

Equalities

- Variable
- expr
- base (num)
- constructor (→)

solved for

solve for

UNIFICATION

$$(w, l) = \Omega$$

Set of constraints
 Each constraint is an eq.
 Each eq. has two terms
 Each term is one of

Unify · set (constraints) →

Substitution
 θ

{ mapping [· solve for ·
 \rightarrow
 $\frac{\cdot}{T+}$]

$t_1 = t_2$

variable or expr

Θ

occurs check

if t_1 in Θ

add $\Theta(t_1) = t_2$ to constr

else

add $t_1 = t_2$ to Θ

and replace t_1 in Θ

w/ t_2

base

if t_2 is base

if same base as t_1

ignore

else error

if t_2 is constructed - error ←

if t_2 is "solve for"

push $t_2 = t_1$ onto constraints

Constr $(t_{1l} \rightarrow t_{2l})$

if t_2 is base - error
 if t_2 is constructed
 $(t_{1r} \rightarrow t_{2r})$

push $t_{1l} = t_{1r}$
 $t_{2l} = t_{2r}$

PRINCIPAL TYPES

$id \equiv (\lambda (x : _) : _ \ x) : \llbracket x \rrbracket \rightarrow \llbracket x \rrbracket$
 $'a \rightarrow 'a$

in $(if (id \ true) \quad 'a = \text{bool}$
 $(id \ 5) \quad 'a = \text{num}$
 $(id \ 6) \quad 'a = \text{num}$