

Lecture 16

MATLAB III: More Arrays and Design Recipe



Last Time (lectures 14 & 15)

Lecture 14: MATLAB I

- “Official” Supported Version in CS4: MATLAB 2018a
- How to start using MATLAB:
 - CS Dept. Machines - run ‘cs4_matlab’
 - Total Academic Handout (TAH) Local Install - software.brown.edu
 - MATLAB Online (currently 2019a) - matlab.mathworks.com
- Navigating the Workspace (command window, variables, etc.)
- Data types in MATLAB (everything is a 64-bit double float by default!)
- MATLAB Programs
 - scripts (like Python)
 - functions (file-based, outputs defined in signature)
- Anonymous functions and overwriting function names (oops!)

Last Time (lectures 14 & 15)

Lecture 15: MATLAB II

- Conditional Statements
 - `if...end`
 - `if...else...end`
 - `if...elseif...else...end`
 - `switch...end`
- Arrays and Matrices (default numeric type)
 - scalars (1x1 value)
 - 1D vectors (1xN or Nx1 arrays)
 - 2D matrices (MxN)
 - `linspace(a, b, n)` vs. `first:step:max`
- Array concatenation, slicing, and indexing
- Array Manipulation
 - zero-padding
 - removing elements
 - row-to-column `x(:)`
- Size of arrays (`numel` and `size`; **not** `length`)

Lecture 16 Goals: MATLAB III

- Multi-dimensional arrays:
 - Applying built-in functions to matrices
 - Scalar operations on matrices
 - Element-wise operations on matrices
 - Logical array comparisons
 - Array indexing with 'find'
 - 3D arrays

Arrays as function arguments

- Many MATLAB functions that work on single numbers will also work on entire arrays; this is very powerful!
- Results have the same dimensions as the input, results are produced “elementwise”
- For example:

```
>> av = abs([-3 0 5 1])
```

```
av =
```

```
    3    0    5    1
```

Powerful Array Functions

- There are a number of very useful function that are built-in to perform operations on vectors, or column-wise on matrices:
 - **min** the minimum value
 - **max** the maximum value
 - **sum** the sum of the elements
 - **prod** the product of the elements
 - **cumprod** cumulative product
 - **cumsum** cumulative sum

min, max Examples

```
>> vec = [4 -2 5 11];  
>> min(vec)  
ans =  
    -2  
  
>> mat = randi([1, 10], 2, 4)  
mat =  
     6     5     7     4  
     3     7     4    10  
  
>> max(mat)  
ans =  
     6     7     7    10
```

- Note: the result is a scalar when the argument is a vector; the result is a $1 \times n$ vector when the argument is an $m \times n$ matrix

sum, cumsum vector Examples

- The **sum** function returns the sum of all elements; the **cumsum** function shows the running sum as it iterates through the elements (4, then 4+-2, then 4-2+5, and finally 4-2+5+11)

```
>> vec = [4 -2 5 11];
```

```
>> sum(vec)
```

```
ans =
```

```
18
```

```
>> cumsum(vec)
```

```
ans =
```

```
4      2      7      18
```


What is the value of b?

`a = [2 3 1; -2 0 -6; 8 7 -1];`

`b = min(a);`

What is the value of b?

A) -6

B) [-2 0 -6]

C) [1 -6 -1]

D) [-6 -6 -6]

What is the value of b?

`a = [2 3 1; -2 0 -6; 8 7 -1];`

`b = min(a);`

What is the value of b?

A) -6

B) [-2 0 -6]

C) [1 -6 -1]

D) [-6 -6 -6]

What is the value of b?

$$a = [2 \ 3 \ 1; -2 \ 0 \ -6; 8 \ 7 \ -1];$$

$$b = \min(a');$$

What is the value of b?

A) -6

B) [-2 0 -6]

C) [1 -6 -1]

D) [-6 -6 -6]

What is the value of b?

$a = [2 \ 3 \ 1; -2 \ 0 \ -6; 8 \ 7 \ -1];$

$b = \min(a');$

What is the value of b?

A) -6

B) [-2 0 -6]

C) [1 -6 -1]

D) [-6 -6 -6]

What is the value of b?

```
a = [2 3 1; -2 0 -6; 8 7 -1];
```

```
b = min(a(:));
```

What is the value of b?

A) -6

B) [-2 0 -6]

C) [1 -6 -1]

D) [-6 -6 -6]

What is the value of b?

```
a = [2 3 1; -2 0 -6; 8 7 -1];
```

```
b = min(a(:));
```

What is the value of b?

A) -6

B) [-2 0 -6]

C) [1 -6 -1]

D) [-6 -6 -6]

sum, cumsum matrix Examples

- For matrices, most functions operate column-wise:

```
>> mat = randi([1, 10], 2, 4)
```

```
mat =
```

```
     1     10     1     4
     9      8     3     7
```

```
>> sum(mat)
```

```
ans =
```

```
    10    18     4    11
```

```
>> cumsum(mat)
```

```
ans =
```

```
     1     10     1     4
    10    18     4    11
```

The **sum** is the sum for each column; **cumsum** shows the cumulative sums as it iterates through the rows

prod, cumprod Examples

- These functions have the same format as **sum/cumsum**, but calculate products

```
>> v = [2:4 10]
v =
     2     3     4    10
>> cumprod(v)
ans =
     2     6    24   240
>> mat = randi([1, 10], 2,4)
mat =
     2     2     5     8
     8     7     8    10
>> prod(mat)
ans =
    16    14    40    80
```


Overall functions on matrices

- When functions operate column-wise for matrices, make nested calls to get the function result over all elements of a matrix, e.g.:

```
>> mat = randi([1, 10], 2,4)
```

```
mat =
```

```
 9  7  1  6  
 4  2  8  5
```

```
>> min(mat)
```

```
ans =
```

```
 4  2  1  5
```

```
>> min(min(mat))
```

```
ans =
```

```
 1
```

Overall functions on arrays

- Alternatively, since linear indexing arranges all the elements of an array into a column, you can also use this approach.

```
>> m = max(A(:)) % Find max of A, regardless of  
dim.
```

Scalar operations

- Numerical operations can be performed on every element in an array
- For example, *Scalar multiplication*: multiply every element by a scalar

```
>> [4  0  11] * 3
ans =
    12     0    33
```

- Another example: scalar addition; add a scalar to every element

```
>> zeros(1,3) + 5
ans =
     5     5     5
```

Array Operations

- **Array operations** on two matrices A and B:
 - these are applied between individual elements
 - this means the arrays must have the same dimensions
 - In MATLAB:
 - matrix addition: $A + B$
 - matrix subtraction: $A - B$ or $B - A$
 - For operations that are based on multiplication (multiplication, division, and exponentiation), a dot must be placed in front of the operator. Unless you're doing linear algebra, this point-wise approach is generally what you want.
 - array multiplication: $A .* B$
 - array division: $A ./ B$, $A .\ B$
 - array exponentiation $A .^ 2$
- **matrix multiplication: $A * B$ is NOT an element-wise operation**

Logical Vectors and Indexing

- Using relational and logical operators on a vector or matrix results in a **logical** vector or matrix

```
>> vec = [44 3 2 9 11 6];
```

```
>> logv = vec > 6
```

```
logv =
```

```
1 0 0 1 1 0
```

- Can use this to index into a vector or matrix, index and matrix dimensions must agree (logical linear indexing also OK)

```
>> vec(logv)
```

```
ans =
```

```
44 9 11
```

Element-wise logical operators

- `|` and `&` applied to arrays operate elementwise; i.e. go through element-by-element and return logical 1 or 0

```
>> [1 2 3 -1 1]>[0 1 2 1 0]
```

```
ans = 1x5 logical array
```

```
     1     1     1     0     1
```

- `||` and `&&` are used for scalars

True/False

- **false** equivalent to `logical(0)`
- **true** equivalent to `logical(1)`

- **false(m,n)** and **true(m,n)** create matrices of all **false** or **true** values

Logical Built-in Functions

- **any**, works column-wise, returns true for a column, if it contains any true values
- **all**, works column-wise, returns true for a column, if all the values in the column are true

```
>> M = randi([-5 100], m, n)
```

```
>> any(M<0 | M==5) % returns a 1 x n vector
```

```
% elements are true if corresponding
```

```
% column in M has any negative
```

```
% entries or any 5s in it.
```

```
>> all(M(:)>0) % true if all elements strictly positive
```


Finding elements

- **find** finds locations and returns indices

```
>> vec
vec =
    44     3     2     9    11     6
>> find(vec>6)
ans =
     1     4     5
```

- **find** also works on higher dimensional arrays

```
[i,j] = find(M>0) % returns non-zero matrix
indices
ind = find(A>0) % returns linear array indices
```

Comparing Arrays

- The **isequal** function compares two arrays, and returns logical **true** if they are equal (all corresponding elements) or **false** if not

```
>> v1 = 1:4;
>> v2 = [1 0 3 4];
>> isequal(v1,v2)
ans =
    0

>> v1 == v2
ans =
     1     0     1     1

>> all(v1 == v2)
ans =
    0
```

3D Matrices

- A three dimensional matrix has dimensions $m \times n \times p$
- Can create with built-in functions, e.g. the following creates a $3 \times 5 \times 2$ matrix of random integers; there are 2 layers, each of which is a 3×5 matrix

```
>> randi([0 50], 3,5,2)
ans(:,:,1) =
    36    34     6    17    38
    38    33    25    29    13
    14     8    48    11    25
ans(:,:,2) =
    35    27    13    41    17
    45     7    42    12    10
    48     7    12    47    12
```

Functions diff and meshgrid

- **diff** returns the differences between consecutive elements in a vector
- **meshgrid** receives as input arguments two vectors, and returns as output arguments two matrices that specify separately x and y values

```
>> [x y] = meshgrid(1:3,1:2)
```

```
x =
```

```
    1    2    3  
    1    2    3
```

```
y =
```

```
    1    1    1  
    2    2    2
```

Where could meshgrid be useful?

Common Pitfalls

- Attempting to create a matrix that does not have the same number of values in each row
- Confusing matrix multiplication and array multiplication. Array operations, including multiplication, division, and exponentiation, are performed term by term (so the arrays must have the same size); the operators are `.*`, `./`, `.\`, and `.^`.
- Attempting to use an array of **double** 1s and 0s to index into an array (must be **logical**, instead)
- Attempting to use `||` or `&&` with arrays. Always use `|` and `&` when working with arrays; `||` and `&&` are only used with logical scalars.

Programming Style Guidelines

- Extending vectors or matrices is not very fast, avoid doing this too much
- To be general, avoid assuming fixed dimensions for vectors , matrices or arrays. Instead, use **end** and **colon :** in context, or use **size** and **numel**

```
>> len = numel(vec);  
>> [r, c] = size(mat);  
>> last_col = mat(:, end);
```

- Use **true** instead of **logical(1)** and **false** instead of **logical(0)**, especially when creating vectors or matrices.

DESIGN Recipe

Testing

- Even simple functions can be deceptively hard to verify as correct just by “looking at them”
- However, it is easy to test functions on data you understand (and know what the correct answer should be)
- As functions and programs (which may use lots of functions) get more complicated this becomes very important

assert

In MATLAB, the `assert` function allows one to easily perform a test

```
assert(expr, message)
```

Stops execution and prints out the message when `expr` evaluates to false.

Examples

- test_triArea.m
- test_myQuadRoots.m

Testing is Programming

- We've discovered developing tests first (before writing any functions) often speeds the development process and helps ensure programs work correctly
- In fact, designing tests should be viewed as a part of programming even though you aren't actively coding a solution.

Design Recipe

Design Recipe

1. Develop important Test Cases – (actually code them, requires you to first create function header)
2. Code function body
3. Test!
4. Fix code, re-Test until working correctly

Example: myFtoC

- Use the Design Recipe to solve the following problem:

“Write a function converts degrees Fahrenheit to degrees Celsius.”

Example: myFtoC

1. Write test_myFtoC
2. Write myFtoC
3. Run test_myFtoC
4. Fix code, re-test until working correctly
5. Look at code, identify any pertinent additional tests
6. Retest, until working correctly

Done!

Example: myFtoC

- test_myFtoC.m
- myFtoC.m

Example: quadMin

- Use the Design Recipe to solve the following problem:

“Write a function that finds x that minimizes
 ax^2+bx+c
in the interval $[L,R]$. Assume $a \geq 0$, $L < R$.”

Example: quadMin

“Write a function that finds x that minimizes

$$ax^2+bx+c$$

in the interval $[L,R]$. Assume $a \geq 0$, $L < R$.”

What kind of tests should we have?

What are the cases?

Example: quadMin

- test_quadMin.m

