate result for each distinct House Representative. As HReps has no duplicates, neither will this collection of cities. Similarly, every district has a unique collection of major cities and every city has a unique mayor. Therefore, the collections of mayors generated as an intermediate result of the "Mayors" query will not require duplicate elimination.

Rewritten versions of these queries that do not perform duplicate elimination are shown below the original queries. The query rewrite resulting in these queries is similar to the relational query rewrite presented at the onset of this chapter. However, this rewrite is more general in that it can be applied to queries that cannot be expressed as relational queries (such as object queries with path expressions or subqueries as data functions). For the object version of this rewrite to be correct, a query's data function need not be a key attribute but any *injective* function (of which keys comprise a special case). And whereas

<sup>&</sup>lt;sup>2</sup>Again, according to our simplifying assumption.

```
set ! (iterate (K<sub>p</sub> (true), f) ! HReps)

s.t.: f = lgst\_cit \circ reps

\downarrow

iterate (K<sub>p</sub> (true), f) ! HReps

s.t.: f = lgst\_cit \circ reps
```

KOLA Equivalents of the "Major Cities" Query (Before and After Rewriting)

set ! (iterate (K<sub>p</sub> (true), f) ! HReps) s.t.: f =iterate (K<sub>p</sub> (true), mayor)  $\circ$  cities  $\circ$  reps  $\downarrow$ iterate (K<sub>p</sub> (true), f) ! HReps

s.t.:  $f = iterate (K_p (true), mayor) \circ cities \circ reps$ 

KOLA Equivalents of the "Mayors" Query (Before and After Rewriting)

Figure 5.2: KOLA Translations of Figures 5.1a and 5.1b

a relational query rewriter need only consult metadata files (e.g., the database schema) to determine whether a query's data function is a key, this approach is inadequate for deciding the injectivity of functions that might appear in object queries. The number of injective path expressions alone might be very large and even infinite. (Aside from *x*.reps.lgst\_cit, other injective path expressions on House Representatives are *x*.name, *x*.reps, *x*.reps.cities, *x*.reps.lgst\_cit.mayor and so on.) Thus, it is unlikely that metadata files can be scaled to keep track of all injective data functions, and inference is required instead.

Figure 5.2 shows KOLA equivalents of the "Major Cities" query and "Mayors" query both before and after the application of a semantic query rewrite to remove duplicate elimination (set). The KOLA translations of the data functions (f) for these two queries are:

• lgst\_cit o reps, equivalent to the "Major Cities" query path expression,

x.reps.lgst\_cit,

and

• iterate (K<sub>p</sub> (true), mayor)  $\circ$  cities  $\circ$  reps, equivalent to the "Mayors" query subquery,

> SELECT d.mayor FROM d IN x.reps.cities.

#### 5.1.1 Expressing Semantic Query Rewrites in COKO-KOLA

To express semantic rewrites in COKO, we introduce two new kinds of *declarative* rules to the language:

- Conditional Rewrite Rules resemble (unconditional) rewrite rules, but can include semantic conditions on the subexpressions of matched query expressions. These conditions can, for example, indicate that a given KOLA function must be injective or that a given KOLA collection must be a set. Like unconditional rules, conditional rewrite rules can be fired within COKO transformations.
- Inference Rules specify how semantic conditions can be inferred of KOLA functions, predicates, objects and collections. A *property* is a set of rules that can be used to infer the same condition. We have modified our COKO compiler to compile properties into code that gets executed during rule firing.

#### **Conditional Rewrite Rules in COKO**

Conditional rewrite rules have the form,

$$C :: L \stackrel{\rightarrow}{=} R$$

such that L and R are patterns of KOLA expressions (i.e., such that  $L \stackrel{=}{=} R$  is an unconditional rewrite rule), and C is a set of semantic conditions that must hold of various subexpressions of query expressions that unify with L. Figure 5.3 shows two example conditional rewrite rules that eliminate redundant duplicate elimination. Inj1 can be fired on either the "Major Cities" query or the "Mayors" query. (Inj2 will be discussed in Section 5.1.3.) The head pattern of this rule matches queries that remove duplicates (with set) from the results of iterate queries. The rule's body pattern shows the same query as the rule's head pattern, but with the invocation of set removed. The conditions of the rule state that the rule is correct provided that function f is injective and collection A is a set. Therefore, conditional rewrite rules specify query rewrites that should only be fired if certain conditions hold.

```
inj1: is_inj(f), is_set(A) ::
set ! (iterate (p, f) ! A) \stackrel{\rightarrow}{=} iterate (p, f) ! A
inj2: is_inj(f), is_set(g ! _) ::
set \circ iterate (p, f) \circ g \stackrel{\rightarrow}{=} iterate (p, f) \circ g
```

Figure 5.3: Conditional Rewrite Rules to Eliminate Redundant Duplicate Elimination

#### Inference Rules (Properties) in COKO

To perform a query rewrite that removes redundant duplicate elimination, a rewriter must determine that a query's data function is injective and that a collection is a set. Like most semantic properties of functions, injectivity is undecidable in general. Determination of whether or not a given collection is a set could be made at runtime, but this requires processing (sorting the collection and scanning for duplicates) that the conditional rewrite rules of Figure 5.3 are intended to avoid. Therefore, it is not realistic to assume that a complete reasoning system for user-defined properties is possible or even desirable. But with guidance, a rewriter can infer that properties such as injectivity hold in some cases. Incomplete inference is preferable to not performing inference at all for at least in these cases, rewriting might improve the evaluation of the query. Therefore, we care about soundness and not about completeness in inferring semantic properties.

Guidance comes from two sources:

- *metadata* provided by the user that declares object types, integrity (including key) constraints, etc., and
- *inference rules* defined by the optimizer developer.

For example, a user might state that a particular attribute of a type is a key.<sup>3</sup> As well, a user might identify the *types* of objects that are globally named, thus identifying some named collections as sets and others as bags. The depth and accuracy of the information supplied by the user determines the quality and correctness of rewriting.

<sup>&</sup>lt;sup>3</sup>In the relational world, a key is typically thought of as a property of a collection (i.e., a relation) rather than a property of a type. However, relations are often used to represent the extent of a type and in this case the association of key with type is natural. Further, equality definitions for types must be defined in terms of keys for sets of objects of that type to be well-behaved. (See our DBPL '95 paper [23] for the argument as to why this is so.) Therefore, keys can be thought of as properties of types and not just collections.

The inference rules supplied to the optimizer enable inference of conditions that are not explicitly stated. For example, a user might identify  $lgst_cit$  and reps as being key attributes for sets of Congressional districts and House Representatives respectively, but is unlikely to identify longer path expressions (such as  $x.reps.lgst_cit$ ) as keys given that there can be too many path expressions to anticipate and consider. But an inference rule can be used to infer that a path expression is injective given that each of the attributes in its path is a key. Or, it can be used to infer that a tuple construction is injective if any of its fields is derived from a key.

A rewriter constructed using the COKO compiler could infer that some functions are injective according to the *inference rules* defined in the *property* definitions of Figure 5.4a. Inference rules have the form,

$$body \implies head$$

(or just *head* which states a *fact* that is unconditionally true). The *head* of an inference rule names a condition (e.g.,  $is_ij(f)$ ) to infer. A condition is an uninterpreted logical relation whose arguments can be either KOLA expressions or pattern variables (such as f) that implicitly are universally quantified. The *body* of an inference rule is a logical sentence (i.e., consisting of conjunctions ( $\land$ ), disjunctions ( $\lor$ ) and negations ( $\neg$ ) of terms), whose terms are conditions that must be satisfied to infer the head condition. To illustrate, the rules of Figure 5.4a should be interpreted as follows:

- 1. the identity (id) function is injective,
- 2. a KOLA function is injective if it is a key (is\_key is a built-in property generated from metadata specific to a database schema),
- 3. KOLA function  $f \circ g$  is injective if both f and g are injective,
- 4. KOLA function  $\langle f, g \rangle$  is injective if either f or g is injective, and
- 5. KOLA query function iterate  $(K_p (true), f)$  is injective if f is injective.

Figure 5.4b shows a COKO property definition to help decide if collections are sets. The rules contained in this property state that:

- the result of invoking the function, set, on any collection is a set (as with COKO's GIVEN statement, a "don't care" expression (\_) in a pattern denotes a variable whose binding is irrelevant),
- 2. a collection A is a set if its declared type is a set,

PROPERTY Injective BEGIN is\_inj (id). (1) is\_key (f)  $\implies$  is\_inj (f) (2) is\_inj (f)  $\land$  is\_inj (g)  $\implies$  is\_inj (f  $\circ$  g) (3) is\_inj (f)  $\lor$  is\_inj (g)  $\implies$  is\_inj ( $\langle$ f, g $\rangle$ ). (4) is\_inj (f)  $\implies$  is\_inj (iterate (K<sub>p</sub> (true), f)) (5) END (a)

```
PROPERTY Is_Set
BEGIN
is_set (set ! __).
                                                            (1)
is\_type(A, set(\_)) \implies is\_set(A).
                                                            (2)
is\_type (m, \_, set(\_)) \implies is\_set (m ! \_).
                                                           (3)
is_set (A) \land is_set (B) \Longrightarrow is_set (A \times B).
                                                           (4)
is_set (A) \lor is_set (B) \Longrightarrow is_set (A \cap B).
                                                           (5)
is\_set(A) \Longrightarrow is\_set(A - B).
                                                            (6)
END
                              (b)
```

Figure 5.4: Properties Defining Inference Rules for Injective Functions (a) and Sets (b)

- 3. a method m whose range type is a set returns a set when invoked,
- 4. the Cartesian product of two sets is a set,
- 5. the intersection of any two collections, of which one is a set, is a set, and
- 6. taking the difference of any collection from a set returns a set.

Provided that a query rewriter can discern from metadata that reps and lgst\_cit are keys and that HReps is a set of House Representatives, Rules 2, 3 and 5 of Figure 5.4a, and Rule 2 of Figure 5.4b are sufficient to decide that the "Major Cities" query and "Mayors" query can be safely rewritten.

#### 5.1.2 Correctness

Semantic query rewrites expressed in COKO can be verified with LP. Correctness proofs require that all conditions that appear in a conditional rewrite rule be given a formal **iterate**  $(C_p \text{ (eq, "NSF")} \oplus \text{topic, } f)$  ! HouseRes s.t.  $f = \langle \text{name, set} \circ \text{iterate} (K_p \text{ (true), lgst_cit} \circ \text{reps}) \circ \text{spons} \rangle$ 

Figure 5.5:  $NSF_{1k}$ : The "NSF" Query of Figure 2.4 expressed in KOLA

specification. For example, is\_inj would be defined in Larch with the axiom:

Condition is\_set is defined by the axiom:

$$\forall$$
 A: bag [T] (is\_set (A) ==  $\forall$  x:T  $\neg$ (x  $\in$  (A - x))).

Once formally specified, the inference rules that infer these conditions and the conditional rewrite rules that use them are straightforward to verify. A conditional rewrite rule,

$$C :: L \stackrel{\rightarrow}{=} R$$

is correct if C implies that L = R:

$$C \Rightarrow (L == R).$$

An inference rule,  $B \Longrightarrow H$  is correct if the conditions in the body of the rule (B) imply the condition in the head of the rule (i.e., if  $B \Rightarrow H$ ). The inference rules and conditional rewrite rules presented in this section were verified with the LP theorem prover scripts of Appendix B.5.

#### 5.1.3 Revisiting the "NSF" Query of Chapter 2

Figure 5.5 shows the KOLA equivalent of the "NSF" query of Figure 2.4. It might be remembered that this query associates the name of every House resolution concerning the NSF with the set of universities that are largest in the regions represented by one of the resolution's sponsors.

As with the "Major Cities" and "Mayors" queries, the duplicate elimination performed in the data function of this query is unnecessary. That is, the subfunction,

set  $\circ$  iterate (K<sub>p</sub> (true), lgst\_cit  $\circ$  reps)  $\circ$  spons

can be rewritten to

iterate (K<sub>p</sub> (true), lgst\_cit  $\circ$  reps)  $\circ$  spons.

This rewrite requires the inference rules of Figure 5.4 along with the conditional rewrite rule, inj2 of Figure 5.3. In particular, because **reps** is a key for any set of House Representatives, and **lgst\_cit** is a key for any set of Congressional districts, by inference rule (3) of Figure 5.4a,

#### lgst\_cit o reps

is an injective function. Also, the schema of Table 2.1 indicates that when applied to a House resolution, **spons** returns a set of House Representatives. Therefore, the conditions guarding **inj2** are satisfied by this query.

Rule inj2 resembles inj1, but is defined on compositions rather than invocations of functions. That is, inj2 rewrites a composition of functions,  $(set \circ f)$  to f unlike inj1, which rewrites an invocation of functions (set ! (f ! x)) to (f ! x). The need for two rules reflects the fact that query expressions can denote collections or data functions (in the case of nested queries). Inj1 gets fired on query expressions denoting collections, as in the "Major Cities" and "Mayors" queries. Inj2 gets fired on query expressions denoting functions, as in the "NSF" query.<sup>4</sup>

#### 5.1.4 More Uses for Injectivity

Another conditional rewrite rule conditioned on the injectivity of a function is shown below:

is\_inj (f) :: iterate (p, f) ! (A  $\cap$  B)  $\stackrel{\rightarrow}{=}$  (iterate (p, f) ! A)  $\cap$  (iterate (p, f) ! B).

Intersection is typically implemented with joins. Thus, this rule effectively pushes selections (p) and projections (f) past joins. Function f must be injective for the rewrite to be correct, for if it is not, then the query that results from firing this rule might return more answers than the original query. (For example, if f is the noninjective squaring function, A contains 3 but not -3, and B contains -3 but not 3, then the query resulting from firing this rule may include 9 in its result whereas the original query will not.)

If  $HReps_2$  is another collection of House Representatives, then this rule could be used with the inference rules described earlier to rewrite a query that returns the largest cities of all districts represented by House Representatives in both  $HReps_2$  and  $HReps_2$  who have served at least 5 terms,

iterate (C<sub>p</sub> (lt, 5)  $\oplus$  terms, lgst\_cit  $\circ$  reps) ! (HReps  $\cap$  HReps<sub>2</sub>)

<sup>&</sup>lt;sup>4</sup>If translation into KOLA translates **all** expressions into functions, then only rule **inj2** is necessary. In fact, our OQL  $\rightarrow$  KOLA translator translates all KOLA expressions into functions or predicates as we show in Chapter 6.

into the equivalent query,

(iterate (C<sub>p</sub> (lt, 5)  $\oplus$  terms, lgst\_cit  $\circ$  reps) ! HReps)  $\cap$ (iterate (C<sub>p</sub> (lt, 5)  $\oplus$  terms, lgst\_cit  $\circ$  reps) ! HReps<sub>2</sub>).

The initial query first takes a potentially expensive intersection of collections of House Representatives before filtering the result for those who have served more than 5 terms. The transformed version of this query filters the collections of House Representatives for their senior members before performing the intersection of the presumably smaller collections that result.

# 5.2 Example 2: Predicate Strength

In this section, we show another example of a condition (this time concerning predicates rather than functions) whose inference enables a number of useful query rewrites. *Predicate strength* is unlike injectivity in that it holds of two predicates rather than of individual functions. A predicate p is "stronger" than a predicate q (is\_stronger (p, q)) if p always implies q. Predicate strength is specified in Larch with the following axiom:

$$\forall p,q: pred [T]$$
  
is\_stronger  $(p, q) = (\forall x:T (p ? x \Rightarrow q ? x)).$ 

As with the injectivity examples, the query rewrites presented in this section are not new — many are implemented in commercial database systems and some were proposed in the context of relations by Levy, et al. in [71]. What is new is their expression with declarative rules that simplifies their verification and extension.

#### 5.2.1 Some Rewrite Rules Conditioned on Predicate Strength

Predicate strength is used as a condition for two kinds of rewrite rules:

- If p is stronger than q and a query requires that both p and q be invoked on some object, x, then the query can be rewritten to one that only invokes p. This rewrite is advantageous in certain circumstances because it saves the cost of invoking q.
- If p is stronger than q and a query requires that p be invoked on some object, x, then the query can be rewritten to one that invokes both p and q. This rewrite is advantageous in cases where q is much cheaper to invoke than p, and therefore invoking q before invoking p limits the objects on which p must be invoked.

Figure 5.6: Rewrite Rules Conditioned on Predicate Strength

```
PROPERTY is_stronger
USES is_inj
BEGIN
is_stronger (p, p).
                                                                                                         (1)
is_stronger ((eq \oplus (f \times g)) & (p \oplus f \oplus \pi_1), p \oplus g \oplus \pi_2).
                                                                                                         (2)
is_stronger ((eq \oplus (f \times g)) & (p \oplus g \oplus \pi_2), p \oplus f \oplus \pi_1).
                                                                                                         (3)
is_stronger (eq \oplus (f \times f), eq \oplus ((g \circ f) \times (g \circ f))).
                                                                                                         (4)
is_stronger (p, q) \land is_stronger (p', q') \implies is_stronger (p \& p', q \& q').
                                                                                                         (5)
is_stronger (p, r) \lor is_stronger (q, r) \implies is_stronger (p \& q, r).
                                                                                                         (6)
\texttt{is_inj}(f) \implies \texttt{is\_stronger}(eq \oplus (f \times f), eq \oplus (g \times g)).
                                                                                                         (7)
END
```

Figure 5.7: A COKO Property for Predicate Strength

Figure 5.6 shows rewrite rules conditioned on predicate strength. Rule str1 says that if p is stronger than q, then the conjunction of p and q can be rewritten to p. Rule str2 is the *inverse* of rule (1). Rules str3, str4 and str5 state that quantification with a weaker predicate over the result of filtering a collection with a stronger predicate can be simplified to avoid traversing the collection at all (Rules str3 and str5) or to quantify over an unfiltered collection (Rule str4).

#### 5.2.2 A COKO Property for Predicate Strength

Figure 5.7 shows a COKO property with inference rules for inferring predicate strength. Rule (1) states that any predicate is stronger than itself. Rule (2) states that if

and predicate p is known to be true of (f ! x), then p must also be true of (g ! y). Rule (3) similarly infers that p is true of (f ! x) if p is true of (g ! y) and (f ! x == g ! y). Rule (4) states that equality of partial path expressions implies equality on full path expressions. That is:

$$\begin{array}{rcl} x.a_1.\ldots.a_i &=& y.a_1.\ldots.a_i \implies & \\ & x.a_1.\ldots.a_i\ldots.a_n &=& y.a_1.\ldots.a_i\ldots.a_n \end{array}$$

Rules (5) and (6) show how predicate strength can be inferred of predicate conjuncts. Rule (7) uses the injectivity property described earlier to say that equality of keys implies equality of all other attributes.

#### 5.2.3 Example Uses of Predicate Strength

Below we show some example OQL queries whose KOLA equivalents can be rewritten using the conditional rewrite rules of Figure 5.6 and the the inference rules of Figure 5.7.

**Example 1:** The OQL predicate expression below applies a universally quantified predicate to the result of a subquery. The subquery performs a join of Senator collections, Sens and Sens<sub>2</sub> returning a collection of Senator pairs representing the same state. FOR ALL returns true if the largest cities of the states represented by each pair of Senators is the same.

FOR ALL 
$$y$$
 IN  $\begin{pmatrix} \text{SELECT STRUCT (one : } s1, \text{ two : } s2) \\ \text{FROM } s1 \text{ IN Sens, } s2 \text{ IN Sens}_2 \\ \text{WHERE } s1.\text{reps == } s2.\text{reps} \end{pmatrix}$ :

```
y.one.reps.lgst_cit == y.two.reps.lgst_cit.
```

Because all pairs of Senators resulting from the subquery represent the same state, the largest cities of the states represented by the pairs of Senators will also be the same. Therefore, this complex expression can be transformed into the constant, true.

Expressed over KOLA, this query rewrite transforms the predicate invocation,

$$\begin{array}{l} \mathbf{fa} \ (\mathbf{eq} \oplus ((\texttt{lgst\_cit} \circ \texttt{reps}) \times (\texttt{lgst\_cit} \circ \texttt{reps}))) \ ?\\ (\mathbf{join} \ (\mathbf{eq} \oplus (\texttt{reps} \times \texttt{reps}), \ \mathbf{id}) \ ! \ [\texttt{Sens}, \texttt{Sens}_2]) \end{array}$$

to the constant true. This rewrite is captured by the conditional rewrite rule, str5 of Figure 5.6 and uses inference rule (3) of Figure 5.7.

**Example 2:** Whereas the previous example used predicate strength to avoid invoking predicates unnecessarily, the following examples *add* predicates to queries to make them more efficient to evaluate. These examples evoke the spirit of "predicate move-around" rewrites [71].

The OQL query below joins House Representatives from collections HReps and HReps<sub>2</sub> who have served the same number of terms such that the House Representative from HReps has served more than 5 terms. As this query stands, it likely would be evaluated by first filtering House Representatives in HReps to include only those who have served more than 5 terms, and then joining this result with HReps<sub>2</sub>.

SELECT \* FROM h1 IN HReps, h2 IN HReps<sub>2</sub> WHERE (h1.terms > 5) AND (h1.terms == h2.terms)

A better form of this query introduces a new predicate (h2.terms > 5) on House Representatives in HReps<sub>2</sub>:

```
SELECT *
FROM h1 IN HReps, h2 IN HReps<sub>2</sub>
WHERE (h1.terms > 5) AND (h1.terms == h2.terms) AND (h2.terms > 5)
```

The addition of this predicate does not change the semantics of the query, as any House Representatives from  $HReps_2$  that appear in the original query result will have served more than 5 terms because they will have served the same number of terms as some House Representative in HReps who has served more than 5 terms. Put another way, this query rewrite is correct because the predicate,

```
(h1.terms > 5) AND (h1.terms == h2.terms)
```

is stronger than the predicate, h2.terms > 5. This rewrite is advantageous as it makes it likely that *both* HReps and HReps<sub>2</sub> will be filtered for their senior House Representatives, before being submitted as inputs to the join.

The KOLA equivalents of these two queries are shown below. The first query would be expressed in KOLA as,

join  $(\rho, id)$  ! [HReps, HReps\_k]

such that  $\rho$  is:

 $(\mathbf{eq} \oplus (\mathtt{terms} \times \mathtt{terms})) \& (C_p (\mathbf{lt}, 5) \oplus \mathtt{terms} \oplus \pi_1).$ 

The second query is

$$\mathbf{join}~(
ho$$
 &  $au,~\mathbf{id})$  ! [HReps, HReps $_2$ ]

such that  $\tau$  is:

$$C_p$$
 (lt, 5)  $\oplus$  terms  $\oplus$   $\pi_2$ .

The transformation of  $\rho$  to  $\rho \& \tau$  is justified by rewrite rule str2 of Figure 5.6 with p set to  $\rho$  and q set to  $\tau$ . That p is stronger than q is justified by inference rule (2) of Figure 5.7 (setting p to  $C_p$  (lt, 5) and f and g to terms).

**Example 3:** Predicate strength rules can be used to generate *new* predicates and not just to duplicate existing ones as the following example shows. The query below pairs House Representatives in HReps who represent Congressional districts whose largest cities have more than 100 000 people, with mayors in Mays who are the mayors of those cities:

SELECT \* FROM h IN HReps, m IN Mays WHERE (h.reps.lgst\_cit.popn > 100K) AND (h.reps.lgst\_cit == m.city)

The KOLA equivalent to this query is, join  $((\rho \oplus \gamma \oplus \pi_1) \& \tau, id)$  ! [HReps, Mays] such that

$$\rho = C_p (lt, 100K) \oplus popn,$$
  

$$\gamma = lgst\_cit \circ reps, and$$
  

$$\tau = eq \oplus (\gamma \times city).$$

Rule (2) of Figure 5.7 can be used to generate a **new** predicate that can filter the mayors that participate in the join. Specifically, by setting f to  $\gamma$ , g to city and p to  $\rho$ , the new predicate,

 $extsf{C}_p \; ( extsf{lt}, \; extsf{100K}) \, \oplus \; extsf{popn} \, \oplus \; extsf{city} \, \oplus \, \pi_2$ 

can be determined to be weaker than

$$(
ho \oplus \gamma \oplus \pi_1)$$
 &  $au$ 

Thus, applying rewrite rule (2) of Figure 5.6 leaves a query that would be expressed in OQL as:

```
SELECT *
FROM h IN HReps, m IN Mays
WHERE (h.reps.lgst_cit.popn > 100K) AND
    (h.reps.lgst_cit == m.city) AND
    (m.city.popn > 100K)
```



Figure 5.8: A Conditional Rewrite Rule Firer

such that m.city.popn > 100K is a *new* predicate and not just a copy of a predicate that appeared elsewhere in the original query. If the number of mayors who serve cities with populations over 100 000 is small, or if mayors are indexed on the populations of their cities, then this rewrite is likely to make the query more efficient to evaluate.

## 5.3 Implementation

In this section, we show how both conditional rewrite rules and properties (inference rules) are processed in our implementation.

#### 5.3.1 Implementation Overview

A key component of a rule-based query rewriter is a *rule firer*, which accepts representations of a query and a rule as inputs and produces a new query representation (resulting from firing the rule) as a result. We implemented the ideas presented in this chapter by extending the operation of the traditional pattern-matching-based rule firer. The modified rule firer, illustrated in Figure 5.8, extends the traditional rule firer in two ways:

- Inference: The modified rule firer can consult an *inference engine* to infer conditions relevant to the firing of conditional rewrite rules. The rule firer can issue *inference queries* such as:
  - *is the function*, lgst\_cit o reps *injective*?, or
  - can any predicate be generated that is weaker than:

 $(C_p (lt, 5) \oplus terms \oplus \pi_1) \& (eq \oplus (terms \times terms))?$ 

The inference engine answers queries with a simple yes or no (as in the first inference query above) or with KOLA expressions that satisfy the inference query (as in the second inference query above).

• *Conditional Rule Firing:* The modified rule firer accepts conditional rewrite rules (as well as unconditional rules) as inputs. When such rules are fired, inference queries are posed to the inference engine and the answers interpreted.

Section 5.3.2 presents the inference engine component of our optimizer. Section 5.3.3 describes the operation of our rule firer in the presence of conditional functions.

#### 5.3.2 Performing Inference

Our inference engine is the Sicstus Prolog interpreter [83]. Using a Prolog interpreter as an inference engine makes our implementation a prototype rather than one of commercial quality. We envision replacing the Prolog interpreter with specialized matching routines that operate directly on KOLA queries as future work.

The interpreter's inputs are Prolog programs that are:

- built-in facts and rules describing aspects of the data model that are invariant (e.g., rules for inferring subtyping, type information for KOLA operators, etc.),
- facts and rules generated from inference rules, and
- facts generated from metadata information specific to a given database instance, such as types contained in the schema, signatures of attributes, types of persistent data, and attributes that are keys.

Presently, metadata based rules are generated manually. However, Prolog facts and rules are generated automatically by compiling COKO properties.

COKO inference rules are either of the form " $B \Longrightarrow H$ " or simply "H", such that H names a condition to infer and B is a logical sentence of conditions. Compilation of the latter generates the Prolog fact, " $\overline{H}$ " (described below). Compilation of the former generates the Prolog rule, " $\overline{H} := \overline{B}$ ." such that  $\overline{B}$  is the Prolog translation of the logic sentence, B.

Conditions generally have the form,

ident 
$$(k_1,\ldots,k_n)$$

such that each  $k_i$  is a KOLA pattern. These terms are translated into Prolog terms,

$$ident(\overline{k_1},\ldots,\overline{k_n})$$

such that the translation,  $\overline{k_i}$  of KOLA pattern  $k_i$ :

- prepends KOLA's pattern variables with an uppercase "V" (Prolog requires all variables to begin with a capital letter),
- translates all built-in primitive functions and predicates (e.g., **id**) into corresponding Prolog constants (e.g., **id**),
- translates all user-defined primitive functions and predicates (e.g., reps) into Prolog terms that associate a function with its domain and range (e.g., fun (kreps, kRepresentative, kDistrict)),
- translates all KOLA object names (e.g., HReps) into Prolog terms prepended with a lower-case 'o' (e.g., oHReps), and
- translates KOLA's formers into prefix notation. For example, the function pattern,  $f \circ g$  is translated into the string "compose (Vf, Vg)" while invocation (f ! A) is translated into the string "invoke (Vf, VA)".

Translation of logical expressions into Prolog expressions translates conditions as described above, and maps:

- conjunctive expressions " $p_1 \wedge p_2$ " to " $\overline{p_1}, \overline{p_2}$ ",
- disjunctive expressions " $p_1 \vee p_2$ " to " $\overline{p_1}$ ;  $\overline{p_2}$ ",
- negation expressions "not  $(p_1)$ " to "not  $(\overline{p_1})$ ",
- equations " $p_1 = p_2$ " to " $\overline{p_1} = \overline{p_2}$ ", and
- arithmetic comparisons " $p_1 < p_2$ " to " $\overline{p_1} < \overline{p_2}$ ", etc.

To illustrate translation into Prolog, the result of compiling property is\_inj of Figure 5.4a is the set of Prolog rules and facts shown below:

is_inj (id).		
is_inj (times).		
is_inj (Vf)	: –	is_key (Vf).
$\texttt{is\_inj} (\texttt{compose} (\texttt{Vf}, \texttt{Vg}))$	: –	is_inj (Vf), is_inj (Vg).
is_inj (sum (Vf, Vg))	: –	<pre>is_inj (Vf); is_inj (Vg).</pre>
<pre>is_inj (iterate (const (true), Vf))</pre>	: -	is_inj (Vf).

Any conditional rule will consult the Prolog rules and facts compiled from the properties named in the USES clause of the containing transformation. As well, two more Prolog files are consulted automatically. The first of these is a collection of facts and rules automatically generated from database metadata (for now this file is generated manually). These include typing information for all global names and all attributes and methods, and semantic information (such as key constraints) specific to the database. The second file consulted is a set of built-in rules that provide information that is invariant across database populations. These built-in rules include typing rules regarding KOLA's primitives and formers.

#### 5.3.3 Integrating Inference and Rule Firing

Below we illustrate the steps that are performed when a conditional rewrite rule is fired on a query. We demonstrate these steps by tracing the firing of rule inj1 of Figure 5.3 on the KOLA version of the "Major Cities" query (Figure 5.2: 1a).

- 1. The head pattern of the rule above is matched with the "Major Cities" query generating an *environment* of bindings for pattern variables: p (bound to  $K_p$  (true)), f (bound to lgst\_cit  $\circ$  reps) and A (bound to HReps).
- 2. A Prolog query is generated. First, Prolog subqueries of the form,  $V_i = T_i$  are generated for each variable,  $V_i$  appearing in the head pattern (p, f and A). For a given variable  $V_i$ ,  $T_i$  is the Prolog translation of the subexpression bound to  $V_i$ . In the case of the "Major Cities" query, the generated subqueries are:

These Prolog subqueries are then added to a Prolog subquery generated by translating the conditions of the conditional rewrite rule. The Prolog query generated from firing the conditional rewrite rule on the "Major Cities" query is

3. The generated Prolog query is issued to the Prolog interpreter with the built-in rules described earlier, and the relevant Prolog facts and rules generated from inference

rules and metadata. In the case of the "Major Cities" query, the relevant Prolog rules would be those resulting from the compilation of the inference rules of Figure 5.4a and 5.4b, and the metadata facts:

pis\_key (fun(klgst\_cit, kDistrict, kCity)),
pis\_key (fun(kreps, kRepresentative, kDistrict)), and
pis\_type (oHReps, set(oRepresentative)).

4. The Prolog query is posed of the Prolog interpreter and the results interpreted. If the results include new variable bindings to KOLA expressions expressed as Prolog terms, these terms are translated back into KOLA expressions and added to the environment of (variable, subexpression) bindings generated in Step (1). For the "Major Cities" query, the Prolog interpreter uses the translations of inference rules (2) and (3) (Figure 5.4a) and (2) (Figure 5.4b) to reduce the inference query generated in step (2) to the simpler queries,

pis\_key (fun(klgst\_cit, kDistrict, kCity)),
pis\_key (fun(kreps, kRepresentative, kDistrict)) and
pis\_type (oHReps, set(\_)).

These simpler queries all are satisfied by facts generated from metadata.

5. The environment generated in steps (1) and (4) is used to instantiate the pattern variables appearing in the body pattern of the conditional rewrite rule. The instantiated pattern is then returned as the output of rule firing. In the case of the "Major Cities" query, the returned query is: **iterate** ( $K_p$  (true), lgst\_cit  $\circ$  reps) ! HReps.

#### 5.4 Discussion

#### 5.4.1 Benefits to this Approach

The examples presented in this chapter demonstrate our approach to *expressing* semantic query rewrites. The query rewrite presented at the chapter's onset that eliminates redundant duplicate elimination is used in many commercial relational database systems. It is also presented as one of the Starburst query rewrites in [79]. In Starburst, this rewrite is used as a normalization step before view merging. Subqueries that perform duplicate elimination make view merging impossible because duplicate semantics are lost as a result of the merge. Starburst uses this rewrite in order to recognize subqueries that can be transformed into equivalent queries that perform no duplicate elimination so that view merging

can take place. The rewrites of Section 5.2 that use predicate strength have also been considered elsewhere. Those that remove quantification from complex predicates (Example 1 of Section 5.2) are standard techniques that one can find in many textbooks. Those that introduce new predicates (Examples 2 and 3 of Section 5.2) are similar to the "predicate move-around" techniques for transforming relational queries [71].

What is unique in our work is the use of declarative conditional rewrite rules and inference rules to express these complex transformations. With our approach we can verify all of the rules presented in these sections with a theorem prover. (See Appendix B.5 for LP theorem prover scripts for these rules.) Verification of conditional rewrite rules establishes that query semantics are preserved when these rules are fired on queries satisfying the rules' semantic preconditions. Verification of inference rules establishes that semantic conditions are inferred only when appropriate (soundness).

The other contribution of this approach concerns extensibility. Starburst and "predicate move-around" rewrites use the ideas discussed in Sections 5.1 and 5.2 in the context of relational databases. To simulate their results, we do not need all of the inference rules of Figure 5.4a that infer injectivity, nor do we need all of the inference rules of Figure 5.7 that infer predicate strength. For example, to capture the duplicate elimination query rewrite presented in Starburst for relational queries, we only need inference rules that establish an attribute to be injective if it is a key (Figure 5.4a, Rule (2)) and if it is a pair (equivalently, a relational tuple) containing a key (Figure 5.4a, Rule (4)). Rule (3) of Figure 5.4a is not needed as there is no notion of a composed data function in the relational data model. But if the relational version of this rewrite were expressed in our framework, it would be straightforward to *extend* this rewrite (to work for example, in an object database setting) simply by adding a verified inference rule such as Rule (3) of Figure 5.4a. Note that the addition of this one inference rule makes the rewrite rules conditioned on injectivity fired in a greater variety of contexts (e.g., when queries include path expressions with keys, or tuples with fields containing path expressions with keys etc.). By similar reasoning, not all of the predicate strength inference rules of Figure 5.7 are required to express the "predicate move-around" rewrites when confined to relations (e.g., Rule (4) of Figure 5.7 is unnecessary because of its use of function composition). Again, rules such as this one can be added to simply extend a relational optimizer to work robustly in an object setting.

#### 5.4.2 The Advantage of KOLA

We argued in Chapter 3 that the combinator flavor of KOLA makes declarative rewrite rules easy to express. The meaning of a KOLA subexpression is context-independent. Therefore, code supplements are not required to identify subexpressions, nor are code supplements required to formulate new queries that reuse identified subexpressions in new contexts.

The advantage of combinators extends to the formulation of conditional rewrite rules and inference rules. Conditional rewrite rules must identify subexpressions upon which to express conditions. Inference rules also must identify subexpressions because conditions tend to be inferred from conditions held of subexpressions (e.g., the injectivity of complex functions can be inferred from the injectivity of their subfunctions). Again, variables in a query representation complicate the identification of these subexpressions.

Consider as an example, the data functions appearing in the "Major Cities" query and the "Mayors" query. The KOLA forms of these functions are:

> lgst\_cit  $\circ$  reps, and iterate (K<sub>p</sub> (true), mayor)  $\circ$  cities  $\circ$  reps.

These two functions are both injective by similar reasoning: they are compositions of other functions that are injective. Inferring injectivity of the OQL forms of these data functions,

x.reps.lgst\_cit, and

SELECT DISTINCT d.mayor FROM d IN x.reps.cities

is more complicated. The identification of both of these data functions as being compositions of other functions requires machinery beyond what can be expressed with rewrite rules. Specifically, determining exactly what are the subfunctions of these functions requires reversing the process of substituting expressions for variables by factoring the complex expressions denoting the functions into two expressions for which the substitution of one for a variable in the other reproduces the original expression. For the path expression,  $x.reps.lgst_cit$ , these subfunctions are x.reps and  $x.lgst_cit$  (as substituting the first of these expressions for x in the second expression reproduces the original path expression). For the subfunctions are, x.reps.cities and

> SELECT DISTINCT d.mayor FROM d IN x

as again, substituting the first expression for x in the second expression results in the original expression. The decomposition required to identify subfunctions is inexpressible with declarative rewrite rules and instead requires calls to supplemental code.

# 5.5 Chapter Summary

This chapter presents our approach to extending the expressive power of rewrite rules without compromising the ease with which they can be verified. The techniques proposed here target the expression of query rewrites that are too specific to be captured with rewrite rules. The correctness of these rewrites depends on the semantics, and not just the syntax of the queries on which they fire.

This work builds upon the foundation laid with KOLA. We introduced *conditional rewrite rules*; rewrite rules whose firing depends on the satisfaction of semantic conditions of matched expressions. We then introduced *inference rules* that tell query rewriters how to decide if these semantic conditions hold. In the spirit of KOLA, both conditional rewrite rules and inference rules are expressed declaratively and are verifiable with LP.

This work contributes to the extensibility and verifiability of query rewriters. With respect to verification, the declarative flavor of both forms of rules makes them amenable to verification with a theorem prover. This approach is in stark contrast to the code-based rules of existing rule-based systems such as Starburst [79] and Cascades [42], which express conditions and condition-checking with code. With respect to extensibility, the separation of a condition's inference rules from the rewrite rules that depend on them, achieves a different form of extensibility than was provided by rewrite rules alone. Whereas rewrite rules make optimizers extensible by making it simple to change the potential actions taken by an optimizer, inference rules make optimizers extensible by making it simple to change the contexts in which these rules get fired.

# Chapter 6

# **Experiences With COKO-KOLA**

The goal of the work presented in this chapter was to determine the feasibility of the COKO-KOLA approach in an industrial setting. The COKO-KOLA approach clearly offers large gains in the formal methods aspects of query optimizer development; it is the first rule-based optimizer framework whose inputs can be verified with a theorem prover. But do these gains come at some practical cost? Can fully functional query optimizers be built within this framework or are we limited to toy examples with trivial functionality? Just how expressive is COKO for expressing the kinds of query rewrites that get used in real optimizers?

To address these questions, we teamed up with researchers from the IBM Thomas J. Watson Research Center and the IBM AS/400 Divisions to build a query rewriting component for a query optimizer for an object-oriented database. The IBM San Francisco project implements an Object-Oriented database using the relational database, DB2. Our contribution to this project was to use COKO-KOLA build a query rewriter that translates object queries on this object-oriented database (expressed in an experimental subset of OQL, informally called Query Lite) into equivalent SQL queries over the underlying DB2 relations. This project thereby provided a workbench with which we could consider the following issues concerning the practicality of the COKO-KOLA approach:

- *Integration:* How easy is it to use query rewriters generated from COKO transformations with existing query processors? That is, can we use COKO-KOLA to generate components that improve upon the behavior of an optimizer (either by making it work over a larger set of queries or by making it produce "better" plans), without having to make changes to optimizer code?
- Ease-Of-Use: How straightforward is it to express useful query rewrites? For the

Query Lite project, how many COKO transformations, KOLA rewrite rules and lines of firing algorithm code would be required to express the object  $\rightarrow$  relational query mapping?

This chapter begins in Section 6.1 with background on the San Francisco project and Query Lite. Sections 6.2 and 6.4 describe additions to the COKO-KOLA implementation required to complete this project, including translators to translate:

- Query Lite queries (and more generally, OQL's set-and-bag queries) into KOLA (Section 6.2), and
- KOLA queries into SQL (Section 6.4).

Section 6.3 describes the COKO transformations developed for the San Francisco project. These include a normalization transformation described in Section 6.3.2, whose purpose is to normalize KOLA queries resulting from translation (from Query Lite or OQL) into a form that makes query rewriting straightforward, and a transformation (presented in Section 6.3.3) to rewrite these normalized queries into a form that can be translated into SQL. Section 6.5 considers the feasibility issues in light of these transformations. Section 6.6 summarizes the chapter.

# 6.1 Background

The San Francisco project uses relational technology to implement an object-oriented database. Specifically, the database implementation for this project uses DB2 as its relational backbone.

#### 6.1.1 San Francisco Object Model

The object model for San Francisco is similar to the ODMG object model outlined in [14], and therefore similar also to the KOLA data model described in Section 3.2.2. Specifically, objects have unique immutable identifiers (OID's), and are classifiable by their types. An object type defines a set of public *methods* that can be invoked on collections of objects of that type in a query. These methods can have any arity, are invoked using message passing syntax, and can return values of basic types (e.g., integers), OID's for other objects, or references to collections. These methods can either be *attribute-based* (meaning they simply return a value associated with the object, as with *instance variables*) or *derived*, in which case the returned value is computed rather than retrieved. Objects themselves can be contained in any number of object collections and will at least be included in the automatically maintained collection of instances of objects of the same type (the type's *extent*).

#### 6.1.2 Relational Implementation of the Object Model

The relational implementation of objects is straightforward, and similar to schemes described elsewhere (e.g., [60]). Firstly, any collection of objects of a particular type (including a type extent) is represented by a relation. The structure of this relation is derived from the interface of the associated object type in the following way:

- A column (which for simplicity we will name OID) is dedicated to denote each object's unique identifier. Such identifiers are typically strings.
- Columns are reserved for each attribute-based method (except those that are collectionvalued.) Atribute-based methods that return values of some basic type (e.g., integers) are represented by columns with values of that type. Attribute-based methods that return other objects are represented by columns whose values are strings denoting object identifiers.

To illustrate the object  $\rightarrow$  relational mapping, a relational implementation of a portion of the object schema illustrated in Figure 2.1 is described. Object collections **Sens** and **Sts** would be implemented with the relations **Sens** and **Sts** shown below with their respective structures:

```
Sens: (OID: String, name: String, reps: String, pty: String, terms: Int)
Sts: (OID: String, name: String, lu: String)
```

An object population that included Senator objects s1 and s2 representing Rhode Island ("R.I"), and named "Jack Reed" and "John Chafee" respectively would result in the following entries in these relations:

Sens						
OID	name	reps	pty	terms		
"s1"	"Jack Reed"	"r1"	"Dem"	1		
"s2"	"John Chafee"	"r1"	"GOP"	5		

Sts				
OID	name	lu		
"r1"	"R.I."	"University of R.I."		

Objects with attribute-based methods returning collections are treated as a special case in the relational implementation. Specifically, these methods are represented with their own relations that associate OID's with the values or OID's of objects contained in the collection. For example, the collection SRs of Senate resolution objects (as defined in Figure 2.1) would be implemented with the relations shown below:

> SRs: (OID:String, topic:String) SRs--spons: (OID1:String, OID2:String).

Relation SRs stores Senate resolution object identifiers with the values of their non-collection attribute-based method, topic. Relation SRs-spons stores Senate resolution object identifiers with the OID's of objects contained in the collection returned by attribute-based method, spons. For example, if sr1 is a Senate resolution object whose topic is "NSF funding", and that is sponsored by the Senators, s1 and s2, then relations SRs and SRs-spons would include the following entries:

SRs		SRs-spons	
		OID1	OID2
UID	JID topic	"ar1"	"c1"
"sr1"	"NSF Funding	51 I	ы " о"
		"srl″	"s2″

#### 6.1.3 Querying

A query processor for San Francisco is under development. Early releases will support a limited subset of OQL called Query Lite. Query Lite restricts queries to those of the form,

```
SELECT x
FROM x IN A
[WHERE BoolExp]
[ORDER BY OrderExp]
```

such that [...] denotes an optional component, *BoolExp* denotes a boolean expression consisting of conjunctions, disjunctions and negations of simple comparison expressions, and *OrderExp* is either the name of an externally defined comparison function or a list of unary methods defined on the objects in A. Like OQL, Query Lite queries can contain invocations of methods with multiple arguments and path expressions (although only in their WHERE clause). But Query Lite supports neither join queries nor embedded collections. A full grammar for Query Lite is shown in Table 6.1.

#### 6.1.4 Our Contribution

Our contribution was to build a query rewriter (using COKO-KOLA) that transforms Query Lite queries with path expressions, into equivalent SQL queries over the underlying relational implementation.<sup>1</sup> For example, the Query Lite query,

> SELECT x FROM x IN Sens WHERE x.reps.name == "R.I."

gets rewritten by our rewriter into the SQL query,

SELECT x
FROM x IN Sens, y IN Sts
WHERE x.reps == y.OID AND y.name == "R.I."

(assuming the scheme for representing object collections as relations described in the previous section). This effort required that we (1) translate Query Lite queries with path expressions into KOLA, (2) rewrite the KOLA path expression queries into KOLA join queries, and (3) translate the KOLA join queries into SQL.<sup>2</sup> The components required for each of these tasks are illustrated in Figure 6.1. Sections 6.2, 6.3 and 6.4 present the designs and implementations of these components.

# 6.2 Translating Query Lite Queries into KOLA

The simplicity of Query Lite makes a Query Lite  $\rightarrow$  KOLA translator straightforward to design. However, as the eventual goal of the San Francisco project is to support querying in OQL, a sophisticated approach to translation is required. In this section, we describe the reasoning behind our approach to translation, which accounts for an eventual migration to OQL.

<sup>&</sup>lt;sup>1</sup>Because KOLA does not yet have support for lists, we only address Query Lite queries that do not contain an ORDER BY clause.

 $<sup>^{2}</sup>$ A fourth step to provide an object view over the relational data returned by the SQL queries is not considered here.



Figure 6.1: An Architecture for the Query Lite Query Rewriter

Constants, Variables and Path Expressions Exp : c (c a non-Bool constant/global name) **IDENT** (an identifier denoting the name of a variable) Exp . IDENT Exp . IDENT ( Exp , Exp , ..., Exp ) Arithmetic Expressions - ( Exp ) ABS ( Exp ) Exp + ExpExp - ExpExp \* ExpExp / ExpExp MOD ExpQuery Expressions SELECT x (Any variable name can be substituted for x) FROM x IN IDENT Query : [WHERE BoolExp] [ORDER BY OrdExp] Boolean Expressions BoolExp : TRUE FALSE Exp IS NULL Exp IS NOT NULL Exp == ExpExp != Exp

| Exp : Exp | Exp < Exp | Exp > Exp | Exp <= Exp | Exp >= Exp | NOT ( BoolExp ) | BoolExp AND BoolExp | BoolExp OR BoolExp

#### Ordering Expressions

OrderExp : IDENT . IDENT, ..., IDENT . IDENT Direction | IDENT Direction

Direction : ASC | DESC

Table 6.1: The Syntax of Query Lite

#### 6.2.1 Translation Strategies

Translation from Query Lite into KOLA is straightforward. Given a Query Lite query e,

```
SELECT x
FROM x IN A
WHERE p(x),
```

KOLA equivalent of  $e(\mathbf{T} \llbracket e \rrbracket)$  is

```
iterate (T \llbracket p \rrbracket, id) ! A.
```

This simplistic approach says that translation generates a KOLA query of the form,

f ! x,

such that x (the *data component* of the KOLA query) is generated from the expression in the query's FROM clause, and f (the *function component* of the KOLA query) is generated from the expressions in the query's SELECT and WHERE clauses.

We decided against this translation strategy because it does not generalize well to OQL, the language that eventually will be used as the query language for San Francisco. Specifically, determining which parts of a query correspond to the data and function components of the KOLA translation becomes blurred in the presence of nested queries and embedded collections. Consider for example, the OQL query of Figure 6.2*a*, which finds all committees with Republican members. This query invokes the method mems to return the embedded collection of members of any given committee. The simplistic assumption that what appears in a query's FROM clause is automatically the data component of a query is violated here, as a collection of committee. Therefore, the simplistic translation strategy that works for Query Lite queries does not work for queries such as this.

#### An Alternative Strategy: The 1st Collection in a FROM Clause is Data

Consider the following alternative translation strategy: rather than designating all expressions appearing a query's FROM clause as data components, instead designate only the *first* collection named in the FROM clause as a data component. Therefore, translation of the query of Figure 6.2a would designate Coms as the only data component of the query, and produce a KOLA query on Coms:

(iterate (eq  $\oplus \langle pty \circ \pi_2, K_f ("GOP") \rangle, \pi_1) \circ unnest (id, mems)) ! Coms.$ 

SELECT DISTINCT x FROM x IN Coms, y IN x.mems WHERE y.pty == "GOP"

a. A Query with a Path Expression (x.mems) in its FROM Clause

 $\begin{array}{l} \text{SELECT} \left( \begin{array}{c} \text{SELECT} \ y \\ \text{FROM} \ y \ \text{IN} \ x.\text{mems} \\ \text{WHERE} \ y.\text{terms} \ > \ 5 \end{array} \right) \\ \text{FROM x IN Coms} \\ \text{WHERE} \ x.\text{topic} == "NSF" \end{array}$ 

b. A Nested Query

Figure 6.2: OQL Queries that make Translation into KOLA Difficult

This query first pairs every committee with each of its members (**unnest**), and then determines which (committee, member) pairs satisfy the condition that member is a Republican (**iterate**).

Once queries can be nested, this strategy also fails. Consider the nested query of Figure 6.2b which finds the senior members of committees in Coms that study the NSF. The subquery

SELECT 
$$y$$
  
FROM  $y$  IN  $x$ .mems  
WHERE  $y$ .terms > 5

has the path expression, *x.mems* in its FROM clause. This expression is not a data component and instead must be mapped to a function, even though it is the first expression in the FROM clause. Therefore, this translation strategy must treat *outer* queries (queries that include subqueries, which must get translated to function invocations) differently from *inner* queries (queries that are subexpressions of outer queries, which must get translated into functions).

#### **Our Strategy: Everything Generates a Function**

The solution we take is to designate *all* parts of the query as function components. This approach to translation simplifies the design of the translator greatly as it removes the need to analyze each subexpression to see if it constitutes data or function. However, the consequence of this design decision is that translation returns KOLA expressions that are not intuitive. This problem is addressed after translation by a normalization (defined in COKO) to rewrite translated queries into more intuitive forms. SELECT x FROM x IN Sens WHERE x.terms > 5 a. A Query Lite Query (iterate (gt  $\oplus$  (terms  $\circ \pi_2$ , K<sub>f</sub> (5)),  $\pi_2$ )  $\circ$ unnest (id, K<sub>f</sub> (Sens))  $\circ$ single) ! NULL b. Translation Into KOLA

iterate  $(\mathbf{gt} \oplus \langle \mathbf{id}, K_f(5) \rangle \oplus \mathbf{terms}, \mathbf{id})$  ! Sens c. After Normalization

Figure 6.3: A Query Lite Query (a), its Translation (b) and its Normalization (c)

Figures 6.3a and 6.3b show a simple Query Lite query (that finds all Senators who have served more than 5 terms) and the result of translating this query according to this strategy. Note that translation produces a function that gets invoked on NULL. NULL is an arbitrary argument to this function; in fact the function would return the same result no matter what was its argument (i.e., the function generated by the translator is a *constant function*). This translation strategy makes the result of translation counterintuitive, as the query that is produced does not get invoked on one or more collections, but on a constant that does not even figure in the final result.

The result of translation shown in 6.3b is not as intuitive a translation as the equivalent KOLA query shown in Figure 6.3c, which simply filters Senators in **Sens** who have served more than 5 terms. However, the KOLA expression of Figures 6.3b has the same semantics as the initial Query Lite query, as is demonstrated by the reduction below:

(iterate (gt  $\oplus \langle \text{terms} \circ \pi_2, K_f(5) \rangle, \pi_2) \circ$ unnest (id,  $K_f$  (Sens))  $\circ$  single) ! NULL

- $\stackrel{1}{\rightarrow} \text{ iterate } (\mathbf{gt} \oplus \langle \texttt{terms} \circ \pi_2, \mathsf{K}_f (5) \rangle, \pi_2) !$   $(\mathbf{unnest} (\mathbf{id}, \mathsf{K}_f (\texttt{Sens})) ! (\mathbf{single} ! \texttt{NULL}))$
- $\stackrel{2}{\rightarrow} \quad \textbf{iterate} \ (\textbf{gt} \oplus \langle \texttt{terms} \circ \pi_2, \texttt{K}_f \ (5) \rangle, \ \pi_2) \ ! \ (\textbf{unnest} \ (\textbf{id}, \texttt{K}_f \ (\texttt{Sens})) \ ! \ \{\texttt{NULL}\}\}$
- $\stackrel{3}{\rightarrow} \text{ iterate } (\mathbf{gt} \oplus \langle \texttt{terms} \circ \pi_2, \mathsf{K}_f (5) \rangle, \pi_2) ! \\ (\{ (\mathbf{id} ! [x, s])^{ij} \mid x^i \in \{\texttt{NULL}\}, s^j \in (\mathsf{K}_f (\texttt{Sens}) ! x) \} )$
- $\stackrel{4}{\rightarrow} \text{ iterate } (\mathbf{gt} \oplus \langle \texttt{terms} \circ \pi_2, \texttt{K}_f (5) \rangle, \pi_2) ! (\{[x, s]^{ij} \mid x^i \in \{\texttt{NULL}\}, s^j \in \texttt{Sens}\}$

$$\begin{array}{l} \stackrel{5}{\rightarrow} & \text{iterate } (\mathbf{gt} \oplus \langle \text{terms } \circ \pi_2, \, \mathsf{K}_f(5) \rangle, \, \pi_2) \, ! \quad (\{[\texttt{NULL}, \, s]^j \, | \, s^j \in \texttt{Sens}\} \\ \stackrel{6}{\rightarrow} & \{(\pi_2 \, ! \, [\texttt{NULL}, \, s])^j \, | \, s^j \in \texttt{Sens}, \, (\mathbf{gt} \oplus \langle \texttt{terms} \circ \pi_2, \, \mathsf{K}_f(5) \rangle) \, ? \, [\texttt{NULL}, \, s]] \} \\ \stackrel{7}{\rightarrow} & \{(\pi_2 \, ! \, [\texttt{NULL}, \, s])^j \, | \, s^j \in \texttt{Sens}, \, \mathbf{gt} \, ? \, (\langle \texttt{terms} \circ \pi_2, \, \mathsf{K}_f(5) \rangle \, ! \, [\texttt{NULL}, \, s])\} \\ \stackrel{8}{\rightarrow} & \{s^j \, | \, s^j \in \texttt{Sens}, \, \mathbf{gt} \, ? \, [(\texttt{terms} \circ \pi_2) \, ! \, [\texttt{NULL}, \, s], \, \mathsf{K}_f(5) \, ! \, [\texttt{NULL}, \, s]]\} \\ \stackrel{9}{\rightarrow} & \{s^j \, | \, s^j \in \texttt{Sens}, \, \mathbf{gt} \, ? \, [\texttt{terms} \, ! \, (\pi_2 \, ! \, [\texttt{NULL}, \, s]), \, \mathsf{K}_f(5) \, ! \, [\texttt{NULL}, \, s]]\} \\ \stackrel{10}{\rightarrow} & \{s^j \, | \, s^j \in \texttt{Sens}, \, \mathbf{gt} \, ? \, [\texttt{terms} \, ! \, s, \, \mathsf{K}_f(5) \, ! \, [\texttt{NULL}, \, s]]\} \\ \stackrel{11}{\rightarrow} & \{s^j \, | \, s^j \in \texttt{Sens}, \, \mathbf{gt} \, ? \, [s.\texttt{terms}, \, \mathsf{K}_f(5)]\} \\ \stackrel{12}{\rightarrow} & \{s^j \, | \, s^j \in \texttt{Sens}, \, s.\texttt{terms} \, > \, 5\} \end{array}$$

Step 1 of this reduction follows from the definition of  $\circ$ . Step 2 follows from the definition of **single**. Step 3 follows from the definition of **unnest**. Step 4 follows from the definitions of **id** and  $K_f$ . Step 5 follows from the fact that  $x^i$  is being drawn from a singleton set. Step 6 follows from the definition of **iterate**. Step 7 follows from the definition of  $\oplus$ . Step 8 follows from the definition of  $\langle \rangle$ . Step 9 follows from the definition of  $\circ$ . Step 10 follows from the definition of  $\pi_2$ . Step 11 follows from the definition of function attribute primitives and  $K_f$ . Step 12 follows from the definition of **gt**.

Our approach to translation is similar to how Query Lite or OQL queries would be given a denotational semantics. Because arbitrary Query Lite and OQL expressions can have occurences of free variables (e.g., x in "x > 5"), the semantics of such expressions is dependent on an *environment* that defines what is referred to by the free variables appearing within the expression. More precisely, an *environment* is a list of (variable, value) pairs

$$((v_1, d_1), (v_2, d_2), \dots, (v_n, d_n))$$

providing the bindings of all free variables,  $v_1, \ldots, v_n$  appearing in a given expression. (If an environment  $\rho$  gives bindings to every free variable in an expression, e, we say that eis *well-formed* with regard to to  $\rho$ .) The denotational semantics of a Query Lite or OQL expression, e is a function (**Eval**  $[\![e]\!]$ ) that maps all environments for which it is well-formed to values. For example,

Eval 
$$[x > 5]$$
  $\rho$ 

is true if  $\rho = ((x, 6))$  but false if  $\rho = ((x, 4))$ . Queries that do not appear as subexpressions of other queries will have no free variables, and therefore are well-formed with regard to the empty environment, (). The denotational semantics of these expressions are constant functions. The idea behind this translation strategy is to map every expression e to the KOLA function  $\mathbf{T} [\![e]\!]$  whose operational semantics coincides with e's denotational semantics. More precisely, if e is well-formed with respect to some environment,

$$\rho = ((v_1, d_1), (v_2, d_2), \dots, (v_n, d_n)),$$

then  $\mathbf{T}$  [[e]] is a KOLA function satisfying the constraint that

$$\mathbf{T} \llbracket e \rrbracket \ ! \ (\overline{\rho}) = \mathbf{Eval} \ \llbracket e \rrbracket \ \rho$$

such that  $\overline{\rho}$  is the KOLA nested pair representation of environment  $\rho$ ,

$$[\ldots [d_1, d_2], \ldots d_n].^3$$

Queries that are well-formed with regard to the empty environment get mapped to constant KOLA functions. The choice of NULL as an argument to these functions can be thought of as reflecting how KOLA represents the empty environment (i.e.,  $\overline{()} = \text{NULL}$ ).

#### 6.2.2 T: The Query Lite $\rightarrow$ KOLA Translation Function Described

We have defined a translator from a set-and-bag-based subset of OQL to KOLA. This subset of OQL is a superset of Query Lite. The part of the translator that processes Query Lite queries is described here. (The full OQL translator is described and proven correct in [17].<sup>4</sup>)

The translation of a Query Lite query q, is

```
\mathbf{T} \llbracket q \rrbracket ! NULL
```

such that  $\mathbf{T} \llbracket q \rrbracket$  is as defined in Table 6.2. Below we examine this translation function, defined over all Query Lite queries and expressions.

#### **Translating Constants**

All non-Bool constants (e.g., -3, 5.322, "Hello World", NULL, ...) are translated into constant functions (K<sub>f</sub> (-3), K<sub>f</sub> (5.32), K<sub>f</sub> ("Hello World"), K<sub>f</sub> (NULL), ...). (Bool constants are translated into constant predicates K<sub>p</sub> (TRUE) and K<sub>p</sub> (FALSE).)

 $\mathbf{T} \llbracket b \rrbracket ? (\overline{\rho}) = \mathbf{Eval} \llbracket b \rrbracket \rho.$ 

<sup>&</sup>lt;sup>3</sup>A boolean expression b would similarly be mapped to KOLA predicate,  $\mathbf{T} \llbracket b \rrbracket$  such that

<sup>&</sup>lt;sup>4</sup>In fact, an older translator that translates a *set-based* (as opposed to a set-and-bag based) subset of OQL is presented and proven correct in a technical report [17]. The correctness proof (by structural induction) is nonetheless highly suggestive of what the correctness proof for this version of the translator will involve. The updated correctness proof is future work.

Constants, Variables and Path Expressions  $\mathbf{T} \begin{bmatrix} c \end{bmatrix} = K_f(c) (c \text{ a non-Bool constant/global name})$  $\mathbf{T} \llbracket V_0 \rrbracket = \pi_2$  $\mathbf{T} \llbracket V_i \rrbracket = \mathbf{T} \llbracket V_{i-1} \rrbracket \circ \pi_1 \quad (\text{for } i > 0)$  $\mathbf{T} \llbracket Exp \text{. IDENT} \rrbracket = \text{IDENT} \circ \mathbf{T} \llbracket Exp \rrbracket$  $\mathbf{T} \llbracket Exp$ . IDENT  $(Exp_1, Exp_2, \ldots, Exp_n) \rrbracket =$  $\mathsf{IDENT} \mathrel{\circ} \langle \mathbf{T} [\![Exp]\!], \langle \langle \dots \langle \mathbf{T} [\![Exp_1]\!], \mathbf{T} [\![Exp_2]\!] \rangle, \dots \rangle, \mathbf{T} [\![Exp_n]\!] \rangle \rangle$ Arithmetic Expressions  $\mathbf{T} \llbracket - (Exp) \rrbracket = \mathbf{C}_f (\mathbf{mul}, -1) \circ \mathbf{T} \llbracket Exp \rrbracket$  $\mathbf{T} \llbracket \mathtt{ABS} \ (Exp) \rrbracket = \mathbf{abs} \ \circ \ \mathbf{T} \llbracket Exp \rrbracket$  $\mathbf{T} \llbracket Exp_0 + Exp_1 \rrbracket = \mathbf{add} \circ \langle \mathbf{T} \llbracket Exp_0 \rrbracket, \mathbf{T} \llbracket Exp_1 \rrbracket \rangle$  $\mathbf{T} \llbracket Exp_0 - Exp_1 \rrbracket = \mathbf{sub} \circ \langle \mathbf{T} \llbracket Exp_0 \rrbracket, \mathbf{T} \llbracket Exp_1 \rrbracket \rangle$  $\mathbf{T} \llbracket Exp_0 * Exp_1 \rrbracket = \mathbf{mul} \circ \langle \mathbf{T} \llbracket Exp_0 \rrbracket, \mathbf{T} \llbracket Exp_1 \rrbracket \rangle$  $\mathbf{T} \llbracket Exp_0 / Exp_1 \rrbracket = \mathbf{div} \circ \langle \mathbf{T} \llbracket Exp_0 \rrbracket, \mathbf{T} \llbracket Exp_1 \rrbracket \rangle$  $\mathbf{T} \llbracket Exp_0 \text{ MOD } Exp_1 \rrbracket = \mathbf{mod} \circ \langle \mathbf{T} \llbracket Exp_0 \rrbracket, \mathbf{T} \llbracket Exp_1 \rrbracket \rangle$ Query Expressions  $\mathbf{T} \left[ \begin{array}{c} \text{SELECT } x \\ \text{FROM } x \text{ IN IDENT} \\ \text{WHERE } BoolExp \end{array} \right]$ iterate (**T**  $[BoolExp], \pi_2$ )  $\circ$ single Boolean Expressions  $\mathbf{T}$  [TRUE] =  $K_p$  (TRUE)  $\mathbf{T}$  [FALSE] =  $K_p$  (FALSE)  $\mathbf{T} \llbracket Exp \text{ IS NULL} \rrbracket = \text{ isnull} \oplus \mathbf{T} \llbracket Exp \rrbracket$  $\mathbf{T} \llbracket Exp \text{ is not null} 
ightharpoonup$ = isnotnull  $\oplus \mathbf{T} \llbracket Exp \rrbracket$  $\mathbf{T} \llbracket Exp_0 == Exp_1 \rrbracket = \mathbf{eq} \oplus \langle \mathbf{T} \llbracket Exp_0 \rrbracket, \mathbf{T} \llbracket Exp_1 \rrbracket \rangle$  $\mathbf{T} \llbracket Exp_0 != Exp_1 \rrbracket = \mathbf{neq} \oplus \langle \mathbf{T} \llbracket Exp_0 \rrbracket, \mathbf{T} \llbracket Exp_1 \rrbracket \rangle$  $\mathbf{T} \llbracket Exp_0 < Exp_1 \rrbracket = \mathbf{lt} \oplus \langle \mathbf{T} \llbracket Exp_0 \rrbracket, \mathbf{T} \llbracket Exp_1 \rrbracket \rangle$  $\mathbf{T} \llbracket Exp_0 > Exp_1 \rrbracket = \mathbf{gt} \oplus \langle \mathbf{T} \llbracket Exp_0 \rrbracket, \mathbf{T} \llbracket Exp_1 \rrbracket \rangle$  $\mathbf{T} \llbracket Exp_0 \leq Exp_1 \rrbracket = \mathbf{leq} \oplus \langle \mathbf{T} \llbracket Exp_0 \rrbracket, \mathbf{T} \llbracket Exp_1 \rrbracket \rangle$  $\mathbf{T} \llbracket Exp_0 \geq Exp_1 \rrbracket = \mathbf{geq} \oplus \langle \mathbf{T} \llbracket Exp_0 \rrbracket, \mathbf{T} \llbracket Exp_1 \rrbracket \rangle$  $\mathbf{T} [[NOT (BoolExp)]] = \sim (\mathbf{T} [[BoolExp]])$  $\mathbf{T} \llbracket BoolExp_0 \text{ AND } BoolExp_1 \rrbracket = \mathbf{T} \llbracket BoolExp_0 \rrbracket \& \mathbf{T} \llbracket BoolExp_1 \rrbracket$  $\mathbf{T} \llbracket BoolExp_0 \ \mathsf{OR} \ BoolExp_1 \rrbracket = \mathbf{T} \llbracket BoolExp_0 \rrbracket \mid \mathbf{T} \llbracket BoolExp_1 \rrbracket$ 

Table 6.2: **T**: The Query Lite  $\rightarrow$  KOLA Translation Function
#### **Translating Variables**

The translation of variables is perhaps the most complex aspect of translation. Conceptually, variable translation works from a preprocessed version of the query in which all variable references are replaced by deBruijn variables [30]. A deBruijn variable is a variable *index*  $(V_i \text{ for } i \ge 0)$  that indicates the position of a variable reference relative to its declaration. (Higher values of *i* indicate a greater "distance" between reference and declaration.  $V_0$ always refers to the most "recently" declared variable.)

The preprocessing step that converts variable references into deBruijn variables must first associate every referenced variable with its declaration. Variable declarations typically occur in a query's FROM clause, as in "x IN COLL", which declares variable x to range over the elements of collection COLL. In OQL, variable declarations can also occur in a query's WHERE clause if it contains a *quantifier expression*, as in

EXISTS 
$$x$$
 IN COLL:  $p(x)$ 

which also declares variable x to range over the elements of collection COLL.

The algorithm followed during this preprocessing step visits each subexpression of a given query expression's FROM, SELECT and WHERE clauses in turn. Each subexpression is associated with a *scope list* which is a list of variables that can be referenced by the subexpression.<sup>5</sup> Scope lists of subexpressions are propagated and amended during each step of the expression traversal. That is, the visit of a subexpression will accept the scope list associated with a previously visited subexpression (its *incoming* scope list). If the subexpression declares a new variable, this variables is appended to the incoming scope list to produce a scope list for subexpressions still to be visited (its *outgoing* scope list).

The algorithm is described below with respect to the generic OQL query of Figure 6.4.<sup>6</sup> In this figure,  $E_s$ ,  $E_w$ , and  $E_i$ , ...,  $E_m$  ( $0 \le i \le m$ ) are OQL subexpressions that potentially include free occurences of variables. For this example, it is assumed that this query has

$$(x_0,\ldots,x_{i-1})$$

as its incoming scope list. (If the query is not a subexpression of another query, then its incoming scope list is (). That is, i = 0.)

The subexpressions of this query are visited and processed as follows:

<sup>&</sup>lt;sup>5</sup>The variables in a subexpression's scope list are those that must be bound by any environment for which that subexpression is well-formed.

<sup>&</sup>lt;sup>6</sup>The algorithm is described in terms of an OQL query rather than a Query Lite query because every Query Lite query declares exactly one variable, making preprocessing trivial.

SELECT  $E_s$ FROM  $x_i$  IN  $E_i, \ldots, x_m$  IN  $E_m$ WHERE  $E_w$ 

Figure 6.4: A Prototypical OQL Query

- 1. for each FROM subexpression:  $E_k$   $(i \le k \le m)$ :
  - $E_k$ 's incoming scope list is  $(x_0, \ldots, x_{k-1})$ .
  - conversion into deBruijn notation replaces each  $x_j$  appearing in  $E_k$  with  $V_{k-j-1}$ .
  - $E_k$ 's outgoing scope list is  $(x_0, \ldots, x_k)$ . (That is,  $x_k$  is appended to the incoming scope list.)
- 2. for SELECT subexpression,  $E_s$  and WHERE subexpression  $E_w$ :
  - $E_s$ 's and  $E_w$ 's incoming scope lists are both  $(x_0, \ldots, x_m)$ .
  - conversion into deBruijn notation replaces each  $x_j$  in  $E_s$  or  $E_w$  with  $V_{m-j}$ .

To illustrate the algorithm, we trace its effects on the OQL query of Figure 6.2b that is nested in its SELECT clause. Assume that the outer query does not appear as a subexpression of another query (i.e., the outer query is defined with respect to the empty environment, ()). The algorithm visits subexpressions of this query in the following order:

- 1. " $x \text{ IN } K_f \text{ (Coms)}$ ":
  - 1's Incoming Scope List: ()
  - 1's Outgoing Scope List: (x)

Expression 1's outgoing scope list is the result of appending its declared variable x to its incoming scope list, ().

2. "SELECT y FROM y IN x.mems WHERE y.terms > 5":

2's Incoming Scope List: (x)

(a) "y IN x.mems" (in inner query's FROM clause):
2a's Incoming Scope List: (x)
2a's deBruijn Conversion: variable reference x is replaced by V<sub>0</sub>
2a's Outgoing Scope List: (x, y)

```
\begin{array}{l} \text{SELECT} \left(\begin{array}{c} \text{SELECT} \ V_0 \\ \text{FROM} \ y \ \text{IN} \ V_0.\text{mems} \\ \text{WHERE} \ V_0.\text{terms} \ > \ 5 \end{array}\right) \\ \text{FROM x IN Coms} \\ \text{WHERE} \ V_0.\text{topic} == \text{``NSF''} \end{array}
```



Expression 2a's outgoing scope list is the result of appending its declared variable y to its incoming scope list, (x).

(b) "SELECT y" (in inner query):

2b's Incoming Scope List: (x, y)

2b's deBruijn Conversion: variable reference y is replaced by  $V_0$ 

Variable y was the most "recently" declared variable in the incoming scope list and hence its reference is replaced by  $V_0$ . Had this reference instead been to x, it would have been replaced by  $V_1$ .

(c) "WHERE y.terms > 5" (in inner query):
2c's Incoming Scope List: (x, y)
2c's deBruijn Conversion: variable reference y is replaced by V<sub>0</sub>

After preprocessing of this query is completed, we are left with the query of Figure 6.5. Note that the relative referencing of deBruijn notation means that the same deBruijn index can refer to multiple variables within a single query. In the query of Figure 6.5, deBruijn variable  $V_0$  refers to a committee in **Coms** in the WHERE clause of the outer query and the FROM clause of the inner query, but refers to a committee member in the SELECT and WHERE clauses of the inner query.

The translation of a deBruijn variable  $(V_i)$  into KOLA is defined as follows:

- **T**  $[\![V_0]\!] = \pi_2$ , and
- **T**  $\llbracket V_i \rrbracket$  (for i > 0) = **T**  $\llbracket V_{i-1} \rrbracket \circ \pi_1$

The result of translation then, is a function that can be invoked on the KOLA representation  $(\overline{\rho})$  of the environment  $(\rho)$  associated with the translated variable. When invoked on this representation, the value bound to the variable in the environment is returned. For example, suppose that variable reference x is associated with the incoming scope list,

and is therefore well-formed with regard to environment  $\rho$ :

$$((w, 3), (x, 5), (y, -7.3), (z, "Hello")).$$

The translation of x into KOLA first generates the deBruijn variable,  $V_2$  and then produces the KOLA function,  $\pi_2 \circ \pi_1 \circ \pi_1$ . When invoked on the KOLA pair,  $\overline{\rho}$ :

[[[3, 5], -7.3], "Hello"],

this function returns 5; the value that had been associated with x in  $\rho$ .

## **Translating Path Expressions:**

The translation of a unary method invocation,

$$Exp$$
 . m

is

$$\mathtt{m} \, \circ \, \mathbf{T} \, \llbracket Exp \rrbracket.$$

The translation of an *n*-ary method invocation,

$$Exp$$
.m  $(Exp_0, Exp_1, \ldots, Exp_{n-1})$ 

is

$$\mathbf{m} \circ \langle \mathbf{T} \ \llbracket Exp \rrbracket, \ \langle \langle \dots \langle \mathbf{T} \ \llbracket Exp_0 \rrbracket, \mathbf{T} \ \llbracket Exp_1 \rrbracket \rangle, \ \dots \rangle, \ \mathbf{T} \ \llbracket Exp_{n-1} \rrbracket \rangle \rangle.$$

Assuming that Exp. m and Exp. m ( $Exp_0, Exp_1, \ldots, Exp_{n-1}$ ) are well-formed with regard to some environment,  $\rho$ , the results of invoking their KOLA translations on  $\overline{\rho}$  are:

$$m ! (\mathbf{T} \llbracket Exp \rrbracket ! \overline{\rho})$$

and

$$\mathbf{m} \mid [\mathbf{T} \llbracket Exp \rrbracket \mid \overline{\rho}, \ [\dots [\mathbf{T} \llbracket Exp_1 \rrbracket \mid \overline{\rho}, \ \mathbf{T} \llbracket Exp_2 \rrbracket \mid \overline{\rho}], \ \dots, \ \mathbf{T} \llbracket Exp_n \rrbracket \mid \overline{\rho}]$$

respectively. Because m is a method, these expressions reduce to

$$(\mathbf{T} \llbracket Exp \rrbracket ! \overline{\rho})$$
 . m

and

$$(\mathbf{T} \llbracket Exp \rrbracket ! \overline{\rho}) \cdot \mathbf{m} (\mathbf{T} \llbracket Exp_1 \rrbracket ! \overline{\rho}, \mathbf{T} \llbracket Exp_2 \rrbracket ! \overline{\rho}, \dots, \mathbf{T} \llbracket Exp_n \rrbracket ! \overline{\rho})$$

respectively, the KOLA equivalents of the original method invocations.

#### **Translating Arithmetic Expressions:**

Every arithmetic operator (e.g., '+') has a corresponding KOLA primitive (e.g., **add**). The translation of any arithmetic subexpression,

$$Exp_0 ArithOp Exp_1,$$

is the KOLA function,

$$\overline{ArithOp} \circ \langle \mathbf{T} \ \llbracket Exp_0 \rrbracket, \ \mathbf{T} \ \llbracket Exp_1 \rrbracket \rangle$$

such that  $\overline{ArithOp}$  is the KOLA primitive corresponding to ArithOp.

## **Translating Query Expressions:**

For any OQL or Query Lite query, q:

$$\mathbf{T} \begin{bmatrix} \text{SELECT } E_s \\ \text{FROM } x_0 \text{ IN } E_0, \dots, x_n \text{ IN } E_n \\ \text{WHERE } E_w \end{bmatrix} = \\ \text{iterate } (\mathbf{T} \llbracket E'_w \rrbracket, \mathbf{T} \llbracket E'_s \rrbracket) \circ \\ \text{unnest } (\text{id}, \mathbf{T} \llbracket E'_n \rrbracket) \circ \dots \circ \text{ unnest } (\text{id}, \mathbf{T} \llbracket E'_0 \rrbracket) \circ \\ \text{single} \end{bmatrix}$$

such that each  $E'_i$  (for  $i \in \{0, ..., n, s, w\}$ ) is equivalent to  $E_i$  but for the replacement of all variable references with their deBruijn equivalents. The translation of a Query Lite query (for which n = 0) follows from the more general translation of OQL queries shown here.

That the translation of query expressions preserves semantics is demonstrated below. Suppose that q (above) is well-formed with regard to some environment,  $\rho$ . Then **T**  $\llbracket q \rrbracket$  !  $(\overline{\rho})$  reduces as follows:

- 1. Function single is invoked to create the singleton bag,  $\{\overline{\rho}\}\)$ .
- 2. Successive invocations of **unnest** (id,  $E'_0$ ), ..., **unnest** (id,  $\mathbf{T} \llbracket E'_n \rrbracket$ ) generate the collection,

$$\{ [\dots [[\overline{\rho}, e_0], e_1], \dots e_n] \mid e_0 \in (\mathbf{T} [[E'_0]] ! (\overline{\rho})), \\ e_1 \in (\mathbf{T} [[E'_1]]] ! ([\overline{\rho}, e_0])), \\ \dots, \\ e_m \in (\mathbf{T} [[E'_n]]] ! ([\dots [[\overline{\rho}, e_0], e_1], \dots, e_{n-1}])) \}.$$

The result above is a bag of KOLA pairs,

$$[\ldots [\overline{\rho}, e_0], e_1], \ldots e_n]$$

such that  $e_i$   $(0 \le i \le n)$  is an element of the collection denoted by  $E_i$  with regard to  $\rho$  supplemented with pairs,

$$((x_0, e_0), \ldots, (x_{i-1}, e_{i-1})).$$

Put another way, this result is an (n + 1)-way cartesian product of the collections denoted by  $E_0, \ldots, E_n$  with regard to the environments derived from  $\rho$ , and from elements of preceeding collections.

3. Query iterate ( $\mathbf{T} \llbracket E'_w \rrbracket$ ,  $\mathbf{T} \llbracket E'_s \rrbracket$ ) is invoked on the result of 2, thereby applying the expression in the original query's SELECT clause ( $\mathbf{T} \llbracket E'_s \rrbracket$ ) to every tuple produced in 2 that satisfies the query's WHERE clause ( $\mathbf{T} \llbracket E'_w \rrbracket$ ).

#### **Translating Boolean Expressions:**

The translation of Boolean expressions is straightforward, resembling the translation of non-Boolean expressions but with combination  $(\oplus)$  replacing composition  $(\circ)$ .

### 6.2.3 Sample Traces of Translation

In this section, we trace the application of the translation function on two queries: the Query Lite query of Figure 6.3 and the OQL query of Figure 6.2*b*. The result of translating the Query Lite query is shown in Figure 6.3b. The result of translating the OQL query and also that of Figure 6.2a are shown in Figure 6.6.

# Tracing the Translation of the Query Lite Query of Figure 6.3

The translation of the Query Lite query of Figure 6.3 first converts all variable references to deBruijn variables, producing the query,

```
SELECT V_0
FROM x IN Sens
WHERE V_0.terms > 5.
```

Translation then proceeds as follows:

**T** [SELECT  $V_0$  FROM x IN Sens WHERE  $V_0$ .terms > 5]

a: (set  $\circ$  iterate (eq  $\oplus \langle pty \circ \pi_2, K_f ("GOP") \rangle, \pi_2 \circ \pi_1) \circ$ unnest (id, mems  $\circ \pi_2$ )  $\circ$  unnest (id,  $K_f (Coms)$ )  $\circ$  single) ! NULL

$$b: \qquad \begin{array}{l} (\textbf{iterate } (\textbf{eq} \oplus \langle \texttt{topic} \circ \pi_2, \texttt{K}_f \ (\texttt{``NSF"}) \rangle, \ f) \\ \textbf{unnest } (\textbf{id}, \ \texttt{K}_f \ (\texttt{Coms})) \ \circ \ \textbf{single}) \ ! \ \texttt{NULL} \end{array}$$

such that  $f = (\text{iterate } (\text{gt} \oplus \langle \text{terms} \circ \pi_2, \text{K}_f (5) \rangle, \pi_2) \circ \text{unnest } (\text{id}, \text{mems} \circ \pi_2) \circ \text{single})$ 

Figure 6.6: Results of Translating the OQL queries of Figure 6.2

- = iterate (T  $[V_0.terms > 5]$ , T  $[V_0]$ )  $\circ$  unnest (id, T [Sens])  $\circ$  single
- = iterate (T [[ $V_0$ .terms > 5]],  $\pi_2$ )  $\circ$  unnest (id, K<sub>f</sub> (Sens))  $\circ$  single
- $= \text{ iterate } (\mathbf{gt} \oplus \langle \mathbf{T} \llbracket V_0.\texttt{terms} \rrbracket, \mathbf{T} \llbracket \texttt{5} \rrbracket \rangle, \pi_2) \circ \mathbf{unnest} (\mathbf{id}, \texttt{K}_f (\texttt{Sens})) \circ \mathbf{single}$
- $= \text{ iterate } (\mathbf{gt} \oplus \langle \texttt{terms} \circ \mathbf{T} \llbracket V_0 \rrbracket, \, \texttt{K}_f \ (\texttt{5}) \rangle, \, \pi_2) \ \circ \ \mathbf{unnest} \ (\mathbf{id}, \, \texttt{K}_f \ (\texttt{Sens})) \ \circ \ \mathbf{single}$
- $= \text{ iterate } (\textbf{gt} \oplus \langle \texttt{terms} \circ \pi_2, \texttt{K}_f (\texttt{5}) \rangle, \pi_2) \circ \textbf{unnest } (\textbf{id}, \texttt{K}_f (\texttt{Sens})) \circ \textbf{single}$

# Tracing the Translation of the OQL Query of Figure 6.2b

The translation of the OQL query of Figure 6.2b first converts all variable references to deBruijn variables, producing the query of Figure 6.5. Translation then proceeds as follows:

$$\mathbf{T} \begin{bmatrix} \operatorname{SELECT} & \left( \begin{array}{c} \operatorname{SELECT} V_{0} \\ \operatorname{FROM} y \text{ IN } V_{0}.\operatorname{mems} \\ \operatorname{WHERE} V_{0}.\operatorname{terms} > 5 \end{array} \right) \\ \operatorname{FROM} x \text{ IN Coms} \\ \operatorname{WHERE} V_{0}.\operatorname{topic} == "\operatorname{NSF}" \end{bmatrix} \end{bmatrix}$$
$$= \begin{array}{c} \operatorname{iterate} & \left( \mathbf{T} \left[ V_{0}.\operatorname{topic} == "\operatorname{NSF}" \right] \right) \\ \operatorname{unnest} & \left( \operatorname{id}, \mathbf{T} \left[ \operatorname{Coms} \right] \right) \\ \operatorname{unnest} & \left( \operatorname{id}, \mathbf{T} \left[ \operatorname{Coms} \right] \right) \\ \operatorname{s.t.} f = \mathbf{T} \begin{bmatrix} \operatorname{SELECT} V_{0} \\ \operatorname{FROM} y \text{ IN } V_{0}.\operatorname{mems} \\ \operatorname{WHERE} V_{0}.\operatorname{terms} > 5 \end{bmatrix} \end{bmatrix}$$

- $= \begin{array}{l} \text{iterate } (\mathbf{T} \llbracket V_0.\texttt{topic} == \texttt{``NSF"} \rrbracket, f) \circ \\ \text{unnest } (\text{id}, \mathbf{T} \llbracket \texttt{Coms} \rrbracket) \circ \text{single} \\ \\ s.t. \ f \ = \begin{array}{l} \text{iterate } (\mathbf{T} \llbracket V_0.\texttt{terms} \ > \ 5 \rrbracket, \mathbf{T} \llbracket V_0 \rrbracket) \circ \\ \text{unnest } (\text{id}, \mathbf{T} \llbracket V_0.\texttt{mems} \rrbracket) \ \circ \text{ single} \end{array}$
- $= \begin{array}{c} \text{iterate } (\mathbf{eq} \oplus \langle \mathbf{T} \llbracket V_0.\texttt{topic} \rrbracket, \mathbf{T} \llbracket \texttt{"NSF"} \rrbracket \rangle, f) \circ \\ \mathbf{unnest} \ (\mathbf{id}, \mathbf{T} \llbracket \texttt{Coms} \rrbracket) \circ \mathbf{single} \end{array}$

$$s.t. \ f = \begin{array}{c} \mathbf{iterate} \ (\mathbf{gt} \oplus \langle \mathbf{T} \ \llbracket V_0. \mathbf{terms} \rrbracket, \ \mathbf{T} \ \llbracket 5 \rrbracket \rangle, \ \mathbf{T} \ \llbracket V_0 \rrbracket) \circ \\ \mathbf{unnest} \ (\mathbf{id}, \ \mathbf{T} \ \llbracket V_0. \mathbf{mems} \rrbracket) \ \circ \ \mathbf{single} \end{array}$$

$$= \begin{array}{c} \textbf{iterate } (\textbf{eq} \oplus \langle \textbf{T} \llbracket V_0.\texttt{topic} \rrbracket, \texttt{K}_f \ (\texttt{``NSF''}) \rangle, \ f) \circ \\ \textbf{unnest } (\textbf{id}, \texttt{K}_f \ (\texttt{Coms})) \ \circ \ \textbf{single} \end{array}$$

$$s.t. \ f = \begin{array}{c} \mathbf{iterate} \ (\mathbf{gt} \oplus \langle \mathbf{T} \ \llbracket V_0.\mathtt{terms} \rrbracket, \ \mathtt{K}_f \ (5) \rangle, \ \mathbf{T} \ \llbracket V_0 \rrbracket) \circ \\ \mathbf{unnest} \ (\mathbf{id}, \ \mathbf{T} \ \llbracket V_0.\mathtt{mems} \rrbracket) \ \circ \ \mathbf{single} \end{array}$$

$$= \begin{array}{ccc} \mathbf{iterate} \ (\mathbf{eq} \oplus \langle \mathtt{topic} \circ \mathbf{T} \ \llbracket V_0 \rrbracket, \, \mathtt{K}_f \ (\texttt{``NSF"}) \rangle, \ f) \circ \\ \mathbf{unnest} \ (\mathbf{id}, \, \mathtt{K}_f \ (\mathtt{Coms})) \ \circ \ \mathbf{single} \end{array}$$

$$s.t. \ f = \frac{\text{iterate } (\mathbf{gt} \oplus \langle \texttt{terms} \circ \mathbf{T} [ [V_0] ], \texttt{K}_f (5) \rangle, \ \mathbf{T} [ [V_0] ]) \circ}{\text{unnest } (\mathbf{id}, \texttt{mems} \circ \mathbf{T} [ [V_0] ]) \circ \texttt{single}}$$

 $= \begin{array}{ccc} \mathbf{iterate} \ (\mathbf{eq} \oplus \langle \mathtt{topic} \circ \pi_2, \mathtt{K}_f \ (\texttt{``NSF"}) \rangle, \ f) \circ \\ \mathbf{unnest} \ (\mathbf{id}, \mathtt{K}_f \ (\mathtt{Coms})) \ \circ \ \mathbf{single} \end{array}$ 

s.t. 
$$f =$$
 iterate (gt  $\oplus \langle \text{terms} \circ \pi_2, \text{K}_f(5) \rangle, \pi_2) \circ$   
unnest (id, mems  $\circ \pi_2$ )  $\circ$  single

The bravehearted can now follow the reduction of this function when invoked on NULL, to confirm that translation has preserved query semantics.

(iterate (eq  $\oplus$  (topic  $\circ \pi_2$ , K<sub>f</sub> ("NSF")), f)  $\circ$ unnest (id, K<sub>f</sub> (Coms))  $\circ$  single) ! NULL

 $s.t. \ f = \begin{array}{c} \mathbf{iterate} \ (\mathbf{gt} \oplus \langle \mathbf{terms} \circ \pi_2, \, \mathbf{K}_f \ (5) \rangle, \ \pi_2) \circ \\ \mathbf{unnest} \ (\mathbf{id}, \ \mathbf{mems} \circ \pi_2) \ \circ \ \mathbf{single} \end{array}$ 

$$= \frac{\text{iterate } (\text{eq} \oplus \langle \text{topic} \circ \pi_2, \text{K}_f (\text{"NSF"}) \rangle, f) !}{(\text{unnest } (\text{id}, \text{K}_f (\text{Coms})) ! (\text{single ! NULL}))}$$

s.t. 
$$f = \frac{\text{iterate } (\text{gt} \oplus \langle \text{terms} \circ \pi_2, \text{K}_f(5) \rangle, \pi_2) \circ}{\text{unnest } (\text{id}, \text{mems} \circ \pi_2) \circ \text{single}}$$

$$= \frac{\text{iterate } (\mathbf{eq} \oplus \langle \texttt{topic} \circ \pi_2, \texttt{K}_f (\texttt{"NSF"}) \rangle, f) !}{(\mathbf{unnest } (\mathbf{id}, \texttt{K}_f (\texttt{Coms})) ! \{\texttt{NULL}\})}$$

s.t. 
$$f =$$
 **iterate** (**gt**  $\oplus \langle \text{terms} \circ \pi_2, \text{K}_f(5) \rangle, \pi_2) \circ$   
**unnest** (**id**, mems  $\circ \pi_2$ )  $\circ$  **single**

$$= \text{ iterate } (\mathbf{eq} \oplus \langle \texttt{topic} \circ \pi_2, \texttt{K}_f (\texttt{``NSF"}) \rangle, f) ! \{ ([\texttt{NULL}, c])^i | c^i \in \texttt{Coms} \}$$
  
s.t. 
$$f = \frac{\text{ iterate } (\mathbf{gt} \oplus \langle \texttt{terms} \circ \pi_2, \texttt{K}_f (5) \rangle, \pi_2) \circ$$
  
$$\mathbf{unnest } (\mathbf{id}, \texttt{mems} \circ \pi_2) \circ \mathbf{single}$$

$$= \{ (f ! [NULL, c])^i | c^i \in Coms, (eq \oplus \langle topic \circ \pi_2, K_f ("NSF") \rangle) ? [NULL, c] \}$$
  
s.t. 
$$f = \frac{iterate (gt \oplus \langle terms \circ \pi_2, K_f (5) \rangle, \pi_2) \circ}{unnest (id, mems \circ \pi_2) \circ single}$$

$$= \{ (f ! [NULL, c])^i | c^i \in Coms, eq ? [c.topic, "NSF"] \}$$
  
.s.t.  $f =$   
$$\begin{array}{l} \text{iterate } (\mathbf{gt} \oplus \langle \text{terms} \circ \pi_2, K_f(5) \rangle, \pi_2) \circ \\ \text{unnest } (\mathbf{id}, \text{mems} \circ \pi_2) \circ \text{single} \end{array}$$

The invocation of f on [NULL, c] then reduces as follows:

$$f : [NULL, c] = (\text{iterate } (\text{gt} \oplus \langle \text{terms} \circ \pi_2, \text{K}_f(5) \rangle, \pi_2) \circ \text{unnest } (\text{id, mems } \circ \pi_2) \circ \text{single}) ! [NULL, c]$$

$$= (\text{iterate } (\text{gt} \oplus \langle \text{terms} \circ \pi_2, \text{K}_f(5) \rangle, \pi_2) ! (\text{unnest } (\text{id, mems } \circ \pi_2) ! (\text{single } ! [NULL, c]))$$

$$= (\text{iterate } (\text{gt} \oplus \langle \text{terms} \circ \pi_2, \text{K}_f(5) \rangle, \pi_2) ! (\text{unnest } (\text{id, mems } \circ \pi_2) ! \{[\text{NULL, } c]\})$$

$$= (\text{iterate } (\text{gt} \oplus \langle \text{terms} \circ \pi_2, \text{K}_f(5) \rangle, \pi_2) ! ([(\text{INULL, } c], m])^j | m^j \in ((\text{mems } \circ \pi_2) ! [(\text{NULL, } c]))\}$$

$$= (\text{iterate } (\text{gt} \oplus \langle \text{terms} \circ \pi_2, \text{K}_f(5) \rangle, \pi_2) ! (([(\text{INULL, } c], m])^j | m^j \in c.\text{mems})\}$$

$$= ((\pi_2 ! [[(\text{NULL, } c], m])^j | m^j \in c.\text{mems}) = (m^j | m^j \in c.\text{mems}, m.\text{terms} > 5)$$

,

The result of this reduction then is

$$\{\{m^j \mid m^j \in c.\texttt{mems}, m.\texttt{terms} > 5\}\}^i \mid c^i \in \texttt{Coms}, c.\texttt{topic} == \texttt{``NSF"}\}$$

which is a nested bag of committee members for committees whose topic concerns the NSF (i.e., the result specified by the original OQL query).

#### 6.2.4**Translator Implementation**

The translator described above was implemented with the Ox compiler generator tool [8]. Ox is an attribute-grammar [3] based compiler tool in the spirit of Lex and Yacc [55]. Lex is a tool for generating lexical scanners and Yacc is a tool for generating parsers. Lex specifications designate a set of tokens (or terminal symbols) and associate regular expressions with each. The generated scanner maps text to tokens according to these specifications. Yacc specifications are context-free grammars consisting of non-terminals and tokens. The generated parser finds parse trees for strings according to the grammar specification, and can also invoke semantic actions based on the parse.

Ox generalizes the operation of Yacc in the same manner that attribute grammars generalize context-free grammars. Ox specifications are Lex and Yacc specifications that are augmented with definitions of attributes that are either *synthesized* (passed up the parse tree) or *inherited* (passed down the parse tree). Ox then uses these specifications to generate a program that constructs and decorates attributed parse trees. Ox facilitates the generation of compilers by making it possible to succinctly specify actions for those aspects of compiler generation for which Yacc falls short, such as type checking, code generation and so on.

To use Ox for the OQL/Query Lite  $\rightarrow$  KOLA translator, we used a grammar augmented with attributes denoting:

- functions and predicates: As described earlier, our translator returns a function or predicate as the result of translating every expression. The function or predicate for any given expression is constructed from the functions and predicates of its subexpressions, as the translation function **T** of Table 6.2 illustrates. Therefore, **func** and **pred** are synthesized attributes of all expression non-terminals.
- *incoming and outgoing scope lists*: Scope lists are propagated from subexpression to subexpression; one subexpression's outgoing scope list becomes the next visited subexpression's incoming scope list. Therefore, **insl** is an *inherited* attribute denoting the incoming scope list of all expressions, and **outsl** is a *synthesized* attribute denoting the outgoing scope list.

# 6.3 Query Rewriting

This section presents COKO transformations that rewrite KOLA translations of Query Lite queries into a form that can be translated into SQL. Section 6.3.1 presents a library of general purpose COKO transformations used by these transformations. Section 6.3.2 presents a specialized COKO transformation that normalizes KOLA queries resulting from translation into a more intuitive form.<sup>7</sup> Section 6.3.3 presents a specialized COKO transformation that rewrites the resulting normalized KOLA queries into equivalent KOLA queries that can be translated into SQL.

# 6.3.1 A Library of General-Purpose COKO Transformations

Many of the transformations defined for the Query Lite rewrites serve a more generalpurpose as *normalization* or *simplification* transformations. Whereas normalizations rewrite

<sup>&</sup>lt;sup>7</sup>These normalizations are strictly unnecessary, but make it easier to implement rewrites proposed in the literature in terms of the more intuitive expressions of queries.

```
TRANSFORMATION LBComp

USES

sft: f \circ (g \circ h) \longrightarrow (f \circ g) \circ h

BEGIN

BU {sft \rightarrow

{GIVEN f \circ \_F DO LBComp (f);

LBComp}

}

END
```

Figure 6.7: Transformation LBComp

expressions into structurally characterizable forms, simplifications make expressions "smaller" by removing redundancies or trivial subexpressions. In this section, we describe the library of general-purpose transformations defined for this task.

## Normalizations

**Left-Bushy Compositions** LBComp (shown in Figure 6.7) is a normalization transformation that gets fired on KOLA functions. If the function is of the form,

$$f_0 \circ f_1 \circ \ldots \circ f_n$$

(with compositions associated in any way), this transformation returns the equivalent function in "left-bushy" form:

$$(\ldots(f_0 \circ f_1) \circ \ldots \circ f_n).$$

The transformation of Figure 6.7 is similar to transformation LBComp from Figure 4.10 (Chapter 4). The firing algorithms and rewrite rules for these transformations are identical, but for the use LBComp's use of a composition former where LBConj has a conjunction former, and LBComp's use of function variables where LBConj has predicate variables.

**Left-Bushy Joins** Transformation LBJoin (Figure 6.8) gets applied to KOLA **join** queries that have subqueries that are also **joins**. The effect of this transformation is to rewrite a query with multiple applications of KOLA's **join** operator into left-bushy form. For example, the bushy join,

**join** 
$$(p, f)$$
 ! [**join**  $(q, g)$  ! [ $A_1, A_2$ ], **join**  $(r, h)$  ! [ $B_1, B_2$ ]]

gets transformed into the left-bushy join,

join (p', f') ! [join (K<sub>p</sub> (true), id) ! [join (K<sub>p</sub> (true), id) ! [A<sub>1</sub>, A<sub>2</sub>], B<sub>1</sub>], B<sub>2</sub>]

such that p' is derived from p, q and r, f' is derived from f, g and h, and **join** ( $K_p$  (**true**), **id**) is the KOLA equivalent of the Cartesian product operator.

LBJoin is defined in terms of auxiliary transformations LBJAux (shown in Figure 6.8), LBJAux2 (shown in Figure 6.9) and PullFP (also shown in Figure 6.9). Its firing algorithm does the following:

- 1. Step 1: The auxiliary transformation, PullFP, "pulls up" all data functions and predicates from join subqueries into the outermost join. The effect of this step is to return a new join query that has the same structure as the initial query, but with all but the outermost join replaced with Cartesian products.
- 2. Step 2: In this step, the large data predicate and data function now contained in the outermost join (i.e., p and f in join (p, f)) are simplified by calls to COKO transformations SimpPred and SimpFunc respectively. (These simplification transformations are presented in the next section.)
- 3. Step 3: This step performs all the necessary reassociations of joins to make the expression left-bushy. Transformation LBJAux (shown in Figure 6.8) invokes LBJAux2 in bottom-up fashion. LBJAux2 reassociates individual join by firing rule sft, which rewrites a right associated join to a left associated join by combining (composing) the data function (data predicate) instantiating the outermost join with shr (shift right).
- 4. Step 4: This step repeats the action of Step 2 to simplify the data function and data predicate in the outermost **join** operator.

#### Simplifications

**Function Simplification** Figure 6.10 shows the COKO transformation SimpFunc and its auxiliary transformations. These transformations simplify functions built from the KOLA primitives, id,  $\pi_1$ ,  $\pi_2$ , shr and shl, and the KOLA formers,  $\circ$ ,  $\langle \rangle$  and  $K_f$ . SimpFunc first normalizes functions so that all composition chains (i.e., functions of the form  $f_0 \circ \ldots \circ f_n$ ) contained as subfunctions are made left-bushy (via a call to LBComp). Next, auxiliary transformation SFAux is invoked. This transformation applies the simplifying identities of transformations BSAux1 and BSAux2 in a bottom-up fashion. If none of the rules in these latter transformations fires on a given subquery, rules sft and dis are successively fired to see if reassociation of compositions or distribution of compositions over function pairs ( $\langle \rangle$ )

```
TRANSFORMATION LBJoin
 -- Convert n-ary join to left-bushy join
 USES
  cu: iterate (K<sub>f</sub> (true), id) ! A \longrightarrow A,
  SimpPred,
  SimpFunc,
  PullFP,
  LBJAux
 BEGIN
  -- Step 1: Pull Up Data Predicates and Data Functions
  PullFP;
  -- Step 2: Simplify Top-Most Predicate and Data Function
  {GIVEN iterate (p, f) ! A DO {SimpPred (p); SimpFunc (f); cu}} ||
     {GIVEN join (p, f) ! _O DO {SimpPred (p); SimpFunc (f)}};
  -- Step 3: Reorder
  LBJAux;
  -- Step 4: Simplify
  {GIVEN iterate (p, f) ! A DO {SimpPred (p); SimpFunc (f); cu}} ||
     {GIVEN join (p, f) ! _O DO {SimpPred (p); SimpFunc (f)}}
 END
TRANSFORMATION LBJAux
 -- Helps to Convert n-ary join to left-bushy join
 USES
 LBJAux2
 BEGIN
  BU {GIVEN join (_P, _F) ! _O DO LBJAux2}
 END
```

Figure 6.8: Transformations LBJoin and LBJAux

```
TRANSFORMATION LBJAux2
  -- Helps to Convert n-ary join to left-bushy join
  USES
   pull1: join (p, f) ! [join (q, g) ! [A1, A2], B] \longrightarrow
                join ((q \oplus \pi_1) & (p \oplus \langleg \circ \pi_1, \pi_2 \rangle), f \circ \langleg \circ \pi_1, \pi_2 \rangle) !
                  [join (K_f (true), id) ! [A1, A2], B],
              join (p, f) ! [A, join (q, g) ! [B1, B2]] \longrightarrow
   pull2:
                join ((q \oplus \pi_2) & (p \oplus \langle \pi_1, g \circ \pi_2 \rangle), f \circ \langle \pi_1, g \circ \pi_2 \rangle) !
                  [A, join (K<sub>f</sub> (true), id) ! [B1, B2]],
   sft: join (p, f) ! [A, join (K<sub>f</sub> (true), id) ! [B1, B2]] \longrightarrow
               join (p \oplus shr, f \circ shr) ! [join (K<sub>f</sub> (true), id) ! [A, B1], B2],
   SimpFunc,
   SimpPred
  BEGIN
   pull1 ||
   {\text{pull}2 \rightarrow \text{sft} \rightarrow {\text{GIVEN join (p, f) ! [A, _0] D0 LBJAux2 (A)}}
  END
TRANSFORMATION PullFP
 -- Pull all data functions and data predicates into top-most
 -- iterate or join
 USES
  ru1:
           iterate (p, f) ! (iterate (q, g) ! A) \longrightarrow
              iterate (q & (p \oplus g), f \circ g) ! A,
           iterate (p, f) ! (join (q, g) ! [A, B]) \longrightarrow
  ru2:
              join (q & (p \oplus g), f \circ g) ! [A, B],
           join (p, f) ! [iterate (q, g) ! A, B] \longrightarrow
  ru3:
              join ((q \oplus \pi_1) & (p \oplus \langleg \circ \pi_1, \pi_2 \rangle), f \circ \langleg \circ \pi_1, \pi_2 \rangle) ! [A, B],
          join (p, f) ! [A, iterate (q, g) ! B] \longrightarrow
  ru4:
              join ((q \oplus \pi_2) & (p \oplus \langle \pi_1, g \circ \pi_2 \rangle), f \circ \langle \pi_1, g \circ \pi_2 \rangle) ! [A, B],
  ru5: join (p, f) ! [join (q, g) ! [A1, A2], B] \longrightarrow
              join ((q \oplus \pi_1) & (p \oplus \langleg \circ \pi_1, \pi_2 \rangle), f \circ \langleg \circ \pi_1, \pi_2 \rangle) !
                  [join (K_f (true), id) ! [A1, A2], B],
  ru6: join (p, f) ! [A, join (q, g) ! [B1, B2]] \longrightarrow
              join ((q \oplus \pi_2) & (p \oplus \langle \pi_1, g \circ \pi_2 \rangle), f \circ \langle \pi_1, g \circ \pi_2 \rangle) !
                  [A, join (K<sub>f</sub> (true), id) ! [B1, B2]]
 BEGIN
  BU {GIVEN _F ! _O DO {ru1 || ru2 || {{ru3 || ru5}; {ru4 || ru6}}}}
 END
    Figure 6.9: Transformations LBJAyx2 and PullFP Auxiliary Transformations
```

```
TRANSFORMATION SFAux
                                                                            USES
                                                                              SFAux1,
                                                                              SFAux2,
                                                                              sft: (f \circ g) \circ h \longrightarrow f \circ (g \circ h),
                                                                              dis: \langle f, g \rangle \circ h \longrightarrow \langle f \circ h, g \circ h \rangle,
TRANSFORMATION SimpFunc
  USES
                                                                              LBComp
                                                                            BEGIN
    SFAux,
   LBComp
                                                                              BU {SFAux1 ||
  BEGIN
                                                                                      SFAux2 ||
                                                                                      sft \rightarrow {SFAux; sft INV} \parallel
    TD LBComp;
                                                                                      dis \rightarrow {SFAux; dis INV} ||
    SFAux;
    TD LBComp
                                                                                       dis INV \rightarrow
  END
                                                                                        \{GIVEN f \circ _F DO
                                                                                               {SFAux (f);
                                                                                                 REPEAT {SFAux1 || SFAux2}}
                                                                                        }
                                                                                    }
                                                                            END
TRANSFORMATION BSAux1
                                                                          TRANSFORMATION BSAux2
  USES
                                                                            USES
    ru1: shl \circ shr \longrightarrow id,
                                                                              ru9:
                                                                                         \langle \pi_2, \pi_2 \rangle \longrightarrow \langle \mathbf{id}, \mathbf{id} \rangle \circ \pi_2,
    ru2: \operatorname{shr} \circ \operatorname{shl} \longrightarrow \operatorname{id},
                                                                              ru10: \langle K_f(\mathbf{x}), K_f(\mathbf{y}) \rangle \longrightarrow K_f([\mathbf{x}, \mathbf{y}]),
    ru3: \pi_1 \circ \mathbf{shr} \longrightarrow \pi_1 \circ \pi_1,
                                                                             rull: K_f(\mathbf{x}) \circ \mathbf{f} \longrightarrow K_f(\mathbf{x}),
    ru4: \pi_2 \circ \mathbf{shl} \longrightarrow \pi_2 \circ \pi_2,
                                                                             ru12: \pi_1 \circ \langle f, g \rangle \longrightarrow f,
    ru5: f \circ id \longrightarrow f,
                                                                                            \pi_2 \circ \langle \mathbf{f}, \mathbf{g} \rangle \longrightarrow \mathbf{g},
                                                                              ru13:
    ru6: id \circ f \longrightarrow f,
                                                                                            \langle K_f(\mathbf{x}), \mathbf{f} \rangle \longrightarrow \langle K_f(\mathbf{x}), \mathbf{id} \rangle \circ \mathbf{f},
                                                                              ru14:
    ru7: \langle \pi_1, \pi_2 \rangle \longrightarrow \mathbf{id},
                                                                                            \langle \mathbf{f}, \mathbf{K}_f (\mathbf{x}) \rangle \longrightarrow \langle \mathbf{id}, \mathbf{K}_f (\mathbf{x}) \rangle \circ \mathbf{f},
                                                                              ru15:
    ru8: \langle \pi_1, \pi_1 \rangle \longrightarrow \langle \mathbf{id}, \mathbf{id} \rangle \circ \pi_1,
                                                                              LBComp
    ru9: \pi_1 \circ \mathbf{shl} \longrightarrow \langle \pi_1, \pi_1 \circ \pi_2 \rangle,
                                                                            BEGIN
    ru10: \pi_2 \circ \mathbf{shr} \longrightarrow \langle \pi_2 \circ \pi_1, \pi_2 \rangle
                                                                              ru9 || ru10 || ru11 || ru12 || ru13 ||
                                                                              GIVEN \langle K_f(\mathbf{x}), \mathbf{id} \rangle DO SKIP ||
  BEGIN
                                                                              GIVEN \langle \mathbf{id}, K_f(\mathbf{x}) \rangle DO SKIP ||
    ru1 || ru2 || ru3 || ru4 || ru5 ||
    ru6 || ru7 || ru8 || ru9 || ru10
                                                                              {ru14 || ru15} \rightarrow BU {LBComp}
  END
                                                                            END
```

Figure 6.10: Transformation SimpFunc and Its Auxiliary Transformations

makes it possible for these rules to be fired. The second attempt to fire the rules of BSAux1 and BSAux2 is triggered by a recursive firing of transformation SFAux.

**Predicate Simplification** Transformation SimpPred of Figure 6.11 simplifies predicates in a manner similar to how SimpFunc simplifies functions. Predicates simplified are those

formed from predicate formers, &,  $|, \sim, \oplus$  and K<sub>p</sub>. SimpPred visits a predicate's subpredicates and subfunctions in bottom-up fashion (as achieved via recursive calls at the beginning of the firing algorithm.) Then, auxiliary transformation SimpDisj is called on disjunct subpredicates  $(p \mid q)$ , SimpConj is called on conjunct subpredicates (p & q), SimpNeg is called on negation subpredicates  $(\sim (p))$ , and SimpOpls is called on combination subpredicates  $(p \oplus f)$  (after a call of REPEAT sft first moves as much of the function out of the predicate p as possible). Each of these specialized transformations attempts to fire rules to simplify predicates that are specific to the kind of predicate for which they are named. As with SimpFunc, failure to fire any of the rules in the specialized auxiliary transformations makes SimpPred attempt to reassociate predicate combinations.

**Common Path Expression Elimination** Transformation PullComFunc is shown in Figure 6.13 along with its auxiliary transformation, PCFAux. PullComFunc rewrites predicates of the form,

$$(p_1 \oplus f_1)$$
 & ... &  $(p_n \oplus f_n)$ 

by grouping common functions,  $f_i$  leaving a predicate of the form,

$$(p_1'\oplus f_1)$$
 & ... &  $(p_m'\oplus f_m)$ 

such that  $m \leq n$  and no two functions,  $f_i$  and  $f_j$   $(i \neq j)$  are the same. Step 1 of the firing algorithm for PullComFunc first normalizes input conjunction predicates into left-bushy form (via a call to LBConj). Then in Step 2, auxiliary transformation PCFAux is called on every conjunction subpredicate in bottom-up fashion.

To illustrate the effects of PCFAux, Figure 6.12 shows the parse tree for the *i*th conjunction subpredicate visited. The call of PCFAux on this subtree is intended to merge subpredicate  $p_{i+1}$  with a subpredicate below it,  $p_j$  provided that  $f_{i+1} = f_j$ . Merging is accomplished by comparing  $f_{i+1}$  with each of the functions  $f_i$ ,  $f_{i-1}$ , ... in turn, until one or none is found that is the same as  $f_{i+1}$ . (Note that the invariant for this algorithm establishes that because PCFAux is called in bottom-up fashion on successive subtrees, that each of the functions  $f_1, \ldots, f_i$  is distinct). PCFAux handles each of the possible cases for function comparisons as described below:

• Case 1:  $i = 1, f_2 = f_1$ 

This case is handled by the successful firing of rule fac1 leaving

$$(p_i \& p_{i+1}) \oplus f_i$$

```
TRANSFORMATION SimpPred
              USES
                 sft: (p \oplus f) \oplus g \longrightarrow p \oplus (f \circ g),
                SimpFunc,
                SimpConj,
                SimpDisj,
                SimpOpls,
                SimpNeg
              BEGIN
               GIVEN p & q DO {SimpPred (p); SimpPred (q); SimpConj} ||
               GIVEN p | q DO {SimpPred (p); SimpPred (q); SimpDisj} ||
               GIVEN \sim (p) DO {SimpPred (p); SimpNeg} ||
               {REPEAT sft;
                GIVEN p \oplus f DO {SimpPred (p); SimpFunc (f); SimpOpls}
                REPEAT {sft INV}}
              END
TRANSFORMATION SimpDisj
                                                    TRANSFORMATION SimpConj
  USES
                                                       USES
         p \mid K_p \text{ (true)} \longrightarrow K_p \text{ (true)},
                                                        c1: p \& K_p (true) \longrightarrow p,
    d1:
    d2: K_p (true) | p \longrightarrow K_p (true),
                                                        c2: K_p (true) & p \longrightarrow p,
    d3: p \mid K_p \text{ (false)} \longrightarrow p,
                                                        c3: p \& K_p \text{ (false)} \longrightarrow K_p \text{ (false)},
    d4: K_p (false) | p \longrightarrow p,
                                                        c4: K_p (false) & p \longrightarrow K_p (false),
    d5: p | p \longrightarrow p,
                                                        c5: p \& p \longrightarrow p,
    d6: p \mid \sim (p) \longrightarrow K_p (true),
                                                        c6: p \& \sim (p) \longrightarrow K_p (false),
    d7: \sim (p) | p \longrightarrow K<sub>p</sub> (true)
                                                        c7: \sim (p) & p \longrightarrow K<sub>p</sub> (false)
  BEGIN
                                                       BEGIN
                                                        c1 || c2 || c3 || c4 ||
    d1 || d2 || d3 || d4 ||
    d5 || d6 || d7
                                                        c5 || c6 || c7
                                                       END
  END
  TRANSFORMATION SimpOpls
                                                   TRANSFORMATION SimpNeg
     USES
                                                      USES
      opls1: p \oplus id \longrightarrow p,
                                                       neg1: \sim (K_p \text{ (false)}) \longrightarrow K_p \text{ (true)},
      opls2: K_p (b) \oplus f \longrightarrow K_p (b)
                                                       neg2: ~ (K_p (true)) \longrightarrow K_p (false)
     BEGIN
                                                      BEGIN
      opls1 || opls2
                                                       neg1 || neg2
     END
                                                      END
```

Figure 6.11: Transformation SimpPred and Its Auxiliary Transformations



Figure 6.12: An Input KOLA Parse Tree to  $\tt PCFAux$ 

• Case 2:  $i > 1, f_{i+1} = f_i$ 

This case is handled by the successful firing of rule fac2, which will rewrite the current predicate into the form,

$$\overline{p} \& ((p_i \& p_{i+1}) \oplus f_i)$$

such that  $\overline{p}$  is

$$(p_1 \oplus f_1)$$
 & ... &  $(p_{i-1} \oplus f_{i-1})$ .

• Case 3:  $i = 1, f_2 \neq f_1$ 

In this case, none of the rules successfully fires and the predicate is not rewritten.

• Case 4:  $i > 1, f_{i+1} \neq f_i$ 

In this case,  $f_{i+1}$  must be compared to the functions "below"  $f_i$ :  $f_{i-1}, \ldots, f_1$ . These comparisons are accomplished by firing rule **swtch** which switches the order of subpredicates,  $(p_{i+1} \oplus f_{i+1})$  and  $(p_i \oplus f_i)$ , and then calling **PCFAux** recursively on the left bushy conjunct subpredicate that now has  $(p_{i+1} \oplus f_{i+1})$  as its right-most branch.

# Analysis

Table 6.3 summarizes the contents of the COKO transformations presented in this Section. The table has 5 columns:

- the *name* of the transformation,
- the *figure* in which the transformation appears,
- the number of KOLA rewrite rules fired by the transformation,
- the number of the above rules that have been verified thus far with LP, and
- the *number of lines* of (firing algorithm) code that the transformation contains.

Admittedly, the number of lines of code is largely dependent on programming style; what may be a single line of code for some, may be broken up into many lines of code for others. The style used for the transformations in this chapter attempts to achieve readability and clear presentation. For that reason, our line count is likely generous. Further, we count all lines in a firing algorithm including white space, comments, and even the lines with the reserved words BEGIN and END.

The library then, is quite small (roughly 100 lines of code) and dominated by rules (over 50) in all. All of the rewrite rules used for the transformations in the library have been verified with the theorem prover, LP [46].

TRANSFORMATION PullComFunc

```
-- given a conjunctive predicate, rewrites it to the form
-- ((p11 & ... & p1n) OPLUS f1) & ... ((pm1 & ... & pmn) OPLUS fm)
-- by factoring common functions from separate conjuncts
USES
 sft: p \oplus (f \circ g) \longrightarrow p \oplus f \oplus g,
 PCFAux,
 LBConj
BEGIN
 -- Step 1: Next make Conjunct Left Bushy
 LBConj;
 -- Step 2: Then Pull Up Common Subfunctions
 BU {GIVEN _P & _P DO PCFAux}
END
   TRANSFORMATION PCFAux
    -- Helper transformation for PullComFunc, rewriting
    -- conjunctive predicates to the form
    -- ((p11 & ... & p1n) \oplus f1) & ... ((pm1 & ... & pmn) \oplus fm)
    -- by factoring common functions from separate conjuncts
    USES
     fac1: (p \oplus f) \& (q \oplus f) \longrightarrow (p \& q) \oplus f,
     fac2: (p \& (q \oplus f)) \& (r \oplus f) \longrightarrow p \& ((q \& r) \oplus f),
     swtch: (p & q) & r \longrightarrow (p & r) & q
    BEGIN
      -- Either merge the two leaf conjuncts or switch them
     -- and try with the next two
     {\tt fac1} 
ightarrow {\tt GIVEN} \ {\tt p} \oplus \_{\tt F} \ {\tt DO} \ {\tt PCFAux} \ ({\tt p}) \ ||
       fac2 \rightarrow GIVEN _P & (p \oplus _F) DO PCFAux (p) ||
       swtch \rightarrow GIVEN p & _P DO PCFAux (p)
     }
    END
```

Figure 6.13: Transformation PullComFunc and Its Auxiliary Transformation

Transformation	Figure	No. Rules	No. Verified	No. Lines in
			Rules	Firing Algorithm
LBComp	6.7	1	1	6
LBJoin	6.8	1	1	15
LBJAux	6.8	0	0	3
LBJAux2	6.9	3	3	4
PullFP	6.9	6	6	3
SimpFunc	6.10	0	0	5
SFAux	6.10	2	2	11
BSAux1	6.10	10	10	4
BSAux2	6.10	7	7	6
SimpPred	6.11	1	1	9
SimpDisj	6.11	7	7	4
SimpConj	6.11	7	7	4
SimpOpls	6.11	2	2	3
SimpNeg	6.11	2	2	3
PullComFunc	6.13	1	1	7
PCFAux	6.13	3	3	8
Total	—	53	53	95

Table 6.3: Analysis of the General-Purpose COKO Transformations

# 6.3.2 Normalizing the Results of Translation

Translation of Query Lite and OQL queries, q generate KOLA functions,  $\mathbf{T}\;[\![q]\!],$  of the form,

iterate  $(p, f) \circ$  unnest  $(id, f_n) \circ \ldots \circ$  unnest  $(id, f_0) \circ$  single.

This function gets applied to KOLA representations of environments for which the original query is well-formed. For example, if q is well-formed with regard to  $\rho$ , then  $\mathbf{T} \llbracket q \rrbracket ! \overline{\rho}$  reduces to:

$$\{ f \ ! \ [\dots [\overline{\rho}, e_0], \dots e_n] \ | \\ e_0 \in (f_0 \ ! \ (\overline{\rho})), \\ e_1 \in (f_1 \ ! \ ([\overline{\rho}, e_0])), \\ \dots, \\ e_n \in (f_n \ ! \ ([\dots [\overline{\rho}, e_0], \dots e_{n-1}])), \\ p \ ? \ [\dots [\overline{\rho}, e_0], \dots, e_n] \}.$$

set ! (iterate (eq  $\oplus \langle id, \text{"GOP"} \rangle \oplus pty \oplus \pi_2, \pi_1$ ) ! (unnest (id, mems) ! Coms))

Figure 6.14: The KOLA Query of Figure 6.6a After Normalization

When  $\rho = ()$  ( $\overline{\rho} =$ NULL), this expression is:

```
\begin{split} \{f \ ! \ [\dots [\text{NULL}, \ e_0], \ \dots e_n] \ | \\ e_0 \in (f_0 \ ! \ (\text{NULL})), \\ e_1 \in (f_1 \ ! \ ([\text{NULL}, \ e_0])), \\ \dots, \\ e_n \in (f_n \ ! \ ([\text{L} \dots [\text{NULL}, \ e_0], \ \dots e_{n-1}])), \\ p \ ? \ [\dots [\text{NULL}, \ e_0], \ \dots, e_n] \}. \end{split}
```

The purpose of the COKO transformation presented in this section is to rewrite the translations that are invoked on NULL into a more intuitive form. More formally, this transformation rewrites KOLA expressions of the form,

```
(iterate (p, f) \circ
unnest (id, f_n) \circ \ldots \circ unnest (id, f_1) \circ single) ! NULL
```

into the equivalent KOLA expression,

```
iterate (p', f') !
(unnest (id, f'_m) ! (... ! (unnest (id, f'_1) ! A)...))
```

such that:

- $0 \le m < n$  (i.e., at least one and as many as all **unnest** functions are removed), and
- A is either the name of a collection, or a query expression that invokes **iterate** or **join** on one or more named collections.

For example, this normalization converts the Query Lite translation of Figure 6.3b into the KOLA expression of Figure 6.3c. The latter expression is much simpler, and unlike the former expression, performs no operations with NULL. This normalization also converts the KOLA expression of Figure 6.6a to the more intuitive expressions shown in Figure 6.14a. The normalized queries differ from the unnormalized queries in that they invoke functions on collections that figure into the result (i.e., Coms in Figure 6.14a) rather than invoking functions on NULL.

```
TRANSFORMATION NormTrans
 -- get rid of NULL appearing in translated query
 USES
  nonull: K_f (x) ! y \longrightarrow x,
  comp: (f \circ g) ! x \longrightarrow f ! (g ! x),
  un2j: unnest (f, K_f (B)) ! A \longrightarrow join (K_f (true), f) ! [A, B],
  collij: iterate (p, f) ! (join (q, g) ! [A, B]) \longrightarrow
              join (q & (p \oplus g), f \circ g) ! [A, B],
  colljj: join (p, f) ! [join (q, g) ! [A1, A2], B]) \longrightarrow
              join ((q \oplus \pi_1) & (p \oplus \langle g \oplus \pi_1, \pi_2 \rangle), f \circ \langle g \circ \pi_1, \pi_2 \rangle)!
                 [join (K_p (true), id) ! [A1, A2], B],
  FactorK, SimpFunc, SimpPred, OrdUnnests, LBComp
 BEGIN
  -- Step 1: First get rid of NULL's
     GIVEN f ! _O DO {FactorK (f); nonull}
  -- Step 2: Next, normalize to ensure result is of form
  -- (f1 ! (f2 ! ...(fn ! x)...))
     GIVEN f ! _O DO LBComp (f);
     REPEAT comp;
  -- Step 3: Reorder Unnests so Joins on Constant
  -- Expressions are Evaluated 1st
      OrdUnnests;
  -- Step 4: Convert unnests over constant collections to joins
     BU \{un2j\};
  -- Step 5: Collapse composed iterates and joins
     BU {{collij || colljj} \rightarrow
           GIVEN join (p, f) ! _O DO {SimpPred (p); SimpFunc (f)}}
 END
```

Figure 6.15: Transformation NormTrans

```
TRANSFORMATION OrdUnnests
USES
comm: unnest (f, K<sub>f</sub> (B)) ! (unnest (g, h) ! A) \longrightarrow
    unnest (f \circ \langle \langle \pi_1 \circ \pi_1, \pi_2 \rangle, \pi_2 \circ \pi_1 \rangle, h \circ \pi_1 \rangle !
    (unnest (id, K<sub>f</sub> (B)) ! A,
SimpFunc
BEGIN
BU {GIVEN _F \circ unnest (_F, K<sub>f</sub> (_O)) DO SKIP ||
    comm \rightarrow {GIVEN unnest (f, g) ! _O DO {SimpFunc (f); SimpFunc (g)};
    GIVEN _F ! x DO OrdUnnests (x)
    }
}
END
```

Figure 6.16: Transformation OrdUnnests

# Transformation NormTrans

Transformation NormTrans (Figure 6.15) is the "main" COKO transformation that removes NULL from the result of translation. If the original query has more than one collection expression in its FROM clause, this transformation also reorders the FROM clause expressions so that all named collections appear before all path expressions. For example, the OQL query,

```
SELECT x
FROM x IN Coms, y IN x.mems, z IN Sens
```

gets rewritten to

SELECT xFROM x IN Coms, z IN Sens, y IN x.mems

so that the path expression *x.mems* appears after the named collection Sens. (In terms of KOLA, the resulting expression will have all **unnest** functions appearing before all **join** functions.)

The firing algorithm for NormTrans has 5 steps, described below in terms of their effects on the translation of the OQL join query of Figure 6.17a shown in Figure 6.17b:  $q_0 =$ 

(iterate (eq  $\oplus \langle pty \circ chair \circ \pi_2 \circ \pi_1, pty \circ chair \circ \pi_2 \rangle, \pi_2 \circ \pi_1) \circ$ unnest (id, K<sub>f</sub> (SComs))  $\circ$  unnest (id, K<sub>f</sub> (Coms))  $\circ$  single) ! NULL.

**Step 1:** In the first step, transformation FactorK and rule nonull combine to remove NULL from the query produced by translation. In general, when called on a KOLA expression of

```
SELECT x

FROM x IN Coms, y IN SComs

WHERE x.chair.pty == y.chair.pty

(a)

(iterate (eq \oplus \langle pty \circ chair \circ \pi_2 \circ \pi_1, pty \circ chair \circ \pi_2 \rangle, \pi_2 \circ \pi_1) \circ

unnest (id, K<sub>f</sub> (SComs)) \circ unnest (id, K<sub>f</sub> (Coms)) \circ single) ! NULL

(b)
```

Figure 6.17: An OQL Join Query (a) and Its Translation into KOLA (b)

the form,

```
(iterate (p, f) \circ
unnest (id, f_n) \circ \ldots \circ unnest (id, f_0) \circ single) ! NULL,
```

FactorK returns an expression,  $K_f(A)$  ! NULL such that A is of the form,

(iterate  $(p', f') \circ$ unnest (id,  $f_n$ )  $\circ \ldots \circ$  unnest (id,  $f_0$ )) ! B

and B is either a named collection or an expression iterate (p, f) ! B', such that B' is a named collection. Put simply, FactorK rewrites the KOLA expression produced by translation into an invocation of a constant function on NULL:  $K_f(A) !$  NULL. Rule nonull then rewrites this expression to A. To illustrate, FactorK transforms the query  $q_0$  above to  $q_1 = K_f(A) !$  NULL such that A is:

(iterate (eq  $\oplus \langle pty \circ chair \circ \pi_1, pty \circ chair \circ \pi_2 \rangle, \pi_1) \circ$ unnest (id, K<sub>f</sub> (SComs))) ! Coms

Nonull then rewrites this expression to A. The firing algorithm for FactorK is described later in this chapter.

Step 2: Steps 2 and 3 prepare the query expression resulting from Step 1 for application of rule un2j which rewrites unnest functions to joins. Step 2 first removes compositions from the query A resulting from step 1, replacing them with function invocations. Replacing compositions with invocations is accomplished by making the query function left-bushy by calling LBComp, and then repeatly firing rule comp. In general, this step returns a KOLA query of the form

```
iterate (p', f') !
(unnest (id, f_n) ! (... ! (unnest (id, f_0) ! B)...)).
```

To illustrate this step, its effect on query  $q_1$  resulting from Step 1 is  $q_2$ :

```
iterate (eq \oplus \langle pty \circ chair \circ \pi_1, pty \circ chair \circ \pi_2 \rangle, \pi_1) !
(unnest (id, K<sub>f</sub> (SComs)) ! Coms).
```

**Step 3:** Step 3 reorders the **unnest** functions appearing in the result of Step 2, so that those instantiated with constant functions,

**unnest** (id, 
$$K_f$$
 (A))

are pushed past those that are not. This reordering is accomplished by transformation **OrdUnnests** (Figure 6.16) which traverses a KOLA expression in bottom-up fashion. If during this traversal, two **unnest** functions appear in the wrong order, they are commuted (by firing rule comm) and the **unnest** function with the constant function is then pushed further down with a recursive call to the transformation (much like a bubble sort). In general, this step rewrites queries produced by Step 2 into the form,

iterate (p', f') ! (unnest (id,  $g_m$ ) ! (... (unnest (id,  $g_0$ ) ! (unnest (id,  $K_f (A_k)$ ) ! (... (unnest (id,  $K_f (A_0)$ ) ! B)...)))...))

such that no function  $g_i$  is a constant function. This step has no effect on query  $q_2$  above, which already satisfies the invariant.

Step 4: Step 4 converts all unnest functions that are instantiated with constant functions into joins. Note that for any collections A and B,

unnest (id, K<sub>f</sub> (B)) ! A = {(id ! [a, b])<sup>ij</sup> | 
$$a^i \in A, b^j \in (K_f (B) ! a)$$
}  
= {([a, b])<sup>ij</sup> |  $a^i \in A, b^j \in B$ }  
= join (K<sub>n</sub> (true), id) ! [A, B].

This identity (expressed by rule un2j) gets fired in bottom-up fashion to rewrite queries of the form,

```
iterate (p', f') !

(unnest (id, g_m) ! (... (unnest (id, g_0) !

(unnest (id, K_f (A_k)) ! (... (unnest (id, K_f (A_0)) ! B)...)))...))
```

 $\operatorname{to}$ 

```
iterate (p', f') !

(unnest (id, g_m) ! (... (unnest (id, g_1) !

(join (K<sub>p</sub> (true), id) ! [...join (K<sub>p</sub> (true), id) ! [B, A<sub>1</sub>],...,A<sub>k</sub>]))...)),
```

if k > 0, and

```
iterate (p', f') !
(unnest (id, g_m) ! (... (unnest (id, g_1) ! A_1)...))
```

(such that  $A_1$  is not a **join**) if k = 0. Applied to query  $q_2$ , this step leaves  $q_4$ :

iterate (eq  $\oplus \langle pty \circ chair \circ \pi_1, pty \circ chair \circ \pi_2 \rangle, \pi_1$ ) ! (join (K<sub>p</sub> (true), id) ! [Coms, SComs]).

Step 5: In the final step, rules collii and collij are fired in bottom-up fashion to "collapse" successive joins and iterates. If there are no unnest functions resulting from Step 4 (i.e., if there are no path expressions in the FROM clause of the original OQL or Query Lite query), this step will result in a query of the form,

**join** 
$$(p', f')$$
 !  
[...**join** (K<sub>p</sub> (true), **id**) ! [B, A<sub>1</sub>],...,A<sub>k</sub>].

Applied to  $q_4$ , this step results in the query,

```
join (eq \oplus \langle pty \circ chair \circ \pi_1, pty \circ chair \circ \pi_2 \rangle, \pi_1) ! [Coms, SComs].
```

# Transformation FactorK

Transformation FactorK is called to rewrite query functions resulting from translation into the form

 $K_f(A)$ 

for some collection A. The listing of the transformation's firing algorithm is not shown but is described instead below.

An OQL or Query Lite query q that is well-formed with regard to the empty environment gets translated into a KOLA expression of the form,  $\mathbf{T} [\![q]\!]$ ! NULL, such that  $\mathbf{T} [\![q]\!]$  is:

```
(iterate (p, f) \circ
unnest (id, f_n) \circ \ldots \circ unnest (id, f_0) \circ single).
```

The reduction of  $\mathbf{T} \llbracket q \rrbracket$  ! NULL leaves:

```
\begin{split} \{f \ ! \ [\dots [\text{NULL}, \ e_0], \ \dots e_n] \ | \\ e_0 \in (f_0 \ ! \ (\text{NULL})), \\ e_1 \in (f_1 \ ! \ ([\text{NULL}, \ e_0])), \\ \dots, \\ e_n \in (f_n \ ! \ ([\dots [\text{NULL}, \ e_0], \ \dots e_{n-1}])), \\ p \ ? \ [\dots [\text{NULL}, \ e_0], \ \dots, e_n] \}. \end{split}
```

(1) 
$$f \stackrel{\Rightarrow}{=} (f \circ \mathbf{shl}) \circ \mathbf{shr}$$
  
(2)  $f \circ \pi_2 \circ \mathbf{shl} \stackrel{\Rightarrow}{=} f \circ \pi_2 \circ \pi_2$   
(3)  $f \circ \pi_1 \circ \pi_1 \circ \mathbf{shl} \stackrel{\Rightarrow}{=} f \circ \pi_1$   
(4)  $f \circ \pi_2 \circ \pi_1 \circ \mathbf{shl} \stackrel{\Rightarrow}{=} f \circ \pi_1 \circ \pi_2$ 

#### Figure 6.18: Rewrite Rules in PullP2SHRF

Because  $\mathbf{T}$  [[q]] is a constant function, functions  $f_0, \ldots, f_n$ , do not depend on NULL. Rather,

- $f_0$  can be rewritten to a constant function that returns a collection (i.e.,  $K_f(A_0)$  for some collection  $A_0$ ),
- $f_1$  can be rewritten to a function on  $e_0$  (i.e.,  $f'_1 \circ \pi_2$  for some collection  $f'_1$ ),
- $f_2$  can be rewritten to a function on  $e_0$  and  $e_1$  (i.e.,  $f'_2 \circ \pi_2 \circ \mathbf{shr}$  for some collection  $f'_2$ )),
- ...
- $f_n$  can be rewritten to a function on  $e_0, e_1, \ldots e_n$  (i.e.,

$$f'_n \circ \pi_2 \circ \underbrace{\operatorname{shr} \circ \ldots \circ \operatorname{shr}}_{n-1}$$

for some function  $f'_n$ ).

Similarly, function f can be rewritten to a function on  $e_0, e_1, \ldots, e_n$  (i.e., (i.e.,

$$f' \circ \pi_2 \circ \underbrace{\operatorname{shr} \circ \ldots \circ \operatorname{shr}}_n$$

for some function f') and predicate p can be rewritten to a predicate on  $e_0, e_1, \ldots, e_n$  (i.e.,

$$p' \oplus (\pi_2 \circ \underline{\operatorname{shr}} \circ \dots \circ \underline{\operatorname{shr}})$$

for some predicate p').

The first step performed by transformation FactorK is to normalize all data functions  $f_0, f_1, \ldots, f_n$  and f and the data predicate p in the manner just described. This step uses the rewrite rules listed in Figure 6.18. For each **unnest** function, **unnest** (id,  $f_i$ ), these rules are fired i - 1 times on  $f_i$ . (They are fired n times on f and p of iterate (p, f).) First, rule (1) is fired on  $f_i$  leaving

$$f_i \circ \mathbf{shl} \circ \mathbf{shr}$$

(iterate  $(\overline{p}, \overline{f}) \circ$ unnest (id,  $\overline{f_n}$ )  $\circ$  unnest (id,  $\overline{f_{n-1}}$ )  $\circ \ldots \circ$  unnest (id,  $\overline{f_1}$ )  $\circ$  unnest (id,  $\overline{f_0}$ )  $\circ$ single) ! NULL such that  $\overline{p} = p' \oplus (\pi_2 \circ \operatorname{shr}^n)$   $\overline{f} = f' \circ \pi_2 \circ \operatorname{shr}^n$   $\overline{f_i} = f'_i \circ \pi_2 \circ \operatorname{shr}^{i-1}$  (for i > 0), and  $\overline{f_0} = K_f (A)$ 

Figure 6.19: Translated OQL Queries Following Rewriting of their Data Functions

Then, rules (2) and (3) and (4) are successively fired on

$$f_i \circ \mathbf{shl}.$$

After i - 1 applications of these rules, we are left with a function of the form

$$f_i'' \circ g \circ \underbrace{\operatorname{shr} \circ \ldots \circ \operatorname{shr}}_{i-1}.$$

Note that  $f_i$  is a function that gets invoked on arguments of the form,

[...[NULL, 
$$e_0$$
], ... $e_{i-1}$ ].

The invocation of

$$f_i^{''} \circ g \circ \underbrace{\operatorname{shr} \circ \ldots \circ \operatorname{shr}}_{i-1}.$$

on this argument reduces to

$$f_i''$$
 !  $(g ! [NULL, [e_0, \dots [e_{i-2}, e_{i-1}] \dots]]).$ 

As  $f_i$  ignores NULL, g must be  $\pi_2$ . Therefore, the effect of this step is to leave a query expression of the form shown in Figure 6.19.

The rest of this transformation proceeds in five steps and uses the rules of Figure 6.20. In this figure and in the text, we use the notation " $\delta_i$ " to denote a KOLA function defined for  $i \ge 0$  as follows:

$$\begin{aligned} \delta_0 &= \mathbf{shr} \\ \delta_i &= \langle \pi_1, \, \delta_{i-1} \circ \pi_2 \rangle, & \text{for } i > 0 \end{aligned}$$

Substituting for  $\delta$  in rules (10) and (11) of Figure 6.20 reveals these rules to be strictly unnecessary: rule (11) follows from rule (7), and rule (12) follows from rule (9) (fired n

- (1)iterate  $(p \oplus (f \circ h), g \circ h) \circ unnest (h1, h2) \equiv$ iterate  $(p \oplus f, g) \circ unnest (h \circ h1, h2)$
- (2)unnest  $(f \circ shr \circ shr, g \circ shr) \circ unnest (h1, h2) \stackrel{\rightarrow}{=}$ unnest  $(f \circ \delta_1 \circ shr, g) \circ unnest (shr \circ h1, h2)$
- **unnest** (f  $\circ \pi_2 \circ \mathbf{shr}, \mathbf{g} \circ \pi_2$ )  $\circ \mathbf{unnest}$  (h1, h2)  $\stackrel{\rightarrow}{=}$ (3)unnest (f, g)  $\circ$  unnest ( $\pi_2 \circ$  h1, h2)
- **unnest**  $(\pi_2 \circ \mathbf{shr}, \mathbf{f} \circ \pi_2) \circ \mathbf{unnest} (\mathbf{id}, \mathbf{K}_f (\mathbf{A})) \circ \mathbf{single} \stackrel{\rightarrow}{=}$ (4) $K_f$  (unnest (id, f) ! A)
- $\begin{array}{rcl} (5) & \mathbf{f} \circ \mathbf{K}_{f} \ (\mathbf{x}) & \stackrel{\rightarrow}{=} & \mathbf{K}_{f} \ (\mathbf{f} \ \mathbf{x}) & (6) & \mathbf{f} & \stackrel{\rightarrow}{=} & \mathbf{f} \circ \mathbf{shl} \circ \mathbf{shr} \\ (7) & \pi_{2} \circ \langle \mathbf{f}, \mathbf{g} \rangle & \stackrel{\rightarrow}{=} & \mathbf{g} & (8) & \mathbf{f} \circ \mathbf{id} & \stackrel{\rightarrow}{=} & \mathbf{f} \\ (9) & \mathbf{shr} \circ \langle \pi_{1}, \mathbf{f} \circ \pi_{2} \rangle \circ \mathbf{shl} & \stackrel{\rightarrow}{=} & \langle \pi_{1}, \langle \pi_{1}, \mathbf{f} \circ \pi_{2} \rangle \circ \pi_{2} \rangle \end{array}$
- (10)  $\pi_2 \circ \delta_i \qquad \stackrel{\rightarrow}{=} \delta_{i-1} \circ \pi_2$  (11)  $\mathbf{shr}^i \circ \delta_1 \circ \mathbf{shl}^i \stackrel{\rightarrow}{=} \delta_{i+1}$

Figure 6.20: Rewrite Rules in FactorK and FKAux

times). In fact the COKO implementations of these transformations cannot express rules (10) and (11) (and instead would fire rules (7) and (10) as many times as necessary) because the matching of these rules to queries would require counting. (Note however that we can fire rule (2) once we substitute  $\langle \pi_1, \mathbf{shr} \circ \pi_2 \rangle$  for  $\delta_1$ .) We include these "macro rules" here to simplify the description of this transformation.

The normalization firing algorithm proceeds by visiting each subfunction of the form,  $f \circ g$  of the query shown in Figure 6.19. Therefore, the first subfunction visited is

iterate 
$$(p, f) \circ \mathbf{unnest} (\mathbf{id}, f_n)$$

the second is

```
unnest (id, f_n) \circ unnest (id, f_{n-1})
```

(modulo the normalizations of p, f and  $f_n$  and the changes made to **unnest** (id,  $f_n$ ) after visiting the first subfunction) and so on. These visits are described below.

**Step 1:** Substituting for p and f, the first visited subfunction is

iterate  $(p' \oplus (\pi_2 \circ \mathbf{shr}^n), f' \circ \pi_2 \circ \mathbf{shr}^n) \circ \mathbf{unnest} (\mathbf{id}, \overline{f_n}).$ 

Rule (1) of Figure 6.20 fires on this function n + 1 times, and rule (9) fires once, leaving a query of the form,

(iterate  $(p', f') \circ$ unnest  $(\pi_2 \circ \operatorname{shr}^n, \overline{f_n}) \circ \operatorname{unnest} (\operatorname{id}, \overline{f_{n-1}}) \circ \ldots \circ \operatorname{unnest} (\operatorname{id}, \overline{f_1}) \circ \operatorname{unnest} (\operatorname{id}, \overline{f_0}) \circ$ single) ! NULL

such that p', f' and  $\overline{f_i}$  are as defined in Figure 6.19.

Step 2: In this step, each pair of adjacent unnest subfunctions in the composition chain,

**unnest** 
$$(\pi_2 \circ \mathbf{shr}^n, \overline{f_n}) \circ \mathbf{unnest} (\mathbf{id}, \overline{f_{n-1}}) \circ \ldots \circ \mathbf{unnest} (\mathbf{id}, \overline{f_0})$$

is visited in turn. The purpose of this is to "push" the data function " $\pi_2 \circ \mathbf{shr}^n$ " from the left-most **unnest** function into the **unnest** functions to its right. Each "push" loses one of the "**shr**" subfunctions, and so the effect of this step is to rewrite the above composition chain into

unnest 
$$(g_n, f_n) \circ$$
  
unnest  $(g_{n-1}, \overline{f_{n-1}}) \circ$   
 $\dots \circ$   
unnest  $(g_2, \overline{f_2}) \circ$   
unnest  $(\pi_2 \circ \operatorname{shr}, \overline{f_1}) \circ$   
unnest  $(\operatorname{id}, \overline{f_0})$ 

for some functions  $g_2, \ldots, g_n$ .

Substituting for  $\overline{f_i}$ , the visit of the  $(n-i+1)^{th}$  pair of **unnest** functions,

unnest 
$$(\pi_2 \circ \mathbf{shr}^i, f'_i \circ \pi_2 \circ \mathbf{shr}^{i-1}) \circ \mathbf{unnest} (\mathbf{id}, f_{i-1})$$

pushes the data function " $\pi_2 \circ \mathbf{shr}^{i-1}$ " out of the left **unnest** function and into the right. This is captured by the "macro rule",

unnest 
$$(\pi_2 \circ \mathbf{shr}^i, \mathbf{f} \circ \pi_2 \circ \mathbf{shr}^{i-1}) \circ \mathbf{unnest} (\mathbf{id}, \mathbf{g} \circ \pi_2 \circ \mathbf{shr}^{i-2}) \stackrel{\rightarrow}{=}$$
  
unnest  $(F, \mathbf{f}) \circ \mathbf{unnest} (\pi_2 \circ \mathbf{shr}^{i-1}, \mathbf{g} \circ \pi_2 \circ \mathbf{shr}^{i-2})$ 

for some function F. Again, this rule is not expressible in COKO and instead we specify a COKO transformation that achieves the same result with the KOLA rules of Figure 6.20. In visiting the  $(n - i + 1)^{th}$  pair of **unnest** functions (for  $i \ge 2$ ),

unnest 
$$(\pi_2 \circ \mathbf{shr}^i, f'_i \circ \pi_2 \circ \mathbf{shr}^{i-1}) \circ \mathbf{unnest}$$
 (id,  $f_{i-1}$ ),

this transformation first fires rule (2) and rule (8), leaving:

unnest 
$$(\pi_2 \circ \operatorname{shr}^{i-2} \circ \delta_1 \circ \operatorname{shr}, f'_i \circ \pi_2 \circ \operatorname{shr}^{i-2}) \circ \operatorname{unnest} (\operatorname{shr}, f_{i-1}).$$

Next, rule (6) fires i - 2 times, leaving:

unnest 
$$(\pi_2 \circ \gamma \circ \operatorname{shr}^{i-1}, f'_i \circ \pi_2 \circ \operatorname{shr}^{i-2}) \circ \operatorname{unnest} (\operatorname{shr}, f_{i-1}).$$

such that

$$\gamma = \mathbf{shr}^{i-2} \circ \delta_1 \circ \mathbf{shl}^{i-2}.$$

The firing of "macro rule" (11) (equivalently, (i-2) firings of rule (9)) on  $\gamma$  leaves:

unnest 
$$(\pi_2 \circ \delta_{i-1} \circ \operatorname{shr}^{i-1}, f'_i \circ \pi_2 \circ \operatorname{shr}^{i-2}) \circ \operatorname{unnest} (\operatorname{shr}, f_{i-1}).$$

Then, the firing of "macro rule" (10) (equivalently, rule (7)) leaves:

unnest 
$$(\delta_{i-2} \circ \pi_2 \circ \operatorname{shr}^{i-1}, f'_i \circ \pi_2 \circ \operatorname{shr}^{i-2}) \circ \operatorname{unnest} (\operatorname{shr}, f_{i-1}).$$

This pass is repeated for every occurrence of "shr" that needs to be passed from right to left. In this case, (i-1) passes are completed in all, leaving

unnest 
$$(\delta_{i-2} \circ \ldots \circ \delta_0 \circ \pi_2 \circ \operatorname{shr}, f'_i \circ \pi_2) \circ \operatorname{unnest} (\operatorname{shr}^{i-1}, f_{i-1}).$$

Subsequently, rule (3) fires, leaving:

**unnest** 
$$(\delta_{i-2} \circ \ldots \circ \delta_0, f'_i) \circ$$
 **unnest**  $(\pi_2 \circ \mathbf{shr}^{i-1}, f_{i-1})$ 

and, substituting for  $\overline{f_{i-1}}$  the next adjacent pair of **unnest** functions,

unnest 
$$(\pi_2 \circ \operatorname{shr}^{i-1}, f'_i \circ \pi_2 \circ \operatorname{shr}^{i-2}) \circ \operatorname{unnest} (\operatorname{id}, f_{i-2})$$

is visited. In all, n-1 visits are made of adjacent **unnest** functions, leaving a query of the form,

```
(iterate (p', f') \circ

unnest (\delta_{n-2} \circ \ldots \circ \delta_0, f'_n) \circ unnest (\delta_{n-3} \circ \ldots \circ \delta_0, f'_{n-1}) \circ

\ldots \circ

unnest (\delta_0, f'_2)

unnest (\pi_2 \circ \operatorname{shr}, f'_1 \circ \pi_2) \circ unnest (id, K<sub>f</sub> (A)) \circ single) ! NULL.
```

Transformation	Figure	No. Rules	No. Verified	No. Lines in
			Rules	Firing Algorithm
NormTrans	6.15	4	3	14
OrdUnnests	6.16	1	0	7
FactorK	6.20	13	9	15
Total	_	18	12	36

Table 6.4: Analysis of the COKO Normalization Transformations

Steps 3, 4 and 5: In the next step,

unnest  $(\pi_2 \circ \mathbf{shr}, f'_1 \circ \pi_2) \circ \mathbf{unnest} (\mathbf{id}, \mathtt{K}_f (A)) \circ \mathbf{single}$ 

is rewritten by rule (4) leaving

(iterate  $(p', f') \circ$ unnest  $(\delta_{n-2} \circ \ldots \circ \delta_0, f'_n) \circ$  unnest  $(\delta_{n-3} \circ \ldots \circ \delta_0, f'_{n-1}) \circ$   $\ldots \circ$ unnest  $(\delta_0, f'_2) \circ K_f$  (unnest (id,  $f'_1) ! A$ )) ! NULL.

Then, rule (5) is fired in bottom-up fashion, leaving

 $\begin{array}{l} \mathsf{K}_{f} \ (\text{iterate} \ (p', \ f') \ ! \\ (\text{unnest} \ (\delta_{n-2} \circ \ldots \circ \delta_{0}, \ f'_{n}) \ ! \ (\text{unnest} \ (\delta_{n-3} \circ \ldots \circ \delta_{0}, \ f'_{n-1}) \ ! \ \ldots \ ! \\ (\text{unnest} \ (\delta_{0}, \ f'_{2}) \ ! \ (\text{unnest} \ (\text{id}, \ f'_{1}) \ ! \ A)))))) \ ! \ \texttt{NULL}. \end{array}$ 

Thus, the original query expression has been rewritten to the form  $K_f(A)$  ! NULL fos eome collection A.

# Analysis

Table 6.4 summarizes the transformations required to perform the normalization of translated KOLA queries. As before, the normalization is expressed with little code (fewer than 40 lines of firing algorithm code) and mostly in terms of rewrite rules.

Transformation NormTrans has been tested with over 100 Query Lite and OQL queries of varying complexity, including the Query Lite query of Figure 6.3 and the OQL queries of Figures 6.6a and  $6.17b.^{8}$ 

 $<sup>^{8}</sup>$ As yet this transformation does not work over queries nested in their SELECT clauses such as that of Figures 6.6b.

SELECT s FROM s IN Sens WHERE  $s.{\tt reps.lgst_cit.popn}~>~1M$ 

a. Query Lite Query 1

iterate  $(\mathbf{gt} \oplus \langle \mathbf{id}, \mathtt{K}_f (10) \rangle \oplus \mathtt{popn} \oplus \mathtt{lgst\_cit} \oplus \mathtt{reps}, \mathbf{id})$  ! Sens

b. Its Normalization

c. Its Rewrite by PEWhere

SELECT s FROM s IN Sens, r IN Sts, c IN Cits WHERE (c.popn~>~1M) AND  $(r.\texttt{lgst\_cit} == c.\texttt{OID})$  AND (s.reps == r.OID)

d. Its Translation Into SQL

Figure 6.21: Query 1 (a), Normalization (b), Rewrite by PEWhere (c) In SQL (d)

```
SELECT s
                                {\tt FROM}\;s\;\;{\tt IN}\;{\tt Sens}
                                WHERE (s.reps.lgst_cit.popn > 1M) AND
                                             (s.terms > 5) AND
                                             (s.reps.lgst_cit.mayor.bornin.popn > 1M)
                                                           a. Query Lite Query 2
iterate ((\mathbf{gt} \oplus \langle \mathbf{id}, \mathsf{K}_f (1M) \rangle \oplus \mathsf{popn} \oplus \mathsf{lgst\_cit} \oplus \mathsf{reps}) &
                 (\mathbf{gt} \oplus \langle \mathbf{id}, \mathsf{K}_f (5) \rangle \oplus \mathtt{terms}) \&
                 (\mathbf{gt} \oplus \langle \mathbf{id}, \mathtt{K}_f (1M) \rangle \oplus \mathtt{popn} \oplus \mathtt{bornin} \oplus \mathtt{mayor} \oplus \mathtt{lgst\_cit} \oplus \mathtt{reps}), \mathbf{id}) !
  Sens
                                                             b. Its Normalization
                 ((p_6 \& p_7) \oplus \langle \pi_1, (\pi_1 \circ \pi_2) \rangle)) \oplus
                                \langle \pi_1, \langle \pi_1 \circ \pi_1, \operatorname{shr} \circ \langle \pi_2 \circ \pi_1, \pi_2 \rangle \rangle \circ \pi_2 \rangle \oplus \operatorname{shr} ) \oplus
                                 \langle \langle \pi_1 \circ \pi_1 \circ \pi_1, \mathbf{shr} \circ \langle \langle \pi_2 \circ \pi_1, \pi_2 \rangle \circ \pi_1, \pi_2 \rangle \rangle \circ \pi_1, \pi_2 \rangle
                             \pi_1 \circ \langle \pi_1 \circ \pi_1 \circ \pi_1, \mathbf{shr} \circ \langle \langle \pi_2 \circ \pi_1, \pi_2 \rangle \circ \pi_1, \pi_2 \rangle \rangle \circ \pi_1 \rangle!
                               [join (K_p (true), id) !
                                [join (K_p (true), id) !
                                  [join (K<sub>p</sub> (true), id) ! [Sens, Sts], Cits], Mays], Cits]
                                                                       such that
                                      p_1 = \mathbf{gt} \oplus \langle \mathbf{id}, \mathsf{K}_f (1M) \rangle \oplus \mathsf{popn} \oplus \pi_2
                                      p_2 = \mathbf{eq} \oplus \langle \mathtt{bornin} \circ \pi_1, \, \mathtt{OID} \circ \pi_2 \rangle
                                      p_3 = \mathbf{eq} \oplus \langle \mathtt{mayor} \circ \pi_1, \, \mathtt{OID} \circ \pi_1 \circ \pi_2 \rangle
                                      p_4 = \mathbf{gt} \oplus \langle \mathbf{id}, \mathsf{K}_f (1M) \rangle \circ \mathsf{popn} \oplus \pi_1
                                      p_5 = \mathbf{eq} \oplus \langle \mathtt{lgst\_cit} \circ \pi_1, \ \mathtt{OID} \circ \pi_1 \circ \pi_2 \rangle
                                      p_6 = \mathbf{gt} \oplus \langle \mathbf{id}, \, \mathtt{K}_f \, (5) \rangle \oplus \, \mathtt{terms} \oplus \pi_1
                                      p_7 = \mathbf{eq} \oplus \langle \mathbf{reps} \circ \pi_1, \, \mathsf{OID} \circ \pi_2 \rangle
                                                        c. Its Rewrite by PEWhere
               SELECT \boldsymbol{s}
               FROM s IN Sens, r IN Sts, c IN Cits, m IN Mays, x IN Cits
               WHERE (x.popn > 1M) AND (m.bornin = x.OID) AND
                            (c.mayor == m.OID) \text{ AND } (c.popn > 1M) \text{ AND}
                           (r.lgst_cit == c.OID) AND (s.terms > 5) AND (s.reps == r.OID)
                                                       d. Its Translation Into SQL
```

Figure 6.22: Query 2 (a), Normalization (b), Rewrite by PEWhere (c) In SQL (d)
```
SELECT s
                             FROM s IN Sens
                             WHERE s.bornin.mayor.terms < 4 AND
                                     s.pty.name == "GOP" AND
                                     s.reps.lgst_cit.mayor.bornin.popn > 1M AND
                                     NOT (s.\texttt{bornin.popn} > 1M) AND
                                     s.\texttt{reps.popn} > 10M AND
                                     s.reps.lgst_cit.mayor.terms < 3 AND
                                     s.terms > 5 \text{ AND}
                                     s.bornin.mayor.pty == "Dem" AND
                                     NOT (s.reps.lgst_cit.name == "Providence")
                                                         a. Query Lite Query 3
iterate ((lt \oplus (id, K<sub>f</sub> (40)) \oplus terms \oplus mayor \oplus bornin) &
                 (\mathbf{eq} \oplus \langle \mathbf{id}, \mathtt{K}_f (\mathtt{GOP}) \rangle \oplus \mathtt{name} \oplus \mathtt{pty}) \&
                 (\mathbf{gt} \oplus \langle \mathbf{id}, \mathtt{K}_f (1M) \rangle \oplus \mathtt{popn} \oplus \mathtt{bornin} \oplus \mathtt{mayor} \oplus \mathtt{lgst\_cit} \oplus \mathtt{reps}) \&
                 (\sim (\mathbf{gt}) \oplus \langle \mathbf{id}, \mathtt{K}_f (1M) \rangle \oplus \mathtt{popn} \oplus \mathtt{bornin}) &
                 (\mathbf{gt} \oplus \langle \mathbf{id}, \mathsf{K}_f (10M) \rangle \oplus \mathsf{popn} \oplus \mathsf{reps}) &
                  (\mathbf{lt} \oplus \langle \mathbf{id}, \mathtt{K}_f (30) \rangle \oplus \mathtt{terms} \oplus \mathtt{mayor} \oplus \mathtt{lgst\_cit} \oplus \mathtt{reps}) \&
                 (\mathbf{gt} \oplus \langle \mathbf{id}, \mathtt{K}_f (50) \rangle \oplus \mathtt{terms}) \&
                 (\mathbf{eq} \oplus \langle \mathbf{id}, \, \mathtt{K}_f \, (\, \texttt{``Dem''}) 
angle \oplus \, \mathtt{pty} \oplus \, \mathtt{mayor} \oplus \, \mathtt{bornin}) &
                 (\sim (\mathbf{eq}) \oplus \langle \mathbf{id}, K_f ("Providence") \rangle \oplus \mathsf{name} \oplus \mathsf{lgst\_cit} \oplus \mathsf{reps}), \mathbf{id}) !
  Sens
```

## b. Its Normalization

Figure 6.23: Query 3 (a), Normalization (b), ...

**join**  $(((((((p_1 \& p_2) \oplus \pi_2) \& (p_3 \& p_4)) \oplus \pi_2) \&$  $((p_{10} \And p_{11}) \oplus \langle \pi_1, \ \pi_1 \circ \pi_2 \rangle)) \oplus \pi_2)$  &  $((p_{12} \& p_{13}) \oplus \langle \pi_1, \pi_1 \circ \pi_2 \rangle)) \& p_{14}) \oplus \pi_1) \& p_{15}) \oplus$  $\langle \pi_1, \pi_1 \circ \pi_2 \rangle) \oplus \mathbf{shr}) \oplus \langle \langle \langle \pi_1 \circ \pi_1 \circ \pi_1 \circ \pi_1 \circ \pi_1, \langle \pi_2 \circ \pi_1 \circ \pi_1 \circ \pi_1, \mathbf{shr} \rangle \rangle$  $\circ \langle \langle \pi_2 \circ \pi_1, \pi_2 \rangle \circ \pi_1 \rangle, \pi_2 \rangle \rangle \circ \pi_1, \pi_2 \rangle \circ \pi_1, \pi_2 \rangle,$  $\pi_1 \circ \pi_1 \circ \langle \pi_1 \circ \pi_1 \circ \pi_1 \circ \pi_1 \circ \pi_1, \langle \pi_2 \circ \pi_1 \circ \pi_1 \rangle$  $\pi_1 \circ \pi_1, \, \mathbf{shr} \circ \langle \langle \pi_2 \circ \pi_1, \, \pi_2 \rangle \circ \pi_1, \, \pi_2 \rangle \rangle \rangle \circ \pi_1, \, \pi_2 \rangle \circ \pi_1) \, !$ [join ( $K_p$  (true), id) ! [Sens, Sts], Cits], Mays], Cits], Cits], Mays] such that  $p_1 = \mathbf{eq} \oplus \langle \texttt{OID}, \texttt{K}_f (\texttt{``Dem''}) \rangle \oplus \texttt{pty}$  $p_2 = \mathbf{lt} \oplus \langle \texttt{OID}, \texttt{K}_f (40) \rangle \oplus \texttt{terms}$  $p_3 = \sim (\mathbf{gt}) \oplus \langle \texttt{OID}, \texttt{K}_f (1) \rangle \circ \texttt{popn} \oplus \pi_1$  $p_4 = \mathbf{eq} \oplus \langle \mathtt{mayor} \circ \pi_1, \ \mathtt{OID} \circ \pi_2 \rangle$  $p_5 = \mathbf{gt} \oplus \langle \texttt{OID}, \texttt{K}_f (1) \rangle \circ \texttt{popn} \oplus \pi_2$  $p_6 = \mathbf{lt} \oplus \langle \texttt{OID}, \texttt{K}_f (30) \rangle \circ \texttt{terms} \oplus \pi_1$  $p_7 = \mathbf{eq} \oplus \langle \mathtt{bornin} \circ \pi_1, \mathtt{OID} \circ \pi_2 \rangle$  $p_8 = \sim (\mathbf{eq}) \oplus \langle \mathsf{OID}, \mathsf{K}_f ("\mathsf{Providence"}) \rangle \circ \mathsf{name} \oplus \pi_1$  $p_9 = \mathbf{eq} \oplus \langle \mathtt{mayor} \circ \pi_1, \mathtt{OID} \circ \pi_2 \rangle$  $p_{10} = \mathbf{gt} \oplus \langle \texttt{OID}, \texttt{K}_f (1) \rangle \circ \texttt{popn} \oplus \pi_1$  $p_{11} = \mathbf{eq} \oplus \langle \mathtt{lgst\_cit} \circ \pi_1, \, \mathtt{OID} \circ \pi_2 \rangle$  $p_{12} = \mathbf{eq} \oplus \langle \texttt{OID}, \texttt{K}_f (\texttt{"GOP"}) \rangle \circ \texttt{pty} \oplus \pi_1$  $p_{13} = \mathbf{eq} \oplus \langle \mathtt{reps} \circ \pi_1, \, \mathtt{OID} \circ \pi_2 \rangle$  $p_{14} = \mathbf{gt} \oplus \langle \texttt{OID}, \texttt{K}_f (50) \rangle \circ \texttt{terms} \oplus \pi_1$  $p_{15} = \mathbf{eq} \oplus \langle \mathtt{bornin} \circ \pi_1 \circ \pi_1, \, \mathtt{OID} \circ \pi_2 \rangle$ c. Its Rewrite by PEWhere SELECT s

FROM s IN Sens, r IN Sts, c IN Cits, m IN Mays, x IN Cits, y IN Cits, z IN Mays WHERE (z.pty == "Dem") AND (z.terms < 4) AND (NOT (y.popn > 1M)) AND (y.mayor == z.OID) AND (x.popn > 1M) AND (m.terms < 3) AND (m.bornin == x.OID) AND (NOT (c.name == "Providence")) AND (c.mayor == m.OID) AND (r.popn > 1M) AND  $(r.lgst_cit == c.OID)$  AND (s.pty == "GOP") AND (s.reps == r.OID) AND (s.terms > 5) AND (s.bornin == y.OID)

d. Its Translation Into SQL

Figure 6.24: Query 3 (cont.) ..., Rewrite by PEWhere (c) In SQL (d)

## 6.3.3 Transforming Path Expressions to Joins

This section describes a COKO transformation (**PEWhere**) that rewrites Query Lite queries with path expressions in their WHERE clause into SQL join queries. Specifically, Query Lite queries that are translated and then normalized with the transformations described in Section 6.3.2 are those affected by **PEWhere** and its auxiliary transformation, **PEWAux**.

Unlike those of the previous section, the COKO transformations described in this section are few (2 in all) and short, requiring 3 rewrite rules, 2 inference rules and fewer than 20 lines of firing algorithm code in all. In addition, the transformations presented here demonstrate a novel application of the semantic query rewrite facility described in Chapter 5. The semantic property concerns foreign keys.

#### Path Expression Elimination Overview

Consider Query Lite Query 1 of Figure 6.21a that finds all Senators in **Sens** who represent states whose largest cities have a population of over 1 million people. This query includes the path expression,

## s.reps.lgst\_cit.popn

in its WHERE clause to find the population of the largest city in the state represented by Senator s. Specifically, for any Senator s:

- s.reps returns the object denoting the state that s represents,
- *s.***reps.lgst\_cit** returns the object denoting the largest city of the state that *s* represents, and
- *s*.reps.lgst\_cit.popn returns the integer denoting the population of the largest city of the state that *s* represents.

The relational implementation of San Francisco described in Section 6.1 uses relations to implement each type extent, with the OID columns as keys. For the object schema of Figure 2.1,

- Sens is a relation representing the extent of objects of type Senator,
- Sts is a relation representing objects of type *Region* that are states, and
- Cits is a relation representing objects of type *City*.

As a result, for path expression *s*.reps.lgst\_cit.popn, method reps is a *foreign key* for Sts, and lgst\_cit is a foreign key for Cits. This information makes it possible to rewrite the Query Lite query of Figure 6.21 into the SQL join query,

SELECT 
$$s$$
  
FROM  $s$  IN Sens,  $r$  IN Sts,  $c$  IN Cits  
WHERE  $(c.popn > 1M)$  AND  $(r.lgst_cit == c.OID)$  AND  $(s.reps == r.OID)$ 

The COKO transformations described in this section perform the rewrite above. These transformations exploit semantic knowledge of foreign keys (metadata information that is assumed to be available to the optimizer), to decide when methods in a path expression can be translated into relational joins. More precisely, these transformations rewrite Query Lite queries of the form,

SELECT xFROM x IN AWHERE  $Comp_1$  AND ... AND  $Comp_m$ 

such that each  $Comp_i$  is a simple comparison predicate involving a path expression such as,

 $x.m_0...m_n op k$ 

or

NOT 
$$(x.m_0...m_n op k)$$
.

As well, these transformations have the following characteristics:

• comparisons can appear in the opposite order, as in,

$$k op x.m_0...m_n$$
,

- WHERE clauses can also contain disjunctions provided that the disjunctions disappear when the WHERE clauses is converted into CNF,
- *sharing* of path expressions is recognized.

To illustrate sharing, consider Query Lite Query 2 of Figure 6.22a, which finds senators who have served more than 5 terms, and who represent a state whose largest city: (1) has more than 1 million people, and (2) has a mayor who was born in a city with more than 1 million people. This query contains two path expressions that contain the common subexpression,

The transformations presented here rewrite this query into the SQL query,

```
SELECT s

FROM s IN Sens, r IN Sts, c IN Cits, m IN Mays, x IN Cits

WHERE (x.popn > 1M) AND (m.bornin == x.OID) AND

(c.mayor == m.OID) AND (c.popn > 1M) AND

(r.lgst_cit == c.OID) AND (s.terms > 5) AND (s.reps == r.OID)
```

rather than to the more naive translation,

```
SELECT s

FROM s IN Sens, r IN Sts, c IN Cits, m IN Mays, x IN Cits, r_2 IN Sts, c_2 IN Cits

WHERE (x.popn > 1M) AND (m.bornin == x.OID) AND

(c.mayor == m.OID) AND (c.popn > 1M) AND

(r.lgst_cit == c.OID) AND (s.terms > 5) AND (s.reps == r.OID) AND

(r_2.lgst_cit == c_2.OID) AND (c_2.mayor == m.OID) AND (s.reps == r_2.OID)
```

which is a 7-way join rather than a 5-way join, redundantly joining collections Sts and Cits twice (once for each occurrence of the common subexpression).

The transformations described here not only recognize common subexpressions in path expressions, but do so for:

- any number of path expressions in a WHERE clause,
- any degree of sharing amongst path expressions, and
- any number of path expressions sharing a given subexpression (even when path expressions with shared subexpressions are not adjacent).

An example application of this transformation is shown in Figures 6.23a. Figure 6.23a and 6.23b show the original Query Lite query and the result of its translation and normalization. Figure 6.24c show the result of rewriting this query by **PEWhere**. Figure 6.24d shows this same query after its translation into SQL.

Query 3 includes path expressions with varying degrees of sharing, such as:

- s.bornin.mayor.terms < 4, which shares:
  - s.bornin with: NOT (s.bornin.popn > 1M), and
  - s.bornin.mayor with: s.bornin.mayor.pty == "Dem", and
- $s.reps.lgst_cit.mayor.bornin.popn > 1M$ , which shares:

- s.reps with: s.reps.popn > 1M,
- s.reps.lgst\_cit with: NOT (s.reps.lgst\_cit.name == "Providence"), and
- $-s.reps.lgst_cit.mayor with: s.reps.lgst_cit.mayor.terms < 3.$

The result of rewriting shown in Figure 6.24 exploits this sharing and joins as few collections as possible.

#### Transformation PEWhere and Its Auxiliary Transformation

Translation of Query Lite queries generates KOLA expressions of the form,

```
(iterate (p, id) \circ unnest (id, K_f(A)) \circ single) ! NULL.
```

After normalization using the transformations of Section 6.3.2, these queries are of the form,

```
iterate (q, id) ! A.
```

If Query Lite queries have WHERE clauses as characterized in the previous section (i.e., conjunctions of simple comparisons), then the predicate p in the query produced by translation is of the form,

$$p_0$$
 & ... &  $p_m$ 

such that each  $p_i$  is of the form

$$op \oplus \langle \mathtt{m}_{\mathtt{i}_{\mathtt{n}}} \circ \ldots \circ \mathtt{m}_{\mathtt{0}} \circ g_{i}, \mathtt{K}_{f} (k) \rangle$$

or

$$\sim (op \oplus \langle \mathtt{m}_{\mathtt{i}_{\mathtt{n}}} \circ \ldots \circ \mathtt{m}_{\mathtt{0}} \circ g_i, \mathtt{K}_f (k) \rangle)$$

*op* is a KOLA comparison primitive (such as eq), each  $m_j$  is a method primitive and k is a constant. For these same queries, normalization results in predicates p' of the form,

$$op \oplus \langle \mathbf{id}, \mathsf{K}_f (k) \rangle \oplus \mathtt{m}_{\mathtt{i}_n} \circ \ldots \circ \mathtt{m}_{\mathtt{O}} \circ g_i$$

or

$$\sim$$
  $(op)$   $\oplus$   $\langle \mathbf{id}, \, \mathtt{K}_f \, (k) 
angle \oplus \mathtt{m}_{\mathtt{i}_\mathtt{n}} \oplus \, \ldots \, \oplus \, \mathtt{m}_\mathtt{O} \oplus \, g_i$ 

(as illustrated by the normalized translations of Query Lite Queries: 1 (Figure 6.21b), 2 (Figure 6.22b), and 3 (Figure 6.23b)).

**PEWhere** (Figure 6.25) gets invoked after translation and normalization, and therefore affects queries of the form,

$$\mathbf{iterate} \ (p_1' \And \dots \And p_m', \mathbf{id}) \ ! \ A$$

```
TRANSFORMATION PEWhere
   -- Transforms QL queries with where predicates of the form,
   -- x.a1()...an() op k, or k op x.a1()...an()
   -- into join queries using scoping rules for attributes
   USES
    LBJoin,
    PEWAux,
    PullComFunc,
    SimpFunc,
    SimpPred
   BEGIN
    -- Step 1: Find common subfunctions of conjuncts and factor out
    GIVEN iterate (p, _F) ! _O DO PullComFunc (p);
    -- Step 2: Call PEWAux
    PEWAux;
    -- Step 3: Recombine iterate's and joins into left-bushy join tree
    LBJoin
   END
TRANSFORMATION PEWAux
 USES
  pe2j: scope (B, f, A) ::
           iterate (p \oplus f, id) ! A \longrightarrow
            join (eq \oplus \langle f \circ \pi_1, OID \circ \pi_2 \rangle, \pi_1) ! [A, iterate (p, id) ! B],
            iterate (p \& q, id) ! A \longrightarrow iterate (p, id) ! (iterate (q, id) ! A),
  splcon:
  SimpPred
 INFERS
  Scope
 BEGIN
  splcon \rightarrow GIVEN _F ! x DO {PEWAux (x); PEWAux};
  pe2j \rightarrow GIVEN join (p, _F) ! [_O, B] DO PEWAux (B)
 END
```

Figure 6.25: Transformation PEWhere and its Auxiliary Transformation

such as those of Figures 6.21, 6.22 and 6.23. **PEWhere** operates in 3 steps, which are demonstrated in terms of their effect on the query of Figure 6.22b: the result of translating and normalizing the Query Lite Query 2 of Figure 6.22a.

Step 1: In the first step of this transformation, PullComFunc (Section 6.3.1) rewrites conjunction predicates,

$$p_1$$
 & ... &  $q_n$ 

into the form,

$$(q_1 \, \oplus \, f_1)$$
 &  $\dots$  &  $(q_m \, \oplus \, f_m)$ 

such that  $m \leq n$  and no two functions  $f_i$  and  $f_j$   $(i \neq j)$  are the same. This step extracts the common subexpressions from distinct path expressions.

Applied to Query 2:

When applied to the query of Figure 6.22b, this step results in the expression, Q:

iterate 
$$(((q_{1a} \& q_{1b}) \oplus lgst\_cit \oplus reps) \& q_2, id)$$
 ! Sens

such that

Step 2: The second step of this transformation invokes auxiliary transformation, PEWAux on the expression resulting from 1. PEWAux has two key rules. The first is rule splcon, which splits an **iterate** function instantiated with a conjunction predicate into two. When applied to queries of the form,

iterate 
$$(q_1 \& \ldots \& q_m, id) ! A$$

such as those resulting from Step 1 of PEWhere's firing algorithm, this rule returns

iterate 
$$(q_1, id)$$
 ! (iterate  $(q_2 \& \ldots \& q_m, id)$  ! A.

The effect of the recursive calls to PEWAux that follow the successful firing of splcon is to invoke PEWAux successively on subqueries:

• iterate  $(q_m, id) ! A$ ,

```
scope (Sts, reps, Sens).
scope (Cits, reps, Mays).
scope (Cits, bornin, Sens).
scope (Cits, bornin, Mays).
scope (Cits, lgst_cit, Rgs).
scope (Cits, lgst_cit, Sts).
scope (Mays, mayor, Cits).
```

Figure 6.26: Scope Facts Assumed Known for these Examples

- iterate  $(q_{m-1}, \operatorname{id}) ! (\operatorname{iterate} (q_m, \operatorname{id}) ! A),$
- iterate  $(q_{m-2}, id)$  ! (iterate  $(q_{m-1}, id)$  ! (iterate  $(q_m, id)$  ! A)), etc.

The second rule, pej2, is a conditional rewrite rule that depends on the condition, scope (B, f, A). This condition holds of collections A and B and function f if f is a function on elements of A and is also a foreign key of B. Figure 6.26 shows the scope facts that are assumed to hold (and to be part of the schema accessible by our optimizer) for the examples in this chapter.

Figure 6.27 shows a property definition for **Scope** that lists three inference rules for inferring this property. The first of these rules,

scope (B, f, A) 
$$\implies$$
 scope (B, f, iterate (p, id) ! A)

says that if f is a foreign key for B that is defined on A, then it is also a foreign key for B that is defined on any selection on A. The second and third rules,

scope (B, f, A)  $\implies$  scope (B, f, join (p,  $\pi_1$ ) ! [A, \_O]). scope (B, f, A)  $\implies$  scope (B, f, join (p,  $\pi_2$ ) ! [\_O, A]).

say that if f is a foreign key for B that is defined on A, then it is a foreign key for B that is defined on (left and right) semi-joins on A.

Provided that scope is inferred to be true for collection B, function f and collection A, the query,

iterate 
$$(p \oplus f, id) ! A$$

can be rewritten to a join of A and the subcollection of B satisfying p:

join (eq  $\oplus \langle f \circ \pi_1, \text{OID} \circ \pi_2 \rangle, \pi_1$ ) ! [A, iterate (p, id) ! B].

```
PROPERTY Scope

BEGIN

scope (B, f, A) \implies scope (B, f, iterate (p, id) ! A).

scope (B, f, A) \implies scope (B, f, join (p, \pi_1) ! [A, _O]).

scope (B, f, A) \implies scope (B, f, join (p, \pi_2) ! [_O, A]).

END
```



This query screens B for those elements satisfying p, and then joins the result with A to return those elements of A whose values for f are represented on the subcollection of B. In terms of Query Lite queries, the left-hand side of the rule denotes queries of the form,

```
SELECT x
FROM x IN A
WHERE p (f (x)).
```

In terms of SQL queries, the right-hand side of the rule denotes queries of the form,

```
SELECT x
FROM x IN A, y IN B
WHERE f(x) == y AND p(y).
```

Each time pe2j is successfully fired, it returns a query of the form,

join (eq  $\oplus \langle f \circ \pi_1, \text{OID} \circ \pi_2 \rangle, \pi_1$ ) ! [A, iterate (p, id) ! B],

and PEWAux is called recursively on the second argument to the join,

```
iterate (p, id) ! B.
```

This recursive call ensures that all methods appearing in a path expression contribute to the rewrite into a join query.

Applied to Query 2:

1. First, splcon successfully fires and triggers a recursive call of PEWAux on

```
iterate (q_2, id) ! Sens.
```

scope (B, terms, Sens)

holds.) Therefore, a second recursive call to PEWAux is made on

 $\mathbf{iterate} \ ((\mathtt{q_{1a}} \And \mathtt{q_{1b}}) \oplus \mathtt{lgst\_cit} \oplus \mathtt{reps}, \, \mathbf{id}) \ ! \ (\mathbf{iterate} \ (\mathtt{q_2}, \, \mathbf{id}) \ ! \ \mathtt{Sens}).$ 

2. The call of PEWAux on this query fails to fire splcon, but succeeds in firing pe2j. The first inference rule for Scope in Figure 6.27 together with the fact,

```
scope (Sts, reps, Sens),
```

makes it possible to infer,

scope (Sts, reps, iterate  $(q_2, id)$  ! Sens),

and therefore pej2 successfully fires. This results in the query,

join (eq  $\oplus \langle \text{reps} \circ \pi_1, \text{OID} \circ \pi_2 \rangle, \pi_1$ ) ! [iterate (q<sub>2</sub>, id) ! Sens, iterate ((q<sub>1a</sub> & q<sub>1b</sub>)  $\oplus$  lgst\_cit, id) ! Sts].

3. The successful firing of rule pe2j triggers another recursive call of PEWAux, this time on

 $\mathbf{iterate} \ ((\mathtt{q_{1a}} \And \mathtt{q_{1b}}) \oplus \mathtt{lgst\_cit}, \ \mathbf{id}) \texttt{ ! Sts}.$ 

Again, pe2j successfully fires on this subquery because of the fact,

```
scope (Cits, lgst_cit, Sts).
```

This leaves the subexpression,

join (eq  $\oplus$  (lgst\_cit  $\circ \pi_1$ , OID  $\circ \pi_2$ ),  $\pi_1$ ) ! [Sts, iterate (q<sub>1a</sub> & q<sub>1b</sub>, id) ! Cits].

4. Next, PEWAux is recursively called on

iterate  $(q_{1a} \& q_{1b}, id)$  ! Cits,

or equivalently,

**iterate** 
$$((\mathbf{gt} \oplus \langle \mathbf{id}, \mathsf{K}_f (1M) \rangle \oplus \mathsf{popn}) \&$$
  
 $(\mathbf{gt} \oplus \langle \mathbf{id}, \mathsf{K}_f (1M) \rangle \oplus \mathsf{popn} \oplus \mathsf{bornin} \oplus \mathsf{mayor}), \mathbf{id}) ! \mathsf{Cits}.$ 

First splcon is fired leaving,

iterate (gt  $\oplus \langle id, K_f(1M) \rangle \oplus popn, id)$  !

(iterate (gt  $\oplus \langle id, K_f(1M) \rangle \oplus popn \oplus bornin \oplus mayor, id)$  ! Cits).

Then PEWAux is fired on

iterate  $(\mathbf{gt} \oplus \langle \mathbf{id}, \mathsf{K}_f (1M) \rangle \oplus \mathsf{popn} \oplus \mathsf{bornin} \oplus \mathsf{mayor}, \mathbf{id})$  ! Cits.

The fact

scope (Mays, mayor, Cits),

leads to a successful firing of pej2, leaving

join (eq  $\oplus \langle \text{mayor} \circ \pi_1, \text{OID} \circ \pi_2 \rangle, \pi_1$ ) ! [Cits, iterate (gt  $\oplus \langle \text{id}, K_f (1M) \rangle \oplus \text{popn} \oplus \text{bornin, id})$  ! Mays].

5. Next, PEWAux is again called recursively on

iterate  $(\mathbf{gt} \oplus \langle \mathbf{id}, K_f (1M) \rangle \oplus \text{popn} \oplus \text{bornin}, \mathbf{id}) !$  Mays.

The fact scope (Cits, bornin, Mays) leads pej2 to fire, leaving,

join (eq  $\oplus$  (bornin  $\circ \pi_1$ , OID  $\circ \pi_2$ ),  $\pi_1$ ) ! [Mays, iterate (gt  $\oplus$  (id, K<sub>f</sub> (1M))  $\oplus$  popn, id) ! Cits].

The subsequent recursive call of PEWAux on

iterate (gt  $\oplus \langle id, K_f (1M) \rangle \oplus popn, id)$  ! Cits

fails (as there is no collection B such that scope (B, popn, Cits) and the recursion terminates at all levels. Finally, the transformation call is finished leaving the query,

 $\textbf{join} \ (\textbf{eq} \oplus \langle \texttt{reps} \circ \pi_1, \, \texttt{OID} \circ \pi_2 \rangle, \, \pi_1) \ ! \ [\textbf{iterate} \ (\textbf{q}_2, \, \textbf{id}) \ ! \ \texttt{Sens}, \, B]$ 

such that B is:

join (eq  $\oplus \langle lgst\_cit \circ \pi_1, OID \circ \pi_2 \rangle, \pi_1 \rangle$  !
[Sts, iterate (gt  $\oplus \langle id, K_f (1M) \rangle \oplus popn, id)$  !
 join (eq  $\oplus \langle mayor \circ \pi_1, OID \circ \pi_2 \rangle, \pi_1 \rangle$  !
 [Cits, join (eq  $\oplus \langle bornin \circ \pi_1, OID \circ \pi_2 \rangle, \pi_1)$  !
 [Mays, iterate (gt  $\oplus \langle id, K_f (1M) \rangle \oplus popn, id)$  ! Cits]]]].

Transformation	Figure	No. Rules	No. Verified	No. Lines in
			Rules	Firing Algorithm
PEWhere	6.25	1	1	15
PEWAux	6.25	2	1	4
Scope	6.27	2	2	
Total		5	4	19

Table 6.5: Analysis of the Query Lite  $\rightarrow$  SQL Transformations

**Step 3:** The final step of this transformation converts the query resulting from step 2 into a left-bushy join. This step is strictly not required, but simplifies the task of converting the resulting query into SQL as we show in Section 6.4. Applied to the query above, this step returns the query of Figure 6.22c. Expressed in SQL, this query is:

SELECT s FROM s IN Sens, r IN Sts, c IN Cits, m IN Mays, x IN Cits WHERE (x.popn > 1M) AND (m.bornin == x.OID) AND (c.mayor == m.OID) AND (c.popn > 1M) AND  $(r.lgst\_cit == c.OID)$  AND (s.terms > 5) AND (s.reps == r.OID)

### Analysis

Table 6.5 summarizes the transformations and property presented in this section. Note that this complex rewrite is expressed with 3 rewrite rules, 2 inference rules and fewer than 20 lines of firing algorithm code.

## 6.4 Translating KOLA into SQL

Transformation PEWhere leaves Query Lite queries in the form

```
join (p_1 \& \dots \& p_n, f) !

[join (K_p \text{ (true)}, \text{ id}) !

[join (K_p \text{ (true)}, \text{ id}) !

[...[join (K_p \text{ (true)}, \text{ id}) ! [A_1, A_2], ...], A_{m-2}], A_{m-1}], A_m]
```

or in the form **iterate** (p, f) ! A. The sublanguage of KOLA that consists of such expressions only includes primitives: **id**,  $\pi_1$ ,  $\pi_2$ , **shr**, **shl**, **OID**, **m** (**m** a method), **abs**, **add**, **sub**, **mul**, **div**, **mod**, **eq**, **neq**, **lt**, **gt**, **leq**, **geq**; and formers:  $\langle \rangle$ ,  $\circ$ , K<sub>f</sub>, C<sub>f</sub>, **iterate**, **join**,  $\oplus$ , &,

 $\begin{array}{rcl} Int \ and \ Float \ Function \ Primitives \ (i, \ j \ integers \ or \ floats) \\ & \mathbf{T}^{-1} \ \llbracket \mathbf{abs} \ ! \ i \rrbracket &=& \mathbf{abs} \ (\mathbf{T}^{-1} \ \llbracket i \rrbracket) \\ & \mathbf{T}^{-1} \ \llbracket \mathbf{add} \ ! \ [i, \ j \rrbracket \rrbracket &=& (\mathbf{T}^{-1} \ \llbracket i \rrbracket) + (\mathbf{T}^{-1} \ \llbracket j \rrbracket) \\ & \mathbf{T}^{-1} \ \llbracket \mathbf{sub} \ ! \ [i, \ j \rrbracket \rrbracket &=& (\mathbf{T}^{-1} \ \llbracket i \rrbracket) + (\mathbf{T}^{-1} \ \llbracket j \rrbracket) \\ & \mathbf{T}^{-1} \ \llbracket \mathbf{sub} \ ! \ [i, \ j \rrbracket \rrbracket &=& (\mathbf{T}^{-1} \ \llbracket i \rrbracket) - (\mathbf{T}^{-1} \ \llbracket j \rrbracket) \\ & \mathbf{T}^{-1} \ \llbracket \mathbf{mul} \ ! \ [i, \ j \rrbracket \rrbracket &=& (\mathbf{T}^{-1} \ \llbracket i \rrbracket) + (\mathbf{T}^{-1} \ \llbracket j \rrbracket) \\ & \mathbf{T}^{-1} \ \llbracket \mathbf{mul} \ ! \ [i, \ j \rrbracket \rrbracket &=& (\mathbf{T}^{-1} \ \llbracket i \rrbracket) + (\mathbf{T}^{-1} \ \llbracket j \rrbracket) \\ & \mathbf{T}^{-1} \ \llbracket \mathbf{div} \ ! \ [i, \ j \rrbracket \rrbracket &=& (\mathbf{T}^{-1} \ \llbracket i \rrbracket) + (\mathbf{T}^{-1} \ \llbracket j \rrbracket) \\ & \mathbf{T}^{-1} \ \llbracket \mathbf{div} \ ! \ [i, \ j \rrbracket \rrbracket &=& (\mathbf{T}^{-1} \ \llbracket i \rrbracket) + (\mathbf{T}^{-1} \ \llbracket j \rrbracket) \\ & \mathbf{T}^{-1} \ \llbracket \mathbf{mod} \ ! \ [i, \ j \rrbracket \rrbracket &=& (\mathbf{T}^{-1} \ \llbracket i \rrbracket) + (\mathbf{T}^{-1} \ \llbracket j \rrbracket) \\ & \mathbf{T}^{-1} \ \llbracket \mathbf{mod} \ ! \ [i, \ j \rrbracket \rrbracket &=& (\mathbf{T}^{-1} \ \llbracket i \rrbracket) + (\mathbf{T}^{-1} \ \llbracket j \rrbracket) \\ & \mathbf{T}^{-1} \ \llbracket \mathbf{mod} \ ! \ [i, \ j \rrbracket \rrbracket &=& (\mathbf{T}^{-1} \ \llbracket i \rrbracket) + (\mathbf{T}^{-1} \ \llbracket j \rrbracket) \\ & \mathbf{T}^{-1} \ \llbracket \mathbf{mod} \ ! \ [i, \ j \rrbracket \rrbracket &=& (\mathbf{T}^{-1} \ \llbracket i \rrbracket) + (\mathbf{T}^{-1} \ \llbracket j \rrbracket) \\ & \mathbf{T}^{-1} \ \llbracket \mathbf{T}^{-1} \$ 

Basic Predicate Primitives (x and y of type T)  $\mathbf{T}^{-1} [\![\mathbf{eq} ? [x, y]]\!] = (\mathbf{T}^{-1} [\![x]]\!) == (\mathbf{T}^{-1} [\![y]]\!)$   $\mathbf{T}^{-1} [\![\mathbf{neq} ? [x, y]]\!] = (\mathbf{T}^{-1} [\![x]]\!) != (\mathbf{T}^{-1} [\![y]]\!)$   $\mathbf{T}^{-1} [\![\mathbf{isnull} ? x]\!] = (\mathbf{T}^{-1} [\![x]]\!) IS NULL$  $\mathbf{T}^{-1} [\![\mathbf{isnotnull} ? x]\!] = (\mathbf{T}^{-1} [\![x]]\!) IS NOT NULL$ 

String and Int Predicate Primitives (x and y strings or integers)

$\mathbf{T}^{-1}$ [[lt ? [x, y]]]	=	$(\mathbf{T}^{-1} \  \  x \ ) < (\mathbf{T}^{-1} \  \  y \ )$
$\mathbf{T}^{-1}$ [[gt ? [ $x, y$ ]]]	=	$(\mathbf{T}^{-1} \llbracket x \rrbracket) > (\mathbf{T}^{-1} \llbracket y \rrbracket)$
$\mathbf{T}^{-1}$ [[leq ? [ $x, y$ ]]]	=	$(\mathbf{T}^{-1} [\![x]\!]) \iff (\mathbf{T}^{-1} [\![y]\!])$
$\mathbf{T}^{-1}$ [[geq ? [ $x, y$ ]]]	=	$(\mathbf{T}^{-1} \ \llbracket x \rrbracket) \ge (\mathbf{T}^{-1} \ \llbracket y \rrbracket)$

Table 6.6:  $\mathbf{T}^{-1}$ : Applied to KOLA Primitives

 $\sim$ ,  $K_p$ , and  $C_p$ . Further, all queries in this sublanguage are assumed to be **iterate** queries, binary **join** queries, or left-bushy *n*-ary join queries.

A translation function,  $\mathbf{T}^{-1}$  to translate KOLA expressions over this subset of KOLA into SQL is defined in Tables 6.6 and 6.7. Note that Table 6.7 includes two translation definitions for **join**. The first of these is for translating *n*-ary joins (n > 2) only. The second of these is for translating binary joins only.

The following example illustrates this translation function. As shown in Section 6.3.3, when invoked on Query Lite query 1 of Figure 6.21b, transformation PEWhere returns the query of Figure 6.21c. This query gets translated into SQL as follows:

$$\mathbf{T}^{-1} \begin{bmatrix} \mathbf{join} ((((p_1 \And p_2) \oplus \pi_2) \And p_3) \oplus \mathbf{shr}, \ \pi_1 \circ \pi_1) ! \\ [\mathbf{join} (\mathsf{K}_p \ (\mathtt{true}), \mathbf{id}) ! \ [\mathtt{Sens}, \mathtt{Sts}], \mathtt{Cits}] \end{bmatrix}$$

such that

$$p_1 = \mathbf{gt} \oplus \langle \mathbf{id}, \mathsf{K}_f (1M) \rangle \oplus \mathsf{popn} \oplus \pi_2$$
  

$$p_2 = \mathbf{eq} \oplus \langle \mathsf{lgst\_cit} \circ \pi_1, \mathsf{OID} \circ \pi_2 \rangle$$
  

$$p_3 = \mathbf{eq} \oplus \langle \mathsf{reps} \circ \pi_1, \mathsf{OID} \circ \pi_1 \circ \pi_2 \rangle$$

 Reducing the predicates in this expression leaves,

```
SELECT \boldsymbol{s}
FROM s IN Sens, r IN Sts, c IN Cits
WHERE ((((p_1 \& p_2) \oplus \pi_2) \& p_3) \oplus \mathbf{shr})? [[s, r], c])
      SELECT s
 =
      FROM s IN Sens, r IN Sts, c IN Cits
      WHERE (((p_1 \& p_2) \oplus \pi_2) \& p_3)? [s, [r, c]])
      SELECT s
      FROM s IN Sens, r IN Sts, c IN Cits
 =
      WHERE (((p_1 \& p_2) \oplus \pi_2) ? [s, [r, c]]) AND (p_3 ? [s, [r, c]])
      SELECT s
      FROM s IN Sens, r IN Sts, c IN Cits
 =
      WHERE ((p_1 \& p_2) ? [r, c]) AND (p_3 ? [s, [r, c]])
      SELECT \boldsymbol{s}
      FROM s IN Sens, r IN Sts, c IN Cits
 =
      WHERE (p_1 ? [r, c]) AND (p_2 ? [r, c]) AND (p_3 ? [s, [r, c]])
```

Reducing each subpredicate in turn, we get:

$$p_{1} ? [r, c] = (\mathbf{gt} \oplus \langle \mathbf{id}, \mathsf{K}_{f} (1M) \rangle \oplus \mathsf{popn} \oplus \pi_{2}) ? [r, c]$$

$$= (\mathbf{gt} \oplus \langle \mathbf{id}, \mathsf{K}_{f} (1M) \rangle \oplus \mathsf{popn}) ? c$$

$$= (\mathbf{gt} \oplus \langle \mathbf{id}, \mathsf{K}_{f} (1M) \rangle) ? (c.\mathsf{popn})$$

$$= \mathbf{gt} ? [c.\mathsf{popn}, 1M]$$

$$= c.\mathsf{popn} > 1M,$$

$$p_2 ? [r, c] = (\mathbf{eq} \oplus \langle \texttt{lgst\_cit} \circ \pi_1, \texttt{OID} \circ \pi_2 \rangle) ? [r, c]$$
$$= \mathbf{eq} ? [(\texttt{lgst\_cit} \circ \pi_1) ! [r, c], (\texttt{OID} \circ \pi_2) ! [r, c]]$$
$$= \mathbf{eq} ? [r.\texttt{lgst\_cit}, c.\texttt{OID}]$$
$$= r.\texttt{lgst\_cit} == c.\texttt{OID}, \text{ and}$$

$$p_{3} ? [s, [r, c]] = (eq \oplus \langle reps \circ \pi_{1}, OID \circ \pi_{1} \circ \pi_{2} \rangle) ? [s, [r, c]]$$
  
= eq ? [(reps \circ \pi\_{1}) ! [s, [r, c]], (OID \circ \pi\_{1} \circ \pi\_{2}) ! [s, [r, c]]]  
= eq ? [s.reps, r.OID]  
= s.reps == r.OID.

Reduction leaves the SQL query,

SELECT sFROM s IN Sens, r IN Sts, c IN Cits WHERE (c.popn > 1M) AND  $(r.lgst_cit == c.OID)$  AND (s.reps == r.OID)

Other examples of translation are shown for the results of rewriting (with transformation **PEWhere**) Query Lite queries 1 (Figure 6.21d is the SQL translation of Figure 6.21c), 2 (Figure 6.22d is the SQL translation of Figure 6.22c), and 3 (Figure 6.24d is the SQL translation of Figure 6.24c).

## 6.5 Discussion

In this section, we reflect upon our experiences using COKO and KOLA to determine how well this framework met our integration and ease-of-use goals described at the chapter's onset.

#### 6.5.1 Integration Capabilities of COKO-KOLA

COKO-KOLA is a generator of query rewriting components designed to accept queries as inputs and generate inputs for cost-based optimizers. But how easy is it to integrate these query rewriters within real query processing environments?

The integration of the COKO-KOLA framework within the San Francisco project required the development of two translators. The first (described in Section 6.2) translates Query Lite queries (and more generally, all set and bag-based OQL queries) into KOLA. The second (described in Section 6.4) translates a subset of KOLA queries into SQL. Of these translators, the first was by far the easiest to design and implement. This translator has a similar flavor to the many combinator translations of the lambda calculus (e.g., [27]). The availability of sophisticated compiler generator tools such as Ox [8] made this part of the project straightforward.

On the other hand, translation from KOLA to SQL was more tricky. The problem here was specifying *exactly* the sublanguage of KOLA that *could* be translated into SQL.

**Basic Function Formers**  $\mathbf{T}^{-1} \; [\![(f \,\circ\, g) \, ! \,\, x]\!] \quad = \quad \mathbf{T}^{-1} \; [\![f \, ! \,\, (g \, ! \,\, x)]\!]$  $\begin{array}{rcl} \mathbf{T}^{-1} \llbracket \langle f, g \rangle & ! & x \rrbracket & = & [\mathbf{T}^{-1} \llbracket f & ! & x \rrbracket, \ \mathbf{T}^{-1} \llbracket g & ! & x \rrbracket ] \\ \mathbf{T}^{-1} \llbracket \mathsf{K}_{f} & (x) & ! & y \rrbracket & = & \mathbf{T}^{-1} \llbracket x \rrbracket \\ \mathbf{T}^{-1} \llbracket \mathsf{C}_{f} & (f, & x) & ! & y \rrbracket & = & \mathbf{T}^{-1} \llbracket x \rrbracket \\ \end{array}$ Basic Predicate Formers  $\begin{array}{rcl} \mathbf{T}^{-1} \llbracket (p \oplus f) ? x \rrbracket &=& \mathbf{T}^{-1} \llbracket p ? (f ! x) \rrbracket \\ \mathbf{T}^{-1} \llbracket (p \And q) ? x \rrbracket &=& (\mathbf{T}^{-1} \llbracket p ? x \rrbracket) \text{ AND } (\mathbf{T}^{-1} \llbracket q ? x \rrbracket) \\ \mathbf{T}^{-1} \llbracket \sim (p) ? x \rrbracket &=& \operatorname{NOT} (\mathbf{T}^{-1} \llbracket p ? x \rrbracket) \\ \mathbf{T}^{-1} \llbracket \sim (p) ? x \rrbracket &=& \mathbf{T}^{-1} \llbracket p ? x \rrbracket) \\ \mathbf{T}^{-1} \llbracket \mathsf{K}_{p} (b) ? x \rrbracket &=& \mathbf{T}^{-1} \llbracket b \rrbracket \\ \mathbf{T}^{-1} \llbracket \mathsf{C}_{p} (p, x) ? y \rrbracket &=& \mathbf{T}^{-1} \llbracket p ? [x, y] \rrbracket$ Query Function Formers SELECT  $(\mathbf{T}^{-1} \llbracket f ! x \rrbracket)$  $\mathbf{T}^{-1}$  [[iterate (p, f) ! A]] = FROM x IN AWHERE  $(\mathbf{T}^{-1} [\![p ? x]\!])$  $\mathbf{T}^{-1} \begin{bmatrix} \mathbf{join} \ (p, \ f) \ ! \\ [\mathbf{join} \ (\mathbf{K}_p \ (\mathbf{true}), \ \mathbf{id}) \ ! \\ [\dots \\ [\mathbf{join} \ (\mathbf{K}_p \ (\mathbf{true}), \ \mathbf{id}) \ ! \\ [A_1, \ A_2], \dots \ ], \ A_n] \end{bmatrix}$ SELECT  $(\mathbf{T}^{-1} [\![f ! [\ldots [x_1, x_2], \ldots], x_n]\!])$ = FROM  $x_1$  IN  $A_1, \ldots, x_n$  IN  $A_n$ WHERE  $(\mathbf{T}^{-1} [ p ? [ \dots [x_1, x_2], \dots ], x_n ] ])$ SELECT  $(\mathbf{T}^{-1} [\![f ! [x_1, x_2]]\!])$  $\mathbf{T}^{-1}$  [join  $(p, f) ! [A_1, A_2]$ ]  $= \quad \text{FROM } x_1 \text{ IN } A_1, \ x_2 \text{ IN } A_2$ WHERE  $(\mathbf{T}^{-1} [ p ? [x_1, x_2] ] )$ 

Table 6.7:  $\mathbf{T}^{-1}$ : Applied to KOLA Formers

Some restrictions are easy. For example, **flat** can never be translated into SQL because the input to this function (a nested collection) is forbidden by the flatness restrictions of the relational model. Other restrictions are harder to specify. For example, queries of the form, **iterate** (p, f) ! A, can be translated into KOLA, but only in certain cases. For example,

- f cannot be another **iterate** or **join** query,
- f can be a composition of some functions (e.g., add  $\circ \langle \text{terms}, K_f(1) \rangle$ ) but not others (e.g., lgst\_cit  $\circ$  reps) that translate into path expressions.

Our approach to this issue is unsatisfying in the long term. In defining our KOLA  $\rightarrow$  SQL translation function,  $\mathbf{T}^{-1}$ , we assumed that inputs were generated from the pipeline of (1) the Query Lite  $\rightarrow$  KOLA translator, (2) the NormTrans query rewrite, and (3) the PEWhere rewrite. In fact,  $\mathbf{T}^{-1}$  is not defined for all of KOLA, and worse, would translate some queries that were not produced by the pipeline into queries not recognized by SQL.

The long term solution of this problem will be to somehow characterize useful sublanguages of KOLA (depending on the underlying object  $\rightarrow$  relational data model mapping) that can be translated into SQL. We consider this challenge to be extremely important. Query rewriting is likely to become the primary technique for reusing query processing software with new kinds of queries. San Francisco provides one example of this, extending the capabilities of the DB2 query processor to handle object-oriented queries. But we foresee other applications to object database products that want to provide query support for OQL or SQL3 while using existing optimizer technology, and heterogeneous databases that might want to rewrite queries expressed over an entire federation of databases into separate queries specific to the individual databases included within the federation. We believe KOLA to be an ideal intermediate representation for these efforts, both because of its expressive power and because KOLA rewrites are verifiable with a theorem prover. But this will require far more precision in specifying sublanguages of KOLA that will serve as targets for query rewriting (e.g., the sublanguage of KOLA that can be translated into SQL).

In short, the integration of the COKO-KOLA framework within existing query processing systems requires translation to and from KOLA. Translation to KOLA is not a problem; already KOLA is expressive enough to express queries in the most complex of query languages such as OQL, and can be readily extended when it falls short in this regard (e.g., as it does presently with respect to lists and arrays). However, translation *from* KOLA will often be to a language with less expressive power than KOLA (such as SQL). Understanding exactly what are interesting sublanguages of KOLA that can be translated (and therefore is the target for query rewriting) represents a challenging component of future work.

## 6.5.2 Ease-Of-Use of COKO-KOLA

For the San Francisco project, we used COKO-KOLA to generate:

- 1. a library of general-purpose normalization and simplification transformations (presented in Section 6.3.1),
- 2. a normalization to make the KOLA queries resulting from translation from OQL or Query Lite more intuitive (presented in Section 6.3.2), and
- 3. a transformation to rewrite Query Lite queries with path expressions in their WHERE clauses to SQL join queries (presented in Section 6.3.3).

Of these generated rewrites, the third by far was the easiest to write. This transformation rewrites queries with any number of path expressions, of any length, and with any degree of sharing. Yet, the transformation itself required fewer than 20 lines of firing algorithm code. The ease with which this transformation was written is encouraging, as it is exactly these kinds of transformations that are most likely to be developed for optimizers.

On the other hand, by far the most difficult transformation to write was the translation normalization transformation, NormTrans, and all of its auxiliary transformations. This transformation required over 50 rewrite rules, roughly 100 lines of firing algorithm code. Further, this work is not yet complete. This transformation presently does not normalize queries that are nested in their SELECT clauses (i.e., iterate or join queries with iterate or join queries as their data functions). While we believe that this part of the normalization will not be difficult to add (it will likely require merging the functionality of transformations SimpFunc and FactorK), the task has clearly proved to be non-trivial.

Of course, it should be remembered that this normalization need only be written once and users of the COKO-KOLA framework would most likely get NormTrans from a library of rewrites at their disposal, rather than programming it themselves. But on the other hand, our experience writing this transformation was revealing in certain deficiencies of COKO as a programming language and development environment. It is these revelations that will motivate improvements in future versions of the language and compiler. Amongst our observations are the following:

**COKO's Control Language** This exercise provided quite a bit of experience with COKO's language for firing algorithms, and revealed certain parts of the language that could be improved. One aspect of the language that requires some additional thought is the association of success values with statements in the language. For some statements (e.g.,

rule firings and complex statements), success values are quite natural. COKO provides for concise expression of algorithms such as that which exhaustively applies a set of rules:

BU {ru1 || ... || run} 
$$\rightarrow$$
 recursive call

or which conditionally executes a statement  $(S_2)$  if another statement  $(S_1)$  succeeds and a different statement  $(S_3)$  if it fails:

$$S_1 \rightarrow S_2 \parallel S_3.$$

But for other statements, the success values associated with the statements sometimes ran counter to the desired flow of control. The most obvious example of this concerns the GIVEN statement. GIVEN statements have the form,

GIVEN 
$$eqn_1, \ldots, eqn_n$$
 DO S.

and return a success value of *true* if all equations,  $eqn_i$  succeed in unifying and *false* otherwise. While this success result is desirable sometimes, at other times the desired result is to return *true* if all equations succeed in unifying **and** statement *S* succeeds. To address this problem, we could change the default success value for GIVEN statements to return *true* if both equations and follow-up statement succeed. Then, one could simulate the old behavior of GIVEN (i.e., return *true* if all equations succeed regardless of the success value of the follow-up statement) by writing:

GIVEN 
$$eqn_1, \ldots, eqn_n$$
 DO {TRUE S}.

The other part of the firing algorithm language that deserves reconsideration are the success values associated with ";"-separated statements. Presently, a complex statement,

$$S_1; \ldots; S_n$$

succeeds if any statement,  $S_i$  succeeds. Often though, what one desires is for this statement to succeed if one of a particular subset of statements succeeds. The only way to express this presently is to preface those statements that should not figure into the determination of the success value with FALSE, as in:

FALSE 
$$\{S_1\}; \ldots;$$
 FALSE  $\{S_n\}$ 

such that all statements  $S_i$  would be replaced by FALSE  $\{S_i\}$  except for those whose success should influence the success of the entire complex statement. Ideally however, we would like to avoid the use of TRUE and FALSE statements, as their sole purpose is to circumvent the default success values of statements. Eliminating these statements may require us to rethink the entire notion of success values completely, perhaps restricting success values to rule and transformation invocations and adding if-then-else statements to the firing algorithm language to express desired control.

**Parameterized (or Template) COKO Transformations** In Section 6.3.1, we described a COKO transformation (LBComp) that has an identical firing algorithm and rewrite rules to transformation LBConj of Figure 4.10, but for the substitution of one former symbol ( $\circ$ ) for another (&) and one set of variables (function variables) for another (predicate variables). This example suggests another way that COKO could be improved, by allowing the definition of parameterized transformations (e.g., LB) such that different instantiations would generate different COKO transformations (e.g., LB (&, p, q, r) could generate LBConj while LB ( $\circ$ , f, g, h) could generate LBComp.

**Pattern Matching Associative Formers** One of the most time-consuming programming tasks is to account for the various ways that associative functions and predicates (e.g.,  $(f \circ g \circ h)$  or (p & q & r)) can be associated. Presently, we address this problem by normalizing functions and predicates in advance so that a certain association can be assumed (e.g., LBComp and LBConj make compositions and conjunctions left-associative (or "leftbushy")). But determining the associative structure guaranteed of transformation results (when such guarantees are possible) is difficult, and frequently we find ourselves normalizing perhaps unnecessarily, to ensure that functions and predicates are structured in a particular way.

In the long term, we believe that a better approach to this problem will be to adapt our matching algorithm to account for associative function and predicate formers. That is, under this scheme the pattern,

$$f \circ g \circ h$$

would match either possible association of compositions,

$$f \circ (g \circ h)$$
 or  $(f \circ g) \circ h$ .

This approach is taken by theorem provers such as LP [46].

**Speed of Generated Code** The query rewrites that are generated from COKO transformations sometimes have poor performance. For example, while transformation PEWhere performs well on "small queries" such as those of Figures 6.21a and Figures 6.22a, it is noticeably slower with larger queries such as that of Figure 6.23a, requiring upwards of 3 minutes to perform the desired rewrite on a 200Mz Sparcstation 10.

We need to examine our compiler implementation to find the performance bottleneck, but there are many areas that could be contributing factors. Among them:

• As described in Chapter 4, our COKO compiler was designed for simplicity rather than performance. The code it produces generates a parse tree for the compiled transformations, and then invokes a method (exec) on its root (triggering subsequent calls to exec in descendants of the tree). This approach was simple and made it easy to extend the language with new statements (as we did by adding TRUE, FALSE and SKIP statements, and as is done with the definition of every new COKO transformation). However, the resulting code frequently has inadequate performance. For example, the COKO statement,

$$S_1;\ldots;S_n$$

gets compiled into code that builds a binary parse tree of minimum height n, as each ";" appears as a node in the tree with the two statements it separates as its immediate children. This design results in a great deal of information passing (e.g., environments of pattern variables must be passed between parse tree nodes) and thereby puts a strain on performance. Further, the generated parse trees can be so large that the C++ compiler cannot generate the code that builds them. We have often been forced to "break up" COKO transformations into separate subparts in order to get around this deficiency.

• In Chapter 4, we showed an example of the kinds of efficiency one can get by having fine control of rule firing. Transformation CNF exhibited far better performance with a sophisticated and selective firing algorithm, then it did when implemented as an algorithm that exhaustively applies deMorgan rules.

Unfortunately, we have not yet developed a methodology for developing efficient firing algorithms such as that for CNF. Many of the algorithms used for the rewrites presented in this chapter are naive in their application of rewrite rules. For example, transformation PCFAux, an auxiliary transformation to PullComFunc that collapses subpredicates with common subfunctions (see Section 6.3.1), uses an algorithm analagous to a bubble-sort algorithm in order to compare subfunctions appearing in a predicate. Part of the problem lies with the inherent limitations of the rule-based approach which demands that algorithms be composed from local operations (individual rule firings). But at the very least, the performance of firing algorithms used in our library of common normalizations and simplifications should be improved, given how often these transformations are likely to be used. But we look forward to future study of a methodology for writing firing algorithms that minimizes failed rule firings, achieving for all transformations what we were able to achieve for CNF.

• As described in Chapter 5, our implementation of semantic query rewrites invokes a Prolog interpreter druing rewriting to issue a semantic query. As in the case of PEWAux, semantic queries can be posed numerous times during the course of rewriting. (For example, in rewriting the relatively simple query of Figure 6.22a, the conditional rewrite rule, pe2j was fired 9 times (succeeding 4 times).) Each call to the Prolog interpreter incurs a tremendous amount of overhead from loading and initializing the interpreter, and converting to and from Prolog representations of KOLA expressions. We believe that performance of generated rewrites will improve greatly once our Prolog-based implementation of semantic query rewrites is replaced by specialized pattern matching routines for KOLA trees.

In short, the message from our experience is that the COKO-KOLA framework potentially has much to offer in the development of "real-world" query rewriters given its formal foundation. But for this potential to be realized, its implementation must grow beyond its present prototype status. We were especially encouraged by the concise and elegant manner with which we were able to express the path expression-to-join query rewrite described in Section 6.3.3. This rewrite exploited all facets of the COKO-KOLA framework, including the semantic rewrite facility in order to infer knowledge of foreign keys, and recursive firing algorithms to ensure the handling of an unbounded number of path expressions of unbounded length and unbounded degree of subexpression sharing. But while our implementation is adequate as a proof of concept, it still is only a research prototype.

## 6.6 Chapter Summary

In this chapter, we have described our experiences using the COKO-KOLA framework presented in the preceding three chapters. Our challenge was to use COKO-KOLA to develop a query rewriting facility for an experimental language for the IBM San Francisco project. The query rewriter developed would translate object-oriented queries expressed in a simple object-oriented query language, into equivalent SQL queries over the underlying relational implementation of the object-oriented database.

This project allowed us to determine the ease with which generated rewrites could be integrated within existing query processor environments, and with which "real" query rewrites could be expressed. To support integration, we built translators to translate Query Lite and OQL queries into KOLA, and to translate KOLA queries into SQL. This work revealed a challenging future direction in specifying sublanguages of KOLA equivalent in expressive power to other known languages (e.g., SQL), but also showed our framework to be easily integrated into existing query processor settings. To assess ease of use, we analyzed the size and effort required to build COKO transformations that were general purpose normalization and simplification routines, normalizations specific to the result of translation, and Query Lite  $\rightarrow$  SQL rewrites. Surprisingly, the library of normalizations (especially the normalization of translated queries) proved most difficult to build. But the experience revealed to us deficiencies in the COKO language and compiler implementation that must be addressed in future versions. Most encouraging to us was the ease with which we were able to write the transformation that did the "actual work" of the query rewrite. Transformations PEWhere and PEWAux required few rules and few lines of firing algorithm code to express a powerful and useful query rewrite.

## Chapter 7

# **Dynamic Query Rewriting**

In Chapters 3, 4 and 5, we proposed a framework for the expression of query rewrites. In Chapter 3, we presented KOLA: a combinator-based query algebra and representation that supports the expression of simple query rewrites with declarative rules. In Chapter 4, we introduced COKO: a language for expressing complex rewrites in terms of sets of KOLA rules and firing algorithms. And in Chapter 5, we introduced extensions to COKO and KOLA that made it possible to express rewrites whose correctness depended on semantic properties of queries and data. All of the rewrites presented in these chapters are verifiable with a theorem prover. This is due to the combinator flavor of KOLA that makes it possible to express subexpression identification and query formulation without code.

In this chapter, we consider another benefit arising from KOLA. This work concerns when query rewrites get fired rather than how they get expressed. An intelligent decision about how to rewrite or evaluate a query requires knowing the representations and contents of the collections involved (e.g., whether or not collections are indexed, sorted, or contain duplicates). Dynamic query rewriting (query rewriting that takes place during the query's evaluation) incorporates this philosophy in settings where this information is not known until data is accessed (i.e., until run-time). Such settings include:

- *object databases* that permit queries on anonymous, embedded collections whose contents and representations might only become apparent at run-time,
- *network databases* (e.g., web databases) that permit queries on collections whose availability can vary every time the query is executed, and
- *heterogeneous databases* that permit queries on collections maintained by local databases with data models and storage techniques known only to them.

Dynamic query rewriting requires that a query evaluator identify subexpressions of the processed query, and formulate new queries to ship to the query rewriter for further processing. Because KOLA simplifies the expression of these tasks, it is an ideal underlying query representation.

The work described in this chapter is ongoing and focuses on the application of dynamic query rewriting to object databases. We have designed a dynamic query rewriter for the ObjectStore object-oriented database [67], and an implementation of this design is in development.<sup>1</sup> We present this design using the "NSF" query ( $NSF_2$  of Figure 2.6) as a running example. After presenting the design of the dynamic query rewriter for ObjectStore in Section 7.1, we trace the evaluation and rewriting of this query in Section 7.2. Finally, we consider some performance issues that have yet to be addressed and again look at the role of KOLA in the design of the query rewriter in Section 7.3, before summarizing the chapter in Section 7.4.

## 7.1 A Dynamic Query Rewriter for ObjectStore

The potential heterogeneity of collections in an object database makes it sometimes appropriate for evaluation strategies to vary from object to object. In Chapter 2, we introduced the query  $NSF_2$  (Figure 2.6) that pairs every bill concerning the NSF with the largest cities in the regions represented by the bill's sponsors. The collection of bills queried (Bills) can contain both House and Senate resolutions whose sponsors are sets of House Representatives and Senators respectively. The path expression,  $x.reps.lgst_cit$ , that finds the largest city in the region represented by legislator x, is an injective function over objects of type *Representative*, but not over objects of type *Senator*. Therefore, a semantic query rewrite to eliminate redundant duplicate elimination (as described in Section 5.1) must be applied selectively to affect the processing of House resolutions but not the processing of Senate resolutions. Dynamic query rewriting is query rewriting that occurs during a query's evaluation (i.e., at run-time). Selective processing of  $NSF_2$  can be achieved by firing the duplicate elimination query rewrite dynamically as bills are retrieved and their origins (House or Senate) identified.

We have designed a dynamic query rewriter and query evaluator for ObjectStore [67], and the implementation and evaluation of this design is ongoing work. This design deviates from the traditional query processor architecture presented in Chapter 1 (Figure 1.1). The

<sup>&</sup>lt;sup>1</sup>ObjectStore already performs a limited form of dynamic query optimization involving run-time exploitation of indexes, but does nothing by way of dynamic query rewriting.



Figure 7.1: An Alternative Architecture for Object Database Query Processors

new architecture (illustrated in Figure 7.1) introduces a *feedback loop* between evaluation and rewriting (labeled A in Figure 7.1), as well as incorporating the semantic rewrite components described in Chapter 5 (B). The input to the evaluator is not a complete plan, but a *partial plan* with "holes" left for those parts of the plan that will be generated dynamically.

To implement this architecture, our design includes two components:

- a *plan language* that permits expression of partial plans, and
- a *query evaluator* with hooks back to the optimizer.

After describing these two components, we demonstrate their intended behavior with respect to the processing of query  $NSF_2$ .

## 7.1.1 Making ObjectStore Objects Queryable

The present design of our dynamic query rewriter processes queries over ObjectStore. Our eventual goal is for this design to be usable with other databases also. Therefore, a design



Figure 7.2: The ObjectStore Queryable Class Hierarchy

goal was to maintain a loose coupling between the rewriter and ObjectStore.

Loose coupling is achieved by maintaining separate class hierarchies for ObjectStore objects (which can be stored in an ObjectStore database) and KOLA objects (which can be appear in queries). Because of this design, ObjectStore's implementation requires no modification to account for KOLA querying, and our design need not be restricted to processing ObjectStore objects. The cost of this decision is redundancy in the two class hierarchies, and the need to translate between the two representations during a query's evaluation. Because of the latter issue, a non-prototype design of the dynamic query rewriter would likely integrate the two object representations.

The only requirement we introduce of queryable ObjectStore objects is that they belong to a subclass of a class we provide (OSObject). All attributes of these classes should also have types that are subclasses of OSObject (or OSBool if they are boolean-valued attributes). This ensures that all classes of objects maintained in the database will have a KOLA translation function inherited from OSObject and OSBool (kola), even though designers of such classes may not be aware of this. Other queryable ObjectStore object classes are provided as part of our design (e.g., basic classes such as strings (OSStr) and integers (OSInt)) as is illustrated in the ObjectStore class hierarchy presented in Figure 7.2.

Figure 7.2 includes two of the classes defined for the Thomas database of Section 2 — OSLegislator (*Legislator*) and OSRegion (*Region*). Subtypes could be be defined to inherit from these classes (e.g., *State* could be defined as a subtype of *Region* in this way). This figure also includes a subhierarchy of *iterators* rooted at OSIterator. While instances of these classes are data (returned as the results of collection generating queries), the classes themselves comprise the plan language for KOLA. This design is described below.

## 7.1.2 Iterators

The result of a query can be very large. If a query returns a collection, this collection might contain many objects (i.e., the result might have a large *cardinality*). As well, each object in the result might include other collections and other complex objects as attributes (i.e., the result might have a large *arity* also). Thus, it would be inappropriate for a query processor to return a query result "all at once" and instead a more lazy approach is called for.

Like many query processors (e.g., Exodus [13]) KOLA's plan language merges query results with the plans to retrieve them. An *iterator* is a *view* for a given collection with a specialized interface that provides access to the collection one element at a time. Queries that construct collections in fact return iterators. Thus, iterators serve as both data and plan.

Our design defines several kinds of iterators (all subclasses of OSIterator) that can be returned as the result of a query. There is at least one iterator per KOLA query former or primitive, although not all are shown in Figure 7.2. Designed in an object-oriented style, each iterator is obligated to provide implementations of the following methods:

- open: which opens all files required by the iterator to retrieve elements, and which initializes any data structures required for processing,
- next: which returns the next element of the collection maintained by the iterator,
- finished: which returns *true* if there are no more elements to return,
- close: which closes all files and data structures opened or created by the iterator, and
- set: which constructs a new stored collection (and accompanying iterator) with duplicates removed.<sup>2</sup>

 $<sup>^{2}</sup>$ Set builds a new stored collection, because our assumption is that duplicate elimination is necessary

Thus, if one views a plan language as a collection of algorithms, the method implementations for the collection of iterators comprise the KOLA plan language.

Iterators can range over collections stored on disk (access methods), or collections generated on the fly (query operators). Our design introduces the class OSSource to act as the supertype of all access method iterators, and **OSSieve** to act as the supertype of all query operator iterators. Examples of the latter include OSBasicSieve, OSMapSieve and OSFilterSieve. Objects of class OSBasicSieve act as a view with respect to some KOLA predicate p and function f over the result of some other iterator, i. Calling next on an **OSBasicSieve** results in repeated calls of **next** on i until some element is returned that satisfies p (or until the entire collection has been processed at which point an "End-Of-Collection" token is returned). Function f is then applied to this element and the result is returned. On the other hand, an OSMapSieve acts as a view solely with respect to a KOLA function f over the result of some other iterator, i. Calling next on an OSMapSieve results in a single call of next on i, with f applied to the result and returned. Finally, an OSFilterSieve acts as a view with respect to a KOLA predicate p over the result of some other iterator, *i*. As with an OSBasicSieve, calling next on an OSFilterSieve repeatedly calls next on i until some element is returned that satisfies p. Unlike an OSBasicSieve, this element is then returned as is. Our simple plan generator generates an OSBasicSieve for queries of the form,

iterate (p, f) ! A,

an OSMapSieve for queries of the form,

iterate 
$$(K_p (true), f) ! A$$
,

and an OSFilterSieve for queries of the form,

iterate 
$$(p, id) ! A$$
.

Other iterators are defined for other KOLA query formers. For example, there are two *join* iterators, each of which references a KOLA predicate, p, a KOLA function, f and two input iterators,  $i_1$  and  $i_2$ . Class OSNestedLoopSieve does no preprocessing in its open method, and a call to next iterates through  $i_2$  looking for an element that together with the last read element of  $i_1$ , satisfies p. (If none is found, the next element of  $i_1$  is retrieved and the process repeats itself.) Thus, this iterator performs a *nested loop* join. The open

if set is executed. Queries for which duplicate elimination is recognized as unnecessary get rewritten into plans that do not execute set.

method of OSMergeSieve sorts  $i_1$  and  $i_2$ , creating two temporary OSSource iterators for the results of the sorts. A call to next then scans these sorted collections in parallel, thus performing a *sort-merge* join.

The two most important features of these iterators are that they are *extensible* and that they support the *partial specification* of plans. The object-oriented design of iterators (i.e., all iterator implementations inherit from **OSIterator**) makes it straightforward to *extend* the plan language by adding additional iterators. For example, an iterator that uses an index to filter objects contained in a collection could be added as a subclass of **OSSieve**. Objects of this class could then be returned by **iterate** queries when indexes are available on the data predicate. Our present design includes a simplistic plan generator that associates most KOLA query formers with only a single iterator. But because additional subclasses of **OSIterator** such as the ones above can be simply added, plan generation can be made more sophisticated without disrupting the other components of the optimizer.

Iterators also support the partial specification of plans. All query operator iterators (i.e., objects belonging to subclasses of OSSieve) specify one or more iterators from which data elements are drawn, and an operation to perform on these data elements. Data operations are not specified with plans but with KOLA functions and predicates. In this way, an iterator only partially specifies a plan. To complete the specification, each data element retrieved can be packaged with the associated KOLA predicate or function and resubmitted as a new query to the query rewriter. That is, KOLA functions and predicates serve as specifications for the missing components of a plan, describing what the missing plan must produce without committing to an algorithm. Partial specifications of plans make dynamic query rewriting possible, marking the parts of a plan for which details must be supplied at run-time.

## 7.1.3 Combining Rewriting With Evaluation

Translation of OQL queries results in KOLA parse trees. The nodes of KOLA's parse trees are instances of classes whose hierarchy is shown in part in Figure 7.3. The mappings of KOLA functions, predicates, objects and bools to their associated classes within this hierarchy are shown in Table 7.1. All function (predicate) classes are subclasses of KFunction (KPredicate), obligating them to provide implementations for virtually defined methods invoke and exec. As will be described in some detail below, invoke performs partial evaluation and query rewriting, and exec performs full evaluation and plan generation for the function (predicate) denoted by the KFunction (KPredicate) parse tree. All object (bool)



Figure 7.3: The KOLA Representation Class Hierarchy

KOLA Operator $(q)$	Node Class	Comment			
Subclasses of KFunction					
id	KFID	-			
set	KFSet	_			
$\langle f, \ g  angle$	KFPair	one is $f$ , two is $g$			
$f \circ g$	KFCompose	one is $f$ , two is $g$			
iterate $(p, f)$	KFIterate	one is $p$ , two is $f$			
any attribute	KFAttr	val is the name of the attribute			
Subclasses of KPredicate					
eq	KPEqual	_			
$K_p(b)$	KPConst	one is $b$			
$p  \oplus  f$	KPOPlus	one is $p$ , two is $f$			
Subclasses of KObject					
f ! x	KOInvoke	one is $f$ , two is $x$			
[x, y]	KOPair	one is $x$ , two is $y$			
any string constant	KOStr	val is the string constant			
any ObjectStore object	KOWrapper	val is the ObjectStore object			
any object name	KOName	val is the object name			
Subclasses of KBool					
p ? x	KBInvoke	one is $p$ , two is $x$			
true or false	KBConst	val is the truth value			

Table 7.1: Mappings of KOLA Operators to their Parse Tree Representations

classes are subclasses of KObject (KBool), obligating them to provide implementations for virtually defined methods obj and res: methods that call invoke and exec respectively.

In describing how a query is processed, we will refer to KOLA expressions and their parse trees interchangably and rely on context to differentiate between the two. For example, the expression,

$$(set ! A) \rightarrow obj ()$$

denotes a call of method obj on the parse tree representation of (set ! A). In other words, method obj defined in class KOInvoke (written KOInvoke::obj) gets invoked on the associated KOLA tree. As much as possible in this discussion, we will supplement such expressions with descriptions that point out which methods defined in which classes get invoked.

### Partial Evaluation and Query Rewriting

True to object-oriented style, evaluation routines are distributed across the KOLA tree representations they affect. Whereas evaluation (and plan generation) occur as a result of calls to exec (for function and predicate nodes) and res (for object and bool nodes), query

rewriting (and partial evaluation) occur as a result of calls to **invoke** (for function and predicate nodes) and obj (for object and bool nodes).

The processing of a KOLA query, q occurs as a result of the chain of calls,

$$q$$
  $ightarrow$  obj ()  $ightarrow$  res ()

which invokes method obj on the parse tree representation of q, and method **res** on the parse tree resulting from the invocation of obj. The call of obj performs query rewriting and partial evaluation on q. (The call of **res** returns an iterator, as discussed in the next section.) For queries of the form (f ! x) that apply functions or predicates to objects, the call

$$(f ! x) \rightarrow \text{obj}$$
 ()

executes KOInvoke::obj, resulting in the subsequent call of,

$$f \rightarrow \text{invoke} (x \rightarrow \text{obj} ()).$$

Thus, invoke and obj are related functions that initiate query rewriting and partial evaluation.

Invoke is defined differently for different functions and predicates. Basic function formers perform evaluation of the query up to the point where disk access is required or methods are invoked. Thus, the call,

```
id \rightarrow invoke (x)
```

(KFID::invoke) completely evaluates the expression, (id ! x), returning (the parse tree representation of) x. In this case invoke fully evaluates the function invocation (id ! x). On the other hand, for any attribute att,

att 
$$\rightarrow$$
 invoke (x)

(KFAttr::invoke) returns

att ! x

(i.e., a KOLA parse tree rooted by a KOInvoke object), performing no evaluation at all. In general, invoke partially evaluates a query, as in

$$\langle \mathbf{id}, \, \mathtt{att} 
angle \, o \, \mathtt{invoke}$$
 (x)

that returns the partially evaluated KOPair,

[x, att ! x].

When invoked on query functions or predicates, invoke initiates query rewriting. Every KOLA function and predicate node can be associated with its own rewriter generated from a COKO definition. Thus, KOFSet (set) might be associated with a transformation that invokes rules de1 and de2 of Figure 5.3, and KFIterate (iterate) might be associated with a COKO transformation that performs normalization with respect to iterate queries. Most likely, only nodes representing query formers will be associated with rewriters. If the parse tree representation of some function f is instantiated with a COKO transformation object, t, then

$$f$$
  $\rightarrow$  invoke (x)

generates a call to t's exec method (see Section 4.3.3) with the parse tree representation of  $(f \ x)$  as its argument. The rewriter then returns the representation for an equivalent expression that has been normalized in some way. Definitions of obj for some subclasses of KObject and KBool, and invoke for some subclasses of KFunction and KPredicate are presented in the tables of Table 7.2.

#### **Evaluation and Plan Generation**

Just as obj and invoke initiate query rewriting and partial evaluation, res and exec initiate plan generation and complete evaluation. And analagously to obj and invoke, res and exec are related in that the call,

$$(f ! x) \rightarrow \text{res}$$
 ()

for some KOLA function f and KOLA object x generates the call,

$$f \rightarrow$$
 exec ( $x \rightarrow$  res ()).

As with invoke, exec is defined differently for different KOLA functions and predicates. For KOLA query functions and predicates, exec returns an iterator over the collection that the query denotes. For attributes, exec performs attribute extraction. For KOLA's arithmetic functions (add, mul, etc.) exec performs the arithmetic.

Our simplistic plan generator performs no data analysis in deciding upon an iterator to return as the result of evaluating a query. Most formers generate a single iterator. (The former, **iterate** is an exception as it can generate an OSBasicSieve, OSMapSieve or OSFilterSieve.)<sup>3</sup>

 $<sup>^{3}</sup>$ A more sophisticated plan generator would generate multiple iterators and choose a best amongst them based on some cost model that estimates the cost of retrieving elements from each.
KOLA Class	obj ()			
KObject				
KOInvoke	one $ ightarrow$ invoke (two $ ightarrow$ obj ())			
KOStr	self			
KOName	self			
KOWrapper	self			
KOPair	KOPair (one $ ightarrow$ obj (), two $ ightarrow$ obj ())			
KBool				
KBInvoke	one $ ightarrow$ invoke (two $ ightarrow$ obj ())			
KBConst	self			

KOLA Class	invoke (k: KObject)		
KFunction			
KFID	k		
KFMethod	KOInvoke (self, k)		
KFCompose	KOInvoke (one, KOInvoke (two, k))		
KFPair	KOPair (KOInvoke (one, k), KOInvoke (two, k))		
KFSet	Calls optimizer on KOInvoke (self, k)		
KFIterate	Calls optimizer on KOInvoke (self, k)		
KPredicate			
KPEqual	KBInvoke (equal, k)		
KPConst	one		
KPCurry	one $ ightarrow$ invoke (OPair (two, k))		
KPOPlus	one $ ightarrow$ invoke (two $ ightarrow$ invoke (k))		

Table 7.2: Results of Partially Evaluating and Rewriting KOLA Queries

KOLA Class	res ()		
KObject			
KOInvoke	one $ ightarrow$ exec (two $ ightarrow$ res ())		
KOStr	OSStr (val)		
KOName	Performs lookup of val in database.		
	Returns object stored, if not a collection.		
	Returns an OSSource, if a collection.		
KOWrapper	val		
KOPair	STRUCT (one: one $ ightarrow$ res (), two: two $ ightarrow$ res ())		
KBool			
KBInvoke	one $ ightarrow$ exec (two $ ightarrow$ res ())		
KBConst	val		

KOLA Class	exec (o: OSObject)			
KFunction				
KFID	Never called			
KFMethod	Calls method on $\circ$			
KFCompose	Never called			
KFPair	Never called			
KFSet	(o $ ightarrow$ res ()) $ ightarrow$ set ()			
KFIterate	<pre>{ OSMapSieve (two, o), OSFilterSieve (one, o), OSBasicSieve (one, two, o),</pre>	$if \text{ one } = K_p \text{ (true)}$ if  two  = id otherwise		
KPredicate				
KPEqual	o.one == o.two			
KPConst	Never called			
KPCurry	Never called			
KPOPlus	Never called			

Table 7.3: Results of Evaluating KOLA Queries

The definitions of res for some subclasses of KObject and KBool, and exec for some subclasses of KFunction and KPredicate are presented in the tables of Table 7.3. Note that for some function and predicate representation nodes (e.g., KFID, KFCompose), exec will never be called as calling invoke beforehand will transform query representations using these nodes into representations that don't.

 $NSF_k$  = iterate (p, f) ! Bills such that

Figure 7.4:  $NSF_{2k}$ : The KOLA Translation of Query  $NSF_2$  of Figure 2.6

## 7.2 Putting It All Together: The NSF Query

We illustrate our design by tracing the processing of the KOLA version of  $NSF_2$  ( $NSF_{2k}$ ) shown in Figure 7.4. Figure 7.5 illustrates the parse tree representation of this query over which query evaluation takes place via successive calls of obj and res.

## 7.2.1 Initial Rewriting and Evaluation

For query  $NSF_{2k}$ , there is little query rewriting or partial evaluation that can be performed until data is touched. Calling obj on the parse tree representation of this query returns the parse tree untouched. A subsequent call of **res** returns an OSBasicSieve with

- the parse tree representation of  $(C_p (eq, "NSF") \oplus topic)$  as its predicate, p,
- the parse tree representation of

 $\langle \texttt{name, set} \circ \textbf{iterate} \ (\texttt{K}_p \ (\texttt{true}), \ \texttt{lgst\_cit} \circ \texttt{reps}) \circ \texttt{spons} \rangle$ 

as its function, f, and

• The iterator object for Bills (i.e., an OSSource object) as its inner iterator, *i*.

This result is illustrated in Figure 7.6. In this figure and in others that include both KOLA and ObjectStore objects, the two are differentiated by their shape: KOLA objects are drawn with circles while ObjectStore objects are drawn with rectangles.

## 7.2.2 Dynamic Query Rewriting: Extracting Elements from the Result

The only query rewriting performed on  $NSF_{2k}$  occurs when objects are retrieved from the query's iterator result. That is, rewriting occurs dynamically as a result of a call of next on the OSBasicSieve of Figure 7.6. A call of next on this iterator in turn calls next on the OSSource iterator for Bills. With each bill *b* returned by this call, a new KOLA expression is formulated using the predicate (p) associated with the OSBasicSieve. The formulated expression packages p with a predicate invocation node (KBInvoke) and the KOLA translation of b (KOWrapper (b)) to construct the parse tree representation of (p ? [[b]]) (such that [[b]] denotes the KOLA wrapper object referencing b). This is illustrated in Figure 7.7 (A). Figure 7.7 (B) shows the result of calling obj on this tree. Figure 7.7 (C) shows the result of calling res on the KOLA pair that is an argument to the predicate, eq. (Evaluation then proceeds by comparing the one and two fields of the struct in (C).)

A trace of the calls of obj and res that lead to each result illustrated in Figure 7.7 is presented below. Each step in the trace shows the "current" representation and the method that was invoked most recently to generate it.

Suppose that b is a House resolution. Calling res on

eq ? ["NSF", topic ! 
$$\llbracket b \rrbracket$$
]

leads to the comparison of the fields of the ObjectStore STRUCT of Figure 7.7 (C) as illustrated below.

```
(\mathbf{eq} ? ["NSF", topic ! [[b]]] \rightarrow res ())
       eq \rightarrow exec (["NSF", (topic ! [b])] \rightarrow res ())
                                                                                                   (by \; \texttt{KBInvoke} :: \texttt{res})
=
= \mathbf{eq} \rightarrow \mathsf{exec} \; (\mathsf{STRUCT} \; (\mathsf{one:} \; ``\mathsf{NSF}" \rightarrow \mathsf{res} \; (), \; \mathsf{two:} \; (\mathsf{topic} \; ! \; \llbracket b \rrbracket) \rightarrow \mathsf{res} \; ()))
                                                                                                            (by KOPair:res)
\mathbf{e} \mathbf{q} \rightarrow \mathsf{exec} \ (\mathsf{STRUCT} \ (\mathsf{one:} \ ``\mathsf{NSF}", \mathsf{two:} \ (\mathsf{topic} ! \ [\![b]\!]) \rightarrow \mathsf{res} \ ()))
                                                                                                            (by KOString :: res)
= eq \rightarrow exec (STRUCT (one: "NSF", two: topic \rightarrow exec (\llbracket b \rrbracket \rightarrow res ())))
                                                                                                            (by KOInvoke :: res)
\mathbf{e} = \mathbf{e} \mathbf{q} 
ightarrow \mathsf{exec} \; (\mathtt{STRUCT} \; (\mathtt{one:} \; ``\mathtt{NSF}", \; \mathtt{two:} \; \mathtt{topic} 
ightarrow \mathtt{exec} \; (b)))
                                                                                                            (by KOWrapper :: res)
       \mathbf{eq} 
ightarrow \mathbf{exec} \; (\mathtt{STRUCT} \; (\mathtt{one: "NSF", two: } b.\mathtt{topic})) \; \; (by \; \mathtt{KFAttr:: exec})
=
       "NSF" == b.topic
                                                                                                            (by KPEqual :: exec)
=
```

Suppose that *b*.topic == "NSF". Then this expression evaluates to *true* and *b* is packaged with *f* to construct the query tree of Figure 7.8 (A), ( $\langle name, set \circ h \circ spons \rangle$  ! [[*b*]]), such that

 $h = \text{iterate } (K_p \text{ (true)}, \text{lgst_cit} \circ \text{reps}).$ 

Calling obj on this tree results in the query tree of Figure 7.8 (B) as is shown in the

execution trace below.

$$(\langle \operatorname{name, set} \circ h \circ \operatorname{spons} \rangle ! \llbracket b \rrbracket) \to \operatorname{obj} ()$$

$$= \langle \operatorname{name, set} \circ h \circ \operatorname{spons} \rangle \to \operatorname{invoke} (\llbracket b \rrbracket \to \operatorname{obj} ()) \qquad (by \operatorname{KOInvoke} :: \operatorname{obj})$$

$$= \langle \operatorname{name, set} \circ h \circ \operatorname{spons} \rangle \to \operatorname{invoke} (\llbracket b \rrbracket) \qquad (by \operatorname{KOWrapper} :: \operatorname{obj})$$

$$= [\operatorname{name} \to \operatorname{invoke} (\llbracket b \rrbracket), (\operatorname{set} \circ h \circ \operatorname{spons}) \to \operatorname{invoke} (\llbracket b \rrbracket)] \qquad (by \operatorname{KFPair} :: \operatorname{invoke})$$

$$= [\operatorname{name} ! \llbracket b \rrbracket, (\operatorname{set} \circ h \circ \operatorname{spons}) \to \operatorname{invoke} (\llbracket b \rrbracket)] \qquad (by \operatorname{KFAttr} :: \operatorname{invoke})$$

$$= [\operatorname{name} ! \llbracket b \rrbracket, (\operatorname{set} \circ h) \to \operatorname{invoke} (\operatorname{spons} \to \operatorname{invoke} (\llbracket b \rrbracket))] \qquad (by \operatorname{KFAttr} :: \operatorname{invoke})$$

$$= [\operatorname{name} ! \llbracket b \rrbracket, (\operatorname{set} \circ h) \to \operatorname{invoke} (\operatorname{spons} ! \llbracket b \rrbracket)] \qquad (by \operatorname{KFAttr} :: \operatorname{invoke})$$

$$= [\operatorname{name} ! \llbracket b \rrbracket, (\operatorname{set} \circ h) \to \operatorname{invoke} (\operatorname{spons} ! \llbracket b \rrbracket)] \qquad (by \operatorname{KFAttr} :: \operatorname{invoke})$$

(by KFCompose :: invoke)

The next step of this reduction executes Flterate::invoke which fires a COKO transformation to rewrite the query,

iterate (K<sub>p</sub> (true), lgst\_cit  $\circ$  reps) ! (spons !  $\llbracket b \rrbracket$ ).

Suppose that this rewriter has no effect on this query. Then the next step of the execution trace is:

 $[\texttt{name !} \llbracket b \rrbracket, \texttt{ set } \rightarrow \texttt{ invoke (iterate (K_p (true), \texttt{lgst\_cit} \circ \texttt{reps}) ! (\texttt{spons !} \llbracket b \rrbracket))].$ 

At this point, the COKO transformation associated with set is fired to rewrite the query,

 $\texttt{set ! (iterate (K_p (true), lgst_cit \circ reps) ! (spons ! [[b]]))}.$ 

If the COKO transformation is one that eliminates redundant duplicate elimination (firing the rules of Figure 5.3), then the reduction continues as shown below:

1. Firing rule de1 of Figure 5.3 matches the pattern, set ! (iterate (p, f) ! A) with

the above query producing the variable bindings:

$$p = K_p (true)$$
  

$$f = lgst_cit \circ reps, and$$
  

$$A = spons ! [[b]]$$

2. A Prolog query is issued to the Prolog interpreter to determine the truth values of conditions:

and

is\_set (spons ! 
$$\llbracket b \rrbracket$$
).

The latter condition is satisfied by inference rule (2) of Figure 5.4b in combination with schema information establishing the type of **spons** to return a set of House Representatives. The former condition is satisfied by inference rules (2) and (3) of Figure 5.4a in combination with metadata information identifying lgst\_cit as a key for sets of regions, and **reps** as a key for sets of House Representatives.<sup>4</sup>

3. The success of the Prolog query leads to the firing of the conditional rewrite rule, de1, leading to a rewrite of the query that performs duplicate elimination to one that does not:

iterate (K<sub>p</sub> (true), lgst\_cit  $\circ$  reps) ! (spons ! [[b]]).

Thus, the call of next on the OSBasicSieve of Figure 7.6 has led to a dynamic call of the query rewriter to perform the semantic rewrite that eliminates redundant duplicate elimination. The execution trace then concludes, producing the representation,

$$[\texttt{name ! } \llbracket b \rrbracket, h ! (\texttt{spons ! } \llbracket b \rrbracket)]$$

such that

```
h = iterate (K<sub>p</sub> (true), lgst_cit \circ reps).
```

fun (name, D, R)

<sup>&</sup>lt;sup>4</sup>Our implementation resolves overloading (e.g., of attribute **reps**) by translating all references to functions appearing in a schema, metadata files or queries to Prolog terms of the form,

such that name is the name of the function, D is the domain type of the function, and R is the range type of the function. Therefore, fun (kreps, kHouse\_Representative, kRegion) would be identified as a key and fun (kreps, kSenator, kRegion) would not be. A similar representation strategy is applied to predicates.

```
[\texttt{name ! } [b], h] \rightarrow \texttt{res } ()
```

= STRUCT (one: (name ! 
$$\llbracket b \rrbracket$$
)  $\rightarrow$  res (), two:  $h$  ! (spons !  $\llbracket b \rrbracket$ )  $\rightarrow$  res ())  
(by KOPair :: res)

= STRUCT (one: name  $\rightarrow$  exec ( $\llbracket b \rrbracket \rightarrow$  res ()), two: (h ! (spons !  $\llbracket b \rrbracket$ ))  $\rightarrow$  res ()) (by KOInvoke :: res)

= STRUCT (one: name  $\rightarrow$  exec (b), two: (h ! (spons !  $\llbracket b \rrbracket)) \rightarrow$  res ()) (by KOWrapper::res)

= STRUCT (one: *b*.name, two:  $(h \mid (\text{spons } \mid \llbracket b \rrbracket)) \rightarrow \text{res} ()$ ) (by KFAttr :: exec)

 $= \text{ STRUCT (one: } b.\texttt{name, two: } g \to \texttt{exec ((spons ! [\![b]\!]) \to res ()))} \\ (by \;\texttt{KOInvoke :: res)}$ 

= STRUCT (one: *b*.name, two:  $g \rightarrow \text{exec} (\text{spons} \rightarrow \text{exec} (\llbracket b \rrbracket \rightarrow \text{res} ())))$ (*by* KOInvoke :: res)

```
= STRUCT (one: b.name, two: g \rightarrow \text{exec} (spons \rightarrow \text{exec} (b))) (by KOWrapper::res).
Because the bill attribute spons returns a set, the result of the invocation,
```

```
spons \rightarrow exec (b)
```

is an OSSource iterator (which will be expressed through the remainder of the trace as "OSSource (b.spons)". Therefore, the next expression in the execution trace becomes,

STRUCT (one: *b*.name, two:  $g \rightarrow \text{exec}$  (OSSource (*b*.spons))).

Substituting for g, the expression labeled by two is:

```
iterate (K<sub>p</sub> (true), lgst_cit \circ reps) \rightarrow exec (OSSource (b.spons)).
```

Because the predicate argument to **iterate** is  $K_p$  (true), the call of KFIterate::exec generates an OSMapSieve object, which will be written in the remainder of the trace as

"OSMapSieve (lgst\_cit o reps, OSSource (b.spons))". Therefore, the next expression in the execution trace becomes,

STRUCT (one: *b*.name, two: OSMapSieve (lgst\_cit o reps, OSSource (*b*.spons))).

The last step of the trace inserts the field names of the struct (bill and schools) that appeared in the original OQL query and that are retained by translation into KOLA:

#### 7.2.3 Extracting Results from the Nested Query

The result of calling next on the OSBasicSieve of Figure 7.6 itself generates a record (STRUCT) whose second value (schools) is another query operator. As elements from this inner query result can also be extracted via calls to next, this makes it possible for the query rewriter to be called deeply within evaluation. In this case, the function argument of the OSMapSieve is simple enough that the rewriter is not called. A call of next on the OSMapSieve initiates a call of next on the OSSource iterator over b.spons. The result of this latter call (either a Senator or a House Representative, l) results in the formulation of the expression,

$$(\texttt{lgst\_cit} \circ \texttt{reps}) \texttt{!} \llbracket l \rrbracket$$

whose parse tree representation is illustrated in Figure 7.9 (A). A call of obj on this tree generates the KOLA tree of Figure 7.9 (B) as shown below:



Figure 7.5: The Parse Tree Representation of  $NSF_{2k}$ 



Figure 7.6: The result of calling obj and res on the "NSF Query"



Figure 7.7: Calling query  $NSF_{2k}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space{-1.5}\space$ 



Figure 7.8: Calling  $NSF_{2f}{\rm 's}$  data function on a House resolution, b



Figure 7.9: Calling  $NSF_{2k}$ 's inner query function on a House Representative, l

Calling **res** on this KOLA tree generates path expression

```
l.reps.lgst_cit
```

as demonstrated below:

```
(lgst\_cit ! (reps ! [[l]])) \rightarrow res ()
= lgst\_cit \rightarrow exec ((reps ! [[l]]) \rightarrow res ())) \qquad (by KOInvoke :: res)
= lgst\_cit \rightarrow exec (reps \rightarrow exec ([[l]] \rightarrow res ()))) \qquad (by KOInvoke :: res)
= lgst\_cit \rightarrow exec (reps \rightarrow exec (l)) \qquad (by KOWrapper :: res)
= lgst\_cit \rightarrow exec (l.reps) \qquad (by KFAttr :: exec)
= l.reps.lgst\_cit \qquad (by KFAttr :: exec)
```

## 7.3 Discussion

## 7.3.1 Cost Considerations

This chapter describes ongoing work and therefore inspires more questions than answers. Dynamic query rewriting offers potentially enormous benefits for query evaluation given that the wisdom or validity of some rewrites may depend on factors that cannot be determined until run-time. In this chapter, we showed an example query  $(NSF_{2k})$  for which dynamic query rewriting was beneficial. In processing this query, duplicate elimination was avoided in many circumstances where it would have been required otherwise. If duplicate elimination can be avoided multiple times in processing a query and avoided for large collections, enormous savings in evaluation cost are likely.

On the other hand, dynamic query rewriting adds overhead to the cost of evaluating a query. This cost arises because of the need to generate subplans during query evaluation. For ad hoc querying (for which optimization and evaluation occur consecutively), this is not an issue. But for queries that are compiled, an obvious question is whether or not the costs of dynamic optimization outweigh its potential benefits.

Once our implementation is complete, this question will need to be addressed. But there are reasons for optimism. First, dynamic query rewriting need not invoke the large and expensive query rewrite routines that are likely to be invoked statically. Our present design permits distinct COKO transformations to be associated with each KOLA query operator. These rewriters could be quite simple, and perform only those rewrites that offer large cost savings that justify the cost of dynamic rewriting. The rewrite to avoid redundant duplicate elimination is one such example. The cost of the semantic reasoning needed to decide whether duplicate elimination can be avoided is modest, but the potential cost savings from avoiding duplicate elimination (especially for large collections) can be enormous.

A second reason for optimism is that it may be possible to streamline the rewriting that does occur dynamically. For example, *memoization* of the results of semantic queries could greatly improve performance. Consider the example we presented in this chapter. For this example, there are only two possibilities considered during semantic rewriting. Either a bill is a House resolution for which duplicate elimination is avoidable, or it is a Senate resolution for which duplicate elimination is required. Given the present design, the processing of each bill results in one of two semantic queries being generated:

1. Is A a set given that it consists of sponsors of a House resolution, and is

#### lgst\_cit o reps

injective given that it is a function over House Representatives?, or

2. Is A a set given that it consists of sponsors of a Senate resolution, and is

lgst\_cit o reps

injective given that it is a function over Senators?

If the answers to these questions can be memoized when they are first answered, then evaluation of semantic queries becomes trivial for all but the bills processed initially. In fact, the use of a Prolog interpreter makes the implementation of memoization trivial. Prolog facts (such as one that directly states that lgst\_cit o reps is injective if reps ranges over House Representatives) can be *asserted* as they are inferred.

The issues discussed in the Chapter 5 also are material here. Once our COKO compiler generates more efficient code, and our semantic rewriter reasons directly over KOLA trees instead of their Prolog interpretations, we believe that all rewrites (whether fired statically or dynamically) will become more efficient.

Finally, dynamic query rewriting might be circumvented in some cases by allowing for conditional plans (as in the Volcano dynamic optimization work of Graefe and Cole [25]).

Rather than deferring rewriting decisions until run-time, a conditional plan would statically list multiple cases and associate plans to perform for each. Conditional plans could be useful when the cases that will be considered dynamic query rewriter can be anticipated statically, and when these cases are unlikely to change. We believe that dynamic query rewriting should not be replaced by conditional plans in all cases because it can be hard to anticipate all cases statically. For example, in this chapter we have shown that the subtype to which an object belongs can be relevant to the choice of query evaluation strategy. New subtypes are easily defined for object-oriented databases. Therefore, a conditional plan that is unaware of changes to the schema can become obsolete.

#### 7.3.2 The Advantage of KOLA

In previous chapters, we showed how KOLA's combinator style facilitates the expression of declarative rules. Term rewriting and semantic inference are similar in that both must perform subexpression identification and query formulation. Expressed over KOLA queries, neither of these tasks require supplemental code.

In this chapter, we have shown that subexpression identification and query formulation have uses beyond the expression of a query rewrites. Dynamic query rewriting is query rewriting that occurs during a query's evaluation. Typically, dynamic query rewriting requires a query evaluator to identify subexpressions of the query it is processing, and to formulate new queries to dynamically submit to a query rewriter. We have shown that the expression of these two tasks is simplified with the use of KOLA as the underlying query representation. Therefore, dynamic query rewriting provides another example of how KOLA benefits the development of query optimizers.

## 7.4 Chapter Summary

This chapter has described ongoing work in dynamic query rewriting. Query rewriting is most effective when a rewriter has knowledge about the representations and contents of the collections involved. Dynamic query rewriting is useful when this information is unavailable until data is accessed, as in object-oriented databases, network databases and heterogeneous databases.

We have confined our discussion in this chapter to potential benefits and design approaches for dynamic query rewriting over object-oriented databases. We showed an objectoriented query  $(NSF_{2k})$  that could be evaluated efficiently with dynamic query rewriting. Specifically, dynamic query rewriting makes it possible to evaluate this query without having to perform duplicate elimination as many times as would be required otherwise. We described the design of a dynamic query rewriter for ObjectStore for which an implemention is under development. While the work in this area is incomplete, the ideas demonstrate an exciting direction for query processing enabled by a combinator representation of queries.

## Chapter 8

# **Related Work**

In this chapter, we consider work related to the work presented in this thesis. The chapter is divided into four sections that correspond to Chapters 3 (KOLA), 4 (COKO), 5 (Semantic Query Rewriting) and 7 (Dynamic Query Rewriting) respectively.

## 8.1 KOLA

KOLA is both a query algebra and an internal data structure for query optimizers. The association of data structure with algebra is deliberate, and reflects our goal of simplifying both the operation and verification of query rewriting.

The best known query algebra is the relational algebra of Codd [24]. While used to describe logical query rewrites in many database texts (e.g., [66], [80]), the relational algebra is not usually used as a *data structure* within query optimizer implementations.<sup>1</sup> The Starburst query rewriter [79] for example, uses the Query Graph Model (QGM) as its internal representation. QGM query representations resemble instances of the entity-relationship data model. The entities (vertices) for this model are collections such as stored tables or queries. Edges reveal relationships between collections that indicate that one is an input to the other (the other being a query), or that a correlated predicate compares elements from each.

Starburst query rewrite rules are written in C. In [79], it is argued that it is necessary to code rules in this way because QGM is a C data structure. We dispute this conclusion — rules could be expressed more declaratively and a compiler could generate C code

<sup>&</sup>lt;sup>1</sup>Although Microsoft's SQL Server does use a variation of the relational algebra in this way.

from these more abstract specifications. (For example, KOLA's data structures are implemented in C++ and COKO transformations and KOLA rewrite rules are compiled into C++ code.) Instead, we believe that code is necessary to specify Starburst rules because the close association between QGM and SQL makes QGM a variable-based representation.

## 8.1.1 KOLA and Query Algebras

KOLA joins the numerous object query algebras that have been proposed over the years, including AQUA [70], EQUAL [87], EXTRA [99], OFL [40], GOM [61], Revelation [98], LERA [35], ADL [91], and the unnamed algebra of Beeri and Kornatzky [7]. Despite the lack of a standard, there is an encouraging overlap in the operators found in all of these algebras. These operators include:

- generalizations of relational operators (e.g., (1) a mapping operator generalizing relational projection by mapping a function over all members of a collection, (2) a selection operator generalizing relational selection by selecting elements of a collection satisfying a given predicate, and (3) a *join* operator generalizing relational joins by relating elements drawn from multiple collections),
- aggregation operators (such as the fold operator of AQUA [70] and Revelation [98]) that give algebras expressive equivalence with standard query languages with operators such as SUM and COUNT, and
- conversion operators to convert back and forth between flat and non-flat collections (including a grouping or nesting operator to convert a flat collection to a non-flat collection, and a *flattening* or *unnesting* operator to flatten a non-flat collection).

KOLA defines operators in each of the above categories. Mapping and selection are captured by KOLA's **iterate** and **iter** formers. Joins are expressed by a number of query primitives and formers, including **join**, **Isjoin**, **rsjoin** and **int**. Grouping is captured by **njoin**. Collection flattening is captured by **unnest** and **flat**. Thus, KOLA is equivalent in spirit to other object query algebras. The uniqueness of KOLA is in form — KOLA is a combinator-based representation specifically designed to simplify the operation and the verification of the query rewriter.

The KOLA Heritage – The AQUA Family of Query Algebras: The direct ancestors of KOLA are AQUA [70], EQUAL [87], EXTRA [99] and Revelation [98]. AQUA [70] was the immediate predecessor to KOLA. (KOLA was defined in response to difficulties defining a formal specification for AQUA and expressing rewrite rules over AQUA queries.) AQUA was designed by the inventors of EQUAL [87], EXCESS [99] and Revelation [98] who attempted to integrate and reconcile the approaches taken with their predecessor algebras.

AQUA defines a very general set of query operators, each of which can be instantiated with any data function or data predicate. For example, AQUA's join operator can be instantiated with a tuple concatenation function to express a relational join, or with a function that uses a query operator to express a join over an object-oriented database. This approach to query operators influenced the design of KOLA's query formers.

Aside from its combinator style, KOLA's primary distinction from AQUA concerns how it integrates data and query functions and how it constrains the definition of equality predicates. In AQUA, data functions are defined as *lambda expressions* whereas query functions are not. In KOLA, all functions are defined uniformly. This approach simplifies query formulation which need not massage query functions to make them data functions or vice-versa. This is especially important in an object query algebra where the pervasiveness of nesting means that query functions are often used as data functions.

AQUA allows arbitrary equivalence relations to act as equality predicates. Query operators whose semantics depend on equality definitions (such as set and bag union) are defined with equality predicate parameters so that the semantics of these operators can be configured according to their intended use. KOLA demands that equality definitions be confluences (as in CLU [72]): predicates that determine two objects to be equal only if they are indistinguishable. For mutable object types, equality predicates must compare immutable object identifiers. For immutable object types, equality predicates must be keys. KOLA has a more rigid policy with respect to equality predicates because substituting arbitrary equivalence relations for equality predicates can result in unintuitive query results. For example, a query that is instantiated with a non-confluent equality predicate can be issued twice over the same data and return two collections with distinct cardinalities (making these collections unequal by any reasonable interpretation of equality). As well, equality definitions that determine two distinct objects to be equal (perhaps because at the time of comparison, their states were identical) can result in a collection whose cardinality can change as a result of mutating one of its elements. These issues are discussed at length in our DBPL '95 paper [23].

**OFL:** Like KOLA, OFL [40] is inspired by functional programming languages [34]. OFL is an algebra intended to simplify the generation of graph representations of queries. The strategy taken to evaluate the query varies according to how this graph representation is

traversed.

OFL is an alternative intermediate representation to parse structures of standard object algebras. These algebras, it is argued, unnecessarily constrain the choice of execution algorithms. For example, the algebraic representation of path expressions demands evaluation by an inefficient object-at-a-time navigation. On the other hand, the graph-based representation espoused by this work enables the same query to be mapped to a plan that evaluates the query using joins. This then is an alternative approach to solving the normalization problem addressed by query rewriting. The usual example used to motivate query rewriting involves nested queries that force optimizers to choose nested loop evaluation strategies. Rewriting transforms nested queries into equivalent join queries that offer optimizers more algorithmic choice. In Chapter 6, we showed how query rewriting could also normalize queries with path expressions to ensure the consideration of evaluation plans involving joins.

The OFL language consists of both functional and imperative constructs (such as a sequencing operator). The imperative flavor makes OFL more of a plan language than an algebra, as algebraic equivalences are hard to establish and verify when expressions are described by the algorithms that generate them. But we find the alternative to query rewriting proposed by this work intriguing. In short, this approach generates multiple evaluation alternatives by fixing, rather than rewriting, a query's representation and instead varying traversal orders over it. Therefore OFL has some commonality with COKO which is also concerned about the order in which a given query representation is visited, though in the context of rewriting rather than evaluation.

LERA, GOM and ADL: Object query algebras LERA [35, 36], ADL [91] and GOM [61] are generalizations of the relational algebra. All of these algebras support tuple operators such as tuple concatenation (used in joins, unnests and nests). The KOLA data model includes pairs rather than tuples because the fixed number of fields in a pair simplifies its formal specification. Translation of OQL queries into KOLA maps tuples (structs) into (nested) pairs with tuple references replaced by compositions of projections that make appropriate extractions. (Our translator implementation keeps track of field names so that KOLA pair results can be translated back into tuples before they are stored.)

Like KOLA, LERA avoids direct references to variables within queries. But rather then using a combinator notation, LERA uses a numbering scheme to replace a variable reference with an index indicating the collection over which the variable ranges. Therefore, LERA's scheme is similar to the deBruijn [30] scheme (see Chapter 6), but is static. That is, collections appearing in a query are numbered from left to right rather than according to their relative positions within environments. The purpose of this notation is to avoid ambiguity (e.g., if the same collection appears twice in a join). With respect to rewrite rules, this approach still suffers from the same problems that make rewrite rules over query expressions require code. In particular, subexpression identification over such expressions requires code because a variable's index does not indicate whether or not it is free. As well, query formulation requires code because a variable index may have to be adjusted if rewriting results in changes to the collections that appear in a query's FROM clause (e.g., as in a nested query  $\rightarrow$  join query normalization).

GOM [61] and ADL [91] contain semijoin and nested join operators that inspired equivalent operators in KOLA. Specifically, KOLA's **njoin** former was inspired by ADL's **njoin** and GOM's **djoin** operators. ADL also defines semijoin and antijoin operators that are semantically equivalent to instantiations of KOLA's left semi-join former. (The function,

lsjoin (ex (p), id)

is equivalent to ADL's semijoin operator with respect to predicate p, and

lsjoin (fa (
$$\sim$$
 (p)), id)

is equivalent to ADL's antijoin operator with respect to predicate p.) GOM defines a left outer join operator that performs a union on the result of these two functions, but applying different functions (f and g) to the results of the semijoin and antijoin. Left outer-joins are also expressible in KOLA. For any pair of collections A and B, the left outer-join of A with respect to B is:

uni ! [lsjoin (ex (p), f) ! [A, B], lsjoin (fa  $(\sim (p)), g$ ) ! [A, B]].

#### 8.1.2 KOLA and Combinators

KOLA's combinator style was inspired by Backus' functional language, FP. Like FP, KOLA was initially intended to be a user-level language. But we abandoned this approach when it became clear that combinators make languages difficult for users to use.

The use of combinators as internal representations of functional programs originated with Turner's seminal work [93]. Ever since, combinators have been used within strict functional language compilers (e.g., Miranda [94]) as internal representations of lambda expressions. The use of combinators in this way makes evaluation by graph reduction more efficient, as lambda expressions with free variables force unnecessary copying of potentially large function bodies [34]. Approaches to combinator translations can be classified according to whether the combinator set is *fixed* or *variable*. *Fixed* combinator sets consist of a finite set of combinators that are used as the target for all lambda expression translations. The best known of the fixed sets of combinators is the **SKI** combinator set introduced by Schönfinkel [82]. It has been shown that this small set is sufficient to translate all of the lambda calculus (in fact **I** is superfluous), but the size of the resulting code is too large to be of practical use [57]. Variations of the **SKI** combinator sets add additional, redundant combinators (e.g. **B** and **Y**) to reduce the size of the translated code. Curien [27] proposed a set of combinators inspired by Category Theory, which he used to provide an alternative semantics for the lambda calculus. Of all of the combinator translations we found described in the literature, KOLA most closely resembles Curien's combinator set, but adjusted to account for sets and bags rather than lists, and avoiding the overly powerful combinators (**App** and  $\Lambda$ ) that are expressive but difficult to optimize prior to their application to arguments.

Lambda lifting [56] and supercombinators [52] are translation techniques that use variable sets of combinators. These techniques construct new combinators during each translation. The goal of this technique is to keep the number of combinators in the result small (the combinators generated tend to be fairly complicated). Thus, the goal of removing free variables from lambda expressions is achieved without an explosion in the size of the resulting code.

Despite the wide-spread use of supercombinators in functional language compilers, we settled on a fixed set of combinators for KOLA for the following reasons:

- query optimization (which relies on a set of known rewrite rules) must reference a known (i.e., fixed) set of operators, and
- query optimization can tolerate query representations that are larger (within reason) than queries because queries tend to be small compared with functional programs.

KOLA is not the first combinator query algebra or query language. ADAPLAN [31] was proposed as a combinator-style query language, but combinators are difficult for users to master and ill-suited as query languages. FQL [12], NRL [10] and the unnamed algebra of Beeri and Kornatzky [7] are combinator-based query algebras. FQL was an early effort and limited to relational databases. The algebra of Beeri and Kornatzky and NRL are mathematical formalisms rather than optimizer data structures. That is, the purpose of both of these algebras is to simplify the correctness of rules expressing query rewrites. Both algebras are *minimal* in that they include no redundant operators. A minimal algebra

simplifies proof obligations, but is less effective as an optimizer data structure. Redundant operators (such as join operators) are necessary in optimizer implementations because they are highly suggestive of the kinds of algorithms that a plan generator should consider. This redundancy is exactly what query rewriting normalizations exploit — rewriting queries into alternative forms that use operators to suggest alternative evaluation strategies.

#### 8.1.3 KOLA and Query Calculii

A query calculus differs from a query algebra in that it specifies a query in a more declarative way (i.e., by describing the result of the query rather than the sequence of operators that generate it). The declarative flavor of query expressions can make it easier for a plan generator to generate multiple execution plans, and therefore calculus-based query representations have advantages over query algebras for which plan generation is more constrained. Put another way, the translation of queries into a declarative calculus is another way to achieve the normalization goal of query rewriting. But the declarative nature of query calculii makes it difficult to express heuristics that are easily expressed over a query algebra. For example, it is not clear how one would express a rewrite that reorders filter predicates over queries with a calculus-based representation.

As was the case for algebras, a standard for object query calculii has yet to emerge. But perhaps the most common calculus for object queries stems from the monoid homomorphism work of Tannen et al [9]. That work describes *structural recursion*: a simple and highly expressive formalism for specifying both queries and data types, but requiring that functional inputs to homomorphisms satisfy certain undecidable algebraic properties (commutativity, associativity and idempotence). Later work from this group [10] proposed specific instantiations of these homomorphisms that were known to satisfy these properties (e.g., instantiations with set union), but at the expense of expressivity. Further, while ensuring a clean mathematics the idempotence restriction makes it difficult to express certain query operations such as aggregations. For example, SQL's SUM operator cannot be simulated with a homomorphism instantiated with addition ('+'), because '+' is not idempotent.

The Monoid Comprehension calculus of Fegaras and Maier [33] is defined in terms of monoid homomorphisms, but restricts the homomorphisms that can be expressed. In this way, the problem of deciding algebraic properties of functions is avoided, as are other problems inherent in the structural recursion model such as whether or not a given monoid homomorphism instantiation can be evaluated in polynomial time. (All queries expressed in the Monoid Comprehension calculus can be evaluated in polynomial time.) We consider the Monoid Comprehension calculus to be complementary to object query algebras such as KOLA, much as the relational calculus is complementary to the relational algebra. However, unlike the relational calculus and algebra, the Monoid Comprehension calculus is not able to express certain operators found in most object algebras. For example, operators based on OQL's bag intersection and bag difference operators cannot be expressed as homomorphisms and are therefore inexpressible in the Monoid Comprehension calculus.

## 8.2 COKO

In Chapter 4, we introduced a language (COKO) for expressing complex query rewrites. Other rule-based systems express complex query rewrites in one of two ways:

- as individual rewrite rules (usually supplemented with code), or
- as groups of rules.

## 8.2.1 Systems that Express Complex Query Rewrites With Single Rules

Most rule-based systems express complex query rewrites with individual rules. However, the rules of these systems are not declarative rewrite rules that get fired by pattern matching. Some systems (e.g., Exodus/Volcano [13, 43], EDS [36] and OGL [84]) allow rewrite rules to be supplemented with code. Other systems (e.g., Starburst [79], and Opt++ [58]) allow rules to be expressed completely in code, thus avoiding pattern matching altogether. Still other systems (e.g., OGL [84] and Gral [6]) employ a variation of pattern matching to make its effects more drastic. One rule-based optimizer generator (Cascades [42]) does all of these things.

**Starburst:** Starburst [79] fires *production rules* (as in expert systems such as [11]) during query rewriting. These rules consist of two code routines (loosely corresponding to the head and body patterns of a rewrite rule) that are both written in C. Because they are written in C, Starburst's query rewrite rules can express a wide variety of transformations including view merging, nested query unnesting (both discussed in [79]) and magic sets transformations ([74, 86]). However, Starburst rules are difficult to understand and verify, requiring a detailed understanding of the underlying graph-based query representation (QGM).

**Opt++ and Epoq:** Opt++ [58] is not a rule-based system *per se*, but does permit the modular expression of query rewrites. Opt++ is a C++-based framework for the

development of optimizers. This framework includes a family of classes from which optimizer developers can inherit. One of these classes (Tree2Tree) defines objects that transform tree representations of queries. Query rewrite rules would be implemented as instances of subclasses of Tree2Tree. Thus, rules in this system would be code-based. Epoq [73] also defines a framework for building optimizers. The modules for this framework (*regions*) are special purpose optimizers that may or may not be rule-based. Epoq is intended to be flexible enough to support any conception of rule including those defined with code.

**Exodus/Volcano/Cascades:** Exodus [13] and its successors, Volcano [43] and Cascades [42] use rules that resemble rewrite rules, but that can have code supplements. Cascades goes so far as to allow rewrite rules to be replaced by code altogether (such rules are called "function rules"<sup>2</sup>). Cascades also uses a variation on pattern matching. (Cascade rules fire fire on sets of query expressions and returns sets of modified query expressions as a result.) Complex rewrites not expressible in this way would have to be expressed with function rules.

**EDS and OGL:** Like the Exodus family of optimizer generators, EDS [36] and OGL [84] permit code supplements to rules. EDS rules can have the form,

#### $if < term_0 > under < constraint > then execute < method list > rewrite < term_1 > term_1 >$

such that  $term_0$  is a head pattern,  $term_1$  is a tail pattern, and < constraint > and < methodlist> contain calls to supplemental code written in C or C++. OGL rewrite rules can include *condition code* (code supplements to head patterns) and can use meta-patterns to circumvent standard pattern matching (e.g., "\*V" is a *multivariable* that "matches" multiple terms at once). While multivariables make some rules more general (an example shown in [84] demonstrates how a pattern with a multivariable could be reused to reassociate a conjunction expression with any number of conjuncts), other rules that require separating the terms that collectively matched the multivariable become inexpressible. In general, the use of rewrite rules makes the rules of all of these systems simpler to understand and verify than those that are expressed completely with code. However, the code supplements to these rules which enhance their expressive power offset their gains in verifiability.

**Gral:** Of the rule-based systems we looked at, Gral [6] comes closest to ours in its effort to make rules declarative by avoiding code. Gral also expands the expressive power of a

 $<sup>^{2}</sup>$ In fact, a Cascades paper [42] cites a query rewrite analogous to SNF of Chapter 4 as an example rewrite that would be encoded as a function rule.

rewrite rule, but not by adding code supplements as in Exodus of EDS. Instead, Gral uses a variation of pattern matching to recognize rules that have multiple tail patterns. Each tail pattern of a rule is associated with a declarative condition on the queried data. A query that matches a head pattern and satisfies some set of conditions is then rewritten according to the associated tail pattern.

The conditions associated with tail patterns analyze the data that is queried such as its representation, the existence of indices, cardinality etc. Therefore, Gral rules have expressive power above and beyond traditional rewrite rules because they incorporate semantic reasoning into the decision as to whether or not to fire a rule. But a Gral rule resembles a conditional rewrite rule in KOLA rather than a COKO transformation. While useful for expressing semantic rewrites, such rules cannot express the traversal strategies and controlled rule firing that a complex query rewrite requires. Instead, such rewrites must be expressed using the Gral meta-rule language as discussed below.

## 8.2.2 Systems that Express Complex Query Rewrites With Rule Groups

Many systems (e.g., Starburst [79], Gral [6], EDS [36], GOM [61] and OGL [84]) provide some form of meta-control language for rules that includes rule grouping and sometimes sequencing. Rule groups can be associated with *search strategies* that indicate how the rules in a group should be fired.

It is tempting to view COKO as a meta-rule language in this style, and to compare COKO transformations with rule groups and firing algorithms with search strategies and sequencing control. But this analogy is misleading. Firstly, the "rules" that are grouped by these systems are more analagous to COKO transformations than KOLA rules. Secondly, the purpose of rule grouping in these systems is to control the search for a "best" (according to some cost model) alternative to a given query expression. Typically, rules in a rule group will be fired on a query (or set of queries) exhaustively,<sup>3</sup> with each successful firing generating a new candidate query expression. The set of all candidate query expressions is then pruned for those that are considered to be efficient to evaluate. This approach reflects a *competitive* use for rule grouping – group all rules that contribute to some cost-based objective and let the best sequence of rule firings reveal itself through attrition.

Given the competitive model, an exhaustive approach to firing is guaranteed to find an optimal expression relative to some cost-model. Therefore, all of these systems allow rule

<sup>&</sup>lt;sup>3</sup>Exhaustive firing of rule groups resembles exhaustive firing of individual rules — every rule in the rule group is fired on every subexpression on the query repeatedly until rule firing no longer has any effect.

firing to be exhaustive, though many also provide other competitive strategies that are more efficient than exhaustive searches. For example, EDS allows a parameter to be set that limits the number of rule firing passes made of a query. Other systems provide pruning strategies so that only some alternatives are generated (e.g, OGL provide search strategies such as branch-and-bound and simulated annealing). Other systems permit rules (Starburst, GOM and Exodus) or algebraic operators (Gral) to be ranked to help the optimizer decide which rule to fire next thereby reducing the likelihood that poor alternatives are generated.

The purpose of rule grouping in COKO is not to generate alternatives but to modularize the expression of a complex query rewrite. Rules are fired *cooperatively* rather than *competetively*, and according to a firing algorithm tailored to a specific set of rules, rather than to a search strategy that is defined independently. There is no search involved. Rewriting is blind to the data and is concerned with the syntax of the result rather than its expected cost. Therefore, firing algorithms operate differently from search strategies. Of the search strategies listed above, the *exhaustive* strategy can work as a firing algorithm, but only in restricted cases (rewrite rules must form a confluent set) and usually sacrificing performance in the process (as with CNF). Firing algorithms needn't be generic nor exhaustive and instead can be customized to specific, fixed sets of rules. By avoiding exhaustive firing in these cases, rewriting is made more efficient.

In short, rule grouping can be either competitive and cooperative. Competitive rule grouping is supported by many existing rule-based systems, and is complementary to COKO which simply provides a means of specifying the rules that are to be grouped. Cooperative rule grouping is unique to COKO and is a technique for defining complex query rewrites that are efficient to fire and verifiable with a theorem prover.

## 8.2.3 Theorem Provers

Whereas KOLA was designed to enable query rewrites to be verified with LP, COKO was inspired by the use of LP itself. As we showed in Chapter 3, LP proofs are accompanied by *proof scripts* that tell the theorem prover how to complete the proof.<sup>4</sup> Proof scripts resemble handwritten proofs, except that proof methods are interpreted operationally to make the proof executable.

In many ways, a COKO transformation resembles a theorem prover proof script. Both query rewrite and proof rely on the existence of some set of simpler rewrite rules (derived

<sup>&</sup>lt;sup>4</sup>Scripts with similar purposes are found in other theorem provers. For example, tacticals in Isabelle [78] are analogous to LP proof scripts.

from specification axioms in the case of proofs). In some cases, exhaustive firing of these rewrite rules would complete the rewrite or proof. But in other cases, this could lead to nonterminating derivations and in most cases, the rewrite and proof could be performed more efficiently. Both proof script and COKO transformation control when rewrite rules get fired to ensure efficient rewriting and ensure termination.

That having been said, there are of course many differences between LP and COKO. LP includes instructions that correspond to proof techniques such as induction, contradiction and proof by cases. COKO "proofs" are far more straightforward, requiring only the rewriting of terms through successive rule firings. There is no need to rewrite the same term to the same result multiple times with different sets of rewrite rules as is done when an LP proof proceeds by cases or induction. There is no need find inconsistencies in an augmented set of rewrite rules as is done when an LP proof proceeds by contradiction. But COKO provides fine-gained control of rule firing not provided with LP by controlling the order and the subtrees on which rules are fired. This form of firing control ensures that a COKO rewrite is efficient compared to a theorem prover, which would be far too slow to be a query rewriter.

## 8.3 Semantic Query Rewriting

Related work in semantic query rewriting and semantic query optimization<sup>5</sup> either describes specific semantic optimization *strategies*, or describes *frameworks* within which strategies can be expressed.

## 8.3.1 Semantic Optimization Strategies

Most semantic optimization strategies exploit knowledge of integrity constraints. Integrity constraints are assertions that get evaluated during database updates to guard against data corruption. Because integrity constraints guard updates, they are constraints on data values and are expressed primarily by describing data dependencies. For example, a *domain* constraint ensures that specified columns have no values in common. *Referential integrity* constraints ensure that values appearing in one column of a relation also appear as values in a column of another relation. *Functional dependency* constraints ensure that tuples that share values for some columns share values for other columns also.

<sup>&</sup>lt;sup>5</sup>The latter term is more commonly used in the literature.

The very early semantic optimization papers [48, 64, 15] propose rewrites that exploit knowledge about integrity constraints to generate alternative expressions of relational queries. Hammer and Zdonik [48] use inclusion dependencies to substitute smaller collections for larger ones as inputs to queries (*domain refinement*). Many systems (such as Starburst) use key dependencies to determine when duplicate elimination is unnecessary (as described in Chapter 5). Predicate Move-Around [71] exploits knowledge of functional dependencies to generate new filtering predicates for collections used as inputs to joins. Order optimization [89] exploits functional dependencies to determine when sorting can be performed early during evaluation or avoided altogether.

Semantic optimization strategies for object databases [1, 45, 16] exploit not only the semantics of data (i.e., integrity constraints), but the semantics of the functions that appear in queries as well. Aberer and Fischer [1] correctly point out that object query optimizers require semantic capabilities to avoid (when possible) invoking expensive methods that can dominate the cost of query processing. They suggest a number of ways that method semantics can be expressed (e.g., by declaring that one chain of method calls equals another) and used by rewrites over the queries that invoke them. The work of Chaudhuri and Shim [16] and Grant et al. [45] also permit equivalent method expressions to be declared. The latter work also supports the expression of more *algebraic* descriptions of functions (e.g., that a function is monotonic). Beeri and Kornatzky [7] also define rewrites over object queries that depend on algebraic conditions (such as the idempotence of a function). KOLA's semantic capabilities permit expression of integrity constraints as well as function equivalences and algebraic properties of functions. KOLA's uniqueness is in expressing these properties in a manner that allows them to be inferred, and permitting the inference of properties to be easily extended and verified.

#### 8.3.2 Semantic Optimization Frameworks

As discussed in Chapter 5, the contribution of our work is not in presenting new semantic query optimization strategies but in introducing a framework for their expression that their ensures verifiability with a theorem prover. Optimization frameworks that incorporate semantic query optimization strategies can be divided into three categories:

- Category 1: systems that support operator-specific rewrites,
- Category 2: systems that support conditional rewrites, and
- Category 3: systems that support both conditional rewrites and semantic inference.

As we move from the first to the third category, systems get more succinct in describing semantic rewrites and hence more scalable. To illustrate, a category (1) system might permit the expression of a rule such as

$$\operatorname{clip}(\operatorname{blur}(i)) \cong \operatorname{blur}(\operatorname{clip}(i))$$

which says that the result of clipping a blurred image is the same as the result of blurring a clipped image. (The latter is likely more efficient to perform given that blurring tends to be an expensive operation, and clipping results in a smaller image to blur.) For other functions that commute (e.g., an image inversion function (invert) and clip), a similar rule would have to be defined:

$$\texttt{clip}(\texttt{invert}(i)) \stackrel{\rightarrow}{=} \texttt{invert}(\texttt{clip}(i)).$$

A category (2) system would permit the expression of the more general rule,

commutes 
$$(f,g) :: f(g(i)) \stackrel{\rightarrow}{=} g(f(i)),$$

which establishes that any functions f and g can be reordered provided that they commute, and then permit metadata to identify pairs of commuting functions (e.g., *commute* (clip, blur) and *commute* (clip, invert)). Category (2) systems provide a more succinct way to express a semantic rewrite because one rule can be defined to account for all commuting functions, rather that one rule per pair of commuting functions as would be required in a Category (1) system. This difference becomes even more pronounced if other rules are defined that are also conditioned on the commutativity of pairs of functions. These rules can use the same set of metadata facts used by the previous rule.

A category (3) system would allow the commutativity of pairs of functions to be inferred. For example, a category (3) system might infer that a function f commutes with a composition of functions,  $(g \circ h)$  if f commutes with each of g and h. Category (3) systems would allow a rewriter to infer that image clipping commutes with a function that first blurs an image and then inverts it given that clip commutes with each of blur and invert. A category (3) system is more succinct than a category (2) system at expressing semantic rewrites, as a category (2) system would have to list all functions that commute (including clip and (blur  $\circ$  invert)). Below we consider related work in semantic query optimization frameworks, classifying each in terms of these categories.

## Category (1)

Chaudhuri and Shim's work [16] involves optimizations of SQL queries that contain foreign functions. They incorporate rewrite rules over foreign functions to express equivalent expressions. Each equivalence must be captured in a separate rule. These rules are always valid, therefore they perform no inference nor conditional rewrites and fall under category (1).

The work on E-ADT's in the Predator Database System [88] also falls under category (1). One of the goals of this work is to localize semantic optimizations to optimization components that are responsible only for queries involving the associated abstract data types. The rule facility defined for Predator demands that rules be operator-specific. But in fairness, the primary contribution of Predator is architectural. There is no reason that a category (3) semantic rewriting system could not be incorporated into their framework. Schema-specific properties (e.g., establishing that **reps** is a key) could be localized to E-ADT's, and inference rules could be maintained globally.

## Category (2)

Beeri and Kornatsky [7] present several rewrite rules that are conditioned on function properties. For example, several of their rules are conditioned on the idempotence of a function. However, they do not define a mechanism to define how properties such as idempotence are inferred. Therefore the semantic rewriting proposed in this work falls under category (2).

More recent work in the context of object models has looked at semantic rewriting in the presence of methods. Aberer and Fischer [1] consider semantic rewrites that depend on method equivalences, and predicate implications derived from method semantics. Method equivalences are conditioned on the domain of free variables appearing within the expressions, and are used to rewrite query expressions according to a fixed set of rules. For example, an equivalence can establish that two functions, f(x) and g(x) are equivalent for all x in some collection C. The system uses this equivalence to infer that mapping f over C is equivalent to mapping g over C.

The work of Aberer and Fischer falls short of other category (2) systems because the rewrites that can depend on semantic conditions are limited to those provided by the system. Equivalence relationships are only used to rewrite queries involving mapping and selection. Predicate implication (which resembles predicate strength) is used in a rule that rewrites selections (presumably with expensive predicates) to natural joins of collections filtered with the cheaper predicates. No other rewrites that exploit these conditions can be added, and

no other conditions can be defined.

## Category (3)

Grant et al [45] propose a framework for semantic query optimization (SQO) by which object queries expressed in query languages such as OQL get translated into Datalog for semantic processing. Semantic information about the underlying object schema (e.g., subtyping information and methods) get expressed as Datalog rules that infer new integrity constraints to attach to these queries. Various checks are then made of the resulting predicates (e.g., to see if the new predicates introduce inconsistencies thereby eliminating the need to evaluate the query) before the Datalog queries are then translated back into the language in which they were posed.

This work falls under category (3) because of the use of inference to generate new integrity constraints. But the inference performed by SQO is less general in its application than that performed by COKO. SQO performs inference to generate predicates that get attached to queries. COKO properties can infer *any* condition that guards the firing of a rewrite rule, and not just predicate strength. Moreover, inferred conditions can guard the firing of *any* conditional rewrite rule, and not just a rule that adds weaker predicates to existing predicates. Effectively, this rule is the only conditional rule invoked by SQO. Its KOLA equivalent is captured by rewrite rule str2 of Figure 5.6.

SQO improves upon our work in its use of a more powerful inference technique (partial subsumption) to generate new predicates. We are interested in studying this inference technique to see if it could be used to strengthen our inference capabilities and thereby make our semantic rewriting component a better approximation of a complete system.

In summary, related work in semantic query optimization describes strategies and/or frameworks for expressing semantic query rewrites. Semantic optimizations for relational queries primarily use integrity (i.e., data) constraints. Semantic optimizations for object databases reason about the semantics of functions also. This is appropriate given that functions appearing in object queries are not limited to trivial extractions of values from columns, and can dominate the cost of evaluating the query.

Frameworks for semantic query optimization can be classified into three categories that are successively more succinct in expressing classes of query rewrites. Systems in category (1) permit the expression of operator-specific rewrites. Systems in category (2) permit the expression of more general conditional rewrites. Systems in category (3) permit the expression of conditional rewrites and techniques for inferring the conditions that are not explicitly stated. Our work is unique in how it captures data and function-based semantic rewrites within a category (3) framework in a manner supporting extensibility and verification with a theorem prover.

## 8.4 Dynamic Query Rewriting

In this section, we describe work related to our dynamic query rewriting work that is ongoing and presented in Chapter 7. Because our work is ongoing, we do not yet have experimental results to justify or refute our intuitions. Therefore, the comparisons made to other work in the area are confined primarily to approach rather than to a relative analysis of performance.

The dynamic query optimization strategies that have been proposed in the literature have exclusively concerned plan generation. Dynamic plan generation defers the generation of complete execution plans until cost-related factors can be observed at run-time. Such factors can include availability of resources [53], run-time values for host variables in embedded queries [25], or selectivity estimations [5].

The systems discussed here differ primarily by when alternative plans are generated. The first category of systems (described in Section 8.4.1) use dyanmic plan *selection* rather than dynamic plan *generation*. That is, what these approaches have in common is that compile-time optimization produces a fixed set of alternative plans from which a choice is made at run-time. Work falling in this category includes the dynamic optimization work for Volcano of Graefe and Cole [25], parametric query optimization [53] and the dynamic optimization performed by Oracle RDB [5]. The second category of systems (described in Section 8.4.2) perform *adaptive* query optimization. These systems generate complete execution plans at compile-time but permit all or portions of these plans to be replaced during query evaluation. Proposals in this category include the query scrambling work out of the University of Maryland [4] and the mid-query reoptimization work for Paradise of Kabra and DeWitt [59]. Dynamic query rewriting more closely resembles systems in the latter category, but generating partial plans rather than complete plans at compile-time.

Dynamic query rewriting is closely related to partial evaluation [26], as it reduces compile-time query optimization to partial plan generation. We consider this relationship more fully in Section 8.4.3.

## 8.4.1 Dynamic Plan Selection

We classify systems that choose plans dynamically from a fixed set of alternatives generated at compile-time as dynamic plan *selection* strategies. The work of Graefe and Ward [44] and later, Graefe and Cole [25] for Volcano was among the first dynamic plan selection strategies proposed. This work proposes a plan language that includes a *choose-plan* operator that makes it possible to express *conditional plans*. All subplans appearing below a *choose-plan* operator are alternative plans that compute the same result. The execution of this operator performs a cost analysis at run-time to determine which of these alternative plans should be executed.

Graefe and Cole rule out dynamic invocations of the query optimizer, arguing that the overhead involved would offset the performance gains from dynamically generated plans. This is undoubtedly true in certain cases, but ignores certain factors that make dynamic calls to an optimizer (and rewriter) of potential benefit:

• It assumes that a call to a dynamic query optimizer is a call to the same query optimizer that performed compile-time optimization. In fact, there is no reason not to define more streamlined optimizers and rewriters specifically defined to perform optimizations that are quick and most likely to have cost benefit (such as query rewrites). This is the approach taken in Oracle RDB [5] (which has separate optimizer components for their query compiler and query executor)

The Volcano solution can be viewed as dynamically invoking an optimizer that is as streamlined as an optimizer can be, deciding between a fixed set of plans according to a fixed set of metrics. We believe that the optimizers that are invoked dynamically could fall anywhere on a complexity scale, depending on the costs of the optimizations they perform and the potential benefits that they offer to the query being evaluated.

• The more sophistated the reasoning performed by a conditional Volcano plan (i.e., the more *choose-plan* operators that appear in the conditional plan) the larger the generated plan will be. Large plans can end up using resources (e.g., buffer space) that would otherwise be used in evaluating the query. Less sophisticated reasoning will produce smaller plans but are less likely to be effective in general. No study is made in [25] of the sizes of conditional plans and the impact of plan size on evaluation performance.

In short, this work was pioneering in suggesting how to implement a limited form of dynamic query optimization. But the results presented here can be generalized in two ways:
- 1. The complexity of the optimizer invoked dynamically can vary and not be just one that chooses between a fixed set of plans on the basis of a fixed set of cost factors.
- 2. Dynamically invoked optimizers need not be cost-based plan generators/selectors but could be heuristic-based query rewriters that perform semantic inference. In fact, query rewrites typically involve far simpler reasoning than do plan generators and can have far greater impact on performance. This makes them ideal as candidate dynamic optimizations where the cost : benefits ratio is of utmost concern.

Oracle RDB [5] justifies the dynamic optimization it performs by noting that the reliability of compile-time cost (specifically, selectivity) estimation degenerates quickly in the presence of complex predicates (e.g. p AND q). The problem is that the commonly held assumption of predicate independence (i.e., the assumption that the *correlation* between p and q has value 0) is overly simplistic — in fact correlation between predicates can fall anywhere between -1 (meaning that for all  $x, p(x) \Rightarrow \neg q(x)$ ) and 1 (meaning that for all x,  $p(x) \Rightarrow q(x)$ ). When correlation factors are assumed to be non-zero, selectivity estimation of complex predicates such as "p AND q" fall in a (Zipfean) distribution that is relatively constant independent of the individual selectivities of p and q. Therefore, cost estimation provides little guidance to the plan generator which is likely to generate the same plan independently of selectivities associated with specific predicates appearing in the query.

The Oracle RDB optimization strategy chooses multiple plans that are ideal assuming different selectivity scenarios. Evaluation then runs all of these plans in parallel for a short period of time. Zipfean selectivity distributions make it likely that one of these plans will produce a complete result quickly. Dynamic optimization chooses which of these multiple plans to continue in the unlikely event that all plans fail to return a complete result in the small window of time they were given to run.

This solution does not eliminate the need to make better compile-time cost estimations, as these would eliminate the need to perform dynamic optimization and parallel plan execution in some cases (thereby reducing the evaluation overhead of the queries involved). We are interested in determining if knowledge of underlying semantics might help in compiletime cost estimations. For example, predicate strength inferences could potentially be generalized to infer other correlation factors between predicates (predicate strength infers only correlation factors of -1 or 1). Defining inference rules to infer correlation factors in some cases would not be of use in our semantic rewrite scheme where semantic conditions determine the validity of a rewrite. However, it is possible that inferences such as these could be attached to query representations that are passed down to plan generation. The goal of parametric query optimization [53] is to generate a plan-producing function as a result of optimizing a query. This function accepts a vector describing run-time parameters (e.g., available buffers) and produces a plan customized to those conditions. Compile-time optimization divides the k-dimensional space of run-time parameters (k is the length of the vector) into partitions that share the same optimal plan. Run-time optimization finds the partition in which an input vector resides to determine the plan to execute.

This work complements the work of Graefe and Cole [25] by demonstrating a technique for deciding where *choose-plan* operators go in a conditional plan and how to generate the plans from which a dynamic choice is made. As with [25], this work describes dynamic plan *selection* rather than dynamic plan *generation* and says nothing about query rewriting.

## 8.4.2 Adaptive Query Optimization

Adaptive query optimization is distinct from dynamic plan selection in that it involves generating and comparing alternative plans dynamically, and not just selecting from a fixed set of plans generated at compile-time. Query scrambling [4] is one example of adaptive query optimization. The context for this work is widely distributed databases (e.g., web databases). Dynamic optimization is triggered in this setting by the unavailability of queried data sources. Specifically concerned with the orderings of multiple joins, query scrambling dynamically alters a chosen join ordering when processing delays occur due to unavailable data. This affects the plan generated at compile-time (the "join tree") in two phases:

- *Phase 1:* During this phase, scrambling alters the traversal of the join tree (say from a preorder traversal) so that intermediate results from other parts of the tree can be generated.
- *Phase 2:* This phases makes changes to the join tree by reordering joins, so that intermediate results can be generated from available data sources.

Kabra and DeWitt also propose a technique for reoptimizing queries during evaluation [59]. Unlike query scrambling for which dynamic reoptimization is triggered by data unavailability, reoptimization in this setting is triggered by recognition of errors in compiletime cost estimates. An execution plan is generated at compile-time that is annotated with the cost estimates used to generate the plan. Inserted at select positions in the plan are instances of a plan operator that triggers statistical analysis (e.g., cardinality measures). The execution of this plan then performs the indicated statistical analysis when these operators are executed on the basis of data that has been processed. The costs measured at this time are then compared to the statically estimated costs that annotate the tree. Then, depending on factors such as the cost of the query, the error in static cost estimations and so on, reoptimization may be initiated.

Both adaptive query optimization schemes described here differ from dynamic query rewriting in that both involve the *reoptimization* of queries. That is, both of these approaches generate complete plans at compile-time and then dynamically replace these plans as run-time circumstances warrant. On the other hand, dynamic query rewiting generates only partial plans at compile-time, leaving the holes in these plans to fill at run-time. Thus, the goal of dynamic query rewriting is not to reoptimize but to delay optimization. This approach is appropriate in the context of rewriting, which applies heuristics that are independent of physical properties of the environment and underlying database. That is, dynamic query rewriting is triggered, not by the recognition of cost factors that make certain evaluation strategies *inappropriate*, but by semantic properties of objects and functions that make certain rewrites *invalid*.

In short, dynamic query optimization resembles dynamic query rewriting in that it involves making decisions affecting evaluation strategies at run-time. But dynamic query optimization involves making cost-based decisions about evaluation plans at run-time, whereas dynamic query rewriting involves heuristically rewriting query representations depending on their validity established by identifying properties of objects recognized at run-time. Rather than being competitive, in fact the two techniques are complementary — dynamic query rewriting necessarily would precede dynamic query optimization.

## 8.4.3 Partial Evaluation

Partial evaluation is a technique for generating a program by specializing another with respect to some of its inputs [26]. Essentially, the technique requires decoupling the control flow of a program from its inputs. This can be done by *unfolding*, which replaces references to expressions with the code that computes them (as in *inlining*) or by *specializing*, which generates a program that has performed portions of the overall computation given knowledge of certain inputs. Typically, specialization uses *symbolic computation* to partially evaluate the expression computed by the more general program.

Partial evaluation techniques have been used in many areas of computer science including compiler generation [55, 8] and pattern matching [65]. Recently, compiler technology has adopted partial evaluation techniques to provide run-time code generation [69]. Dynamic query optimization and dynamic query rewriting similarly incorporate partial evaluation into code generation for queries.

Dynamic query rewriting and optimization necessitates that certain decisions about plan generation be deferred until run-time. This transforms the static query rewriter and optimizer into system components that produce partial results. If one looks at a generated execution plan as a result of evaluation, then the partial plans generated by static optimizers in this context are produced as a result of partial evaluation.<sup>6</sup>

On the other hand, dynamic query rewriting is in many ways the dual of partial evaluation. The purpose of partial evaluation is to move certain steps of a run-time computation (evaluation) into compile-time to achieve speed-up. But the purpose of dynamic query rewriting is to move certain steps of a compile-time computation (query optimization) into run-time to achieve greater flexibility. Note the essential difference here: query rewriting is made no more efficient as a result of dynamic rewriting. The goal instead is for query rewriting to be more flexible and therefore for the *generated plans* to be more efficient.

<sup>&</sup>lt;sup>6</sup>Of the approaches described in this section, adaptive query optimization least resembles partial evaluation because static optimization produces a complete plan (and not a partial plan) that can get replaced dynamically.

# Chapter 9

# **Conclusions and Future Work**

Query optimizers are perhaps the most complex and error-prone components of databases. The query rewriter is especially difficult to design and implement correctly. A query rewriter is correct if it preserves the semantics of the queries it transforms. Errors in query rewriting have been identified in both in research [63] and practice [41]. To this day, query rewriting techniques are often published with handwaving correctness proofs or worse, without proofs at all. This approach to correctness undermines confidence in the query processors that incorporate these techniques.

This thesis addresses the correctness issue for query rewriting. Our goal was to build query rewriters that could be verified with an automated theorem prover. Theorem provers have been adopted by the software engineering community as tools for reasoning about formal specifications and verifying implementations relative to those specifications. Commonly used for complex and safety-critical systems, query rewriting is yet another natural application of this technology.

The key contribution of this thesis is to define methodologies and tools for meeting this correctness goal. We have introduced COKO-KOLA: a novel framework for the specification and generation of query rewrite rules for rule-based query rewriters. Query rewrite rules generated within this framework are verifiable with the theorem prover LP. The foundation of this work is KOLA, a combinator-based (i.e., variable-free) algebra and internal query representation. Combinators are unintuitive to read and hence ill-suited as query languages. However, combinators are ideal query representations for rule-based query rewriters because combinator representations make it straightforward to declaratively (i.e., without code) specify *subexpression identification* and *query formulation*. Subexpression identification distinguishes the relevant subexpressions of queries that are being rewritten. Successful

identification of these subexpressions indicates that rewriting should proceed and defines a bank of subexpressions that can be used during query formulation. Query formulation uses identified subexpressions to construct new query expressions that are returned as the result of rewriting.

Combinator representations make it possible to express subexpression identification and query formulation with declarative rewrite rules that get fired according to standard pattern matching. This is because combinator expressions, being variable free, contain no occurences of free variables which can make syntactically identical expressions have distinct semantics. Code supplements to rules are required when underlying representations are variable-based. Supplements used for subexpression identification analyze the context of identified subexpressions containing free variables. Supplements used for query formulation massage identified subexpressions to ensure that their semantics are preserved when used in new contexts. These code supplements are unnecessary when variables are removed from the underlying query representation.

KOLA is a fully expressive object query algebra over sets and bags. It contains similar operators as other object algebras, but differs from these algebras in its combinator foundation and its uniform treatment of query and data functions. Because KOLA rewrite rules are expressible without code supplements, they can be verified with an automated theorem prover. We have verified several hundred KOLA rewrite rules with the theorem prover LP [46]. The motivation for KOLA, its semantics and several examples of its use in expressing queries and rewrite rules were presented in Chapter 3.

Rewrite rules are inherently simple. On the other hand, query rewrites can be complex. Therefore, KOLA is insufficient for expressing many of the query rewrites that get used in practice. In Chapters 4 and 5 we proposed techniques for expressing query rewrites that are too general and too specific respectively, to be expressed as rewrite rules. Query rewrites that are too general for rewrite rules include such complex normalizations as CNF — a rewrite to convert query predicates into conjunctive normal form. CNF cannot be expressed as a single rewrite rule because no pair of patterns is both general enough to capture all expressions that can be rewritten into CNF (i.e., all Boolean expressions) and specific enough to express their CNF equivalents. Put another way, any rewrite rule that expresses a predicate and its CNF equivalent will not be general enough to successfully fire on all predicates. To express complex and general rewrites such as this, we introduced the language COKO in Chapter 4.

COKO transformations specify and generate complex query rewrites. Transformations are both extensions and generalizations of KOLA rules. Transformations generalize KOLA rules because they can be fired and succeed or fail as a result. Transformations extend KOLA rules because they supplement sets of KOLA rewrite rules with a firing algorithm that controls the manner in which they are fired. COKO's firing algorithm language supports explicit control of rule firing, traversal control over query representation trees, conditional rule firing, and selective firing over subtrees. COKO makes it possible to express efficient query rewrites as we demonstrated in Chapter 4 with CNF. But while firing algorithms control when and where rules get fired, only rewrite rule firings can modify query representations. Therefore, COKO transformations are correct if the KOLA rewrite rules they fire are correct, and by implication, COKO transformations can be verified with a theorem prover. The motivation for COKO, the semantics of its firing algorithm language, and several applications of COKO that rewrite query expressions into CNF or SNF, push predicates, reorder joins and apply magic sets techniques were presented in Chapter 4.

In Chapter 5, we addressed an expressivity issue that is complementary to that addressed by COKO. This issue concerns query rewrites that are too specific to be expressed as rewrite rules. The validity of such rewrites depends on the semantics and not just the syntax of the queries on which they are fired. To express such rewrites, we added *conditional rewrite rules* and *inference rules* to COKO-KOLA. Conditional rewrite rules get fired like (unconditional) rewrite rules, except that identified subexpressions must also satisfy declaratively expressed conditions. These conditions are specified with *properties*: collections of declarative inference rules that our compiler compiles into code that gets executed during rule firing. Both conditional rewrite rules and inference rules are expressed without code and hence are verifiable with a theorem prover. The motivation and implementation of semantic extensions to COKO-KOLA were presented with examples of their use in Chapter 5.

An example application of the COKO-KOLA framework was presented in Chapter 6. In this chapter, we described and assessed our experience building a query rewriting component for the San Francisco project of IBM. We learned from this experience that the COKO-KOLA framework, while in need of refinement and an industrial strength implementation, makes it possible to express "real" query rewrites succinctly and with confidence.

What is common to KOLA, COKO and the semantic extensions to COKO-KOLA is the need to identify subexpressions and formulate new queries. KOLA's conditional and unconditional rewrite rules identify subexpressions and formulate new queries when they successfully fire. COKO transformations must frequently identify subexpressions of queries on which to fire rules (using the GIVEN statement). Inference rules identify subexpressions of query expressions so that properties of these expressions can be inferred of the expressions that contain them. We showed in Chapter 3 that combinators simplify the expression of these tasks and make them verifiable with a theorem prover. Therefore, the high-level contribution of this work is the recognition of the impact of query representations in general and combinator-based representations in particular on the design, implementation and verification of a query optimizer. When built with combinators, query rewriters can be verified with a theorem prover, thereby achieving the goal we set out at the onset to address the inherent difficulty in building query rewriters correctly.

In Chapter 7, we identified another potential benefit of combinator-based query representations. Whereas previous chapters considered how combinators simplify *how* rewrites get expressed, in this chapter we showed how combinators could be used to change *when* they get fired. Dynamic query rewriting proposes that some query rewriting take place *during* the evaluation of a query. Dynamic query rewriting would be beneficial in settings where the information that justifies the firing of a rewrite rules is unavailable until queried data is retrieved. Such settings include object databases, whose queries may be invoked on anonmymous embedded collections; network databases, whose queries may join collections whose availability may be unknown until runtime; and heterogenous databases whose queries may reference collections that are represented with data structures known only to the local databases they oversee. Dynamic query rewriting requires identifying relevant subqueries and formulating new queries by packaging these subqueries with accessed data. Therefore, dynamic query rewriting also benefits from combinator-based query representations.

# 9.1 Future Directions

Unlike the work presented in previous chapters, dynamic query rewriting is work in progress. Therefore, future directions for this thesis work are primarily concentrated in this area. A design for a dynamic query rewriter and query evaluator for ObjectStore [67] is complete and an implementation is ongoing. Once complete, it will be necessary to run a performance study to determine when (and if) the benefits of dynamic query rewriting outweigh its costs. We plan to construct and populate the Thomas database described in Chapter 2 according to the guidelines described in Section 7.1.1. Thereafter, a testbed of OQL queries will be formulated to query this database. A variety of query rewriters will be generated using the COKO compiler, varying in the degree and kinds of semantic and dynamic query rewriting that each performs. That is, the COKO routines compared will include ones that:

- fire no rewrites,
- fire rewrites, but neither semantic nor dynamic rewrites,

- fire semantic but not dynamic rewrites, and
- fire both semantic and dynamic rewrites.

It should be straightforward to come up with examples (such as the "NSF" Query) for which semantic and dynamic rewriting will prove useful. But the cost of performing dynamic rewriting must be weighed relative to the improved performance of query evaluation. Much of the cost of query processing is incurred when elements are retrieved from the iterators returned as the results of queries. Therefore, these comparisons should include ones that measure the time to retrieve all elements contained in a collection returned by the query.

Our study of dynamic query rewriting has been confined thus far to object databases. We are also interested in the potential benefits of dynamic query rewriting in other settings such as network databases and heterogeneous databases. With respect to the former, we are interested in exploring the potential benefits of this technique to queries posed over dissemination-based data delivery systems [2, 37]. Efficient evaluation of queries posed in these settings will require knowledge of how data has been scheduled for delivery. As schedules are sometimes formulated online and subject to modification, this may require query strategies to be reformulated on-the-fly. We believe this to be a promising application for dynamic query rewriting strategies which provide the processing flexibility required to do this. Heterogeneous database queries typically get posed in higher-order query languages such as SchemaLog [47] that permit queries to be posed over collections of relations. As these relations can vary in representation, sort order, duplicate status and so on, dynamic query rewriting could well prove beneficial here also.

Future directions for KOLA, COKO and semantic extensions to COKO and KOLA will involve refining their designs and implementations. Eventually, we would like KOLA to be an algebra with the same expressivity as OQL and adjust the translator to translate all of OQL to KOLA. This work will require extending the formal specification of KOLA to include lists, arrays and mutable objects. The impact of mutable objects on KOLA and query rewriting correctness was described in a white paper resulting from our joint discussions with the Thor group of MIT [18].

Once an OQL  $\rightarrow$  KOLA translator is complete, we will need to prove its correctness. We proved the correctness of an early version of this translator (see [17]) that translated a set-based subset of OQL into KOLA. This result required a denotational semantics for this subset of OQL and an operational semantics for KOLA in terms of OQL (i.e., each KOLA construct was associated with its OQL equivalent). We then used structural induction to prove that the denotational semantics of any OQL expression e that is well-formed with respect to some environment  $\rho$  (**Eval**  $\llbracket e \rrbracket \rho$ ) is equivalent to the denotational semantics of the OQL expression resulting from first translating of e into a KOLA function that is invoked on the nested pair equivalent of  $\rho$ , and then translating this expression back into OQL (**Eval**  $\llbracket T \llbracket e \rrbracket : \overline{\rho} \rrbracket$  ()). The final translator will be verified in the same way.

Future work for COKO will involve refinements to the firing algorithm language, a new design and implementation for the COKO compiler and the development of a debugging facility. Refinements to the firing algorithm language will be motivated by the experiences of users of the language. (Some refinements based on our experiences were proposed in Chapter 6.) We intend to rethink our decision to associate success values with all statements in the language and determine if a more traditional control language might make COKO simpler to use.

The existing COKO compiler was designed for simplicity rather than efficiency. The compiler produces code that generates a parse tree corresponding to the COKO transformation's firing algorithm, and then invokes a recursive method (exec) on the root of this tree. This design made it straightforward to modify COKO and therefore was an appropriate design for a prototype. However, generated COKO parse trees can be large and unwieldy and therefore, an alternative design is required for industrial use.

Finally, the programming of firing algorithms is. not an easy task. Part of the problem is due to deficiencies in the firing algorithm language. For example, in the discussion section of Chapter 6, we noted the difficulties introduced by associative KOLA formers such as function composition. The problem is that a given KOLA rewrite rule might fail to fire due to the manner in which a composition is associated. While addressing these deficiencies in the language design should make programming somewhat easier, in the long term we envision the development of a debugging environment to support transformation development. Such a debugger could provide standard debugging tools such as breakpoints and stepping through the execution of statements. Ideally, it also will permit the actions of a COKO transformation to be visualized in terms of a graphical representation of a KOLA tree.

Future work for semantic extensions to COKO-KOLA also will involve revisiting the implementation. The current implementation invokes a Prolog interpreter to answer semantic queries. This design has a performance overhead from invoking a foreign interpreter (the rest of the rule firing engine was programmed in C++), and from translating KOLA parse trees to and from Prolog. We intend to replace this design with one that performs reasoning over KOLA trees directly, perhaps replacing the inference algorithm (currently unification-based [81]) with more powerful inference techniques such as those described in

the work of Grant et al [45].

## 9.2 Conclusions

This thesis has addressed the correctness problem for query rewriters. We have defined a framework for generating query rewriters that can be verified with a theorem prover. We have identified the impact of query representations on query optimizer design, showing with several examples how combinator-based query representations simplify the expression of query rewrites. We introduced a novel query algebra (KOLA), a novel language for expressing complex query rewrites (COKO) and novel semantic extensions to the query rewriting process. As well, we have constructed several proofs of concept that include a formal specification of KOLA, several hundred proof scripts verifying KOLA rewrite rules and COKO transformations, a translator mapping OQL queries into their KOLA equivalents, a compiler to map COKO transformations into executable query rewrites, and an example query rewriter for a real database system. In addressing the correctness problem, we have contributed methodology and tools that impose a discipline on the design and implementation of query rewriters. In adhering to this discipline, the "COUNT bug" and its kin should become relics of the past.

# Appendix A

# A Larch Specification of KOLA

# A.1 Functions and Predicates

% Class of Invokable Functions.

introduces

% Invocation Operator.
% -----\_\_\_ ! \_\_\_: fun [T, U], T → U

asserts

 $\forall$  f, g: fun [T, U], x: T

% When are two functions equal? % -----f = g  $\Leftrightarrow \forall x ((f ! x) = (g ! x))$ 

% Class of Invokable Predicates.

introduces

asserts

∀ p, q: pred [T], x: T
% When are two predicates equal?
% -----% p is rewritable to q if they are evaluate to the same result
% for all objects

 $p = q \Leftrightarrow \forall x (p ? x \Leftrightarrow q ? x)$ 

# A.2 Objects

% The trait of Generic KOLA bags (i.e., not mutable or immutable).

includes

### introduces

```
\oslash: \rightarrow bag [T]
insert: T, bag [T] \rightarrow bag [T]
\{\_\}: T \rightarrow bag [T]
\_ \in \_: T, bag [T] \rightarrow Bool
\_ - \_: bag [T], T \rightarrow bag [T]
```

## asserts

```
\forall A, B: bag [T], x, y: T

\sim(insert (x, A) = \oslash)

insert (x, insert (y, A)) == insert (y, insert (x, A))

x \in \oslash == false

x \in insert (y, A) == (x = y) \lor x \in A

{x} == insert (x, \oslash)

\oslash - x == \oslash

\sim (x = y) \Rightarrow insert (x, A) - y = insert (x, A - y)
```

implies

```
\forall A, B: bag [T], x, y: T

\sim (x \in A) \Rightarrow (A - x) = A

x \in (A - y) \Rightarrow x \in A

A = insert (x, B) \Rightarrow (A - x) = B

((x \in A) \land ((A - x) = B)) \Rightarrow A = insert (x, B)
```

includes

BagBasics (T)

#### introduces

-- ∪ --: bag [T], bag [T] → bag [T] -- ∩ --: bag [T], bag [T] → bag [T] -- --: bag [T], bag [T] → bag [T]

asserts

$$(A = \oslash) \lor \exists x \exists B (A = insert (x, B))$$
$$(x \in A) \Rightarrow \exists B (A = insert (x, B))$$

## implies

$$\forall x, y: T, A, B: bag [T]$$

$$A \cup \oslash == A$$

$$A \cup insert (y, B) == insert (y, A \cup B)$$

$$A \cap \oslash == \oslash$$

$$(y \in A) \Rightarrow (A \cap insert (y, B) = insert (y, (A - y) \cap B))$$

$$\sim (y \in A) \Rightarrow (A \cap insert (y, B) = (A \cap B))$$

$$A - \oslash == A$$

$$(y \in A) \Rightarrow (A - insert (y, B) = (A - y) - B)$$

$$\sim (y \in A) \Rightarrow (A - insert (y, B) = A - B)$$

$$x \in (A \cup B) == (x \in A) \lor (x \in B)$$

$$x \in (A \cap B) == (x \in A) \land (x \in B)$$

$$x \in (A - B) == (x \in A) \land (x \in B)$$

% Trait specifying pairs of objects.

introduces

% The Pairing Constructor

```
% ----- [_, __]: T1, T2 \rightarrow pair [T1, T2]
```

asserts

introduces

 $\texttt{Null:} \ \rightarrow \ \texttt{T}$ 

# A.3 Primitives (Table 3.1)

% Trait of the Polymorphic, Invokable Identity Function, id

includes

Function (T, T)

introduces

id :  $\rightarrow$  fun [T, T]

asserts

∀ x: T
% Semantics of id
% ----id ! x == x

% Trait of the Polymorphic, Invokable Projection Functions,  $\pi_1$  and  $\pi_2$  %

- % a. properties of these functions
- $\%\,$  b. semantics of these functions

### assumes

Pairs (T1, T2)

## includes

Function (pair [T1, T2], T1),
Function (pair [T1, T2], T2)

## introduces

 $\pi_1: 
ightarrow$  fun [pair [T1, T2], T1]  $\pi_2: 
ightarrow$  fun [pair [T1, T2], T2]

#### asserts

 $\forall$  x: T1, y: T2

% Semantics of π<sub>1</sub>, π<sub>2</sub> % ----π<sub>1</sub> ! [x, y] == x π<sub>2</sub> ! [x, y] == y

## 

# 

% Trait of the Polymorphic, Left and Right Pair Shifting % Functions  ${\rm shl}$  and  ${\rm shr}$ 

assumes

```
Pairs (T, U),
Pairs (U, V),
Pairs (pair[T, U], V),
Pairs (T, pair[U, V])
```

includes

Function (pair [pair [T, U], V], pair [T, pair [U, V]]),
Function (pair [T, pair [U, V]], pair [pair [T, U], V])

introduces

 ${
m shl}$  : ightarrow fun [pair [T, pair [U, V]], pair [pair [T, U], V]]  ${
m shr}$  : ightarrow fun [pair [pair [T, U], V], pair [T, pair [U, V]]]

asserts

∀ t: T, u: U, v: V
% Semantics of shl, shr
% -----shl ! [t, [u, v]] == [[t, u], v]
shr ! [[t, u], v] == [t, [u, v]]

% Trait of primitive functions and predicates on Integers

#### assumes

```
Integer,
Pairs (Int, Int)
```

#### includes

```
Function (Int, Int),
Function (pair [Int, Int], Int),
Predicate (pair [Int, Int])
```

## introduces

```
% Unary Functions
% -----
  abs: \rightarrow fun [Int, Int]
% Binary Functions
% -----
  add: \rightarrow fun [pair [Int, Int], Int]
  {f sub}\colon 	o fun [pair [Int, Int], Int]
  mul \colon \rightarrow fun [pair [Int, Int], Int]
  div: \rightarrow fun [pair [Int, Int], Int]
  mod: \rightarrow fun [pair [Int, Int], Int]
% Binary Predicates
% -----
  lt: \rightarrow pred [pair [Int, Int]]
  leq: \rightarrow pred [pair [Int, Int]]
  \mathbf{gt}: \rightarrow \texttt{pred} [pair [Int, Int]]
  geq: \rightarrow pred [pair [Int, Int]]
```

% Trait of primitive functions and predicates on Floats

assumes

FloatingPoint (Float for F),
Pairs (Float, Float)

includes

```
Function (Float, Float),
Function (pair [Float, Float], Float),
Predicate (pair [Float, Float])
```

```
introduces
```

```
% Unary Functions
  % ------
     abs: \rightarrow fun [Float, Float]
  % Binary Functions
  % -----
     \mathrm{add}\colon 
ightarrow fun [pair [Float, Float], Float]
    {
m sub:} 
ightarrow fun [pair [Float, Float], Float]
    mul: \rightarrow fun [pair [Float, Float], Float]
    {f div}\colon 	o fun [pair [Float, Float], Float]
  % Binary Predicates
  % -----
    lt: \rightarrow pred [pair [Float, Float]]
    leq: \rightarrow pred [pair [Float, Float]]
    \operatorname{\mathbf{gt}}: 
ightarrow pred [pair [Float, Float]]
    geq: \rightarrow pred [pair [Float, Float]]
asserts
    \forall f1, f2: Float
  % Semantics of Float Function Primitives
  % -----
     abs ! f1 == abs (f1)
```

```
add ! [f1, f2] == f1 + f2
sub ! [f1, f2] == f1 - f2
```

% Trait of primitive functions on Strings

assumes

```
Integer,
String (Char, Str),
Pairs (Str, Str),
Pairs (Str, Int)
```

includes

```
Function (pair [Str, Int], Char),
Function (pair [Str, Str], Str),
Function (pair [Str, Int], Str)
```

introduces

at:  $\rightarrow$  fun [pair [Str, Int], Char]

```
concat: \rightarrow fun [pair [Str, Str], Str]

length: Str \rightarrow Int

asserts

\forall i: Int, s, s': Str

\% Semantics of String Primitives

\% -------

length (empty) == 0

\sim (s = empty) \Rightarrow (length (s) = 1 + (length (tail (s))))

at ! [s, i] == s [i]

(i < length (s)) \Rightarrow

(at ! [concat ! [s, s'], i] = at ! [s, i])

(i >= length (s)) \Rightarrow

(at ! [concat ! [s, s'], i] = at ! [s', i - length (s)])
```

% Trait of primitive functions on Bags

assumes

Bag (T),
Bag (U),
Pairs (T, T),
Pairs (bag [T], bag [T]),

```
Pairs (bag [T], bag [U]),
Pairs (T, bag [U]),
Pairs (T, U),
Bag (bag [T])
```

includes

```
Function (bag [T], T),
Function (T, bag [T]),
Function (bag [T], bag [T]),
Function (bag [bag [T]], bag [T]),
Function (pair [T, bag [U]], bag [pair [T, U]]),
Function (pair [bag [T], bag [U]], bag [pair [T, U]]),
Function (pair [bag [T], bag [T]], bag [T])
```

introduces

```
% Unary Functions
% ------
single: \rightarrow fun [T, bag [T]]
elt: \rightarrow fun [bag [T], T]
set: \rightarrow fun [bag [T], bag [T]]
flat: \rightarrow fun [bag [bag [T]], bag [T]]
% Binary Functions
% -------
uni: \rightarrow fun [pair [bag [T], bag [T]], bag [T]]
int: \rightarrow fun [pair [bag [T], bag [T]], bag [T]]
dif: \rightarrow fun [pair [bag [T], bag [T]], bag [T]]
ins: \rightarrow fun [pair [T, bag [T]], bag [T]]
```

asserts

 $\forall$  x, y: T, A, B: bag [T], X: bag [bag [T]], U: bag [U], u, v: U % Semantics of Unary Function Primitives % -----single  $| x = \{x\}$ **elt** !  $\{x\} = x$ ins ! [x, A] = insert (x, A)set !  $\oslash$  ==  $\oslash$ set ! insert (x, A) == if  $(x \in A)$  then set ! A else insert (x, set ! A)flat !  $\oslash$  ==  $\oslash$ flat ! insert (A, X) == A  $\cup$  (flat ! X) % Semantics of Binary Function Primitives % ----uni ! [A, B] == A  $\cup$  B int ! [A, B] == A  $\cap$  B dif ! [A, B] == A - B

implies

 $\forall x, y: T, A, B: bag [T], X: bag [bag [T]],$  U: bag [U], u, v: U, e: T, z: pair [T, U]  $(set ! A) = (set ! B) == \forall x:T (x \in A \Leftrightarrow x \in B)$   $e \in (set ! A) == e \in A$   $e \in (flat ! X) == \exists A (A \in X \land e \in A)$   $e \in (A \cup B) == (e \in A) \lor (e \in B)$   $e \in (A \cap B) == (e \in A) \land (e \in B)$   $e \in (A - B) == (e \in A) \land \sim (e \in B)$ 

% Trait of the primitive, avg, which averages the % elements in a bag. Bag elements must be integers % or floats.

```
assumes
```

```
Integer,
FloatingPoint (Float for F),
Bag (Int),
Bag (Float),
Count (Int),
Count (Float),
Sum (Int),
Sum (Float)
```

includes

Function (bag [Int], Float),
Function (bag [Float], Float)

introduces

 $\mathbf{avg}$  : ightarrow fun[bag [Int], Float]  $\mathbf{avg}$  : ightarrow fun[bag [Float], Float]

## asserts

∀ A: bag [Int], B: bag [Float]

% Semantics of avg
% ----~(A = ⊘) ⇒
 (avg ! A = (float ((sum ! A) / 1) / float ((count ! A) / 1)))
~(B = ⊘) ⇒
 (avg ! B = ((sum ! B) / float ((count ! B) / 1)))

```
\% Trait of the primitive, {\rm cnt}\,, which counts the \% number of elements in a bag
```

assumes

```
Bag (T),
Integer
```

includes

```
Function (bag [T], Int)
```

introduces

 $\mathbf{cnt}$  : ightarrow fun [bag [T], Int]

asserts

 $\forall$  x: T, A: bag [T]

```
% Semantics of count
% -----
cnt ! @ == 0
cnt ! insert (x, A) == 1 + (cnt ! A)
```

# 

```
\% Trait of the primitive, \max finds the largest \% element in a bag
```

assumes

Bag (T), TotalOrder (T) % T is ok as long as it has a max and min

includes

Function (bag [T], T)

introduces

 ${\bf max}$  :  $\rightarrow$  fun[bag [T], T]

asserts

 $\forall$  x: T, A: bag [T]

% Semantics of max

```
% -----
max ! {x} == x
max ! insert (x, A) == if (x > (max ! A)) then x else (max ! A)
```

% Trait of the primitive,  $\min$  finds the smallest % element in a bag

```
assumes
```

```
Bag (T),
TotalOrder (T) % T is ok as long as it has a max and min
```

```
includes
```

```
Function (bag [T], T)
```

introduces

 ${f min}$  : ightarrow fun[bag [T], T]

asserts

∀ x: T, A: bag [T]
% Semantics of min
% ----min ! {x} == x

min ! insert (x, A) == if (x < (min ! A)) then x else (min ! A)

#### 

% Trait of the primitive,  ${\rm sum}\,,$  which sums the % elements in a bag

assumes

```
Bag (U),
AbelianGroup (U for T, + for ∘, 0 for unit)
% U is ok as long as it has a commutative, associative +
% with identity, 0
```

```
includes
```

```
Function (bag [U], U)
```

introduces

 $\mathbf{sum}$  : ightarrow fun[bag [U], U]

asserts

∀ x: U, A: bag [U]
% Semantics of sum
% -----sum ! ⊘ == 0

## sum ! insert (x, A) == x + (sum ! A)

# 

- % Trait of the Polymorphic, Invokable equality and
- % inequality predicates

includes

Pairs (T, T), Predicate (pair [T, T])

```
introduces
```

```
\begin{array}{l} \mathbf{eq:} \rightarrow \mbox{pred [pair [T, T]]} \\ \mathbf{neq:} \rightarrow \mbox{pred [pair [T, T]]} \end{array}
```

asserts

```
\forall x, y: T
```

% Semantics of eq, neq % ----eq ? [x, y] == x = y neq ? [x, y] == ~(x = y)

# A.4 Basic Formers (Table 3.2)

% Trait of the Polymorphic, Composition Function former, \_  $\circ$  \_

assumes

Function (T, X), % for g
Function (X, U) % for f

## includes

Function (T, U) % for f  $\circ$  g

introduces

 $\_ \circ \_$ : fun [X, U], fun [T, X]  $\rightarrow$  fun [T, U]

asserts

∀ x: T, f: fun [X, U], g: fun [T, X]
% Semantics of ○
% -----(f ○ g) ! x == f ! (g ! x)

% Trait of the Polymorphic, Pairing Function former, <\_\_, \_\_>

#### assumes

```
Function (T, U2), % for g
Function (T, U1) % for f
```

#### includes

```
Pairs (U1, U2),
Function (T, pair [U1, U2]) % for f + g
```

introduces

 $\langle$  \_\_, \_\_  $\rangle$ : fun [T, U1], fun [T, U2]  $\rightarrow$  fun [T, pair [U1, U2]]

asserts

% Trait of the Polymorphic, Product Function former, \_\_ x \_\_

assumes

Function (T2, U2), % for g Function (T1, U1) % for f includes

```
Pairs (T1, T2),
Pairs (U1, U2),
Function (pair [T1, T2], pair [U1, U2]) % for f x g
```

introduces

\_\_  $\times$  \_ : fun [T1, U1], fun [T2, U2]  $\rightarrow$  fun [pair [T1, T2], pair [U1, U2]]

asserts

∀ x: T1, y: T2, f: fun [T1, U1], g: fun [T2, U2]
% Semantics of ×
% -----(f × g) ! [x, y] == [f ! x, g ! y]

% Trait of Constant function former K  $_f$  (\_)

includes

Function (T, U) % for K<sub>f</sub> (e)

introduces
asserts

```
∀ y: U, x: T
% Semantics of K<sub>f</sub>
% -----
K<sub>f</sub> (y) ! x == y
```

```
\% Trait of Curried function, C _f (_, _)
```

assumes

Pairs (T1, T2), % for domain of f Function (pair [T1, T2], U)

includes

```
Function (T2, U) % for C_f (f, e)
```

introduces

 $\mathtt{C}_f$  : fun [pair [T1, T2], U], T1 ightarrow fun [T2, U]

asserts

 $\forall$  f: fun [pair [T1, T2], U], x: T1, y: T2

% Semantics of C

% Trait of the Polymorphic, Conditional Function former, con

assumes

```
Predicate (T)
```

includes

Function (T, U)

introduces

con: pred [T], fun [T, U], fun [T, U]  $\rightarrow$  fun [T, U]

asserts

 $\forall$  x: T, p: pred [T], f, g: fun [T, U]

% Semantics of con

% -----

con (p, f, g) ! x == (if p ? x then f ! x else g ! x)

Combination (T, U): trait

% Trait of the Polymorphic, Combining Predicate former, \_  $\oplus$  \_

assumes

```
Function (T, U),
Predicate (U)
```

includes

```
Predicate (T)
```

introduces

\_\_  $\oplus$  \_\_ : pred [U], fun [T, U]  $\rightarrow$  pred [T]

asserts

 $\forall$  x: T, f: fun [T, U], p: pred [U]

% Semantics of ⊕
% ----(p ⊕ f) ? x == p ? (f ! x)

% Trait of the Polymorphic, Conjunction Predicate former, \_ & \_

assumes

```
Predicate (T)
```

introduces

\_\_ & \_\_ : pred [T], pred [T]  $\rightarrow$  pred [T]

asserts

```
∀ x: T, p, q: pred [T]
% Semantics of &
% ------
(p & q) ? x == (p ? x ∧ q ? x)
```

 $\forall$  e: D, p, q: pred [D]

% Semantics of p & q
% ----(p | q) ? e == (p ? e ∨ q ? e)

% Trait of Inverse Predicate Former p $^{-1}$ 

### assumes

```
Pairs (T1, T2),
Predicate (pair [T1, T2])
```

#### includes

Pairs (T2, T1), Predicate (pair [T2, T1])

## introduces

 $\_\_^{-1}$  : pred [pair[T1, T2]]  $\rightarrow$  pred [pair [T2, T1]]

#### asserts

∀ x: T1, y: T2, p: pred [pair [T1, T2]]
% Semantics of <sup>-1</sup>
% -----(p <sup>-1</sup>) ? [y, x] == p ? [x, y]

% Trait of the Polymorphic, Predicate Product former, \_  $\perp$   $\times$  \_

assumes

```
Predicate (DL),
Predicate (DR),
Pairs (DL, DR)
```

includes

Predicate (pair [DL, DR])

introduces

\_\_  $\times$  \_ : pred [DL], pred [DR]  $\rightarrow$  pred [pair [DL, DR]]

asserts

 $\forall$  e: DL, e': DR, p: pred [DL], q: pred [DR]

% Semantics of p x q
% ----(p × q) ? [e, e'] == p ? e ∧ q ? e'

% Trait of Constant Predicate K  $_p$  (\_\_)

includes

Predicate (T) % for  ${\rm K}_p$  (b)

introduces

 $\mathtt{K}_p$  : Bool ightarrow pred [T]

asserts

```
∀ x: T, b: Bool
% Semantics of K<sub>p</sub>
% -----
K<sub>p</sub> (b) ? x == b
```

```
\% Trait of Curried predicate, C _p (__, _)
```

assumes

Pairs (T1, T2), % for domain of p Predicate (pair [T1, T2])

includes

```
Predicate (T2) % for C_p (p, x)
```

introduces

 $\mathtt{C}_p$  : pred [pair [T1, T2]], T1 ightarrow pred [T2]

#### asserts

 $\forall$  p: pred [pair [T1, T2]], x: T1, y: T2

% Semantics of  ${\rm C}_p$ 

% -----  
$$C_p$$
 (p, x) ? y ==  $C_p$  ? [x, y]

# A.5 Query Formers (Table 3.3)

% Former that emulates SELECT--FROM--WHERE. General Unary % Iterator

assumes

```
Function (T, U),
Predicate (T),
Bag (T)
```

includes

Bag (U), Function (bag [T], bag [U])

introduces

iterate: pred [T], fun [T, U]  $\rightarrow$  fun [bag [T], bag [U]]

asserts

 $\forall$  p: pred [T], f: fun [T, U], A: bag [T], x: T

% Semantics of iterate

% -----

iterate (p, f) ! ⊘ == ⊘
(p ? x) ⇒
 iterate (p, f) ! insert (x, A) = insert (f ! x, iterate (p, f) ! A)
 ~ (p ? x) ⇒
 iterate (p, f) ! insert (x, A) = iterate (p, f) ! A

implies

 $\forall$  p: pred [T], f: fun [T, U], A: bag [T], x: T, e: U e  $\in$  (iterate (p, f) ! A) ==  $\exists$  x (x  $\in$  A  $\land$  (p ? x)  $\land$  e = (f ! x))

% Binary Iterator.

assumes

```
Pairs (T, U),
Pairs (T, bag [U]),
Bag (T),
Pairs (bag [T], U),
Function (pair [T, U], V),
Predicate (pair [T, U])
```

includes

Bag (V),
Function (pair [T, bag [U]], bag [V]),
CurryingP (T, U),
CurryingF (T, U, V),
Iterate (U, V)

introduces

```
iter: pred [pair [T, U]], fun [pair [T, U], V] \rightarrow fun [pair [T, bag [U]], bag [V]]
```

#### asserts

```
∀ p: pred [pair [T, U]], f: fun [pair [T, U], V], A: bag [U], x: T
% Semantics of Iter
% -----
iter (p, f) ! [x, A] == iterate (C<sub>p</sub> (p, x), C<sub>f</sub> (f, x)) ! A
```

implies

∀ p: pred [pair [T, U]], f: fun [pair [T, U], V], A: bag [U], x: T, e: V, u: U e ∈ (iter (p, f) ! [x, A]) == ∃ u (u ∈ A ∧ (p ? [x, u]) ∧ e = (f ! [x, u]))

% Trait of the unnesting former, unnest, which pairs % T elements (t) with each member of some bag that is % generated by invoking a function on t.

assumes

Bag (T),

```
Bag (U),
Pairs (T, U),
Function (pair [T, U], V),
Function (T, bag [U])
```

## includes

```
Bag (V),
Function (bag [T], bag [V]),
```

ConstantP (U), CurryingF (T, U, V), Iterate (U, V)

```
introduces
```

unnest: fun [pair [T, U], V], fun [T, bag [U]]  $\rightarrow$  fun [bag [T], bag [V]]

### asserts

```
\forall f: fun [pair [T, U], V], g: fun [T, bag [U]], x: T, A: bag [T]
```

% Semantics of unnest

% -----unnest (f, g) !  $\oslash$  ==  $\oslash$ unnest (f, g) ! insert (x, A) == (iterate (K<sub>p</sub> (true), C<sub>f</sub> (f, x)) ! (g ! x))  $\cup$  (unnest (f, g) ! A)

## implies

```
∀ f: fun [pair [T, U], V],
g: fun [T, bag [U]], x: T, y: U, A: bag [T], e: V
```

$$\begin{array}{l} \mathsf{e} \ \in \ (\mathbf{unnest} \ (\mathtt{f}, \ \mathtt{g}) \ ! \ \mathtt{A}) \ == \\ (\exists \ \mathtt{x} \ \exists \ \mathtt{y} \ (\mathtt{x} \ \in \ \mathtt{A} \ \land \ (\mathtt{e} \ = \ \mathtt{f} \ ! \ [\mathtt{x}, \ \mathtt{y}]) \ \land \ \mathtt{y} \ \in \ (\mathtt{g} \ ! \ \mathtt{x}))) \end{array}$$

% General Binary Iterator

```
assumes
```

```
Pairs (T1, T2),
Function (pair [T1, T2], U),
Predicate (pair [T1, T2]),
Bag (T1),
Bag (T2),
Pairs (bag [T1], bag [T2])
```

includes

```
Bag (U),
Function (pair [bag [T1], bag [T2]], bag [U]),
CurryingP (T1, T2),
CurryingF (T1, T2, U),
Iterate (T2, U),
InverseP (T1, T2),
Pairs (T2, T1),
Projection (T2, T1),
CurryingP (T2, T1),
CurryingF (T2, T1, U),
Pairing (pair [T2, T1], T1, T2),
Composition (pair [T2, T1], pair [T1, T2], U),
```

```
Iterate (T1, U)
```

#### introduces

```
join: pred [pair [T1, T2]], fun[pair [T1, T2], U] \rightarrow fun [pair [bag [T1], bag [T2]], bag [U]]
```

## asserts

```
∀ p: pred [pair [T1, T2]], f: fun[pair [T1, T2], U],
A: bag [T1], B: bag [T2], x: T1, y: T2
% Semantics of Join
% ------
join (p, f) ! [⊘, B] == ⊘
join (p, f) ! [∞, B] == ⊘
(iterate (C<sub>p</sub> (p, x), C<sub>f</sub> (f, x)) ! B) ∪ (join (p, f) ! [A, B])
```

## implies

```
∀ p: pred [pair [T1, T2]], f: fun[pair [T1, T2], U],
A: bag [T1], B: bag [T2], x: T1, y: T2, e: U
join (p, f) ! [A, ⊘] == ⊘
join (p, f) ! [A, insert (y, B)] ==
(iterate (C<sub>p</sub> (p<sup>-1</sup>, y), C<sub>f</sub> (f ∘ (snd, fst), y)) ! A) ∪
(join (p, f) ! [A, B])
e ∈ (join (p, f) ! [A, B]) ==
∃ x ∃ y (x ∈ A ∧ y ∈ B ∧ (p ? [x, y]) ∧ e = (f ! [x, y]))
```

#### 

```
LSJoin (T1, T2, U): trait
```

% Left semi-join

assumes

```
Bag (T1),
Bag (T2),
Pairs (bag [T1], bag [T2]),
Pairs (T1, bag [T2]),
Predicate (pair [T1, bag [T2]]),
Function (T1, U)
```

includes

Bag (U), Function (pair [bag [T1], bag [T2]], bag [U])

introduces

```
lsjoin: pred [pair [T1, bag [T2]]], fun[T1, U] \rightarrow
fun [pair [bag [T1], bag [T2]], bag [U]]
```

```
asserts
```

```
∀ p: pred [pair [T1, bag [T2]]],
    f: fun[T1, U], A: bag [T1], B: bag [T2], x: T1
% Semantics of lsjoin
% ------
lsjoin (p, f) ! [⊘, B] == ⊘
lsjoin (p, f) ! [∞, B] == ⊘
lsjoin (p, f) ! [insert (x, A), B] ==
  (if p ? [x, B] then
    insert (f ! x, lsjoin (p, f) ! [A, B]) else
    lsjoin (p, f) ! [A, B])
```

implies

```
∀ p: pred [pair [T1, bag [T2]]], f: fun[T1, U],
A: bag [T1], B: bag [T2], e: U, x: T1
```

 $e \in (lsjoin (p, f) ! [A, B]) == \exists x (x \in A \land p ? [x, B] \land e = (f ! x))$ 

% Right semi-join

assumes

Bag (T1),
Bag (T2),
Pairs (bag [T1], bag [T2]),
Pairs (T2, bag [T1]),
Predicate (pair [T2, bag [T1]]),
Function (T2, U)

includes

Bag (U), Function (pair [bag [T1], bag [T2]], bag [U])

introduces

rjoin: pred [pair [T2, bag [T1]]], fun[T2, U]  $\rightarrow$  fun [pair [bag [T1], bag [T2]], bag [U]]

asserts

```
∀ p: pred [pair [T2, bag [T1]]],
    f: fun[T2, U], A: bag [T1], B: bag [T2], y: T2
% Semantics of rjoin
% ------
rjoin (p, f) ! [A, ⊘] == ⊘
rjoin (p, f) ! [A, insert (y, B)] ==
  (if p ? [y, A] then
    insert (f ! y, rjoin (p, f) ! [A, B]) else
    rjoin (p, f) ! [A, B])
```

implies

∀ p: pred [pair [T2, bag [T1]]], f: fun[T2, U], A: bag [T1], B: bag [T2], e: U, y: T2

 $e \in (rjoin (p, f) ! [A, B]) == \exists y (y \in B \land p ? [y, A] \land e = (f ! y))$ 

```
% Trait of the nested-join former, njoin, which is applied
% to a pair of bags (of T1 and T2 elements respectively)
% and returns a bag of [T1, V] pairs such that
% the first member is some element, t of the first bag
% input, and the second member is the result of applying
% a function (g: bag [U] \rightarrow V) to the bag resulting
% from applying another function (f: T2 \rightarrow U) to elements
% in the second bag input that are related by a predicate
% (p: [T1, T2] \rightarrow Bool) to t
```

assumes

```
Bag (T1),
Bag (T2),
Bag (U),
Function (T2, U),
Function (bag [U], V),
Predicate (pair [T1, T2]),
Pairs (T1, T2),
Pairs (bag [T1], bag [T2])
```

### includes

```
Pairs (T1, V),
Bag (pair [T1, V]),
Function (pair [bag [T1], bag [T2]], bag [pair [T1, V]]),
CurryingP (T1, T2),
Iterate (T2, U)
```

#### introduces

```
njoin: pred [pair [T1, T2]] , fun [T2, U], fun [bag [U], V] \rightarrow fun [pair [bag [T1], bag [T2]], bag [pair [T1, V]]]
```

#### asserts

```
∀ A:bag[T1], B:bag[T2], p: pred [pair [T1, T2]],
f: fun[T2, U], g: fun [bag [U], V], x: T1
```

```
\% Semantics of {\bf njoin}
```

```
% ------
```

njoin (p, f, g) ! [ $\oslash$ , B] ==  $\oslash$ 

(x  $\in$  A)  $\Rightarrow$ 

(njoin (p, f, g) ! [insert (x, A), B] = njoin (p, f, g) ! [A, B])  $\sim (x \in A) \Rightarrow$  (njoin (p, f, g) ! [insert (x, A), B] =  $insert ([x, g ! (iterate (C_f (p, x), f) ! B)],$ njoin (p, f, g) ! [A, B]))

implies

∀ A:bag[T1], B:bag[T2], p: pred [pair [T1, T2]], f: fun[T2, U], g: fun [bag [U], V], x: T1, Bs: bag [U], e: pair [T1, V]

 $e \in (njoin (p, f, g) ! [A, B]) ==$  $\exists x \exists Bs (x \in A \land Bs = (iterate (C_p (p, x), f) ! B) \land e = [x, g ! Bs])$ 

% Trait of the general binary quantifier former, ex which forms % binary quantifier formers on pairs.

assumes

Bag (T2),
Pairs (T1, T2),
Predicate (pair [T1, T2])

includes

Pairs (T1, bag [T2]), Predicate (pair [T1, bag [T2]]) introduces

```
ex : pred [pair [T1, T2]] \rightarrow pred [pair [T1, bag [T2]]]
asserts
\forall y: T2, x: T1, p: pred [pair [T1, T2]], A: bag [T2]
% Semantics of ex
% ------
ex (p) ? [x, A] == \exists y (y \in A \land p ? [x, y])
```

# 

% Trait of the general binary quantifier former, fa which forms % binary quantifier formers on pairs.

assumes

```
Bag (T2),
Pairs (T1, T2),
Predicate (pair [T1, T2])
```

includes

```
Pairs (T1, bag [T2]),
Predicate (pair [T1, bag [T2]])
```

## introduces

% Trait of the general quantifier iterator former, exists % form quantifier style predicates on bags of T.

assumes

Bag (T), Predicate (T)

includes

Predicate (bag [T])

introduces

 $\mathbf{exists} \ : \ \mathtt{pred} \ \mathtt{[T]} \ \rightarrow \ \mathtt{pred} \ \mathtt{[bag} \ \mathtt{[T]]}$ 

asserts

 $\forall$  p: pred [T], A: bag [T], x: T

- % Semantics of exists
- % ----
  - exists (p) ? A ==  $\exists x (x \in A \land p ? x)$

% Trait of the general quantifier iterator former, forall % form quantifier style predicates on bags of T.

assumes

Bag (T), Predicate (T)

includes

Predicate (bag [T])

introduces

forall : pred [T]  $\rightarrow$  pred [bag [T]]

asserts

 $\forall$  p: pred [T], A: bag [T], x: T

% Semantics of exists

% -----

forall (p) ? A ==  $\forall x (x \in A \Rightarrow p ? x)$ 

# Appendix B

# LP Proof Scripts

# B.1 Proof Scripts for CNF

Available from ftp://wilma.cs.brown.edu/u/mfc/cnf-scripts.lp.

## **B.2** Proof Scripts for SNF

Available from ftp://wilma.cs.brown.edu/u/mfc/snf-scripts.lp.

# **B.3** Proof Scripts for Predicate Pushdown

Available from ftp://wilma.cs.brown.edu/u/mfc/pushdown-scripts.lp.

## **B.4** Proof Scripts for Magic Sets

Available from ftp://wilma.cs.brown.edu/u/mfc/magic-scripts.lp.

# **B.5** Proof Scripts for Rules of Chapter 5

Available from ftp://wilma.cs.brown.edu/u/mfc/vldb-scripts.lp.

# B.6 Proof Scripts for Rules of Chapter 6

Available from ftp://wilma.cs.brown.edu/u/mfc/exp-scripts.lp.

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