Notre-Dame cathedral: Firefighters tackle blaze in Paris

The fire department said a major operation was under way
Computational Imaging for VLBI Image Reconstruction

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Abstract

Very long baseline interferometry (VLBI) is a technique for imaging celestial radio emissions by simultaneously observing a source from telescopes distributed across Earth. The challenges in reconstructing images from fine angular resolution VLBI data are immense. The data is extremely sparse and noisy, thus requiring statistical image models such as those designed in the computer vision community. In this paper we present a novel Bayesian approach for VLBI image reconstruction. While other methods often require careful tuning and parameter selection for different types of data, our method (CHIRP) produces good results under different settings such as low SNR or extended emission. The success of our method is demonstrated on realistic synthetic experiments as well as publicly available real data. We present this problem in a way that is accessible to members of the community, and provide a dataset website (vlbimaging.csail.mit.edu) that facilitates controlled comparisons across algorithms.

1. Introduction

High resolution celestial imaging is essential for progress in astronomy and physics. For example, imaging the plasma surrounding a black hole’s event horizon at high resolution could help answer many important questions; most notably, it may substantiate the existence of black holes [10] as well as verify and test the effects of general relativity [22]. Recently, there has been an international effort to create an Event Horizon Telescope (EHT) capable of imaging a black hole’s event horizon for the first time [12, 13]. The angular resolution necessary for this observation is at least an order of magnitude smaller than has been previously used to image radio sources [24]. As measurements from the EHT become available, robust algorithms able to reconstruct images in this fine angular resolution regime will be necessary.

Although billions of dollars are spent on astronomical imaging systems to acquire the best images, current reconstruction techniques suffer from unsophisticated priors and a lack of inverse modeling [36], resulting in sub-optimal images. Image processing, restoration, sophisticated inference algorithms, and the study of non-standard cameras are all active areas of computer vision. The computer vision community’s extensive work in these areas is invaluable to the success of these reconstruction methods and can help push the limits of celestial imaging, [16, 17, 27, 43].

Imaging distant celestial sources with high resolving power (i.e., fine angular resolution) requires single-dish telescopes with prohibitively large diameters due to the inverse relationship between angular resolution and telescope diameter [41]. For example, it is predicted that emission surrounding the black hole at the center of the Milky Way subtends $\approx \frac{2.5 \times 10^{-10}}{\text{radians}}$ [15]. Imaging this emission with a $10^{-10}$ radian resolution at a $1.3$ mm wavelength would require a telescope with a $13000$ km diameter. Although a single telescope this large is unrealizable, by simultaneously collecting data from an array of telescopes located around the Earth, it is possible to emulate samples from a single telescope with a diameter equal to the maximum distance between telescopes in the array. Using multiple telescopes in this manner is referred to as very long baseline interferometry (VLBI) [41]. Refer to Figure 1a.

People in the computer vision community integral to effort!

Paper describing technique @ CVPR 2016

Had 11 citations up to last week…
How does it work?

Figure 2. **Simplified Interferometry Diagram**: Light is emitted from a distant source and arrives at the telescopes as a plane wave in the direction \( \hat{s} \). An additional distance of \( B \cdot \hat{s} \) is necessary for the light to travel to the farther telescope, introducing a time delay between the received signals that varies depending on the source's location in the sky. The time-averaged correlation of these signals is a sinusoidal function related to the location of the source. This insight is generalized to extended emissions in the van Cittert-Zernike Thm. and used to relate the time-averaged correlation to a Fourier component of the emission image in the direction \( \hat{s} \).
Problems:

- Very noisy data!
- Significant phase shifts

Computer vision to the rescue!
- Image modeling in Fourier domain -> represent phase
- Data-driven priors using Gaussian mixture models on patches of signal -> represent expected statistics!
- Expected Patch Log Likelihood – Zoran and Weiss ICCV 2011 -> generic prior method for image reconstruction
- Simulated data to build prior
Figure 2: The intuition behind our method. 2a A training image. 2b The prior learned from the image, only the 36 most frequent patches are shown with their corresponding count above the patch - flat patches are the most likely ones, followed by edges with 1 pixel etc. 2c A noisy image we wish to restore. 2d Restoring using non-overlapping patches - note the severe artifacts at patch borders and around the image. 2e Taking the center pixels from each patch. 2f Better results are obtained by restoring all overlapping patches, averaging the results - artifacts are still visible, and a lot of the patches in the resulting image are unlikely under the prior. 2g Result using the proposed method - note that there are very few artifacts, and most patches are very likely under our prior.
Multiple view geometry

Camera calibration

Epipolar geometry

Dense depth map estimation

\[ x = K[R \ t]X \]
Correspondence problem

Multiple match hypotheses satisfy epipolar constraint, but which is correct?

Figure from Gee & Cipolla 1999
Results with window search

Window-based matching
(best window size)

‘Ground truth’
“Shortest paths” for scan-line stereo

Can be implemented with dynamic programming
Ohta & Kanade ’85, Cox et al. ’96, Intille & Bobick, ‘01

Slide credit: Y. Boykov
Coherent stereo on 2D grid

- Scanline stereo generates streaking artifacts

- Can’t use dynamic programming to find spatially coherent disparities/ correspondences on a 2D grid
Stereo matching as energy minimization

\[ E = \alpha E_{\text{data}} (I_1, I_2, D) + \beta E_{\text{smooth}} (D) \]

\[ E_{\text{data}} = \sum_i \left( W_1(i) - W_2(i + D(i)) \right)^2 \]

\[ E_{\text{smooth}} = \sum_{\text{neighbors } i,j} \rho(D(i) - D(j)) \]

Energy functions of this form can be minimized using graph cuts.


Source: Steve Seitz
Better results…

Graph cut method

Boykov et al., Fast Approximate Energy Minimization via Graph Cuts.
International Conference on Computer Vision, September 1999.

For the latest and greatest:  http://www.middlebury.edu/stereo/
SIFT + Fundamental Matrix + RANSAC + dense correspondence

Building Rome in a Day
By Sameer Agarwal, Yasutaka Furukawa, Noah Snavely, Ian Simon, Brian Curless, Steven M. Seitz, Richard Szeliski
Communications of the ACM, Vol. 54 No. 10, Pages 105-112
SIFT + Fundamental Matrix + RANSAC + dense correspondence

The Visual Turing Test for Scene Reconstruction
Supplementary Video

Qi Shan*  Riley Adams*  Brian Curless*
Yasutaka Furukawa*  Steve Seitz**

*University of Washington  *Google

3DV 2013
Stereo correspondence

• Let $x$ be a point in left image, $x'$ in right image

• Epipolar relation
  • $x$ maps to epipolar line $l'$
  • $x'$ maps to epipolar line $l$
How does a depth camera work?

Microsoft Kinect v1

Intel laptop depth camera
Active stereo with structured light

- Project “structured” light patterns onto the object
  - Simplifies the correspondence problem
  - Allows us to use only one camera

Stereo system!

Kinect: Structured infrared light

How does a depth camera work?

Stereo in infrared.
Time of Flight (Kinect V2)

- Depth cameras in HoloLens use *time of flight*
  - “SONAR for light”
  - Emit light of a known wavelength, and time how long it takes for it to come back
With either technique...

...I gain depth maps over time.
Once I have my depth map, what can I do with it?

Measure.
Combining! (Reorganize?)
What if we want to align...
but we have no matched pairs?

• Hough transform and RANSAC not applicable

Problem: no initial guesses for correspondence
Applications

Medical imaging: match brain scans or contours

Vision/Robotics: match point clouds
Iterative Closest Points (ICP) Algorithm

Goal:
Estimate transform between two dense point sets $S_1$ and $S_2$

1. **Initialize** transformation
   - Compute difference in mean positions, subtract
   - Compute difference in scales, normalize

2. **Assign** each point in $S_1$ to its nearest neighbor in $S_2$

3. **Estimate** transformation parameters $T$
   - Least squares or robust least squares, e.g., rigid transform

4. **Transform** the points in $S_1$ using estimated parameters $T$

5. **Repeat** steps 2-4 until change is very small (convergence)
Example: solving for translation

Problem: no initial guesses for correspondence

ICP solution

1. Initialize $t$ by mean point translation
2. Find nearest neighbors for each point
3. Compute transform using matches
4. Move points using transform
5. Repeat steps 2-4 until convergence
Example: aligning boundaries

1. Extract edge pixels \( p_1 \ldots p_n \) and \( q_1 \ldots q_m \)
2. Compute initial transformation (e.g., compute translation and scaling by center of mass, variance within each image)
3. Get nearest neighbors: for each point \( p_i \) find corresponding match \( (i) = \arg\min_j \text{dist}(p_i, q_j) \)
4. Compute transformation \( T \) based on matches
5. Transform points \( p \) according to \( T \)
6. Repeat 3-5 until convergence
ICP demonstration

Time = iterations of ICP
Sparse ICP

Sofien Bouaziz    Andrea Tagliasacchi    Mark Pauly
BundleFusion: Real-time Globally Consistent 3D Reconstruction using Online Surface Re-integration

Angela Dai¹  Matthias Nießner¹
Michael Zollhöfer²  Shahram Izadi³
Christian Theobalt²

¹Stanford University
²Max Planck Institute for Informatics
³Microsoft Research

(contains audio)
ScanNet: Richly-annotated 3D Reconstructions of Indoor Scenes

Angela Dai  Angel X. Chang  Manolis Savva  Maciej Halber
Thomas Funkhouser  Matthias Nießner

Stanford University
Princeton University
Technical University of Munich

CVPR 2017 (Spotlight)