

# Medical Bioinformatics (CSCI295-L)

Genome-Wide Association Studies, Protein Folding and  
Immunogenomics

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SYLLABUS

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# 1 Short Introductions

## Class 1

Topics covered:

1. The Course Sections
  - (a) Genome-Wide Association Studies (GWAS)
  - (b) Immunogenomics
  - (c) Protein Folding
2. SNPs and the Human Genome: SNPs, haplotypes, mutation, recombination, genetic determinants of disease
3. SNP Genetic Variation: A look at the data
4. Fundamental Challenges: (1) Very limited success so far regarding the knowledge of the human genome sequence to the clinical impact ; and (2) Causality of disease mechanism may be unknowable

## Class 2

• Topics covered:

1. Introduction to Immunogenomics: proteomes, peptides, epitopes, T-cells, MHC, T-cell vaccines
2. Introduction to Association Studies: haplotypes blocks, tagging SNPs: block definitions (e.g., 4-gametes block test), the Hudson-Kaplan 4-gametes block decomposition, minimum informative subset of tagging SNPs via Informativeness, graph theory modeling using the minimum set cover problem

• Class readings:

- Guilt by Association
- Viruses in the Sea

## Class 3

• Topics covered:

1. Introduction to Protein Folding: the comparative genomics landscape (1-dimensional = biomolecular sequence analysis, DNA, protein, regulatory regions, SNPs, haplotypes, genome assembly; 3-dimensional = protein structure; logic/chemistry "dimension" = expression, networks), self-avoiding walks, contacts, statistical mechanics, protein structure alignment, fold recognition, the Computational Protein Folding Competition (CASP= Critical Assessment of Structure Prediction), contact maps, contact map overlap structure alignment, fold recognition

2. Introduction to Genome-Wide Association Studies (GWAS): 17 caveats

- Class readings:
  - Drinking from the Fire Hose – Statistical Issues in GWAS

## 2 The Hardy-Weinberg Model

### Class 4

- Topics covered:
  1. Population Genetics Models: population, diploid organism, random mating, non-overlapping generations, genotype-gamete-genotype, genotype frequency, gene frequency
  2. The Hardy-Weinberg model for one locus: Hardy-Weinberg Equilibrium (HWE), Fundamental Theorem 1 (HWE attained in one generation), Fundamental Theorem 2 (constancy of allele frequencies in every generation), HW frequencies satisfy the  $Y^2 = XZ$  equation, the Hardy=Weinberg Theorem (one variable  $x$  only:  $x = X + Y$ )

### Class 5

- Topics covered:
  1. The Hardy-Weinberg model for two loci: Linkage equilibrium (LE), recombination rate  $r$  (do not confuse with  $r^2$  the measure of LD - different  $r$  notations), linkage disequilibrium (LD); double heterozygotes, recombinant and non-recombinant gametes, Lewontin's linkage disequilibrium parameter  $D$ , single locus HWE = no evolution (constancy of frequencies), two loci HW = potential for evolution based on parameters  $D$  and  $r$ .

## 3 Linkage Disequilibrium and GWAS

### Class 6

- Topics covered:
  1. The first measure of linkage disequilibrium:  $D$ . The  $D$  equation,  $D'$  and the independence of allele frequencies
  2. Examples: Evaluation of HWE at each locus, and of LD between them.
  3. The second measure of linkage disequilibrium:  $r^2$ .
  4. Complete LD, Perfect LD, Useful LD.

- Class readings:
  - A haplotype map of the human genome

## Class 7

- Topics covered:
  1. Properties of the LD measure  $r^2$ : its correlation coefficient definition,  $r^2$  as a statistical test, description of the loss in efficiency when one marker is replaced by another marker, its relation to  $\chi^2$ , drawbacks (e.g., measure is pairwise and not clear how to extend to many sites)
  2. Genome-wide association studies: an outline of the methodology (genome is huge so "interesting" pattern occur by chance; HW, Tagging SNPs, Haplotype Phasing are computational methods in active research not yet consensus on how to use and apply them to data; the problem of missing data; case and control samples have different parameters and hard to match and contrast statistically and algorithmically for the most discrepancy (e.g., different rates of missing data); LD is a non-quantitative phenomenon, there is no natural scale for it); tagging SNPs are effective only for capturing common variants, and tagging on one population only poorly performs in another population; population substructure can generate spurious phenotype associations; to phase or not to phase - associations of unphased genotypes is limited but phasing with an adhoc choice of method adds uncertainty as well.
  3. An introduction to HapMap

- Class readings:
  - Linkage disequilibrium and the mapping of complex human traits

## 4 Tagging SNPs and GWAS

### Class 8

- Topics covered:
  1. The architecture of linkage disequilibrium based haplotype blocks across chromosome 6, 21, 22
- Class readings:
  - Blocks of limited haplotype diversity revealed by high-resolution scanning of the human chromosome 21

## Class 9

- Topics covered:
  1. Tagging SNPs and the Minimum Informative Subset of Tagging SNPs
  2. A set of desiderata (axioms) for tagging SNPs selection:
    - (a) To be extendable uniquely to multi markers
    - (b) To be consistent with the LD measures
    - (c) To be haplotype block free (no adhoc definition of block required)
    - (d) To be hypothesis free (e.g., not specific to a certain disease or trait)
    - (e) To be algorithmically sound (practical for genome-wide data)
    - (f) To be statistically sound (no overfitting)
  3. The Informativeness measure satisfies all the above desiderata
  4. The modeling of Informativeness via the Minimum Set Cover Problem
  5. A dynamic programming algorithm for the minimally informative  $K$  SNPs problem.
- Class readings:
  - Efficiency and power in genetic association studies
  - Selecting a maximally informative set of SNPs for association analyses using LD
  - The structure of the Haplotype Blocks in the Human Genome

## 5 Haplotype Phasing and GWAS

### Class 10

- Topics covered:
  1. The Haplotype Phasing Problem: The Clark Method and the Maximum Likelihood Method: genotypes, haplotypes, genotype explanations
  2. The Clark Method: greedy algorithm, Clark rule, three difficulties.
- Class readings:
  - Optimal haplotype block free selection of tagging SNPs for GWAS (and two supplemental documents)
  - Multiple Sclerosis GWAS: Risk alleles for multiple sclerosis identified by a genomewide study

## Class 11

- Topics covered:
  1. The Expectation-Maximization Algorithm of Excoffier-Slatkin for computing haplotype frequencies and haplotype phase: intro to maximum likelihood, the EM algorithm background, computing haplotype frequencies and genotype explanations frequencies iteratively; the EM algorithm for the haplotype frequencies, and its application to haplotype phasing
- Class readings:
  - Inference of haplotypes from PCR-amplified samples of diploid populations
  - Maximum-Likelihood estimation of molecular haplotype frequencies in a diploid population

## Class 12

- Topics covered:
  1. Guest Lecturer: Jonathan Yewdell (NIH): Topics in Immunogenomics
- Class readings:
  - Identifying cytotoxic T-cell epitopes from genomic and proteomic information

## 6 GWAS studies in detail: Multiple Sclerosis and Autism

### Class 13

- Topics covered:
  1. The GWAS for Multiple Sclerosis
- Class readings:
  - Istrail, Yewdell et. al "The immunopeptidome of human and their pathogens"

## 7 Wright-Fisher, Infinite Allels and Urn Models

### Class 14

- Topics covered:
  1. The Wright-Fisher Model and the Infinite Allele Model
  2. Urn Models for population genetics: Polya Urn models
  3. The Wright-Fisher Model: Mutation, Random Genetic Drift, Selection
  4. Wright-Fisher and Markov Chains
  5. The Infinite Allele Model
  6. Stationarity of partitions
  7. Ewens' Sampling Lemma
- Class readings:
  - Genetic mapping of human disease (and supplementary material)

### Class 15

- Topics covered:
  1. The Urn model for the Infinite Allele model is the Hoppe's Urn model
  2. Computing  $Q$  probabilities for the Hoppe's urn model
  3. The Clark Algorithm revisited: the analysis of the three difficulties based on the Infinite Allele model theory

## 8 Computational Complexity of the Haplotype Phasing Problem

### Class 16

- Topics covered:
  1. Computational Complexity of the Haplotype Phasing Problem
    - The Parsimony Haplotype Phasing is NP-complete – The Hubbell Theorem 1.
    - The Global Maximum Likelihood Haplotype Phasing is NP-complete – The Hubbell Theorem 2.
    - The Clark Maximal Resolution Haplotype Phasing is NP-complete.
- Class readings:
  - E. Hubbell's manuscript, 2000

## 9 Tests of Association

### Class 17

- Topics covered:
  1. Tests of Association
    - $2 \times 2$  contingency tables, the hypergeometric distribution and the Fisher's Exact Test
    - Contingency tables of arbitrary size: The Chi-Square Test (the historical test) and the Kullback-Leibler relative entropy test (the right test)
  2. The Coalescent - introduction
    - Coalescent with mutation
    - Gene trees vs allele/haplotype trees vs haplotype networks

## 10 Complex Disease and Heritability

### Class 18

- Topics covered:
  1. Complex Disease and Heritability
    - The "triangle" of the etiology of disease: single gene, polygenic, environment
    - Dichotomous vs continuous traits
    - Polygenic theory: Heritability and Thresholds
    - Polygenic susceptibility to disease
    - Regression, covariance, regression slope, correlation coefficient, Fisher's paper on the correlation between relatives
    - Heritability as a correlation coefficient

### Class 19

- Topics covered:
  1. Guest Lecturer: Sam Broder (Celera, former Director of the National Cancer Institute): "Towards Evidence-Based Medicine: The Human Genome: 3 Billion Letters of Code, But Whos Counting?" followed by a Sweat Box Session on The Missing Heritability Puzzle – "The Genome as a Teacher: In This Class, Does the Teacher Grade on a Curve?"



## Class 20

- Topics covered:
  1. Broad-sense and narrow sense heritability and the "missing heritability" puzzle; common and rare variants
  2. The Coalescent with recombination; ancestral recombination graphs (ARG)
- Class readings:
  - Jon Mclellan and Mary-Claire King "Genetic heterogeneity in human disease," 2010
  - Eichler et al "Missing heritability and strategies for finding the underlying causes of complex disease" 2010

## 11 The Coalescent and GWAS

### Class 21

- Topics covered:
  1. The Miniciello-Durbin ARG reconstruction algorithm
  2. Population Substructure
- Class readings:
  - Miniciello-Durbin "Mapping trait loci by use of inferred ancestral recombination graphs"

## 12 Statistical Hypothesis Testing in GWAS

### Class 22

- Topics covered:
  1. Classical hypothesis testing – the five steps and GWAS
  2. Statistical power
  3. Multiple testing
  4. The Transmission/Disequilibrium test statistic (TDT)
  5. The Cochran-Mantel-Haenzel test statistic

## 13 GWAS and the Missing Heritability Puzzle

### Class 23

- Topics covered:
  1. Disease Models: Common Disease Common Variant
  2. Rare alleles: Common Disease - many rare variants
  3. Genetic heterogeneity in human disease
  4. Missing heritability and strategies for finding underlying causes of complex disease

## 14 Protein Folding and Drug Design

### Class 24

- Topics covered:
  1. Protein Folding in Lattice Models: Ken Dill's HP-Model
- Class readings:
  - F. Lam and S.Istrail "Combinatorial algorithms for protein folding in lattice models: a survey of mathematical results"

### Class 25

- Topics covered:
  1. Protein Folding in Lattice Models: Folding algorithms

### Class 26

- Topics covered:
  1. The Medicinal Chemist Compound Tinkering Problem: chemical graph theory

### Class 27

- Topics covered:
  1. Concepts of drug-likeness, and the Lipinski rule of five

## 15 Immunogenomics

### Class 28

- Topics covered:
  1. Drug resistance, codon-bias, RNA and HIV