AMM Project

Overall, learning about AMMs and primarily looking into Uniswap’s docs and whitepapers has been a great learning experience. It was also extremely interesting to see the smart contracts act as a liquidity pool. AMMs in the defi space seem like an extremely scalable project due to the permissionless nature of smart contracts. If there was a customary, universal contract that could allow people to deploy liquidity pools extremely easily, I feel like this would be a cool niche and defi that web3 developers can take advantage of. I thought that looking into deeper calculations embedded in AMMs really helped me learn and understand how prices work in this exchange mechanism. The following screenshots are my interpretations of divergence loss, linear slippage, angular slippage and load in the context of AMMs.

Divergence Loss: This value helps create equilibrium in the liquidity pools since ratio balance is quintessential. Reading through Uniswap’s smart contracts, it shows that token pairs must contain equal total values and this is the cost to liquidity providers.
Slippage: The reason that slippage is important to consider in liquidity pools, every trade makes an impact on the expected price after the transaction. This includes linear slippage, which calculates the direct impact to the buyer’s price difference. The second is angular slippage, which characterizes how that buyer affects prices for later buyers.

```solidity
// **
// @notice Public linear slippage function for ETH to Token trades with an exact input.
// @param tokens_sold Amount of the token sold.
// @return Linear Slippage of proposed trade.
//
function getTokenToEthLinearSlippage(uint256 tokens_sold) public view returns (uint256) {
    // get the supply of tokens in the pool
    uint256 token_supply = token.balanceOf(address(this));

    // precalculate some values
    uint256 token_supply_sq = token_supply.mul(token_supply);
    uint256 tokens_sold_sq = tokens_sold.mul(tokens_sold);

    uint256 numerator = token_supply_sq.mul(token_supply.add(tokens_sold));
    uint256 denominator = tokens_sold_sq.mul(token_supply_sq).add(2.mul(tokens_sold).mul(token_supply)).add(1);

    return numerator.div(denominator).mul(-1);
}
```

```solidity
// **
// @notice Public linear slippage function for ETH to Token trades with an exact input.
// @param eth_sold Amount of ETH sold.
// @return Linear Slippage of proposed trade.
//
function getEthToTokenLinearSlippage(uint256 eth_sold) public view returns (uint256) {
    // get the supply of eth in the pool
    uint256 eth_supply = address(this).balance;

    // precalculate some values
    uint256 eth_supply_sq = eth_supply.mul(eth_supply);
    uint256 eth_sold_sq = eth_sold.mul(eth_sold);

    uint256 numerator = eth_supply_sq.mul(eth_supply.add(eth_sold));
    uint256 denominator = eth_sold_sq.mul(eth_supply_sq).add(2.mul(eth_sold).mul(eth_supply)).add(1);

    return numerator.div(denominator).mul(-1);
}
```
function getETHToTokenAngularSlippage(uint256 eth_sold) public view returns (uint256) {
    // get the supply of eth in the pool
    uint256 eth_supply_0 = address(this).balance;
    // get the supply of eth in the pool after tx
    uint256 eth_supply_1 = eth_supply_0 - eth_sold;

    // get the supply of tokens in the pool
    token_supply_0 = token.balanceOf(address(this));

    // compute k
    uint256 k = eth_supply_0.mul(token_supply_0);

    // get the supply of tokens in the pool after tx
    token_supply_1 = k / eth_supply_1;

    // calculate valuation before tx
    uint256 v_0 = eth_supply_0.div(token_supply_0.add(eth_supply_0));

    // calculate valuation after tx
    uint256 v_1 = eth_supply_0.div(token_supply_0.add(eth_supply_0));

    uint256 numerator = v_0.sub(v_1);
    uint256 denominator = v_0.mul(v_1).add(1).sub(v_0).add(1).sub(v_1);

    return atanSmall(numerator.div(denominator));
}

function getTokenToETHAngularSlippage(uint256 tokens_sold) public view returns (uint256) {
    // get the supply of tokens in the pool
    uint256 token_supply_0 = token.balanceOf(address(this));
    // get the supply of tokens in the pool after the tx
    uint256 token_supply_1 = token_supply_0 - tokens_sold;

    // get the supply of eth in the pool
    uint256 eth_supply_0 = address(this).balance;

    // compute k
    uint256 k = eth_supply_0.mul(token_supply_0);

    // get the supply of eth in the pool after tx
    eth_supply_1 = k / token_supply_1;

    // calculate valuation before tx
    uint256 v_0 = token_supply_0.div(eth_supply_0.add(token_supply_0));

    // calculate valuation after tx
    uint256 v_1 = token_supply_0.div(eth_supply_0.add(token_supply_0));

    uint256 numerator = v_0.sub(v_1);
    uint256 denominator = v_0.mul(v_1).add(1).sub(v_0).add(1).sub(v_1);

    return atanSmall(numerator.div(denominator));
}
**Load**: This value is simply just a measure of balancing provider and traders costs.

```solidity
/**
   * @notice Public load function for ETH to Token trades with an exact input.
   * @param eth_sold Amount of ETH sold.
   * @return Load of proposed trade.
   */
function getEthToTokenLoad(uint256 eth_sold) public view returns (uint256) {
    return getEthToTokenDivergenceLoss(eth_sold) * getEthToTokenLinearSlippage(eth_sold);
}

/**
   * @notice Public load function for ETH to Token trades with an exact input.
   * @param tokens_sold Amount of the token sold.
   * @return Load of proposed trade.
   */
function getTokenToEthLoad(uint256 tokens_sold) public view returns (uint256) {
    return getEthToTokenDivergenceLoss(tokens_sold) * getEthToTokenLinearSlippage(tokens_sold);
}
```

We propose the following measure to balance provider-facing and trader-facing costs.